

Concepts of Thermodynamics
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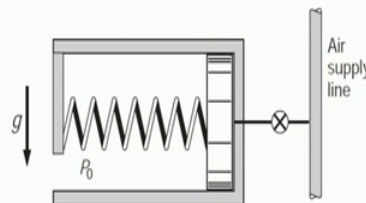
Lecture – 31
First Law for Unsteady Problems – Examples (Contd.)

We have worked out a few problems on unsteady flow so far as first law of thermodynamics is concerned and we will continue with the couple of more problems of that kind to give you a more comprehensive idea of problem solving.

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Problem 4.13: An insulated spring-loaded piston/cylinder, shown in figure, is connected to an air line flowing air at 600 kPa, 700 K by a valve. Initially the cylinder is empty and the spring force is zero. The valve is then opened until the cylinder pressure reaches 300 kPa. By noting that $u_2 = u_{line} + C_v(T_2 - T_{line})$ and $h_{line} - u_{line} = RT_{line}$. Find an expression for T_2 as a function of P_2, P_0, T_{line} . With $P_0 = 100$ kPa, find T_2 .

Ans: $T_2 = \left[\frac{c_v + R}{c_v + \left(\frac{P_0 + P_2}{2P_2}\right)R} \right] T_{line}; T_2 = 773.7 \text{ K}$

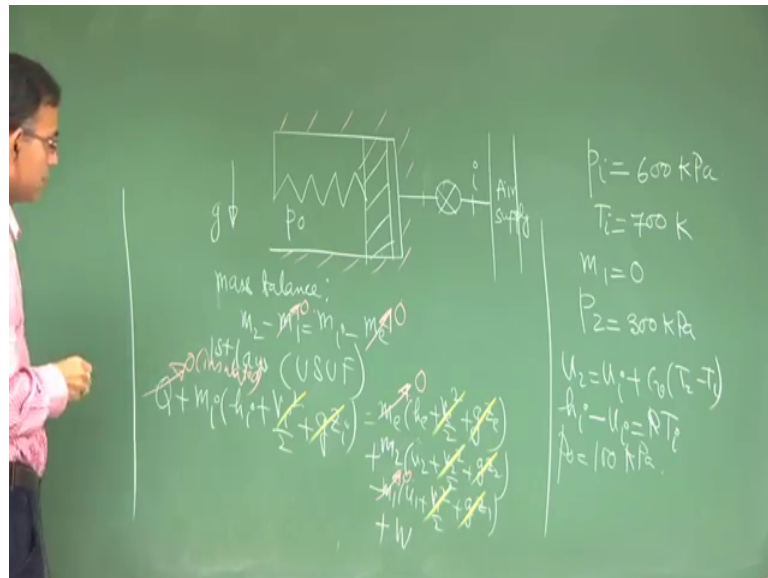


So, the next problem which is problem number 13 is something like this, an insulated spring loaded piston cylinder I have shown in the figure is connected to an air flow line flowing air at 600 kilo Pascal, 700 Kelvin by a valve. Initially the cylinder is empty and the spring force is 0. The valve is then opened until the cylinder pressures reaches 300 kilo Pascal.

Now, some relationship between is given between the internal energy inside the cylinder and internal energy of the line, find an expression for T_2 as a function of P_2, P_0 and T_{line} with P_0 which is the atmospheric pressure 100 kilo Pascal, you find what is T_2 ?

So, this is also a tank filling problem, but you know this is not a rigid tank, this is a variable volume tank. So, this is more involved than the tank filling problem in a sense that because volume of the trapped air within the piston cylinder changes there is a work done associated with it, which was not there for a rigid tank that makes this problem different from a traditional tank filling problem. So, as we have considered earlier.

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So, we will draw schematic, this is the piston and it is spring loaded. So, this is the gravity it shows that you know the weight of the piston is not important because it is the piston is not aligned in the cylinder is not aligned in the direction of gravity ok. So, let us see I mean what is given and what is not. So, this is I the property which is coming out coming in. So, I am writing I here you know not here; why? to be technically correct, see it is given that for the state i the air supply line, pressure is 600 kilo Pascal.

If we put i here there is a pressure drop so pressure is no more 600 kilo Pascal in terms of enthalpy does not matter because this is treated as an ideal gas where enthalpy does not depend on pressure, but depends on temperature. So, enthalpy here is same as enthalpy here and you know so temperature here roughly same as temperature here if it is an ideal gas. For enthalpy does not matter anyway whether it is ideal gas or not for temperature it matters, because if enthalpy here is same as enthalpy here, temperature here is same as

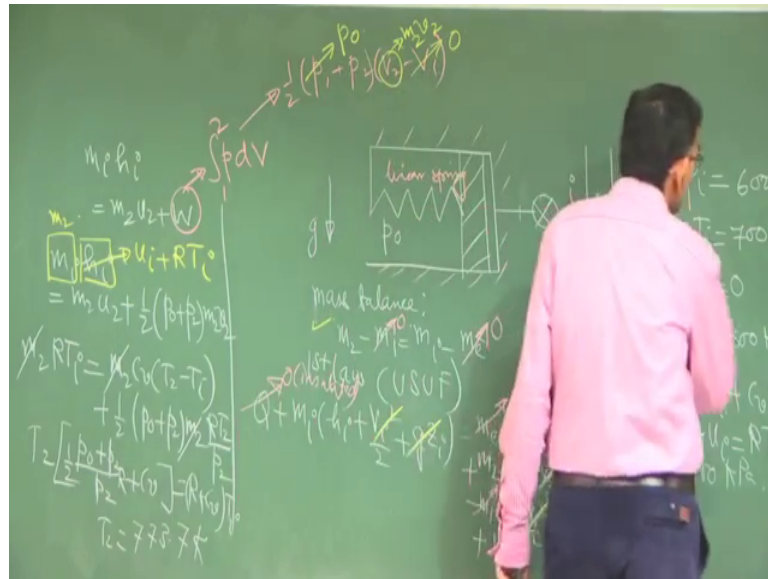
temperature here provided it is an ideal gas you know otherwise not. So, then so this is air supply so, p_i even if it is not required let us write, $T_i = 700$ Kelvin.

Initially the cylinder is empty so m_1 is 0. So, the control volume is the gap between the piston and the cylinder, the air within that. So, it is no more a control mass system despite being a piston cylinder arrangement. So, piston cylinder arrangement by default is not a control mass system, here it is not a control mass system because of continuous mass supply the mass within it is continuously changing with time. So, m_1 equal to 0 and p_2 is 300 kilo Pascal, what is also given as u_2 is equal to $u_i + C_v \text{ into } T_2 - T_i$ and $h_i - u_i$ is equal to $R T_i$, p_{naught} is 100 kilo Pascal.

So, initially although the mass inside is 0, but there is a resistance pressure same as p_{naught} to keep this in equilibrium. So, let us write the first law of or the control valve yes for the control volume first mass balance. So, m_2 so, m_i you have some m_i , there is no m_e , there is no m_1 . So, m_2 is equal to m_i , then we will apply the first law for USUF Uniform State Uniform Flow ok.

Let us see what is the situation for heat transfer, it is told that this is insulated piston cylinder. So, I want to schematically represent that we may show a insulation here. So, this is 0 because it is insulated, then there is no m_2 term 0, there is no m_e term, this is 0 there is no m_1 sorry very sorry, there is no m_1 right initial is 0 right plus m_2 is very much there, there is no m_1 ok. So, then your usual neglecting changes in kinetic energy and potential energy will work for this problem as well.

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So, you are left with $m_1 h_1$ is equal to $m_2 u_2$ plus W right, now a key question what expression we will substitute for W , can we write W as integral $p dV$ from state 1 to state 2? Yes we can write. Some students develop a false idea that integral $p dV$ is valid only for a control mass system, the reason is that it is derived first by taking an example of a control mass system, but it is just work done for a moving system boundary for a simple compressible pure substance undergoing a quasi equilibrium process.

Whether the system is a closed system or open system that is not under the jurisdiction of these, this is this simply follows from the resistance force times the displacement integrated ok. So, that essentially means that you can use here $p dV$ and because it is a linear spring these for a pressure volume diagram will be linear. So, the area under the $P-V$ diagram is area under a trapezium. So, this is eventually half into p_1 plus p_2 into v_2 minus v_1 right.

So, now p_1 is same as p_0 and v_2 you do not know, v_1 is 0 and in place of v_2 you can write mass into specific m_2 into specific volume at state 2. So, let us see how we can write this $m_1 h_1$ is equal to $m_2 u_2$ plus half into p_0 plus p_2 into $m_2 v_2$ then it is just algebra I mean your problem solving is complete here. So, then what is given here you just try to write in place of h_1 you write u_1 plus $R T_1$ right. So, in place of h_1 u_1 plus $R T_1$ and m_1 will be same as m_2 .

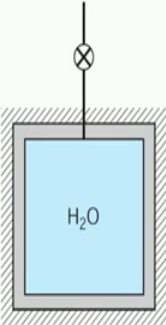
So, you have m_2 into RT_i is equal to now m_2 into u_2 minus u_i , u_2 minus u_i is C_v into T_2 minus T_i . So, $m_2 C_v$ into T_2 minus T_i plus half p_0 plus $p_2 m_2$ and v_2 is $R T_2$ by p_2 right, m_2 gets cancelled from all the terms. So, that gives you an expression for T_2 in terms of T_i right that is what is asked. So, you can write T_2 into p_0 plus p_2 by p_2 into half plus C_v is equal to R plus C_v into T_i right

There is an R here right, P naught plus these into R ok. So, then you can I mean. So, this is the expression where you can substitute all the relevant values and you can get what is T_2 as a function of T_i . So, the answer to this problem is T_2 is 773.7 Kelvin. So, we will work out one last problem related to this before we move on to a different chapter Problem number 14.

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Problem 4.14: A 2-m³ insulated vessel, shown in figure contains saturated vapour steam at 4 MPa. A valve on the top of the tank is opened, and steam is allowed to escape. During the process any liquid formed collects at the bottom of the vessel, so that only saturated vapour exits. Calculate the total mass that has escaped when the pressure inside reaches 1 MPa.

Ans: $m_e = m_2 - m_1 = 27.24$ kg

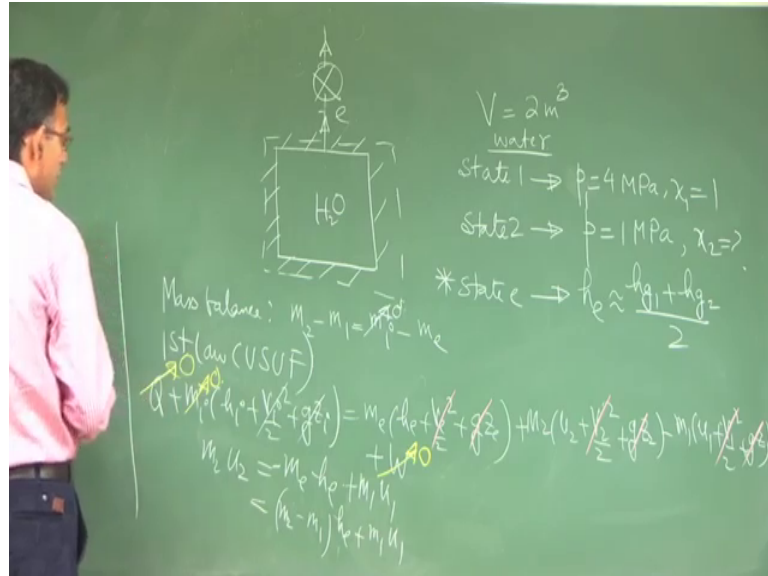


A 2 meter cube insulated vessel shown in a figure contains saturated vapour steam at 4 MPa ok. A valve on the top of the tank is opened, and steam is allowed to escape this is a tank emptying problem, but not for ideal gas. During the process any liquid formed collects at the bottom, so that only saturated vapour exits. So, this sentence tells that the exit state is saturated vapour state, calculate the total mass that has escaped when the pressure inside reached 1 MPa.

So, initially pressure was 4 MPa, the pressure is released as the valve is opened and eventually the final pressure is 1 MPa. So, you have to find out what is the total mass

that has escaped. So, we will work out this problem as per our practice we will draw the schematic in the board.

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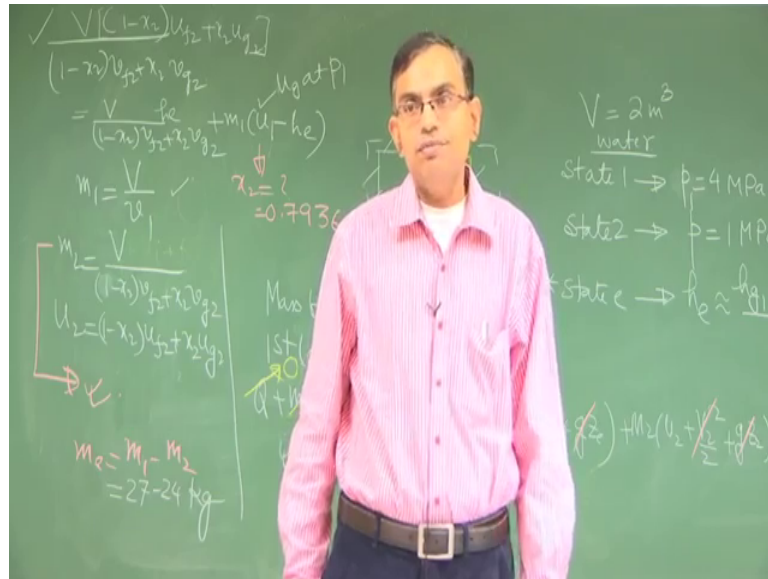
So, this is a rigid vessel let us write what is given V is equal to 2 meter cube state 1. So, fluid is water state 1, x equal p equal to 4 MPa, x equal to 1 state 2 p equal to 1 MPa then in state 2 you have a. So, see the physical situation you have to assess initially there is vapour now vapour is exiting. So, then the energy state of the system is going down and that is reflected in terms of that vapour now getting converted to a 2 phase mixture liquid vapour mixture. So, state 2 will be associated with some quality value. So, x_2 is there, but you do not know what it is.

So, there is a state e here again you have to make an assumption. So, initially it 4 MPa finally, it is 1 MPa so, line pressure here also cannot remain always you know fixed. So, the line pressure exit line pressure will be something which will be varying between 1 MPa to sorry 4 MPa to 1 MPa, but always these what is living is saturated vapour. So, we can argue that for all practical purposes h_e is roughly h_{g1} plus h_{g2} by 2 average of h_g between state 1 and state 2 this is a very important assumption. So, I am putting an asterisk here, you do not make this assumption you cannot proceed further because you have no information on state e you need to have an information on state e .

So, then with this information let us write the mass balance and energy balance, this is your control volume. So, what is m_e it is something which is their m_1 and m_2 there,

there is no m i right, first law USUF. So, heat transfer is 0 because it is insulated work done is 0 because this is rigid tank, there is no m i. So, this term is 0 neglect changes in kinetic energy and potential energy if you do all that of course, here also although it is not really went, but still. So, you have $m_2 u_2$ is equal to $m_e h_e$ sorry minus $m_e h_e$ plus $m_1 u_1$ right and minus m_e is m_2 minus m_1 right.

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So, u_2 we require to find out what is state 2 so, u_2 is ok. So, let us write now, we know what is m_1 and what is we do know we know what is m_1 , but we do not know what is m_2 right. So, m_1 is what? So whatever we know let us write V by v_1 . So, we know m_2 we do not know what is it what we know this is definitely $1 - x_2$ into v_{f2} plus x_2 into v_{g2} . It depends on what is x_2 that what will be the value of m_2 V is fixed u_2 is $1 - x_2$ into u_{f2} plus x_2 into u_{g2} ok.

So, these equation let us write, m_2 is V by $1 - x_2$ into v_{f2} plus x_2 v_{g2} into u_2 $1 - x_2$ into u_{f2} plus x_2 u_{g2} . So, this is the left hand side is equal to m_2 into h_e ; m_2 into h_e is again V by $1 - x_2$ v_{f2} plus x_2 v_{g2} into h_e plus m_1 into u_1 minus h_e u_1 you know from table state 1 u_1 is u_g at P_1 because quality is 1 and h_e is this approximation.

So, this is an equation this equation where you have everything known except x_2 . So, from here you can solve for x_2 what is x_2 . So, if you solve for x_2 , x_2 will be 0.7936 ok. So, if you solve for x_2 then you will immediately find out what is m_2 because m_2

is a function of x^2 . So, then what is m_e is nothing, but $m_1 - m_2$ ok. So, m_e is equal to $m_1 - m_2$ this is 27.24 kg ok. So, again this is quite an involved problem where by using the energy balance you are calculating the quality of a state right, it involves both mass and properties.

So, to summarize we have discussed so far the basic concepts of heat and work and also the first law of thermodynamics considering energy transfer of through heat and work for control mass system and control volume undergoing steady state process as well as unsteady state process. So, that brings us to a junction where we have got a basic feel of how to apply energy balance in the per view of the first law, but all processes which satisfy the energy balance may not actually occur in practice. So, what inhibits those so called unrealistic or impractical processes to occur despite satisfying energy balance, we will consider or take that up in our next lectures.

Thank you.