

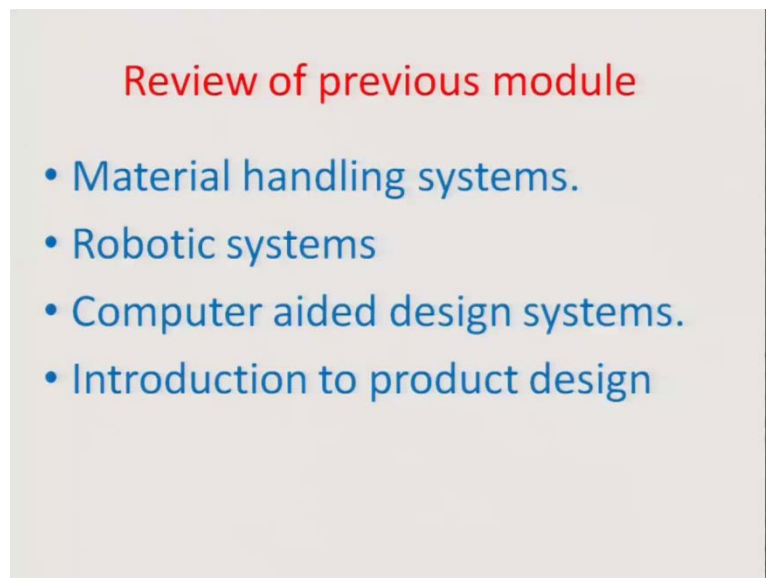
Manufacturing Systems Technology
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Module - 01

Lecture-04

Welcome to this module 4 on Manufacturing Systems Technology, a brief recap of what we did in the last module.

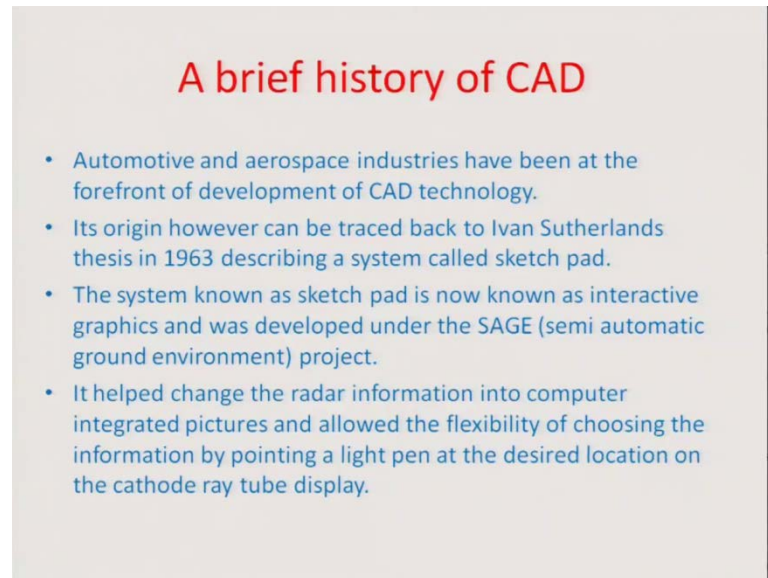
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We talked about certain material handling systems, particularly automated material handling systems of, which rang very well of the modern manufacturing processes. We also discussed certain robotics systems and how the field of robotics has emerged and in fact, details are reserved for later on module. And then, we started discussing about the introduction to product design process, which is a six step process, where we particularly discussed about, what would be the aspirations when you want to design, let us say a notebook type computer, something like that.

And then, in context of that we also made a mention of computer aided design systems, which would be helping to generate more of visualization, more of clarity in the thoughts along the design refinement processes of a product.

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A brief history of CAD

- Automotive and aerospace industries have been at the forefront of development of CAD technology.
- Its origin however can be traced back to Ivan Sutherlands thesis in 1963 describing a system called sketch pad.
- The system known as sketch pad is now known as interactive graphics and was developed under the SAGE (semi automatic ground environment) project.
- It helped change the radar information into computer integrated pictures and allowed the flexibility of choosing the information by pointing a light pen at the desired location on the cathode ray tube display.

Now, if you look at a brief history of how the computer aided design has emerged, in fact, the CAD technology has been necessitated more, because of the automotive and the aerospace industries. These are the mostly sort of, you know the heaviest users you would say of, so called computer aided design technology. And if you really look at how CAD had evolved the basic foot step in the area of computer aided designing was, if you look at the you know the history there is a very famous thesis by Ivan Sutherland in 1963, which talks about the basic sketch pad.

So, the sketch pad is now known as the interactive graphics, which was developed under the SAGE project, which is Semi Automatic Ground Environment project. And the idea was that if you have a radar map coming out of an aerospace or a airplane, can I actually pinpoint to a small zone of the map and blow it up do all the kind of translations, which could be there. So, that I could actually a certain target, that we would have from that radar map clearly pointed out on the screen.

So, if it is about a pen, an interactive infrared pen, which would actually touch up on the various areas of the screens and would create impressions within such a radar

map. So, this was the historically the first step towards, what you know as the modern day computer aided design process.

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CAD/CAM systems

- A wide variety of CAD/CAM systems are currently available.
- Essentially a CAD system comprises of three major components: Hardware, which includes computer and input/output devices, application software, and the operating system software.
- The operating system software act as the interface between the hardware and the CAD application software system.

FIGURE 2.2 Architecture of a CAD system.

- The classification scheme we use in this section is based on hardware of the system.
- More specifically, we classify systems by the host computer that drives the system.
- Generally, CAD/CAM systems are classified into four types:
 1. Mainframe Based systems
 2. Minicomputer based systems
 3. Workstation based systems
 4. Microcomputer based systems

And ever since then, the variety of CAD/CAM systems have evolved, currently there are wide variety of such systems. And if you look at really, what are the different components of such CAD systems so; obviously, the three major components are the hardware, which is the tool which does the computation, the backend computation behind the visual display, the magnificent visual display that you are seeing at the front end and it includes computer input output devices and application software's and operating system software's.

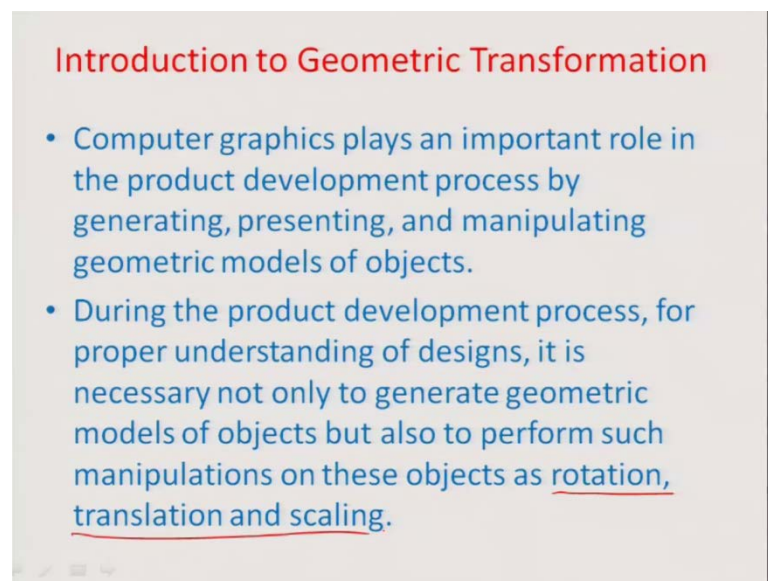
So, these are the major components of any computer aided design system and you can see here for example, in this sketch that there is a database, which the CAD starts with, where the CAD model is really stored or it can be modified or it can be uploaded. The operating system completes sort of, it comprises application software. The graphics utility, the device drivers, which would be able to sort of communicate with a variety of input output devices. Output devices could be something like printers or plotters or whatever you have plotted on a CAD package can be printed successfully.

The input devices can be something, where from which you can machine read the CAD data from a storage unit, you know. Something like a, let us say hard drive or something, where there is a temporary storage, which can be directly mapped etcetera. And;

obviously, there has to be a user interface, which would be able to define the menu in the various modalities of the CAD and try to also make a new design etcetera through this user interface.

So, currently the CAD/CAM systems are now classified into four main types. One is called the mainframe based system, the mini computer based, the work station based and also finally, the micro computer based system. So, the main important aspect here that a person from a technology background should know is that, behind all these so-called visualizations, there is a huge amount of geometrical transformation based calculations, which are being computed by the computer every second and you need to know about such transformations and how geometrically you can manipulate an object. So, that you can magnify it, rotate it, translate it, soon and so forth.

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Introduction to Geometric Transformation

- Computer graphics plays an important role in the product development process by generating, presenting, and manipulating geometric models of objects.
- During the product development process, for proper understanding of designs, it is necessary not only to generate geometric models of objects but also to perform such manipulations on these objects as rotation, translation and scaling.

So, let us look at some of those geometrical transformations and; obviously, the need for translation or transformation is to sort of calculate, when you perform a certain function on the object in question such as rotation, translation, scaling, soon and so forth.

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Introduction to Geometric transformation

- Essentially, computer graphics is concerned with generating, presenting and manipulating models of an object and its different views using computer hardware, software and graphic devices.
- Usually the numerical data generated by a computer at very high speeds is hard to interpret unless one represents the data in graphic format and it is even better if the graphic can be manipulated to be viewed from different sides, enlarged or reduced in size.
- Geometric transformation is one of the basic techniques that is used to accomplish these graphic functions involving scale change, translation to another location or rotating it by a certain angle to get a better view of it.

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Geometric Transformation

- Two dimensional transformation:

Translation: In 2D translation, we can determine the new position of the points in the x-y plane by adding the translation amount to the initial coordinates of the points.

Mathematically, we can write for each point $V(x, y)$ to be moved to the new point $V'(x', y')$ by d_x & d_y units parallel to the x & y-axes as follows:
 $x' = x + d_x$ & $y' = y + d_y$

If we define the points and the distance in column vector form
 $V' = \begin{bmatrix} x' \\ y' \end{bmatrix}$ $V = \begin{bmatrix} x \\ y \end{bmatrix}$ $D = \begin{bmatrix} d_x \\ d_y \end{bmatrix}$
we will have
 $V' = V + D$ where
 $V' \rightarrow$ new variable point vector of the object
 $V \rightarrow$ Original variable point vector of the object
 $D \rightarrow$ distance vector

$V' = V + D$
$$= \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} d_x \\ d_y \end{bmatrix} = \begin{bmatrix} x + d_x = x' \\ y + d_y = y' \end{bmatrix}$$

And let us look at independently now, some of the things related to let say two dimensional translation, that we are talking about, let us say a point in space, which has, which is in the xy coordinate system. So, you have one x value and one y value and we typically call this plane with a x and y axis as a two dimensional plane and there is a point, which is there on the two dimensional plane, which we want to translate. And we want to see if there exists some kind of a universal way by which, we can do this translation, which is easy for a computer system to understand.

So, at the outside I would like to tell you that you know all the data management inside a computer system is becomes easier automatically, when you can identify the location of the data in a big tabular kind of manner. So, you can give the row number and the column number for that particular data and it is very easy for a computer to identify and read that data, once the row number and column number is specified and also it is specified that how to approach that row number and column number.

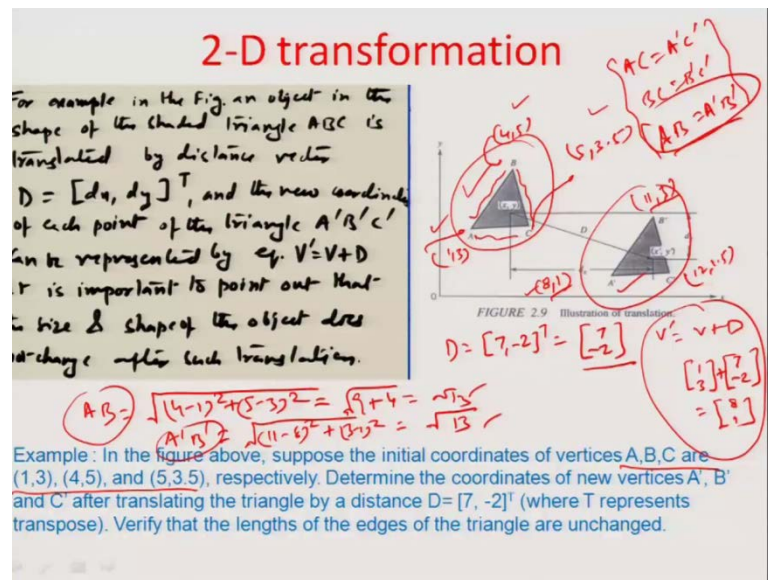
And the best way to handle such system is by giving matrices, where you would actually have all the data packaged in forms of matrices etcetera. And therefore, we would like to emerge a system, where such row number column number based classification is universal across all the different geometrical transformation processes that we would like to look at. So, let us say in this two dimensional translation there is a point which it is you know mathematically defined as v_{xy} .

So, this is that point, where you have a x and y coordinate and you want to move this to a new point $v'_{x' y'}$. And further you know that in a two dimensional coordinate plane like this x and y from the point v , which comprises x and y you are moving exactly a certain distance in the x direction and a certain distance in the y direction, let us say dx distance and dy distance. So, that finally, you are this point x' y' ; obviously, x' is equal to x plus dx and y' is equal to y plus dy .

So, the way to write this whole you know transformation and now linearly transforming this point from v to v' by taking this point literally from v to v' whereas, x' y' are the new coordinates and x , y were the old coordinates. So, you can actually write it in matrix form as v' , which is a matrix x' y' equal to a matrix v , which is xy and plus a matrix d , which is the distance matrix, which is dx plus dy .

Obviously, what it would rule is that $v' = v + d$ means there it is equal to xy plus a matrix dx, dy , which would be x plus dx and y plus dy , which is actually nothing but, x' and y' as was being seen here. So, that is how we actually geometrically transform a certain point from one place to another on a two dimensional plane.

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So, can we do the same thing for a three dimensional figure is the major question for example, two dimensional figure for example, let us say instead of one point now we have a triangle, which are defined by three points and interconnected through three different lines and we want to move out this triangle as is from point A, B, C to the point A dash B dash C dash and we want to see whether the linear transformation that has been applied earlier holds true in this particular case.

So, let us say in this particular figure here you have coordinate x of points A, B and C defines as 1, 3. So, that is the coordinate of A. 4.5 that is the coordinate of B and 0.5, 3.5; that is the coordinate of C. And now, you are basically translating this triangle to the position A dash B dash C dash by a distance matrix, which is actually 7 minus 2 trans; obviously, it means that you can write it as a transformed matrix 7 minus 2 like this.

So, the point A dash as per the equation $v + d = v'$ becomes equal to 8 and 1. Obviously, the v for the point A becomes the location coordinate 1, 3 and the distance transpose matrix becomes 7 minus 2, so this becomes 8 and 1, which I have written it here. And in a similar capacity we can write the d dash as 11, 3 and the C dash as 12 and 1.5. So, we can actually look at all these coordinates and see for example, on the lens side of BC or AC and in this transformation was true if you assume that this transformation is true, then the lens AC should be equal to A dash C dash BC should be equal to B dash C dash and AB should be equal to A dash B dash.

In other words, even though there is a linear transformation the triangle will not change in shape or size all the sides are going to be in the similar length domain. So, let us look at that aspect here for example, if I wanted to calculate the length AB here this would actually result in 4 minus 1 square plus 5 minus 3 square, which is actually equal to 9 plus 4 root, which is root of 13. If I look at A dash B dash and take the new coordinates 8, 1 and 11, 3 we also have the same root of 11 minus 8 square plus 3 minus 1 square, which is root of 13 again.

So, therefore, the lengths are really not changing and therefore, there is no change in scale and the triangle is being linearly moved from place 1 to place 2 just by following the simple $v \text{ dash equal to } v \text{ plus } d$ transformation matrix.

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2-D transformation

- **Scaling**

Scaling in 2D means stretching the points in the x-y plane. It can be accomplished by simple multiplications as follows:

$$\begin{matrix} x' = S_x \cdot x \\ y' = S_y \cdot y \end{matrix}$$

where S_x & S_y represent the scaling coefficients in the x- and y-directions respectively. Scaling can be expressed in vector form as

$$\begin{matrix} x' = S_x \cdot x \\ y' = S_y \cdot y \end{matrix}$$

where S_x & S_y are scaling coefficients in x & y directions

Scaling can be expressed in vector form as

$$v' = [S] v \quad \text{or} \quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} S_x & 0 \\ 0 & S_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

where v' = new variable point vector of the object
 v = original variable point vector of the object
 $[S]$ = scaling coefficient matrix
 The object changes in both size & position when $S_x = S_y$, it is called uniform scaling; otherwise it is differential scaling.

Example: From the figure on the right, show that the length of the edge A'B' is equal to three times that of AB after scaling the object uniformly by factor 3.

FIGURE: Scaling of an object

You can look at all the different other lengths for example, BC comes out to be 3.25B dash C dash comes out to be 3.25 CA and C dash D dash comes out to be 16.25 and 16.25, which means that the transformation is working uniformly for a homogenous transformation of a point on a two dimensional plane. Let us talk about scaling a little bit, so if we wanted to scale an object or scale a particular structure to two times or three times the size, what is the modality which is involved in that.

So, let us say again we compare a two dimensional plane, where there is a certain orbit structure, where you want to magnify that structure into a 3 times or 4 times larger object again on the same two dimensional plane. So, it can be accomplished by simple

multiplications and the transformation matrix that can be used is that if there is a point x on, let us say a point v in certain two dimensional plane and you want to magnify it and transfer to another point x' y' point means that you know it cannot really magnify a point.

But, you can magnify an array of points an array of points can be something like, let us say this pentagon here, which talks about a length AB for example, in the lower base and if you magnify this by 5 times the idea is this length A' B' , which is a spacing between these two points should be exactly five times the value of the AB that we are considering here. So, here for example, x' and y' the new coordinate systems can be envisioned as $s_x x$ and $s_y y$, where s_x and s_y represents the scaling coefficients in the x and y directions respectively and scaling can be expressed in the form of x' is equal to $s_x x$ and y' equal to $s_y y$.

So; obviously, if I wanted to represent in terms of a simpler matrix I would write v' to be equal to some matrix s times of v where this s can be represented as s_x is 0. Now, this is no longer you know a one cross two matrix it is actually a two cross two matrix, which emerges, which we talk about s_x 0 and 0 s_y and x and y , let us look at if we do the product between these two matrices whether we are able to get the x' and y' we already know that the x' and y' is actually represented here as $s_x x$ and $s_y y$ at this particular zone here.

So, if I just product or if I just do the multiplication between these two matrices there would be an emergence of this x' and y' the first term would be $s_x x$ plus 0 times y and; obviously, the second term would be 0 x plus s_y times of y . So, if we finally, calculate it is s_x times of x and s_y times of y that we are considering to be x' and y' as is represented here.

So, therefore, we can see that the whole point you know v' is not to be $s_x x$ and $s_y y$ as predicted here in the earlier transformation through this matrix method. Now, you just look at this example here that there is a length AB , which needs to be magnified to A' B' and whether the same you know theory can be applied to these two points, so that the scaling of this line can be exactly three times. So, suppose you wanted we have coordinates of point A here as A_1 , B_1 and the coordinates of point B as A_2 , B_2 and we wanted to map this to three times scaling as three here.

Obviously, from the expression, which is given here magnification factor x would be the new coordinate. So, we have $3A_1$ and $3B_1$ as the new coordinates of A dash and similarly, $3A_2$ and $3B_2$ as the new coordinate of B dash. So, you can see here that the length AB is exactly equal to one third of the length A dash B dash you know if I calculate the length A dash B dash here, which is three times of A_1 minus three times of B_1 whole square plus A_2 whole square plus three times of B_1 minus 3 times of B_2 whole square whole under the root this becomes exactly three times of A_1 minus A_2 square plus B_1 minus B_2 square.

And the length AB was earlier represented as A_1 minus A_2 square plus B_1 minus B_2 square whole under the root. Therefore, this exactly AB length is a third of the a dash b dash length which is given in this calculation here. So, this is how you can see that even if you are magnifying an object by three times and you put the geometrical transformation simple $s_x x$ and $s_x y$ as the magnification factor times the coordinate the overall length is getting changed by almost three times, because of that magnification.

So, in the next module we would also like to study rotation of an object and then finally, translation and then, we would like to do a very complex geometrical transformation on the three dimensional plane of an object.

Thank you