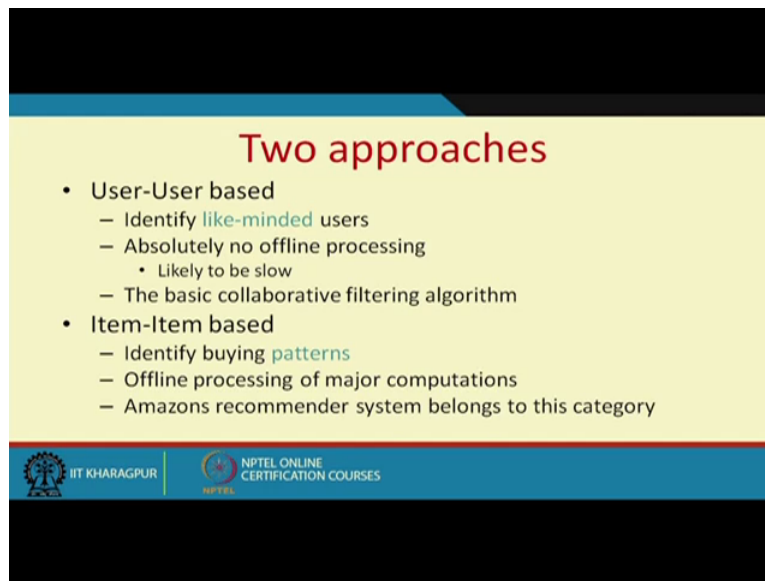


E Business
Professor Mamata Jenamani
Department of Industrial and Systems Engineering
Indian Institute of Technology Kharagpur
Lecture-54
Collaborative Filtering Based Recommender System

Welcome back, we continue our discussion with recommender system and in this particular class we are going to talk about collaborative filtering based recommendation system.

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Two approaches

- User-User based
 - Identify like-minded users
 - Absolutely no offline processing
 - Likely to be slow
 - The basic collaborative filtering algorithm
- Item-Item based
 - Identify buying patterns
 - Offline processing of major computations
 - Amazon's recommender system belongs to this category

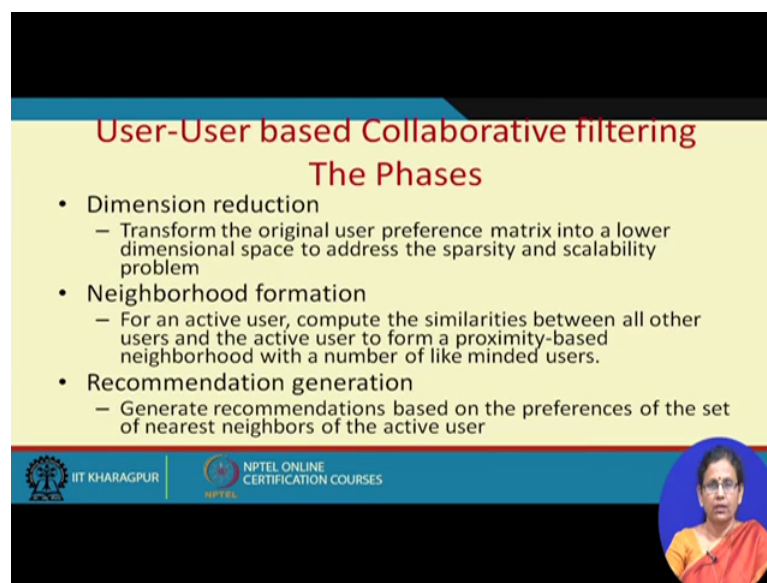
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Here this collaborative filtering based recommender system can be broadly classified into 2 categories; user-user based and item-item based. In fact, there are other collaborative filtering techniques as well but we are limiting ourselves to only these 2 to understand the concept. Now in this user-user based collaborative filtering, the idea is to identify the like-minded users and finding those like-minded users and looking at the preference of one user, you recommend the item to a similar user who have seen who are similar in terms of their in terms of the items they are looking at, so it is about identifying the like-minded users.

So this collaborative filtering algorithm is actually the older of these 2, in fact the social information filtering that we were talking about which was a very first initiative for recommendation generation, this user-user based finding the like-minded users for generating recommendation was used. So now in this particular method which is not very popular in the commercial domain because of its calculation procedure where everything happens in an online environment, as a result the system becomes very slow as the number of users and number of items increase and it is extremely difficult to use them in the commercial setting.

However, for research setting many people still also use this user-user based approach, so it is about identifying like-minded users and this is a basic collaborative filtering, but the corresponding commercial application is bit different where the item-item based on the buying pattern of various users, the item-item based similarity based on the users buying pattern is first computed off-line, then whenever a user comes and looks at an item then that matrix that similarity matrix is preferred to suggest the item. In fact, Amazon in a commercial setting first started this particular item-item based recommendation. So in case of whether it is either item-item or user-user, few steps are followed.

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User-User based Collaborative filtering
The Phases

- Dimension reduction
 - Transform the original user preference matrix into a lower dimensional space to address the sparsity and scalability problem
- Neighborhood formation
 - For an active user, compute the similarities between all other users and the active user to form a proximity-based neighborhood with a number of like minded users.
- Recommendation generation
 - Generate recommendations based on the preferences of the set of nearest neighbors of the active user

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For example, in case of user-user first step is to reduce dimension. So it is about transforming the original user preference matrix into a lower dimension, user preference matrix if you remember for recommender system while discussing about in the very first-class about the basic framework, the important element in a recommender system was the user-user user-item preference matrix. This user-item preference matrix contains the ratings provided by each user to each item, when I said provided by either it is explicitly provided or it is implicitly generated, but whatever it may be the case we assume that we have the user item rating matrix with us okay.

Now, this matrix often will be very large so therefore transforming this preference matrix into all over dimensional matrix to address the sparsity and scalability problem is the first task to be addressed. Then the second is, for each user we have to find out who are the similar users or we will be forming the neighbourhood of each active user, then once we find out the neighbourhood who are the like-minded users then we generate the recommendation.

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Dimension reduction
- Dealing with sparsity and scalability problem

	Andre	Star Wars	Batman	Rambo	Hiver	Whispers
Lyle	y	y				
Ellen	y	y			y	
Fred		y	y			
Dean		y	y	y		
Jason					y	y

	Batman	Rambo	Andre	Hiver	Whispers	Star Wars
Lyle			y			y
Ellen			y	y		y
Jason			y		y	
Fred	y					y
Dean	y	y				y

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So for this dimensionality reduction may be single value decomposition or your PCA can be used. But here we are simply giving some very rudimentary example what exactly we mean by dimensionality reduction. Let us say we have some site users rating some 6 items, now looking at this ratings you can see not every user has seen every movie. So many of these spaces are blank, so this matrix is quite sparse, it is not that sparse but it is quite sparse. But as you can increase as you can imagine if the number of users grow, number of items grow and in each user might not be might not have seen all the movies so therefore only few movies each user must have seen so therefore as the size increases the sparseness will also increase, but the idea here is to see that how it can be grouped together in different groups.

Look, now if we rearrange these rows possibly we can make some 3 groups like action, some outside foreign movie, some classic. And you can see the first group of users are interested in foreign movies and classic and second group are interested in action and classic movies. Now this kind of categorisation if it is done it can be done automatically, it can be but doing it manually is a cumbersome process but at least if we know the category of the movie from let us say some explicit dataset we can try this categorisation as well for grouping the users.

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Methods for dimension reduction

- Semi-manual Methods
 - Use product **features**
 - Cluster **products** first, then cluster **users**
 - Works only if we have **descriptive** features
- Automatic Methods
 - Adjusted Product Taxonomy
 - Latent Semantic Indexing

Dimension

So these methods of dimensionality reduction can be either semi-manual or it can be automated. In case of semi-manual you can use products features like this movie example, whether the whether the movie belongs to a specific category you can try to do some kind of semi-manual activities. Then you can also cluster the products then you can cluster the users to find out the groups. So even if you have I mean only when you have descriptive features of the products available you can go this way, but if not you can actually go for some kind of automatic method, some of this method I mean that this method in general we are not going to discuss as such but some example situation we can see.

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Adjusted Product Taxonomy

- Input : product taxonomy
- Output: **modified** taxonomy with **even** distribution

Level 0: All

Level 1: Clothes, Footwear, Cosmetics, Accessories

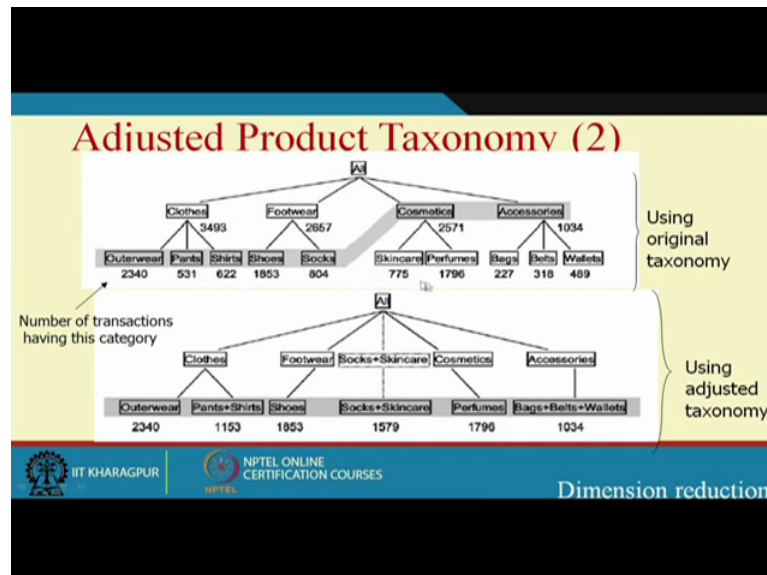
Level 2: Outerwear, Pants, Shirts, Shoes, Socks, Skincare, Perfumes, Bags, Belts, Wallets

Level 3: A grid of counts for each category, showing an uneven distribution.

Dimension

For example in case adjusted product taxonomy, look we have a dataset in which we have clothes, footwear, cosmetic and accessories. Manually this grouping is made and under each group against some subgroup is made and the number of items under each can be found out.

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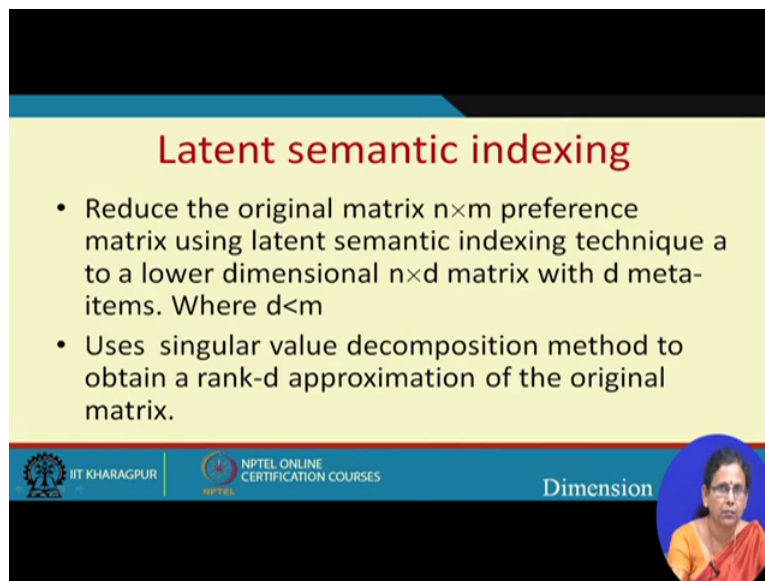
Let us say these are the number of items under each, but the thing is here there are more items, here there are less. So, even if I mean we will try to more or less balance this to for ease of search what can be done, some products can be moved even if they do not belong to this category they can be moved from here to here and make. For example, look clothes were these outerwear pant, shirt, et cetera, and footwear were shoes, socks and so on. Now, they can be adjusted like clothes can contain this, outerwear pant and shirt together because these 2 values were too less, they can be combined and put together.

Footwear can contain only shoes, then this socks and skin care can be put as one socks plus skin care category with these many products, cosmetics under cosmetic you can put only perfume because this value is very high you can put together and these numbers were very small these accessories, along with that I mean all these 3 things can be put together and made one thing. So instead of these many subcategories now we have broken it into a different subcategory though sometimes because no see this was required domain knowledge and user with domain knowledge has some developer with domain knowledge has manually divided this partition, manually partitioned this.

But if you do it automatically taking care of that syntactic things may not be possible but at least the program can take care of adjusting the products in each category so that items

number of items are at least of same number so that they I mean the balance can be maintained by taking a search. So instead of these small-small things kept together they have been combined here, pant-shirt has been combined, then your skincare and socks has combined, perfume is considered as a separate thing and all the accessories has been combined, so that way search becomes little fast.

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Latent semantic indexing

- Reduce the original matrix $n \times m$ preference matrix using latent semantic indexing technique a to a lower dimensional $n \times d$ matrix with d meta-items. Where $d < m$
- Uses singular value decomposition method to obtain a rank- d approximation of the original matrix.

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Dimension



Then there can be some further automatic methods like your Latent semantic indexing, where the original matrix dimensions of the original matrix is reduced by finding the corresponding lower dimensional equivalent matrix okay. So it specifically it uses singular value decomposition method if you are acquainted with, but anyway you do not worry you do not have to be solving problems, this is just to let you know that such methods do exists.

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Neighborhood Formation

- For an active user u_a find a list of *I like minded* users
 - Interested in similar items (meta-items)
- Measuring similarity
 - Pearson correlation coefficient
 - Constraint Pearson correlation coefficient
 - Spearman rank correlation
 - Cosine Similarity
 - Mean-square difference
- Neighborhood Formation
 - Weight threshold
 - Center based best-k neighbors
 - Aggregate based best -k neighbors




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Neighborhood f



Then next task was to, first was the dimensional reduction, next task was to find out the like-minded users, this is done by forming the neighbourhood. So for forming this neighbourhood again there are many methods, one such method is using the most simplistic method is using by the use of some correlation coefficient.

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Measuring similarity

- Pearson correlation coefficient

$$sim(u_a, u_i) = \frac{\sum_{j \in \text{Commonly Rated Items}} (p_{aj} - \bar{p}_a)(p_{ij} - \bar{p}_i)}{\sqrt{\sum_{j \in \text{Commonly Rated Items}} (p_{aj} - \bar{p}_a)^2 \sum_{j \in \text{Commonly Rated Items}} (p_{ij} - \bar{p}_i)^2}}$$

where p_{ij} : preference of i^{th} user for j^{th} item
 $\bar{p}_i$: mean preference of i^{th} user for Commonly Rated Items






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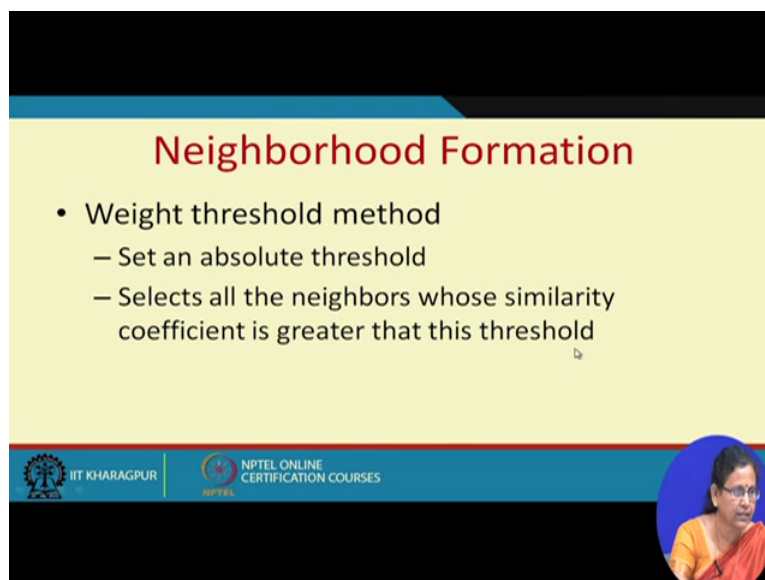
For example, if user u_i and user u_a , user u_a is the active user whose whether he is similar to this user or not can be found out by computing the correlation between this row and this row. This row and this row, but see this person might have been rating many items, this person has already rated many items but all the items this person has rated this person has not rated. Similarly, all the items this person has rated this person has not rated so therefore will be to

find out coordination you need same number of elements in these 2 user vectors. So therefore, if something is rated here and not rated here and you are including, your dimension of the vector will not be same.

If you think of replacing that with 0 in fact, many of the authors do that you can very well do, if the item is not rated you can consider it as 0 but some of the authors view it as a because if the rating is from 1 to 5 let us say in the scale of 1 to 5 then 0 means giving a very lower rating, for computational purpose you can use that 0 but this may lead to certain erroneous result so therefore many of the authors suggest that you take you may win this vector is u_i and u_a for only co-rated items, once you have these co-rated items ready, both these will have same length.

So once they have the same length, you can use this formula and find out the correlation. Once I find out the correlation, this correlation will be treated as the similarity between the active user and some other user, some other user has already given his rating. So therefore, for this user a with all the remaining users you find out this similarity, once the similarity is computed then top few users who are most similar to this active user will be under his neighbourhood.

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The slide is titled "Neighborhood Formation" in red text. It lists a bullet point: "Weight threshold method". Under this, there are two sub-points: "Set an absolute threshold" and "Selects all the neighbors whose similarity coefficient is greater than this threshold". The slide has a yellow background with a blue header and footer. The footer contains the logos of IIT Kharagpur and NPTEL Online Certification Courses, along with a small circular inset image of a woman in an orange sari.

Neighborhood Formation

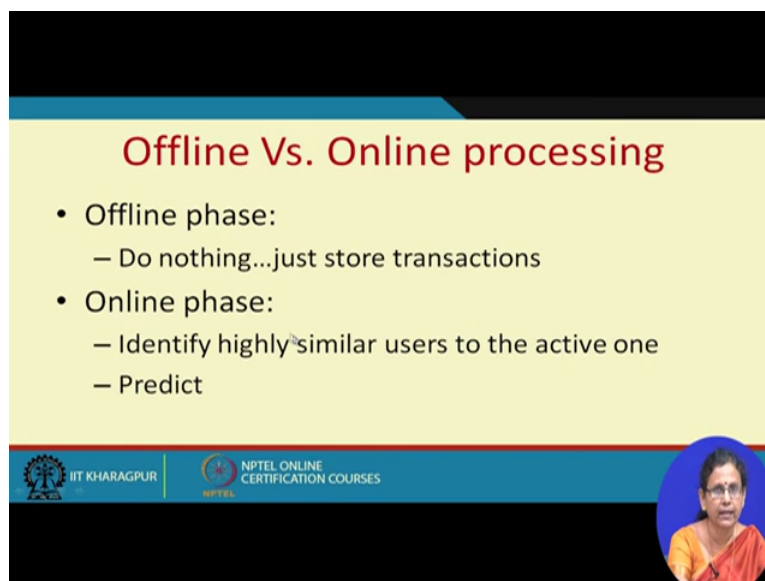
- Weight threshold method
 - Set an absolute threshold
 - Selects all the neighbors whose similarity coefficient is greater than this threshold

So once this neighbourhood is formed and you find out the nearest neighbours, next is generating the recommendation for a newer item, newer item you generate the recommendation. To generate this recommendation there are again see these formulas that I am showing, from author to author this formula vary little bit to adjust to a specific situation

or to incorporate a particular author's viewpoint. But for our application purpose here for our discussion purpose here please limit yourself to the formulas that we discuss, recommender system in a broad topic I have made it clear from the beginning and these ratings, et cetera, the calculation procedure et cetera may vary based on various authors opinions but here we use this.

So to find out the predicted rating of the item j for the active user a , we take the average rating of the active user then the contribution from the similarity of the other user we add to this. So this is found out by the waited value of the deviation of each active user from that specific product rating, this is P_{ij} is the rating given by the i th user for j th product. $\bar{P}_i$ is the average rating given by the i th user so this this deviation from this means into similarity of user A with user i which you have already found out this weighted sum normalised to this sum of the similarity value is added to this average rating score of the user A to generate the predicted rating value. So this predicted rating for all the items which are not seen by user A are found and out of that the top few once are suggested to the user okay.

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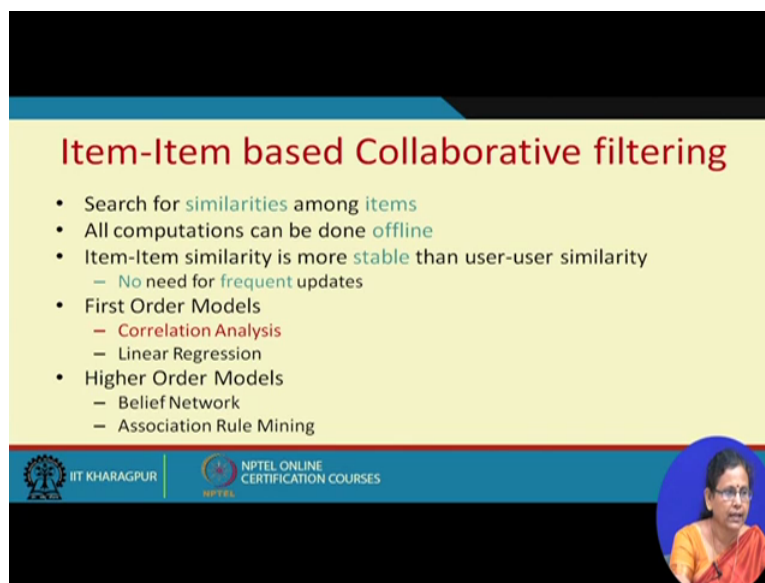


The slide is titled "Offline Vs. Online processing" in red text. It lists two phases: Offline phase and Online phase. The Offline phase involves "Do nothing...just store transactions". The Online phase involves "Identify highly similar users to the active one" and "Predict". The slide features the IIT KHARAGPUR logo and NPTEL ONLINE CERTIFICATION COURSES text at the bottom. A small video inset shows a woman in an orange sari speaking.

- Offline phase:
 - Do nothing...just store transactions
- Online phase:
 - Identify highly similar users to the active one
 - Predict

So here what is the off-line phase? Off-line phase there is nothing, just store the transactions of the past users, in online phase you find out the similarity of the active user with the other users then you predict. This is quite a time-consuming process, as the dataset group this is no more possible so therefore for commercial application this is not a right kind of scenario.

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Item-Item based Collaborative filtering

- Search for **similarities** among **items**
- All computations can be done **offline**
- Item-Item similarity is more **stable** than user-user similarity
 - No need for **frequent** updates
- First Order Models
 - **Correlation Analysis**
 - Linear Regression
- Higher Order Models
 - Belief Network
 - Association Rule Mining

Logos at the bottom: IIT KHARAGPUR, NPTEL ONLINE CERTIFICATION COURSES, and a portrait of a woman in an orange sari.

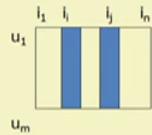
So next but this idea can be extended to a item-item collaborative filtering environment. Here the search for similarity among the item is first made and this all the computations for this generating this item-item similarity matrix based on the user preference as done in off-line manner. Then once this item-item similarity matrix is ready then it can be used for recommendation. By the way, this item-item similarity matrix is more stable, I mean they do not change very frequently like that of your user-user preference matrix because see in an online and environment you do not have really control over your users who is over user come today.

And moreover you do not keep track of your users because most of the users will not login into the site okay, so you can use cookies et cetera but that is again limited by the by the client computer by the client, client may decide not to use the cookies. But anyway, this item-item similarity is understood to be more stable, so there are many methods of doing so we are again going with that correlation base method which we have already discussed.

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Search for similarities among items - Correlation-based Method

- Same as in user-user similarity but on item vectors
- Pearson correlation coefficient
 - Look for users who rated both items

$$sim(i, j) = \frac{\sum_{u \in \text{Users Rated Both Items}} (p_{uj} - \bar{p}_j)(p_{ui} - \bar{p}_i)}{\sqrt{\sum_{u \in \text{Users Rated Both Items}} (p_{uj} - \bar{p}_j)^2} \sqrt{\sum_{u \in \text{Users Rated Both Items}} (p_{ui} - \bar{p}_i)^2}}$$


The diagram shows a grid of items $i_1, i_2, \dots, i_n$ as columns and users u_1, u_m as rows. Blue vertical bars indicate ratings: u_1 has ratings for i_1 and i_2 , and u_m has ratings for i_1 and i_2 .

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Here, instead of the user-user between item-item based on the co-rated users, if many users have commonly rated the items, wherever they have got ratings in both the places that part only is used for predicting the similarity score, the similarity score is nothing but your correlation coefficient. So after this is I am not going to discuss it further because we did it just now.

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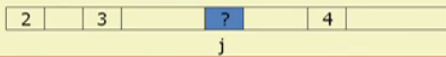
Predict rating - Correlation-based Method

Offline phase:

- Calculate $n(n-1)$ similarity measures
- For each item
 - Determine its k -most similar items

Online phase:

- Predict rating for a given user-item pair as a weighted sum over similar items that he rated

$$p_{aj} = \frac{\sum_{i \in \text{similar items}} sim(i, j) p_{ai}}{\sum_{i \in \text{similar items}} sim(i, j)}$$


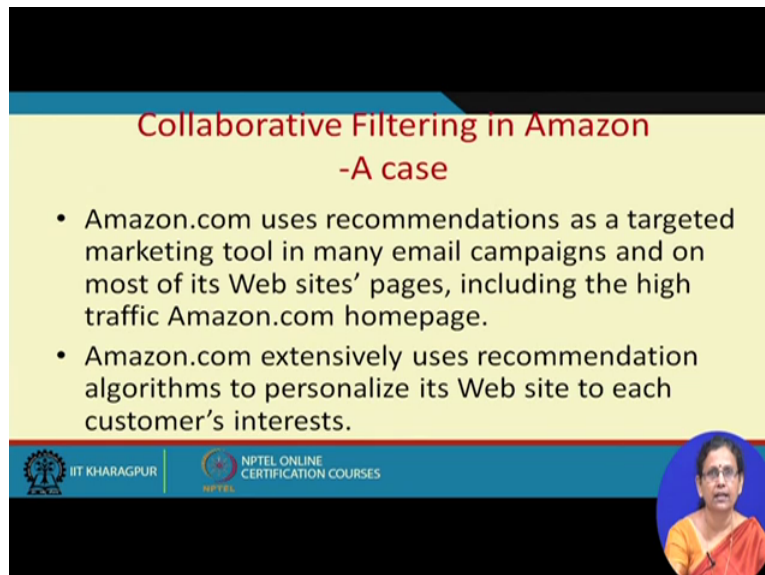
The diagram shows a row of items i_1, i_2, i_3, i_4 as columns. A user's rating vector is shown below: $[2, 3, ?, 4]$. Item i_3 is highlighted with a blue bar, indicating it is a similar item.

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So once this is done you find out this item-item similarity, this is a n cross n matrix but because it is a n cross n symmetric matrix because the similarity of i to j is same as the similarity of j to i you have total n into $n - 1$ number of similarity measures from diagonal to upwards, diagonal matrix it is basically diagonal matrix. So for each case you determine what

are the k similar items and you keep it together. Now in the online phase when a user comes, as soon as he puts one item into the shopping cart or as soon as he views one item, for that item whatsoever is the similar item you find out from this k most similar item list and display, okay.

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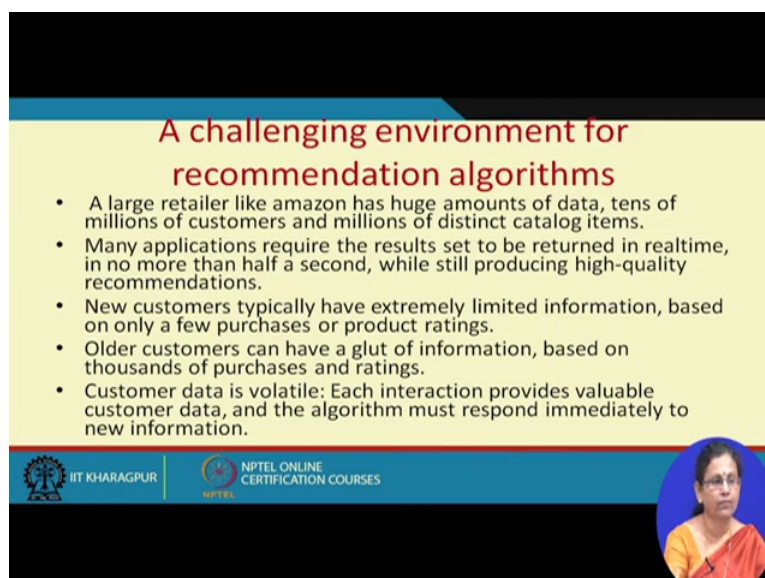
Collaborative Filtering in Amazon
-A case

- Amazon.com uses recommendations as a targeted marketing tool in many email campaigns and on most of its Web sites' pages, including the high traffic Amazon.com homepage.
- Amazon.com extensively uses recommendation algorithms to personalize its Web site to each customer's interests.

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So this is as I told you this particular method is adopted in fact suggested by Amazon, so Amazon uses this particular algorithm.

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A challenging environment for recommendation algorithms

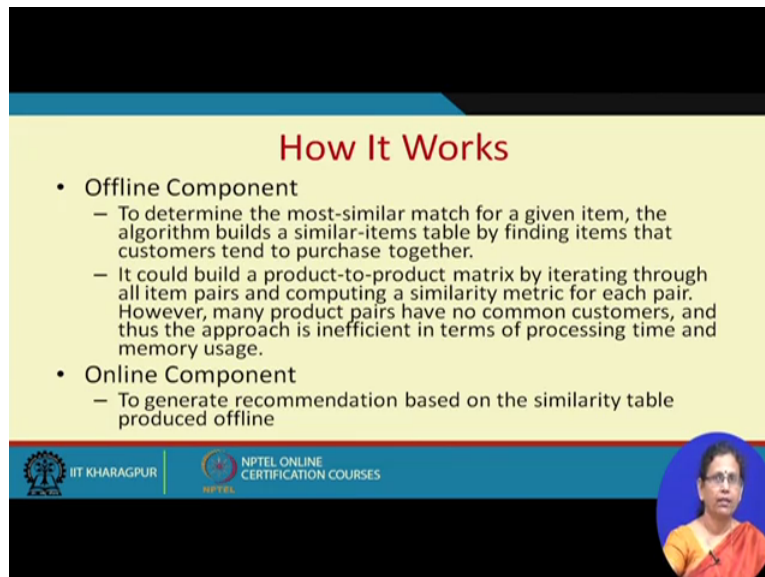
- A large retailer like amazon has huge amounts of data, tens of millions of customers and millions of distinct catalog items.
- Many applications require the results set to be returned in realtime, in no more than half a second, while still producing high-quality recommendations.
- New customers typically have extremely limited information, based on only a few purchases or product ratings.
- Older customers can have a glut of information, based on thousands of purchases and ratings.
- Customer data is volatile: Each interaction provides valuable customer data, and the algorithm must respond immediately to new information.

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But a large retailer like that of Amazon has huge amount of data maybe tens of millions of customers and millions of distinct product items. Now many applications applications require

the results said to be written in real-time so therefore, maybe within few seconds you have to provide your suggestion. So in this deal to deal with this and environment they only suggested this item-item collaborative filtering algorithm.

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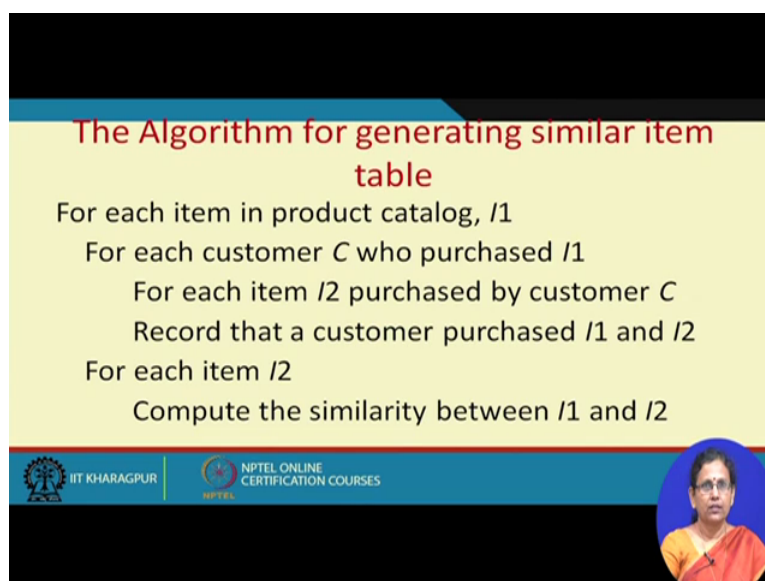
How It Works

- Offline Component
 - To determine the most-similar match for a given item, the algorithm builds a similar-items table by finding items that customers tend to purchase together.
 - It could build a product-to-product matrix by iterating through all item pairs and computing a similarity metric for each pair. However, many product pairs have no common customers, and thus the approach is inefficient in terms of processing time and memory usage.
- Online Component
 - To generate recommendation based on the similarity table produced offline

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In the off-line component, the computation of the item-item similarity matrix is made and in the online component as soon as user enters the item, the similarity is phased from the similarity table and items are suggested.

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The Algorithm for generating similar item table

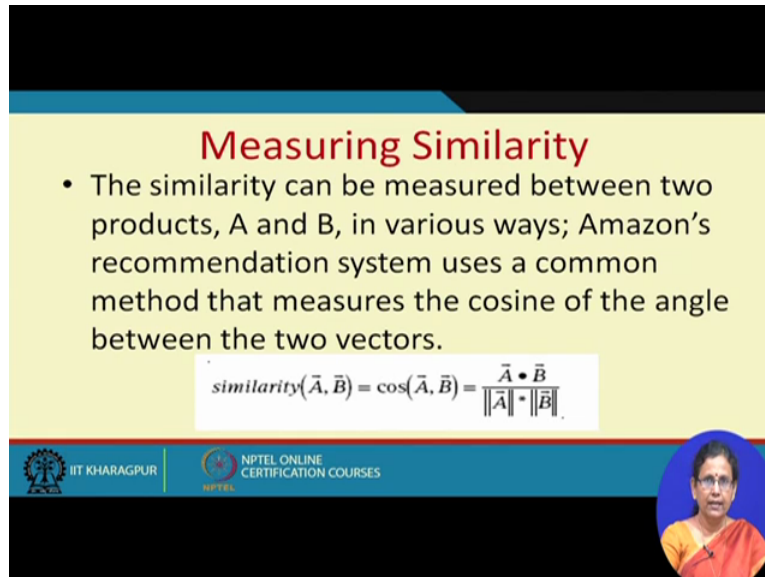
```
For each item in product catalog, I1
  For each customer C who purchased I1
    For each item I2 purchased by customer C
      Record that a customer purchased I1 and I2
  For each item I2
    Compute the similarity between I1 and I2
```

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In this process we use the algorithm like for each item in the product catalogue specific product catalogue let us say I_1 , for each customer who purchased this item I_1 , for each item

I₂ purchased by the customer C, record that the customer has purchased I₀ and I₂, for each item I₂ compute the similarity between I₀ and I₂, this is their method for finding the similarity.

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Measuring Similarity

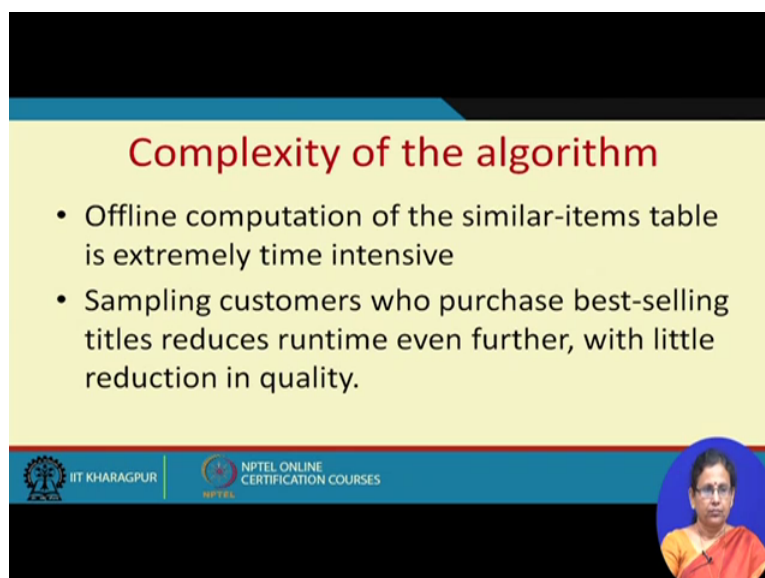
- The similarity can be measured between two products, A and B, in various ways; Amazon's recommendation system uses a common method that measures the cosine of the angle between the two vectors.

$$\text{similarity}(\vec{A}, \vec{B}) = \cos(\vec{A}, \vec{B}) = \frac{\vec{A} \cdot \vec{B}}{\|\vec{A}\| \cdot \|\vec{B}\|}$$

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Next, after similarity once we find out this thing these 2 vectors where they are co-rated, Amazon specifically uses this cosine similarity. I have told you the similarity measures can be of many types, correlation was one but Amazon as such uses cosine similarity so there are many similarity measures.

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Complexity of the algorithm

- Offline computation of the similar-items table is extremely time intensive
- Sampling customers who purchase best-selling titles reduces runtime even further, with little reduction in quality.

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So once this is done, the similarity is computed which is quite time-consuming, in the online environment the recommendation can be very weakly made which depends on I mean you do not really have to have a past history of the user because every user whenever he browses or purchases, their history is instantaneously captured that is kept, item-item similarity matrix is made. So whenever a new user comes in whether he registered or not registered does not matter, as soon as he puts one item that item is the similar items to that item is phased from the similarity table and put back to him as recommendations.

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Collaborative filtering assignment

The i th row in the following matrix represents a single transaction by the buyer b_i . The non-zero entries in a row represent the items bought together during the transactions and the corresponding value represents the preference scores assigned to the items by the buyer. If an active buyer 'a' has put i_4 in his shopping cart, recommend one more item to him. Use item-item collaborative filtering algorithm for recommendation generation.

	Items					
	i_1	i_2	i_3	i_4	i_5	i_6
b_1		5		6	4	
b_2			5		8	
b_3		9	7	8		6
b_4	2	4	6	4		
b_5			8	3	5	
a				*		

Buyers

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So this is the assignment you try doing, here the i th row in this matrix represents the single transaction by a buyer B_i . The nonzero entries in a row represent the items bought together during the transaction and the corresponding value represents the preference score assigned to the items by the buyer. Now if an active buyer A has put item i_4 in his shopping cart, you have to recommend one more item to him. You have to use item-item collaborative filtering algorithm for recommendation generation, use both the cosine similarity as well as Pearson similarity because you know both these to generate this recommendation.

So what you have to do, first you have to build an item-item similarity matrix, once that item-item similarity matrix is made then you have to set, if an active user A has put an i_4 in his shopping cart, which other items have to be recommended to him. Look, there is a problem associated with collaborative filtering which is called cold start problem, we are not anyway going to discuss have a discussion on that. Cold start problem in the sense suppose a new item comes in, no user has rated the item so its similarity with the other items is not available then in all the recommendations it is never going to come so it has to be this particular

situation has to be dealt with separately, possibly using a content based recommender system recommendation approach you find out content wise how similar is this product with others and then you start.

And once you start suggesting it, people will view it, people will purchase it, item's history will be generated then it can have a place in the item-item similarity matrix okay. So with this we finish our lecture and next lecture we will be continuing on this recommender system with a new type of approach, thank you very much.