

Customer Relationship Management
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Lecture - 19
Economics of CRM (Contd.)

Hello everybody. Welcome to the NPTEL Swayam course on Customer Relationship Management. We are in Week-3 and we are discussing customer lifetime value. In this today's class we will discuss about the mathematics part of Customer Lifetime Value. So, we have discussed till now about the excel part of customer lifetime value how excel modeling can be done with customer lifetime value.

But sometimes these problems are much simpler sometimes these problems are not cumbersome or lots of assumptions that you can generate from the data. That kind of assumptions you do not have in your hand sometimes because not always marketing manager will have an access of data in a minute level.

Now, if you do not have the access of a data in the minute level the question comes up is that how I can have few basic information from which I can calculate customer lifetime value of a customer. Now, if I can calculate that, if I have the ability to calculate that — individual level or a group level then I can take multiple marketing decisions based on that.

For example, I can find out that who are my more profitable customers, who are my less profitable customers, how what are the patterns that these more profitable customers are showing, what kind of purchase — products or services that they like, what kind of prices that they like and then I can make my product or service design according to that.

And at the same time, I can also find out that who are my not so profitable customers; and if I can find out who are my not so profitable customers, I can also find out that how to tackle them, how to make sure that they do not clog my resources because if they can clog my resources then there is a problem. Otherwise what I can do is I can attract them, I can give coupons, I can give certain kind of incentives.

So, that they can come in such kind of positions they ask for service or they come for product purchasing some kind of time when my system my resources are less I would say less engaged. For an example, if you know that there are various retail companies.

Let's say grocery company Big Bazaar for example, gives a Wednesday where it is a it is a everyday like Walmart goes for everyday low cost Big bazaar low gives certain kind of discounts on Wednesdays. Now why Wednesday?

So, first of all they wanted to pick up a date day where it will be known for that particular day that, in that this particular day Big Bazaar is giving certain kind of discounts that is number 1. Number 2 is for Big Bazaar, they know the people who are coming in the probably weekdays and in the afternoons of the weekdays are generally those people who don't work, because in weekdays if you have work you will go for job.

So, those who don't work probably are not so profitable customers for them. Now, if these groups of people come on the weekends, then my shop floors will be very I would say congested. And if my shop floors are congested I my actual profitable customers might not prefer to come to me they might go to somewhere else, because shopping is also an experience.

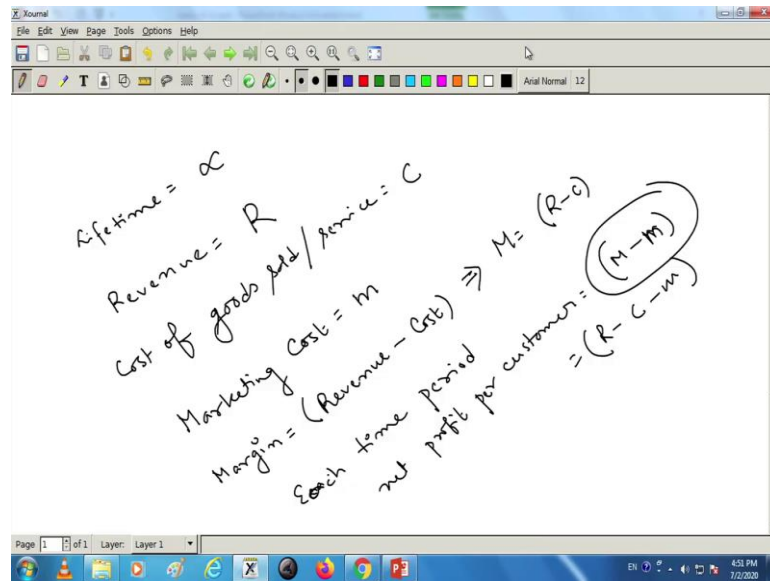
Now, if that is the situation then the Big Bazaar has to do something so, that they can attract this group of customer, who are not as profitable as the actual weekend buyers. Also they don't want to lose this particular customer. So, they don't want to push the price high such that they lose these customers who are not working.

But they also want to keep them but at the same time they don't want them to clog in a certain days or certain dates when other kind of profitable customers' foot fall is expected. So, they give this kind of discounts in the weekdays.

So, everybody will come on the, on Wednesday, then not Thursday not Tuesday, Monday or Friday, Wednesday, which is absolutely the middle of the week. So, you come in the middle of the week and you purchase and you get discounts.

So, these kind of things comes from customer lifetime value unless and until you can calculate customer lifetime value at a personal individual level this becomes a problem. So, in this particular video we will talk about the CLV formula, how the CLV formula was created. So, let me come to this. So, CLV formula comes from the lifetime.

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Now, here I am assuming that the lifetime is basically infinite. So, it's as long as possible lifetime and let's say the revenue that you make is R , the cost of goods sold is a cost of service — cost of goods sold or service is C let's say.

Let's say, along with that the customer also gives you, the company also gives you certain marketing and that marketing cost. So, some kind of advertisement cost, and when we I calculate that marketing cost, at a per customer basis individual customer's marketing cost I can calculate, that comes up to be let's say, let's say something I will write that m or small m okay. And the margin from each purchase then is basically revenue minus cost or this gives me basically: M is equal to R minus C [$M = R - C$.]

Now, these are some simple values that you can get from the, from my past data very easily like per customer revenue, I if I have 5 customer. Let's say in my database I have 5 customers; customer 1, customer 2, customer 3, customer 4, customer 5.

I then take the average of these 5 customers to say that, this is my average revenue which is capital R . Similarly let's say each customer has certain kind of cost like some customer in a, in case of cost of goods sold the cost is fixed, but if it is a service for some customer the cost will be a little bit higher. For some customer the cost will be a little bit lower. So, I can take an average of that also and that becomes my C .

So, then average margin minus average cost becomes my basically sorry average revenue minus average cost becomes my margin. So, that is M is equal to R minus C . And also let's say if I have 100 customers in total and my total marketing cost is something that by 100, that divided by 100 will be my marketing cost per customer. Each customer gets that marketing cost that is his share. So, that is small m and this is the recurring cost every year I do this marketing cost. So, I send certain emails I arrange certain kind of I certain kind of events for the customers. I do some marketing promotion activities. Now, whatever I do it's a bulk cost that bulk capital cost is actually shared by multiple customers. So, that is something that I have right now.

So, then, for each time period; each time period how much is my total net profit per customer? Net profit per customer is capital M by small m [M/m], which is also, can be written as R minus C minus m [$R-C-m$]. So, we will use this capital M minus small m , the margin that you generate minus the marketing cost the per unit marketing cost that you generate. So, this is the money that I gain if the customer stays for 1 year.

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Cost of Marketing Cost = (Revenue - Cost)

Margin = (R - C - m)

Each time period net profit per customer = (R - C - m)

retention rate = r

| y_0 | y_1 | y_2 | y_3 | y_4 | ... |
|-----------|-----------|------------|------------|------------|-----|
| $(M-m)$ | $r(M-m)$ | $r^2(M-m)$ | $r^3(M-m)$ | $r^4(M-m)$ | ... |
| $(1+i)^0$ | $(1+i)^1$ | $(1+i)^2$ | $(1+i)^3$ | $(1+i)^4$ | ... |

So, let's calculate this year 0, year 1, year 2, year 3, year 4 and so on ok. So, if I if the customer stays with me in year 0, how much is the money that I generate? This is capital M minus small m [$M-m$]. I will just delete this, capital M minus small m , fair enough. Now, if he stays in the next year also then what is the amount that I gain?

So, let's say, the retention rate is r . Retention rate is r means that this is the number of people if 1 customer stays, 1 customer stays with me in year 0. Then in year 1 basically r customers will stay, in year 2 r^2 customers will stay, in year 3 r^3 customer will stay.

So, the probability the net money that I can generate here is basically M minus m into r for year 1 [$r(M-m)$]. Let's make it a little bit, for year 1 this is like this. For year 2 out of this r another r will stay. So, M minus m r^2 [$r^2(M-m)$]. In year 3 r^3 into M minus m [$r^3(M-m)$], in year 4 r to the power 4 into M minus m [$r^4(M-m)$], and so on.

So, that is how the money that I will I that I will gain will be calculated. So, if let's say 100 customer stays in the first, then r 100 into r that many customers will stay in year 1, 100 into r into r further another multiplication of r will stay in year 2.

And r^3 into M minus m will stay in year 3 and r to the power 4 into M minus m will stay in year 4 and. So, on now this is the money that I will gain over time. So, the summation of all of these things will be the money that I gain over time. But what happens is there is something called discount rate an interest rate or a discount rate these two things are generally which is which is also called sometimes the time value of money.

How much is the value of money 100 rupees, which you can gain 1 year later what is the today's value of that? So, let's say it is like if you put 100 rupees in the bank and the interest rate is let's say a 10% then in the 1 year later you will get 110 rupees right. Then that means, what that if you whatever you get after 1 year, 110 rupees the current days value of that money is 100 rupees.

Because if I, if you forego 100 rupees now you will get a 110 rupees later. So, then current day is value is 100, 100 rupees then. So, that 10 rupees that you are getting in percentage is basically the time value of money. So, then what then if you get 110 how I will convert that to 100?

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today value $\times (1+i) =$ value one year later

today's value = $\frac{\text{value one year later}}{(1+i)}$

today's value = $\frac{\text{value } t\text{-year's later}}{(1+i)^t}$

$i =$ yearly interest rate

You will say that the time value of money will be today's value, today's value into 1 plus i, where i is the interest rate let's say today's value into 1 plus i is equal to tomorrow's value or 1 year later value not tomorrow basically 1 year.

Because i is always defined in a so value 1 year later, where i is the yearly interest rate where i is the yearly rate. So, this is I can say today's value will be, then what will be that today's value of something that I get later today's value of something that I get later: value 1 year later divided by 1 plus i, that will be today's value. Similarly today's value you can do a little bit of calculation.

And you can say that today's value is equal to value let's say 5 years later divided by 1 plus i to the power 5 $[1 + i^5]$ or in other words if it is t years later, then 1 plus i to the power t $[1 + i^t]$. So, that is what I get. So, if I use this particular formula; if I use this particular formula, then how much is today's value?

Today's value for this 1 is by 1 plus i to the power 0 because that is something that I am getting in this year only. This is by 1 plus i to the power 1, this is 1 plus i square, this is 1 plus i cube and this is 1 plus i to the power 4 and so on. That is what I am getting here. Just check carefully that the 1st year it is 1 plus i to the power 0, in the 2nd year it is 1 plus i to the power of 1, 3rd year.

It is 1 plus i to i square 4th year means corresponding value that of in terms of today's money is this much. So, if I get r squared M minus m in year 2; if I get r square M minus m in year 2 corresponding thing's value in today's market will be this much the denominator divided by 1 plus i square. So, this is what I have got till now, see.

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The image shows a handwritten derivation for Customer Lifetime Value (CLV) in a software application window. The text is written in black ink on a white background. The derivation starts with the equation:

$$\text{today's value} = (M-m) + \frac{(M-m)r}{(1+i)} + \frac{(M-m)r^2}{(1+i)^2} + \frac{(M-m)r^3}{(1+i)^3} + \dots$$

Below this, the CLV is defined as the sum of these terms:

$$\text{CLV} = (M-m) + \frac{(M-m)r}{(1+i)} + \frac{(M-m)r^2}{(1+i)^2} + \frac{(M-m)r^3}{(1+i)^3} + \dots$$

The derivation then shows the factoring of (M-m) and the use of the geometric series formula:

$$= (M-m) \left[1 + \frac{r}{1+i} + \frac{r^2}{(1+i)^2} + \frac{r^3}{(1+i)^3} + \dots \right]$$

The sum of the series is identified as $\frac{1}{1-a}$, where $a = \frac{r}{1+i}$. The final result is:

$$\text{CLV} = (M-m) \frac{1}{1 - \frac{r}{1+i}}$$

Now what will be the CLV then, what will be the customer lifetime value, then? Customer lifetime value is M minus m plus M minus m to the power r by 1 plus i plus M minus m to the power r square by 1 plus, basically the summation of all of those values plus M minus m r cube by 1 plus i cube and so on.

And if that is the case I can take M minus m as common 1 by r plus 1 by i plus r square by 1 plus i squared plus r cube by 1 plus i cube and so on. Now, just think r by 1 plus i, what is this value? Is this smaller than 1? See r is the retention rate, the maximum value retention rate can take is 1 everybody is retained right.

So, that numerator can take the maximum value of 1, the minimum value denominator can take is also 1, the minimum value 1 plus i, when the interest rate is 0 the denominator becomes 1. When the interest rest is anything positive, anything positive the denominator becomes higher 1. So, r by 1 plus i that is why this ratio, r divided by 1 plus i, this ratio will be always smaller than 1.

And if it is a infinite series — infinite GP series. With the value of the GP the multiplication factor is smaller than 1, then we know the formula. So, if it is 1 plus a plus a square plus a cube plus a to the power 4 plus dot-dot-dot upto infinite times. The formula is basically 1 by 1 minus a, that is the formula for this one if you remember that is from GP series basic GP series. So, I just write that particular thing as my formula. So, I will just increase.

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The image shows a handwritten derivation of the CLV formula and a numerical example for Netflix. The derivation starts with the formula:

$$CLV = \frac{(M - m)}{(1 - \frac{r}{1+i})}$$

This is then simplified to:

$$= \frac{(M - m)(1+i)}{(1+i - r)}$$

Below the formula, the following values are noted:

- $r = 60\%$
- $i = 5\%$
- 0.05

The numerical example for Netflix is as follows:

- Revenue (Rv.) = \$120
- Margin = 60%
- $m = \$5$
- Net Profit (M) = \$72
- Net Profit (M) = \$48

The final calculation shown is:

$$\frac{67 \times 1.05}{0.45} = ?$$

So, correspondingly if you just check the maths the formula that I got is CLV is equal to capital M minus m divided 1 minus r by 1 plus i. So, if we simplify it we get. So, this is the basic formula that I get now that is that is the basic formula that you will get in any book the i can be written as d discount factor i write interest rate you can write discount factor.

But the other values probably the margin will be named by the notations can be different the nomenclatures can be different, but ultimately this will be the formula. So, where this applies? Let's say Netflix I am giving you an example let's say there is a company called Netflix.

Let's say Netflix, says that our average. So, Netflix has a fixed amount that they charge every month. So, let's say their yearly revenue is around 20 dollars, no they charge how much 500 rupees per month, if I am not wrong. So that means 10 dollars.

So, 120 dollars let's say Netflix is 120 dollars that is their revenue. And they say that our margin basically is 30% or a little bit higher 60% . So, 60% of 120; that means, around

72 dollars is their margin and they do some marketing costs and at this moment of marketing cost is probably higher.

So, they say that our marketing expenditure per customer is 5 dollars; this is what they have told us this information. Now, these are very basic information you can get now they are us, they are trying to find out that, what is their customer lifetime value?

Now, the customer lifetime value i they are getting at this moment market is not good. So, let's say i is equal to 5% and the retention rate is around let's say 60% .

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The screenshot shows a whiteboard with the following handwritten text:

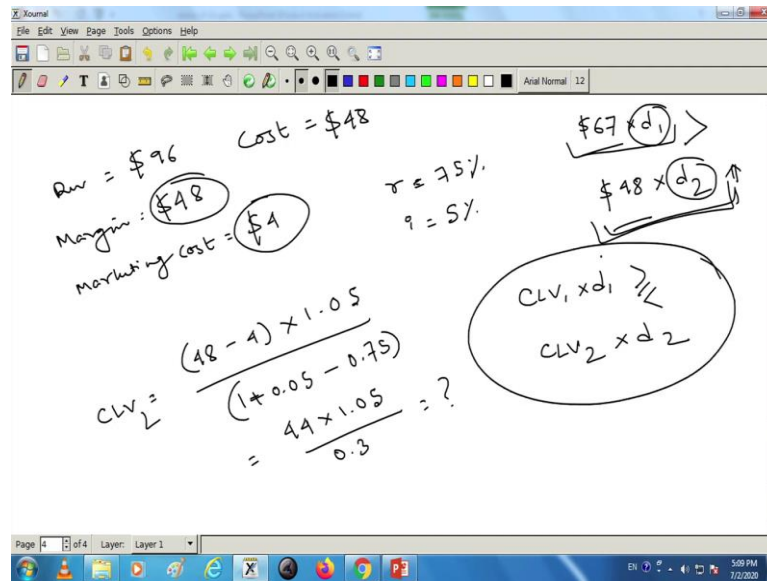
$$i = 5\% \quad r = 60\%$$

$$CLV = \frac{(72 - 5)}{(1 + 0.05 - 0.6)} = \frac{67 \times 1.05}{0.45} = 155.67$$

So, then their CLV calculation will be CLV will be basically, 72 minus 5 into 1 plus 0.05 divided by 1 plus 0.05 minus 0.6. So, this comes 67 into 1.05 and this is 0.54 whatever is the value that you get. So, that is the calculation of CLV the basic calculation. Now, where it applies? This is not that simple that it will be applied nowhere?

So, where it will apply further let's say. So, the values in general remain same that is a they are thinking about giving a small discount. They are thinking that if I change this 10 dollars per month to 8 dollars per month, two things happens; one is my customer base goes up; that means, the marketing cost comes down, but, per customer comes down, but at the same time I am not making revenue. So, that is something we have to take into account. So, 8 dollars per month; that means, my monthly revenue is 19, the yearly revenue is 96 dollars; revenue is 96 dollars.

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The margin is now a little bit lower because 30% if I say, see the cost has not changed. So, 72 minus 120 the cost was, basically how much? The cost was 8 — 48 dollars was the cost. So, the cost did not change I am giving a price discount, but the cost did not change. So, if I give a price discount of 2 dollar per month the cost does not change.

So, the cost still remains 48 dollars per year. So, the cost is 48 dollars per year and that is why the margin is also 48 dollars. This is what they have generated right now. But what else, their marketing cost has come down because the customer base goes up and they do a little bit of maths.

And they find out their marketing cost per customer is now 4 dollars because my customer base went up, because I have given a discount more customer came in customer is going up. So, whatever was 5 dollars previously now it has become 4 dollars. What happens with the customers?

But they have also seen here that not only the customer base went up. The retention rate also went up the more customers stayed back. So, what is the new retention rate now? They find out that around 75% people stays back. Now, see in the blind eye, in the blind eye if I see in the first year they are making loss you see here they are making a gain of as 172 dollars were there margin minus 5.

So, 67 dollar was they are making in the 1st year, in the previous condition 67 dollar was the profit, in the 1st year in this condition 44 dollars is the profit in the 1st year. So, ideally in common sense it is getting dropped. So, I should not do this because it will increase my price probably I do not increase my customer base probably, but the net money that I am generating per customer is going down.

So, you can suggest me that you will only do this if previously it was how much, previously it was as I told 67 dollars 67 dollars with demand at 67 dollars. If this is higher than 48 dollars into demand at demand at the or d1 or d2, just I will write d1 and d2, d1, d2; obviously, here the margin came down the amount of profit that I am making came down, but d1 and d 2, d2 went up than d1.

Now, common — in normal common sense what I will do that if my net income is going up in comparison to the previous income then I will go ahead and do this. That is a myopic view. A myopic view is that if the 1st year's total income is higher than the 1st year's total income in the situation 2, I will go ahead and do this.

But what we have to also take into account that not always it is only the 1st years decision; that whatever you take decision the retention rate also gets affected. And if retention rate gets affected the overall CLV for 1st one customer changes how let's say i is still 5 %. So, here CLV if you remember: it is $48 - 4$ into 1.05 divided by how much? $1 - 0.06$ which is 0.04 , in this case, 0.25 $1 + 0.05$ minus 0.75 .

So, just do the calculation 44 into 1.05 divided by 0.3 . And check this value whatever it is coming and then you will not compare 67 into d1, you will compare the CLV1 into d1 means the CLV at situation 1 into demand at situation 1, whether that is greater than or smaller equal to CLV2 into d2. So, this is CLV2 the previous case was CLV1, you will calculate these.

You will not consider 1 years, whatever sales is happening and etcetera whatever profit you are generating, but you will check for in the lifetime how much profit is generating. That will give you a choice that whether you will go for this discount or this promotion strategy or this strategy or that strategy.

So, when we compare multiple strategies also this comes to, comes in handy. So, thank you very much for being with me in this particular video I will continue with the

discussion of the maths part of CLV in the coming videos also. Be with me, I will see you in the next video.