Conduction and Convection Heat Transfer

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Lecture - 12

Heat Transfer from Extended Surfaces (Contd.)

Good Afternoon, I welcome you all to this session of Conduction and Convection Heat Transfer.

Last class we were discussing heat transfer through extended surfaces know as Fin. The situation

is that extended surfaces are attached to a base surface to enhance the rate of heat transfer from

the base surface and these extended surfaces provide additional surface area for convective heat

transfer from its lateral surfaces along with conductions through these surfaces and through this.

That is by providing additional area for convective heat transfer from lateral surfaces the fin or

extended surfaces enhance the rate of heat transfer from the base surface. And what we discuss

we formulated the differential equation for temperature distribution by applying the conservation

of energy to an element in consideration of one dimensional heat conduction through the field.

That is the extended surface along with the convection from the lateral surface and we are (())

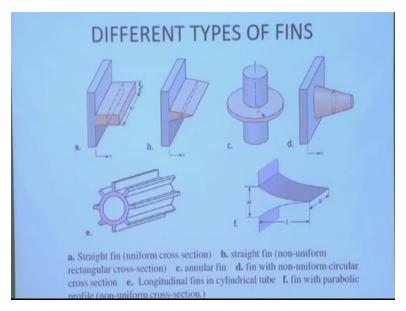
(1:38) for the temperature distribution for different cases or situation of the field which impose

the different boundary condition for the solution of the differential equation for temperature.

Today, we just have an overall summery before that I tell you different types of Fins that are

used.

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Overall view, this is the Straight rectangular fin is the most simple case that the cross-sectional area of the fin is constant, same. This is the base surface as I have just told this is the extended surface know as fin which provide additional surface, this surface top, bottom this surface these are the surfaces, this lateral surface all this surfaces additional surfaces for convective heat transfer along with the conduction to these fin along this direction for which the heat transfer from this base surface where it is (()) (02:52) in hand.

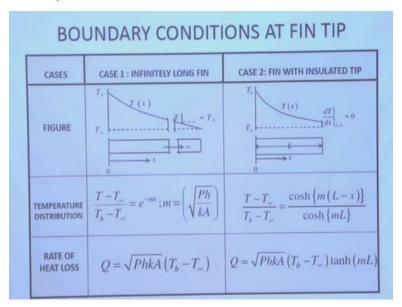
This was discussed and from the conservation of energy principle. We developed the differential equation for temperature and we solve this under different boundary condition, different situation. These are different types of fins, straight fin but non-uniform cross-section. See this is an annular fin sometimes it is known as circumferential fin, in a cylindrical chamber.

These are used sometime in heat exchanges this type of fin are used the circumferential these are annular fin, number of fin may be used here also there may be number of fins only one fin is shown. This one fin with non-uniform circular cross section like a conical shape, circular cross section this is sometimes known as pin fin. Pin with non-uniform circular cross-section this is same thing in a cylindrical tube where the heat transfer from the surface.

For all these case, the heat transfer from the base surface is enhanced by attaching these extended surfaces or pins. Here the pins are longitudinal, parallel to the axis of the cylinder that's why this

is known as longitudinal fin pin cylindrical tube. This is a fin similar type like this is a parabolic profile non-uniform different types of pins are used. This you can get in any classical text book nothing great.

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Now these are the things which we discussed last class that we first discussed infinitely long fin where the base is at a temperature Tb, base temperature is same for all cases. Now if the fin is infinitely long we impose a boundary condition from our physical fin that ultimately the temperature at these exposed ends becomes the surrounding fluid temperature T infinity. In that case our temperature distribution is exponentially decreasing.

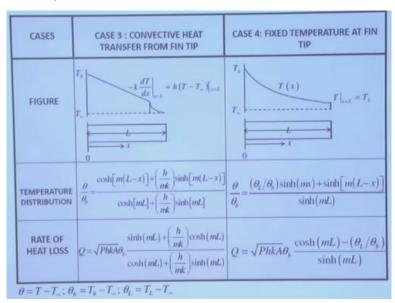
It will be bar minus mx, T minus T infinity by Tb minus T infinity. Tb is the base temperature. T is the temperature at any section x. So, x ten to infinity, it is the infinity so both for T infinity another thing is that this type of solution at the same time gives a zero (()) (5:23) dt dx is zero x, x is got to infinity and x ten to infinity and the heat transfer rate accordingly is given by this hP or PhkA root over Tb minus T infinity.

Case two discuss fin with insulated tip where we impose the boundary condition dt and dx, zero. That means fin tip is insulated no heat is being transferred from these exposed surface, this surface that means all the heat which is being extracted from the base is being convected from the lateral surfaces. So, that here the heat transfer is zero that is the physical function. Boundary

condition is imposed in terms of the temperature gradient whenever there is an insulated surface, adiabatic surface heat transfer boundary condition is in conduction dt by dx is zero because heat transfer is zero like fluid mechanics shear stress is 0, du dy zero, one dimensional case.

Similar thing so that the temperature profile does not attend the T infinity temperature. This temperature is higher than T infinity because of this insulation but the slope is zero. The shape of the curve is such, it becomes parallel to the (()) (6:38) so that dt, dx is zero.

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Number three case that also we discussed in the class that here we impose the most practical situation that we do not insulate these it is open through the atmosphere that means the fin shared heat by convection through this lateral surface, this bottom surface. The side surfaces, both the sides and all through out these exposed surfaces at this end, extreme end. So, this exposed surfaces heat transfer we prescribe the condition of governing through the infinity.

So, therefore while solving the equation within the fin as x is equal to a here well this diagram is little wrong I am sorry to tell you probably it is wrong from the place where it is taken this point this line should coincide with the length of the field because this part is outside. So, it is wrong from the place where it is taken you see event the published thing are sometimes this is because of our overlooking the error while reading the proof.

So, therefore here what happens the temperature changes and it has a flow not zero flow which determine the heat transfer minus K, gt by dx and should be matched with the convective heat transfer at these interface that is this solid exposed surface with the surrounding gas so that this slope is matching with this and this is the temperature distribution by convection after this that means from this surface there is a decrease in temperature in a thin film due to convection which will be dealt in details in convection classes when we will take convection heat transfer.

So, this comes to b this is to understand. And in this case with this type of boundary condition it becomes a routine calculation with little complication as a big manipulation are little tedious so that we get a temperature distribution theta by theta b nomenclature you know theta is the express temperature over the surrounding fluid temperature. Theta d is the base temperature over the surrounding fluid temperature that means theta, the temperature over the excess fluid temperature.

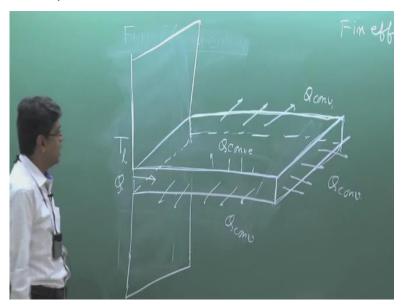
So, accordingly the heat flux is given by these expressions. This gives hyperbolic functions. Another case was pick the pin temperature at the end that means pin temperature is fixed at the end by some arrangement of pulling fluid we keep a fixed fin temperature we are not much bothered how it is done but we think mathematically as if the temperature is given as x is equal to Lca.

So, solve the equation we know the boundary condition x equal to Lt is equal to Tl in that case the temperature distribution is like that and it does not reach the infinity and the temperature distribution if you find out it will be like this. So, this is the fixed temperature at, sorry fixed temperature at the end of the field. Temperature distribution and the heat flux. What is meant by Fin Efficiency? Let us have this base plate.

This is the base and this is the rectangular fin, now Fin efficient, what I meant by fin efficient? Fin efficiency eta f. The fin efficient is defined like this now if the base temperature is Tb the heat is transferred and the amount of heat is transferred Q from this portion of the base where the fin is attached and this portion of the base where pin is attached a huge amount of heat transfer take place because of this heat transfer from this lateral surfaces.

You can show this surface like this also that means the top surfaces this surface, bottom surface this surface again this surface back side all these surfaces the front side this surfaces and this exposed surfaces everywhere the convection Q convection, from this surface also the lateral surface Q convection, through this we already we deal in the last class. Q convection and from this surface also finally convection heat transfer is there.

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If it is not insulated that mean this side, this side top surface, bottom surface that means all lateral surfaces convection heat transfer is there due to this large surface area the convective heat transfer is huge. So, that finally this heat that is coming from this base where it is attached is in hand that is the basic principle of fin. But one thing what we assume that it is one dimensional problem usually for the last fin.

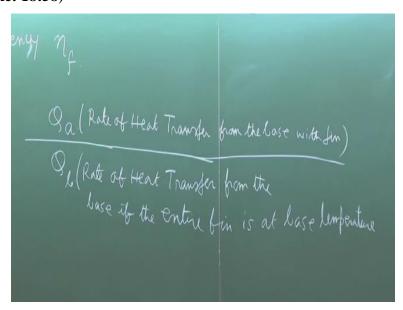
So, that we consider this direction is the x that means this is the x direction from this plane so at any x the temperature is T which is same in this direction fin thickness of the fin or height whatever you can tell that means same temperature but it changes (()) (15:56) and this T is always less than Tb that we have already seen that temperature is maximum at this point and then slowly decreases to a temperature and free stream temperature is T infinite now with this knowledge in background how does the fin enhances the heat transfer.

The efficiency is defined as the actual heat transferred from the base that means this portion of the base where the fin is added let us write this as Qa that is the heat transfer through the base I am not writing it I am telling heat transfer through the base with the attachment of the fin in actual case. So, why I am telling actual case, this case is actual why? That is because the denominator defines a quantity Qb which is the heat transfer, rate of heat transfer from the base where the fin is attached.

If the entire fin would have been at the base temperature that means the entire fin attains the uniform temperature that of the base when it can attain if the thermal conductivity of the fin is infinitely high. Infinitely high thermal conductivity of the fin otherwise in actual case the fin temperature decreases the along the direction x but at any x this is same for all the lateral surfaces.

This we took in deriving the temperature distribution the differential equation for temperature distribution from energy conservation field. So, this is the definition that heat transfer I may write this. Rate of heat transfer from the base with fin. This is the actual rate of heat transfer and this one is rate of heat transfer from the base if the entire pin is at base temperature.

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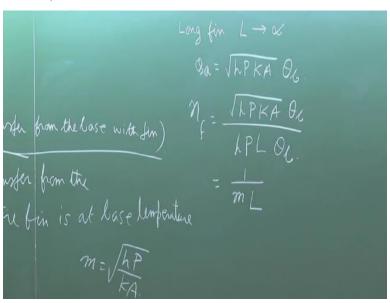


Now Qb therefore can be written like this if h is the heat transfer coefficient with our nomenclature, p as the perimeter of the field that means some of this dimension this plus, this

into two this side and the bottom surface that is the perimeter into the length of the fin, times the Tb minus T infinite, because the entire fin is that base temperature. So, there for the ideal heat transfer that means considering the fin to be infinitely thermal conductive so that having infinite thermal conductivity hPL theta b.

Therefore, the expression of fin efficiency depends upon the expression of QA if you take long fin where the fin length L tends to infinity very large then we know that Qa is equal to this Qa root over hPKA theta b. So, there for in this case theta f is equal to root over hPAA theta b divided by hPL theta b and this becomes if you cancel it 1 by mL where m is given by our nomenclature that root over we denoted m as root over hP by kA.

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So, it is very simple that you substitute the expression in the numerator for the actual heat transfer in case fin with insulated tip. What will be theta f, theta f will be this is hPL theta b and heat transfer which we drive. I have shown it also it will be root over hPKA same thing but tan tan hyperbolic mL into theta b. m is the nomenclature root over hP by K and this becomes tan hyperbolic into mL divided by mL.

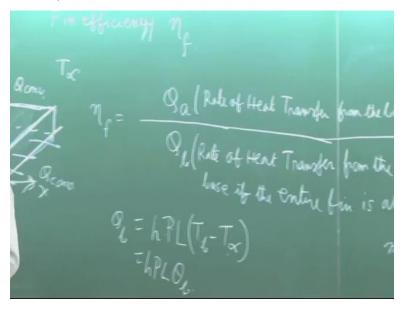
So, depending upon the cases you can find out the efficiency expression so there for the question of fin efficiency comes because of this conducting at the first class I told that we are putting a conduction resistance so we are adding a more convection area to enhance the heat transfer. But

if the conduction resistance is very large because of very low thermal conductivity. So, that there is a drastic dropping temperature along this direction.

So, heat transfer from the lateral surface may not be augmented that way because the heat transfer depends not only on the surface area but also on the temperature difference. So, therefore there is a race between the two that we have to be careful that the fin shouldn't have a large temperature drop we should have a high thermal conductivity and in the most ideal case is that thermal conductivity is that the entire fin at base temperature.

So, if this you compare you define a parameter like this which is known fin efficiency.

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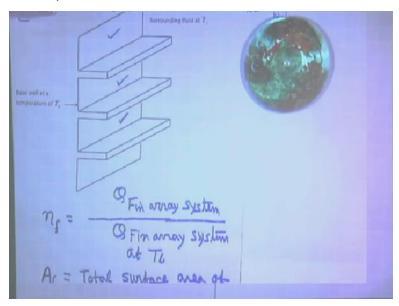
Now here we see a number of fin, array of fin a system with array of fin. This is the base plate number of fins are there. Here there are three fins it is shown. This wall of a temperature of Tb and the surrounding fluid at T. So, here how do you define the fin efficiency? Same thing but little calculation that fin efficiency here it is defined as the Q from the system fin array system Q Fin array system divided by Q from the same Fin array system at Tb.

That means, the entire system is at Tb. What is the difference? Difference is that here Fin array system when you consider Q then we have to consider the heat transfer from the Fin also the heat transfer from the un fin portion. Now if we had a nomenclature like this let us consider Af is the

total surface area of fin and if make this nomenclature At is the total area, total heat transfer area, total surface area.

And this surface area means heat transfer area which takes part in heat transfer. Total surface area including both the surface all surface area fin plus uncovered portion that means these are the uncovered portion AP.

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AP is the total surface area that means uncovered portion plus fin then we can write here Q the numerator QF, system can be written as QFin system is the heat transfer from the fin that means A is the total surface area of the fin then h into Af into theta b, what is theta b, here I write theta b is the Tb minus the infinity. Now here what I want to tell you that how we can write the efficiency of fin system in terms of the individual fin efficient.

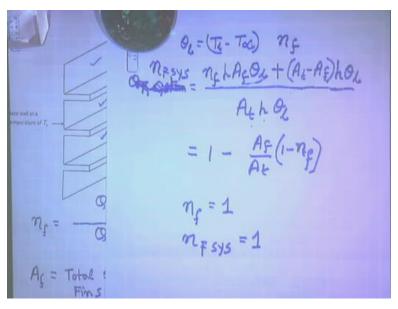
If we assume the individual fin efficiency is beta f which is constant, same for all the fin then we multiply the this with eta f gives the heat transfer from all the field, h A theta b considering fin at base temperature. So, this is the ideal heat transfer and this is multiplied by the fin efficacy of the individual fin as it was defined earlier is the heat transfer from all the fin. Last the un fin portion that is A total minus Af that is the area into h into theta b and the denominator will be the total area At into h into theta b.

That means how to express this if we know the total surface area of the fin and the total surface area including the un fin portion plus fin so minus the fin portion this is the area of the un-fin portion At minus A. This can be written in a simple expression taking At, h theta b separate term 1 minus theta b canceled out, h canceled out At h, theta bh canceled out one minus Af by At into one minus theta f, efficiency theta f sorry, it will be the efficiency of the array system, efficiency fin system not Qa.

I am sorry, it is efficiency of —I wanted to first start with this with the numerator. So, I have done at the same time. I first started to write this expression in the numerator however does not matter the numerator is the Q that is heat transfer of the fin system that is the heat transfer from the fin, that is the heat transfer from the un-fin portion so theta for the fin system is divided is by At, h, theta b divided by the heat transfer of the entire base with the fin when they are all at the temperature Tb.

So, when eta f then equal to 1, eta fin system also equals to one. That means we can express the efficiency of a fin array system in terms of efficiency of individual fin.

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Now, another important concept in practice I will tell you which is very important for engineer we define fin efficacy okay this is the definition we understand the ideal case a highly conductive fin within superconductor whose temperature is equal to the base temperature and we define the

fin efficiency the actual heat transfer with fins and what is the heat transfer if the entire system

with fin that is the same base temperature.

Now question arises whether how much we gain by adding fin sometimes it happens that okay

there is a monotonic gain but what is the return whether it is economic to use that after certain

stage. Under certain case whether fins are really required or not if we have a marginal gain in

enhancing the heat transfer then cost will be provide you cannot judge from the economic point

of view.

Because you have purchase fin you have to go for manufacturing attaching the fin surfaces the

entire fin system has to be fabricated. So, there for a question comes effectiveness of the fin to

judge whether it is effective to use fin. Effectiveness of fin that means to (()) (31:48) Let us

define a parameter the similar way as the efficiency but e effectiveness that means it is known as

effectiveness but frankly speaking physically efficiency and effectiveness is same.

Effectiveness of performance is a efficiency but here it is defined in a little different way.

Efficiency is the effectiveness of his performance when it is performing but now I will judge

what is the difference between the two that is performed or it does not perform that means if we

define effectiveness as Q with fin or Q without fin. Efficiency by definition is always less than

one.

Because fin can never attain Tb temperature like (()) (32:48) cycle like one is the theoretical limit

but here also it is always better than one we have seen always heat transfer will increase but how

much what is the gain? Let us see that. Now in a very simple expression if I write that this is

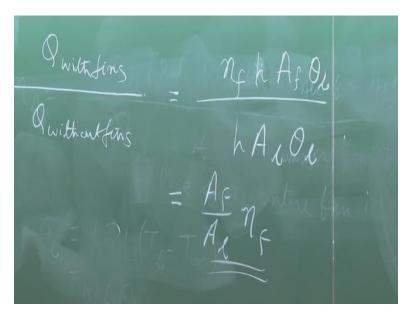
equal to efficiency, fin for example h fin area, surface area of the fin into theta b.

That means simply I multiply with the efficiency of the field h, heat transfer coefficient A,b,c

surface area that is provided by the fin and what is this without fin. Without fin base area theta b

that means I get an expression Af by Ab into eta f is so simple but it says many things.

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That means I gain by using fin because I have a huge value of Af by Ab but I should also consider if eta f is not also not very low. If you multiply with a high value with a very low value eta is very low my gain may not be very high that means I have provided additional surface. But efficiency is not a function of surface area, you go through the expression. The answer to the question lies in the fact that with increasing value of h with eta h decreases.

You have to be careful about eta h if we have a low eta f, there is no point gain is less, very first class that is why I started fin by telling that this provides a conduction resistance though we create more surface area to enhance the heat transfer by convection but provides a conduction resistance and this conduction resistance becomes more and the efficiency becomes less if you have a high heat transfer coefficient.

So, there for one has to judge it but without going for any detailed analysis which is beyond the scope of this class I tell you as an information that where h is high usually fins are not provided because of low eta and we cannot provide a very large surface area because not only the cost but the space, space is a requirement where I am he is telling the (()) (35:37) so therefore we have to fragment enough to have a meaningful gain which is a product of Af by Ab into eta f.

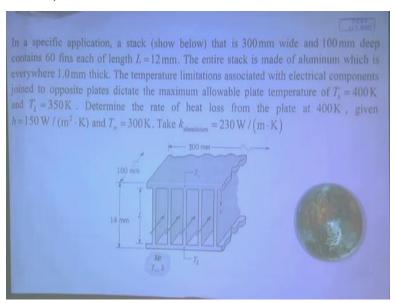
For fluid, especially liquid which has a high thermal conductivity in both convections if they very high heat transfer coefficient in boiling condensation phase change process have high heat

transfer coefficient there, theta is usually low we do not usually give fin. And from a very ready common-sense case when the heat transfer coefficient is very high the exposed where surfaced will be enabled, will be capable enough to transfer heat.

Why you are adding, why you are giving him, you are brilliant student, why are you giving him a tutor. He himself can make it up like that. So, therefore sometimes these question is asked if you have a heat exchanger one side liquid is going and turbulator are there to create more turbulence in the flow field and another side gas is moving with a low velocity which side you will provide fin if you tell gas side you get full mark.

If you say (()) (36:55) liquid side flowing with high turbulence, get out. Zero. Because this is the concept that effectiveness of the fin that means fin shouldn't be used where the heat transfer coefficient is high this is because this side. Now after this we will solve some problem.

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Let me have a very interesting problem that you can take this problem. In a specific application, a stack shown below this is a stack that is 300 mm wide and 100 mm deep contains 60 fins, five are shown that means there are number of fins is a very big size 60 fin. Each of length L, 12 mm. This is the length of the fin this is 12 mm and this is the thickness of the stack plate this is 1.0 mm that is why this is quoted in mm.

This is the length of fin. 60 fin each of length 12mm. The entire stake is made of aluminum which is everywhere 1.0 mm thick that means this one 1.0 mm this one. This was not shown in dimension this is width. The temperature limitation associated with electrical components jointed to opposite plates that this plate. This side of the plate dictate the maximum allowable plate temperature of 400 K.

That means this plate should not be at temperature above 400 K, electronic components will be damaged and TL is 350 K this side the plate is kept at 350 k by an arrangement of air with a T infinity and h heat transfer coefficient we are not much bothered in this side because the problem is prescribed by fixing the 350 K at this temperature. Determine the rate of heat loss from the plate at 400 K that means what is the rate of heat lost from the plane at 400 K.

What are the value given h is 150 watt, per meter square K, T infinity is 300 k. These are the value given h is 150 watt per meter square K, 300 K. Aluminum thermal conductivity that mean the material thermal conductivity 230 watt per meter K. This is precisely the problem so we have to find out the heat transfer from the plate.

Now heat transfer from the plate is due to the heat transfer from the fin which is the heat transfer from this area of the bases where the fin is attached plus the heat transfer from the un-fin portion of the base plus the heat transfer from the top surface of the plane that you have to recognize to solve this problem. Problem is very simple but one thing this type of problem in examination if it comes we will give you the formula here.

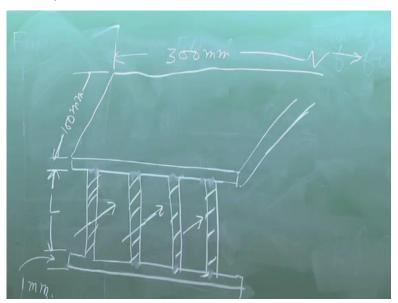
We have to use this heat transfer from the fin where the fin is fixed at two temperatures that means this you consider as base temperature of 400 K and if you consider the fin of length L which is given as what is the length 12 mm the other end is, what is the temperature, 300 K that means fixed temperature at the end. No question of mugging the formula but the formula will be provided or even a big problem you may be told that you derived this formula.

That means you start with governing differential equation theta is C1 into the power mx plus C2 into the power minus mx by control volume energy balance then theta B is C1 plus C2 and x is

equal to zero then theta L is C1 into the power ML plus into the power minus ML from there you can also derive but if teacher is relatively better he will not ask that routine derivation because it is tedious. He will still use this formula for things with temperature prescribed at 2M, base temperature and other.

So, problem boils down to that. So, now let me solve this problem. This is 100 mm. This is the flow of air.

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Now this is the geometry 100 mm depth, 300 mm width, this is continued this is a cut section, numbers of fin 60, fin length L and this is air flowing through this which give the convective heat transfer coefficient which takes the heat from the lateral surface of the fin this is the problem. Now let me first write this is the plate, Plate temperature let we write it as Tb base temperature that plate this is the temperature Tl is 300 K and Tb is 400 K and T infinity.

That is the surrounding fluid is at, the infinity is what? The infinity is 300 K TL is not 300 K, 350 K sorry and this is 300 K. Now let us write the equation, the expression for Q plate is what? Q plate is first two fin, numbers of fin there are 60 fins, identical fin, 60 identical fin. If fin efficiency could have been given I could have been happiest man then we could have found out that a surface area times eight, times TB minus the infinity times the efficiency.

But it is not given that means either I have to mug up that formula or I have to derive. Mugging

mean what now a days no teacher gives that you have to mug up and you just write that.

However, if it is given then it is good but it is a tedious calculation. Let me see do not mind. That

formula is per fin root over hPKA all the nomenclature is known to us as they are conventional

to thermal conductivity, cross sectional area, perimeter, heat transfer coefficient into theta b.

Then it is cos hyperbolic mL minus theta L by theta b with all nomenclature known to us divided

by Sin hyperbolic mL. So, this is the expression of heat transfer when theta b, theta l are fixed for

a fin and number of fin 60. This is the heat transfer from the fin surface then plus heat transfer

from the un-fin surface what is the un-fin surface that area is what un fin surface is .1 into .3.

Now I will put this value afterward.

Now un-fin surface we write this way A un-fin that I will find out afterward into h into Tb minus

T infinity, write simply theta b then A plate, h theta b this is only a tedious calculation nothing

else is there. Now you write down the value h is what? h is 150 watt power meter square K. P is

what perimeter tell me what is P? P is the perimeter that means this way 100 plus that means .1

plus .001 into 2. It is almost equal to 0.2-meter perimeter.

Perimeter is what this side you understand the perimeter that means this plus this. Perimeter is all

right. Lateral surface take this 100 then 1 mm, clear. This is the fin, perimeter now what we

require K. What is K? 230 watt per meter K. What is cross sectional area A of the fin is .001 into

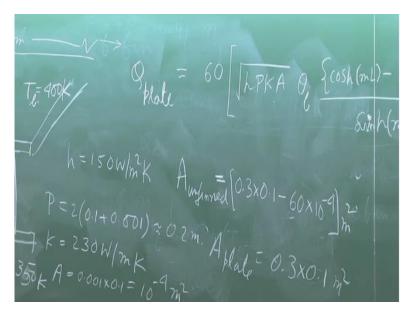
.1 is equal to 10 to the power minus 4 meter square. A is PKA, everything is there. Now A un-

fin, what is A un-fin equals to 0.3 into 0.1 minus 60 into 10 to the power minus four.

This is very simple meter square. Clear? that means, this is the un-fin portion this portion let area

A plate is 0.3 into 0.1 meter square that means .03 clear?

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This is the plate area 300 mm into 100 mm. Un-fin portion, this area minus the cross-sectional area of each fin times 60 times. That's all. So, fin problem I am tell you are all direct applications of the equations that we have developed but you don't have to remember the equation you will only derive the equation. This problem is clear now. If you put all the values in the proper unit then you will see that the order is like this value comes out to be I tell you 6631 watt.

Un-fin portion heat transfer is 375 watt and the top surface of the plate 451 watt. This plate means top surface. A plate means this is top surface this is top surface. Now one thing which I like to mention a comment that you see most of the heat transfer take place through the fin is increased order of magnitude. This is because of what? The huge surface area provided by the 60 fin. Well here.

Bottom surface, this is the bottom surface un fin portion only heat transfer from this place this is the bottom surface. This plate this is not required the question is, what is the heat transfer from this top plate. This is not required this entire stack this part of the stack is not that is not required. Yes, correct you are interested in the entire system heat transfer but this is not asked for. It is only from the top plate.

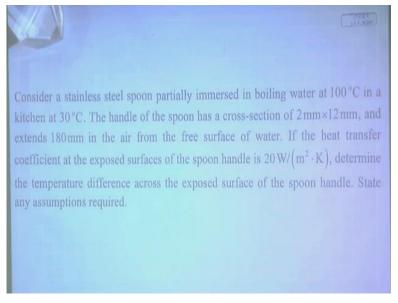
So, top plate has two surfaces bottom surface through fin and un-fin and you see through fin and un-fin the ratio is more than an overall magnitude. Which side, no that is insulated these lateral

surfaces these surfaces all these surfaces fin they transfer heat to the air. That is the convective visual from this side that that is taken care by this formula fin heat transferred from the plate top surface of the plate. This surface this end surface of the plate from the end surface of the plate?

Oh! that is neglected end affect are neglected. He is telling that end surface of the plate that means 100 mm into 1 mm that cross sectional area, very good. That is neglected. Good question. That is neglected. That is not taken. Very good. By neglecting that means from this exposed faces. This face and this face which has a cross sectional area 100 mm into 1 mm eight times the Tb minus T infinity. Good. No that is neglected. Okay. Any other question?

Now I will show you some other problem.

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Consider a stainless-steel spoon partially immersed in boiling water at 100 degree Celsius slowly you may write it in your own language is time is less so all the words can be written or you can in a kitchen at 30 degree Celsius. Now immediately you compile in your own language 100 degree is the base temperature and 30 degree is the kitchen temperature means surrounding fluid T infinity Tb.

The handle of the spoon has a cross-section of 2 mm x 12 mm, 24 mm square is a and extends 180mm in the air that is the length of the EP from the free surface of water. The soon is

extending 180 mm in the air from the free surface of water that means the length of the fin. If the heat transfer coefficient at the exposed surfaces of the spoon and handle is 20 watt per meter square, K that means in all in languages.

Similarly, compiled h is 20 watt per meter square K, determine the temperature difference across the exposed surface of the spoon handle. That means Tb minus Tl take any assumptions required. So, can you tell me this is a fin problem immediately you compile Tb T infinity, cross sectional area length so what is the boundary condition which formula I will use or which formula I will derive theta is T1 into the power of mx plus into the power of minus mx.

I asked one boundary condition know that 100 degree Celsius is the Tb what is that boundary condition? What does it say? HKFC. Very good, speak loudly KfC that means it is a practical case no insolation is there. Oh god. No insolation is there. This is not very infinitely long end temperature is not given that mean there is conductive heat loss at the end. So, that n negative field as a convective heat loss.

So, KfC you will derive the equation we have to derive the equation and use it and get it done. That's all. So, I am not solving this problem because these are only application for power reason. Now another problem.

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One end of a 0.3m long steel rod $(k=20 \text{ W}/(\text{m} \cdot \text{K}))$ is connected to a wall at 240 °C while the other end is connected to a wall that is maintained at 90 °C. Air is blown across the rod so that a heat transfer coefficient of 17 W/(m²·K) is maintained over the entire surface. If the diameter of the rod is 60 mm and the temperature of the air is 40 °C, what is the net rate of heat loss to the air?

This is one very popular type of problem most of the book has this problem. One end of a 0.3 meter long steel rod 20 watt per meter K this is usually the thermal conductivity of steel is connected to a wall at 240 degree Celsius while the other end is connected is a wall that is maintained at 90 degree Celsius. Air is blown across the rod so that a heat transfer coefficient of 17 watt per meter square K is maintained over the entire surface.

If the diameter of the rod is 60 mm and the temperature of the air is 40 degree Celsius what is the net rate of heat loss to the air? That means fin with 60 mm. These are the representative fin problem. So, before concluding the session a generalized formula coming up my lecture about one dimensional steady heat conduction with generation of heat thermal energy without generation of thermal energy cylindrical, spherical or plain wall.

And also fin with lateral convection can be summed up like that. If you consider a variable area wall and take this as a direction of heat flow x which may be x which may be r whatever may be I am denoting it as x where like heat flux is there which may not be same at all section if heat generation is there we cannot say so. If the lateral convection is there we cannot say so that we have seen.

Now let us consider a case that there is lateral convection. I take an element at a distance x with a thickness delta x and I donate Q x as the heat coming in to this face with the in accordance with this nomenclature x and Q x plus delta x is the heat going out and this wall generate heat which is specified by heat generation per unit volume q G at point which is a function of x in general or may be constant whatever may be.

q G may be a function of x, may be constant, may be a function of (()) (01:02:10) function of x because T is a function of x that means T G may vary with x and T and also there is convective heat transfer as I have shown you Q convection from the lateral surface. Now if I have to write the energy balance then I can write that Q x plus delta x which is coming out from this section is equal to Q x plus q G into the area A x. A x is here which is function of x.

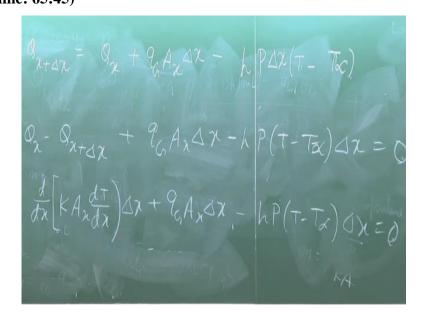
That is why I am writing a x into delta x and at the same time, it continually call this heat just

like just like leaking pipe. It is very similar to fluid flow through a pipe where the surfaces are perforated as the fluid is flowing the water is leaking and ultimately the entire water is drained out at the end, no fluid is coming. No liquid is coming. This type is problem is interesting that from lateral surface the liquid is drained out.

Similarly, the heat is being also convected out minus. Now this convected heat transfer to take care of h, is specified T infinity specified and I use a nomenclature perimeter. So, the P delta is my area and at that location if the temperature is T at x then this will be T minus T infinity. That means Q x plus delta x is qx coming plus this is generating, generational energy minus the convection.

Now Q x plus delta x minus I take it in this side or I take this side that Q x minus Q x plus delta x plus q G S x delta x minus h P into T minus T infinity delta x is zero. Now Q x minus Q x plus delta x we have done several times extending this in delta series and neglecting the higher order term and then substituting the Fourier heat conduction equation Q x is minus k d t, d x. K x a d t d x. Q x plus delta x is Q x plus d d x of delta d x.

That means it will be minus d d x of Q x delta x that is the minus, minus plus that means d by d x of K A x d t by dx delta x plus q G A x delta x minus h P into T minus T infinity delta x is zero. (Refer Slide Time: 65:45)



Or we can write again this thing that d by d x of K A x, dt by dx plus qG Ax minus hP, T minus T infinity is zero and this is precisely the expression for one dimensional heat conduction, with generational of thermal energy and lateral convection heat is going out laterally. Now here in a plane geometry now in cylindrical coordinate x is A r, x is r, cylindrical rod, cylindrical wall axis twice pi rL flowing in the r direction.

In a spherical coordinate x is R and AR will be 4 pi R square. Now if we consider that there is no thermal energy generation this is the fin problem usually fins no thermal energy is generated. If you don't allow the liking of heat laterally I told you stimulation liquid is flowing through a pipe if perforation is there at the surface all liquids will be (()) (01:07:17) that means, there is no lateral convection which we discussed earlier then this plus this is equal to zero and if you take no heat generation this part will be zero.

If we take thermal conductivity constant this will come out and if we take x is constant that is happening only in plane area, plain surface with the same cross-sectional area than the most simple case is d dx or dt dx, zero that means we have a linear temperature profile. So, this expression gives you or if you write this in terms of Qx d dx of Qx then you get the expression for that means another version of this is Q x plus q g A x variable area that means it is the most general expressions.

These two are the same equation in terms of total heat transfer rate in terms of the temperature you can get a generalized expression for heat transfer rate and temperature distribution if any steady one-dimensional flow with or without thermal energy generation, with or without convection from the lateral surface. So, fin is one application of the one-dimensional steady heat conduction problem that that extended surface.

Where one dimensional heat conduction is associated with lateral convection and this is take care of in the simple energy balance. All this thing oh very good. Minus Q a nice, nice very good. Any question? So, with this derivation this is the summery of all my lectures in steady state one dimensional heat conduction. Application is the extended surfaces fin. Any question, ask. The end of the entire conduction chapter we will have one session for tutorial.

Though I have solved number of problems in the class while taking this theory few more problems will be solved, teaching assistance will be there they will solve problems we will there also. Any questions before conclusion I tell you that next class we will discuss two-dimensional steady state heat conduction and that will be taken by Prof. Suman Chakraborty.