

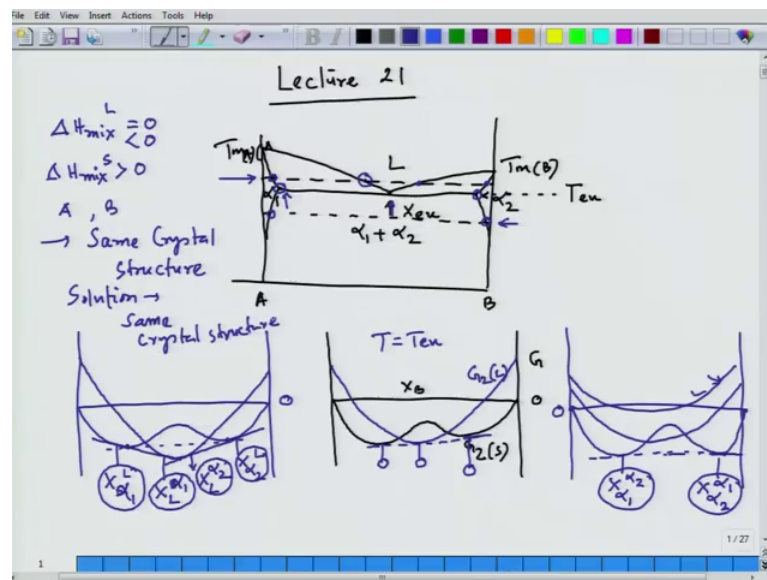
Heat Treatment and Surface Hardening - II
Prof. Kallol Mondal
Prof. Sandeep Sangal
Department of Material Science & Engineering
Indian Institute of Technology, Kanpur

Lecture - 21

Effect of ΔH_{mix} on determination of phase diagrams (same crystal structure)

Let us start lecture 21.

(Refer Slide Time: 00:16)



In our last lecture, we tried to draw an eutectic phase diagram. And that time our condition was that binary system E and B the constituents of that binary system have the same crystal structure. And in the solid state after forming the solution they have the same crystal structure in case of solution. And we tried to consider the situation when enthalpy of mixing for the liquid solution is negative or 0.

And, another case when enthalpy of mixing for solid solution is greater than 0, so because solid solution enthalpy of mixing is greater than 0; so we have experience of phase separation. So, we tried to see this is my eutectic phase diagram. This is my eutectic phase diagram. Where this is liquid this is alpha 1. This is alpha 2. And this is alpha 1 plus alpha 2 and this alpha 1 and alpha 2 both are the same crystal structure and this is my eutectic composition this is X_0 eutectic. And this temperature is $T_{eutectic}$; that means, eutectic temperature this side is A and this side is B pure side this is TMA.

This is TMA. Now we drew free energy composition diagrams at 3 different temperatures, one temperature was chosen this one another temperature was chosen this one. And the third temperature was the eutectic temperature. And we saw a situation that is the locally there equilibrium between different phases.

So, first thing if I try to see free energy composition diagram for a system where for the system is at temperature T eutectic. So, T eutectic both the pure states are in solid condition, but if those are of they are at solid condition then the solid line would be if I try to see this is a reference value which is 0, this is G access this is X B and there liquid would be because in the pure side the liquid would be higher free energy than compared to the solids free energy this is G_2 solid. If I try to draw free energy of liquid this is my free energy of liquid this is G_2 liquid. And now I have a common tangent at this at the compositions.

So, this composition this composition corresponds to this, this composition corresponds to eutectic composition. And this one indicates the composition on the B reach side. And this temperature is basically T eutectic. Now at higher than melting temperature we had a free energy composition diagram this is arbitrary 0 value here also if the temperature is higher than T eutectic; that means, the temperature why I am considering this. So, that case also on the pure site solid free energy should be lowered then the liquid free energy because pure side already it has from solid.

So, it will be again the similar pattern, liquid free energy line will be lower than the equilibrium free energy line; that means, the common tangent between this point and this point and the liquid free energy should be lower than that. So, that is what we have 2 phase common tangent this is X solid in equilibrium with liquid this is X liquid in equilibrium with solid. Now here I have considered I have considered α . So, let me put it at α_1 , this is α_1 and this composition would be X liquid α_2 and this is X α_2 liquid. It means that this is the composition of α_2 of solid solution in equilibrium with liquid. So, if I see that those 4, 4 points. So, this the point which is nothing but X of α_1 .

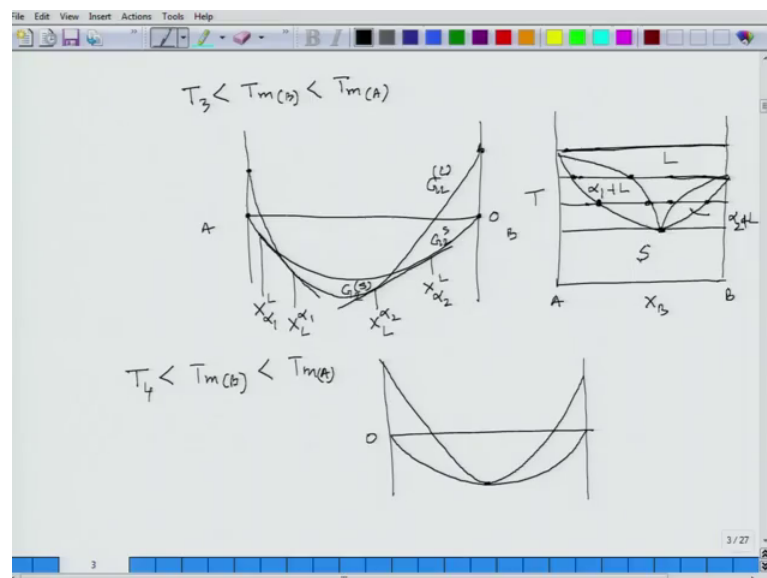
This point is in equilibrium with α_1 . And this composition is the liquid composition this is the liquid composition again in equilibrium with α_2 . And this is the composition which is this one in equilibrium with liquid. And we had another

consideration which is the temperature this one which is below T_{eutectic} . So, that time again of solid would have a lower free energy, and if I take this as a reference value now again this would be having a plot like this. So, this point and this point would go and meet 0 point, but the liquid line would be above this common tangent between 2 solid phases. So, this is X_{α_1} in equilibrium with α_2 . This is X_{α_2} in equilibrium with α_1 , but the liquid line either it could be here or it could be here.

But it would be above that these 2 this common tangent line. So, we cannot have liquid phase as a stable phase. So, depending on the temperature, if that temperature is such that the liquid line goes up to a great extent and it can be temperature could be such that the liquid line could be little lower than that than this, but it should be above this common tangent line this common tangent line. So, that case we have to concentrations which are in equilibrium. This is nothing but this composition and this composition is nothing but these compositions. So, we had an eutectic phase diagram, where our conditions was condition were Δh_{mix} of liquid either it could be 0 considered as 0. Or it could be considered as less than 0 or Δh_{mix} solid another case is greater than 0.

But, since we have a continuous solid solution line here crystal structure of A and B same crystal structures, same crystal structure. And the solution also has the same crystal structure solution. Or the alloy has got the same crystal structure. So, this is one situation, we have talked about.

(Refer Slide Time: 09:15)



Now we have to get into another situation where my conditions are Δh_{mix} of liquid is very low and highly negative; that means, what does it mean if I try to see the construction of ΔG_{mix} , this is my $-\Delta S_{\text{mix}}$. And since Δh_{mix} of liquid is very low; that means, very negative very much negative.

So, it might have very steep this is Δh_{mix} of liquid. So, now, ΔG_{mix} would be just addition of these 2 and this would have a very deep ΔG_{mix} . And accordingly if I try to see what happens to the ΔG_2 ; that means, this is G_1 I know this is pure A G_0 . So, if I try to see G_2 for that particular liquid phase then G_2 would be having very steep situation this is the G_2 . Now if Δh_{mix} of liquid is negative, but not highly negative the only difference would be in the Δh_{mix} thing. So, if I try to plot Δh_{mix} of liquid lower negative. So, this would be this $-\Delta S_{\text{mix}}$ would change. So, ΔG_{mix} would have a lesser dip and then G_2 also would have lesser dip.

So, this is G_2 when this condition is Δh_{mix} of liquid is less than 0. And in this case in this case it is Δh_{mix} of liquid less than less than 0. So, now, these situation when it arises then we have a much deeper G_2 . And another situation could be Δh_{mix} of solid is equal to 0. So, automatically according to this explanation G_2 of solid solution would have less steeper G_2 . Now, let us say I consider a situation T which is greater than T_m of a greater than T_m of b; that means, the melting point of a is higher than melting point of B, means when a cool down from a temperature which is beyond the melting point of A, and has we cool down the first solid phase that would appear is basically the pure A.

Now, if the temperature is greater than T_{MA} and greater than T_{MB} . So, everything would be liquid for the entire composition range. So, our composition free energy composition plot, if I try to plot this is my arbitrary 0 value this is the reference value and then solid liquid. I can say that this is pure liquid pure liquid A and pure liquid B. So, this is my liquid line G_2 which is G_2 liquid which is very steep and solid line should have appeared higher than this because at that temperature, I cannot have any solid. So, solid line would be like this this is G_2 of solid. Now this is G this is X B. So, now, second situation T is T_{MA} , T_{MB} then the temperature is such that the pure A side I would always get a phase pure A solid and on the B side I must get pure B in the form of liquid.

So, if I try to draw this free energy composition diagram this is arbitrary 0 reference on the a reach side or a side pure A pure A should be solid if I considered to be 0. Then the

liquid should be above that because the temperature is such that, this is lower than the temperature melting point of a. So, the a should appear in the pure condition and where as on the B reach side since the temperature is beyond the melting point is greater than the melting point of B. So, there the liquid would be the several stable conditions. So, the liquid line, I can draw it like this whereas, the solid line on the right side this is pure B side B reach side solid must have higher free energy because then only B can appear as a liquid.

So, this is G 2 liquid this is my situation, this is G 2 solid. So, now, I have a common tangent here. So, this is composition X alpha with liquid in equilibrium with liquid and this is X liquid in equilibrium with alpha. Now third condition I can have which is T less than TMB less than TMA so; that means, on both pure A and pure B side I must get solid pure solid of both the components both the elements. So, that time if I arbitrarily draw that particular situation this is 0 it is a reference point. Now this is let us say I start with pure solid because I must get pure solid when T is less than TMA this is a reach and this is B reach. So, the solid will start here and similar on the right side also I must get solid B because the temperature is less than TMB. So, the B also would solidify in the pure condition.

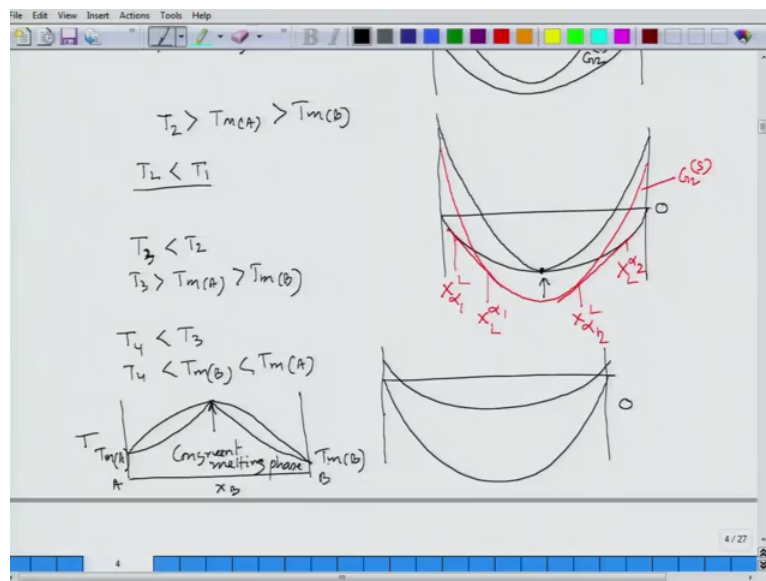
So, now solid line is like this. So, on the pure side liquid lines are like this. So, G 2 this this is G 2 solid since the liquid has got a very steave G 2 line. So, so this G 2 liquid and this is G 2 solid. So, if I see the equilibrium condition, I have this equilibrium at the same time I can have one more equilibrium like this. Now this composition is X alpha in equilibrium with liquid this is X if I considered to be alpha 1 because on the both the sides I am I am getting alpha phase because the free energy line is continuous and they have the same crystal structure. So, this is, but in order to distinguish between to those 2 solids because these 2 solids have different a content and different B content one is a reach another one is B reach. So, that time I can put it as X alpha 2 in equilibrium with liquid and this is X liquid in equilibrium with alpha 2, and this is X liquid in equilibrium with alpha 1.

And now if we go down further the temperature is such which is still TMB is less than TMA I can have a situation the free energy situation free energy line, this is my solid line this is 0 arbitrary reference whether liquid line can just touch at this point. So, now, if I put all these compositions whatever we have drawn. Till now 4 temperatures this is let us

let us go back to this this is temperature, one this is temperature 2. This is temperature 3 and this is temperature 4, if I try to draw there this is X B. This is A this is B pure side. Now I would get a if I try to plot all those temperatures with this temperatures, I just draw 4 temperatures. And here I get this 2 points and then I get these 2 points.

First one is I do not get any points. There actually I do not get any points there because every time it is a liquid stable. So, here I get 2 and I do not get anything, but here I get this this and this 4 points. And finally, I get this. So, if I try to do it complete we would get a plot like this. So, this is liquid this is temperature this is alpha 1 plus liquid this region is alpha 2 plus liquid. And this is solved which is alpha. So, I am getting a situation when I am having you see, because the liquid free energy line is G 2 line is very steep that is what I could get the liquid stability at a very low temperature. Now this situation becomes opposite if I consider.

(Refer Slide Time: 20:32)



Del h mix of solid to be less than less than 0, and del h mix of liquid is either 0 or less than 0.

So, that situation, I would request you to just solve this you can get help from the thermodynamics book of casele. So, there the phase diagram would look like. So, this will be my liquid this will be my solid this is alpha 1 plus liquid. This is alpha 2 plus liquid this is X B, this is temperature and that time I am getting point which has the maximum that solid has the maximum melting point. It is called congruent phase now in

case of a system, where now the situation would be reverse if we consider this conditions. The solid ΔH_{mix} is very negative highly negative, whereas, ΔH_{mix} of liquid is either 0 or slightly negative that time I would have much steeper free energy line for solid solution, but less steeper free energy line for the liquid solution.

So, once a situation would be let us say the temperature is vary is basically higher than T_{MA} and higher than T_{MB} . That time, I would have a free energy plot if I consider this is might arbitrary 0 value, then for the entire composition range the solution would be liquid. This would be G_2 of liquid, but since ΔH_{mix} of solid is highly negative. So, G_2 which is G_1 plus ΔG_{mix} for solid, which will be very steep. I can have G_2 of solid like this. Now if temperature is such that it is greater than T_{MA} and greater than T_{MB} , this is T_1 . This is T_2 still, but T_2 is less than T_1 that time this liquid line would move off and the solid line would move down. So, then I can have a situation like this. This is arbitrary 0 because both the sides pure A pure B both are liquid because the temperature is such that pure metals such that should be should be in the liquid condition.

So, this is my liquid line, but the solid situation is such the solid is just touching the liquid line this point. So, at this point this composition of solid would appear in equilibrium with the liquid. Now if I decrease this temperature further T_3 is less than T_2 , but T_3 is greater than T_{MA} greater than T_{MB} , that time I could have a situation like this on the same diagram situation could be like this. So, that time this is G_2 of solid. And then I would have 2 phase 2 equilibrium common tangent. So, this is be my $X_{\alpha 1}$ in equilibrium with liquid this is X_{liquid} in equilibrium with let us say the on the other side B reach side I considered α_2 . So, this is α_2 this should be my X_{liquid} α_1 this composition would be $X_{\alpha 1}$ liquid.

And finally, I would get a situation I will get a situation T_4 less than T_3 , but T_4 is less than T_{MA} less than T_{MB} , T_{MB} less than T_{MA} . That case I would have a situation like this, this I can do it here. So, solid line would be steep and the liquid line would go like this. So, that case everything would be solid and my phase diagram would look like because T B side, this is a side this is T_{MA} this is T_{MB} . So, I would get a comp a phase diagram like this and this point is called congruent melting phase.

So, let us stop here. We will continue our discussion in our next lecture.

Thank you.