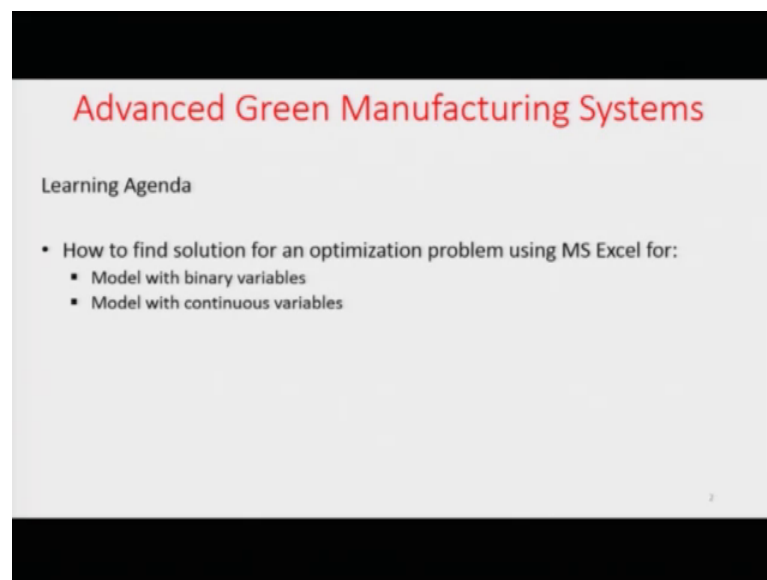


Advanced Green Manufacturing Systems
Prof. Deepu Philip
Department of Industrial & Management Engineering
Indian Institute of Technology, Kanpur

Lecture – 22
Solving optimization problems using MS Excel

Good afternoon students. Welcome back to the course Advanced Green Manufacturing System. So, myself Prabal Pratap Singh; I am the course TA and today we are going to learn how to solve the optimization problem using Microsoft Excel.

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So, our learning agenda for today is how to find the solution for an optimization problem using Microsoft excel for two different problems. The first one is model with the binary variables and the second problem will be the model with continuous variables. So, these two problems have already being discussed by post instructor Dr. Deepu Philip in the previous lectures. And this lecture is the exact continuation of lecture 5 and lecture 7 in which these two problems have been discussed by creating the model manually.

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Optimization Problem with Binary Variables

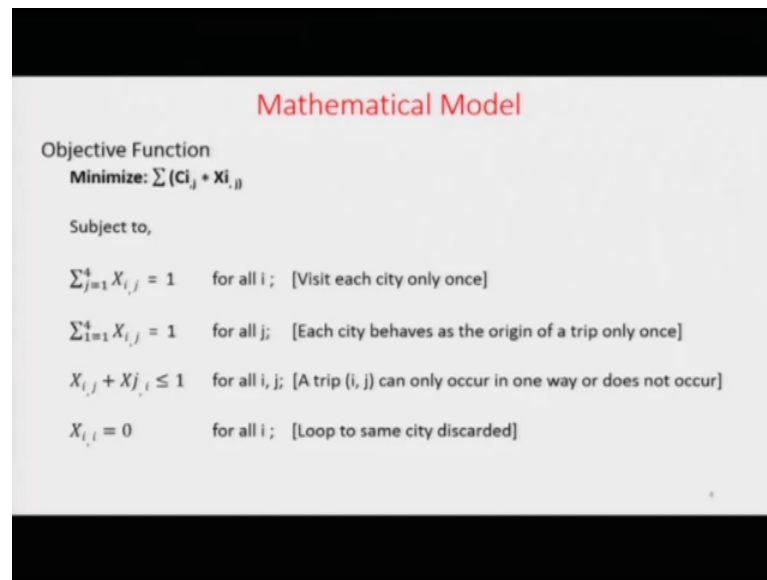
- A prospective college student from Kanpur is planning to visit the campuses of three colleges in India (Bombay, Delhi and Madras) on one extended trip starting from and returning to Kanpur. The student wants to visit each college only once while making the round-trip as cheap as possible. The cost of traveling between cities are given below.

	Kanpur	Delhi	Bombay	Madras
Kanpur	0	2600	3400	7800
Delhi	2600	0	1800	5200
Bombay	3400	1800	0	5100
Madras	7800	5200	5100	0

So, as we know that the first problem which was discussed is optimization problem with binary variable in this problem a prospective college students wants to travel from Kanpur and he is planning to visit the campus of 3 colleges. In India in the city Bombay, Delhi and Madrasa on one extended trip starting from and returning to Kanpur. The students wants to visit each college only once while making round trip as cheap as possible. The cost of travelling between cities are given in the matrix below and now we are going to first recap the exact mathematical model which was discussed in the class. And then we will try to solve the same problem by coding it into Microsoft Excel. There are various different options to get the solution for an optimization problems since this is a linear programming problem with binary variables.

So, first we are going to learn how to do it with Microsoft excel. The other alternatives are Python for in; if you talk about open source programming languages or like the commercial packages like lingo also provides facilities for extensive optimization problems.

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Mathematical Model

Objective Function
Minimize: $\sum (C_{ij} * X_{ij})$

Subject to,

$\sum_{j=1}^4 X_{ij} = 1$ for all i ; [Visit each city only once]

$\sum_{i=1}^4 X_{ij} = 1$ for all j ; [Each city behaves as the origin of a trip only once]

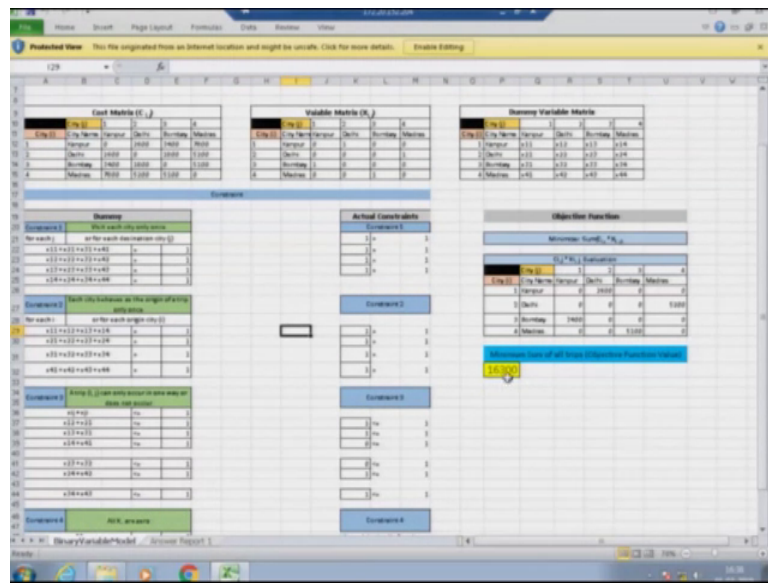
$X_{ij} + X_{ji} \leq 1$ for all i, j ; [A trip (i, j) can only occur in one way or does not occur]

$X_{ii} = 0$ for all i ; [Loop to same city discarded]

So, this problem has the objective function as given here in which we have to minimise the total cost of the trip. And the variables are c_{ij} into x_{ij} . So, we are here reducing cost to the minimum. And this objective function is subjected to these different constraints. In which the first constraint will talk about that each city should be visited only once. The next constraint will talk about each city behaves as the origin of a trip only once. And in the next trip next constraint will talk about that a trip can only occur in one way or does not occur.

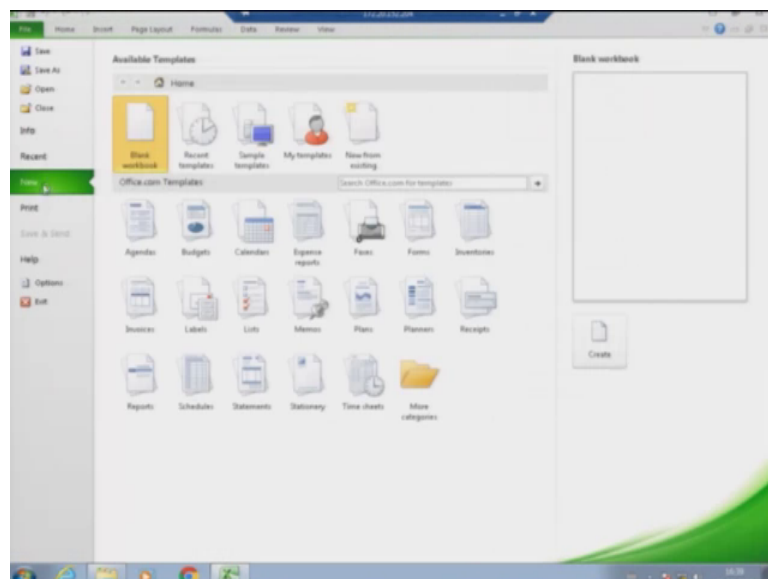
There is also a constraint in which we are saying that all the x_{11} x_{22} x_{33} or x_{44} since we are only talking about (Refer Time: 03:11) will be equal to 0. Because we do not want to loop to same city and these value should be discarded in the optimization model.

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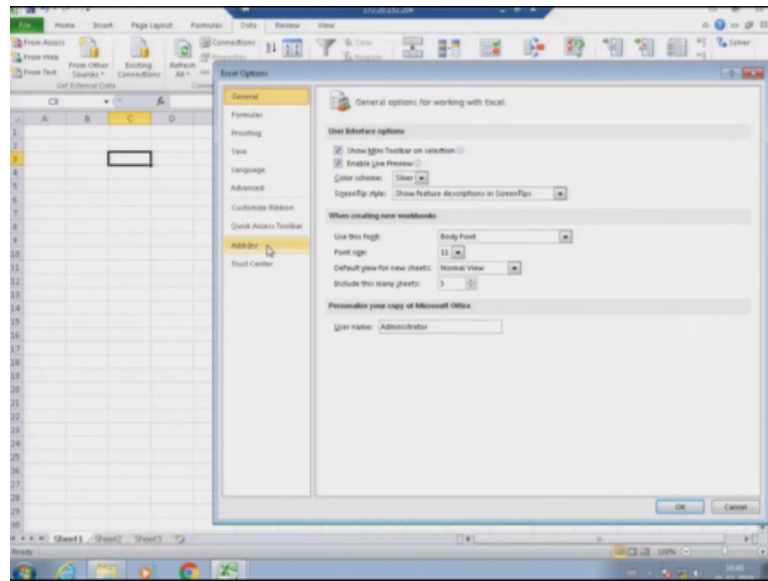


So, let us start with the Microsoft excel. So, we have already coded this into an excel file. And it is shown here. This is the complete model and what this is showing is that this yellow coloured cell is showing the minimum sum of all trips. Now this is a kind of decision making which can be done by using Microsoft excel. And we are going to learn to make this type of a spreadsheet from scratch.

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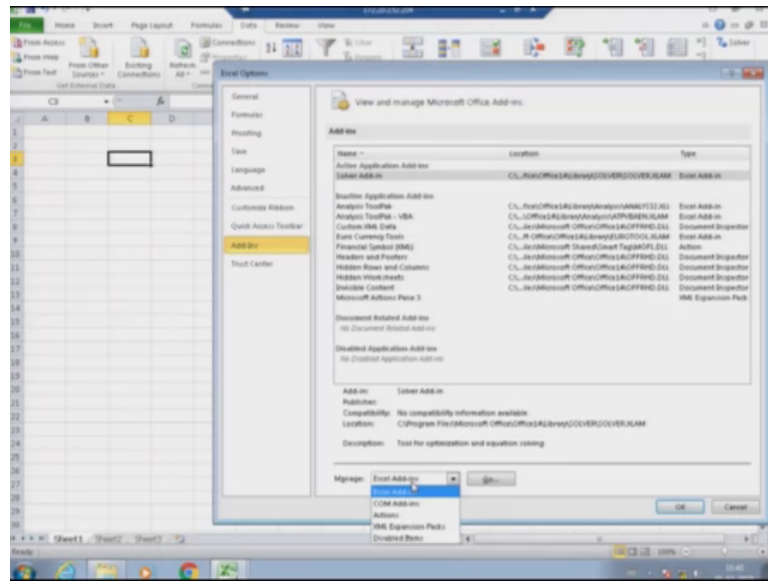
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So, let us start a new spreadsheet. Now the basic installation of Microsoft office will give you different applications. One of which is Microsoft excel, but the basic installation will not provide you with the solver capabilities. So, to get the solver capabilities, we first need to inspect whether we are getting the option of solver here. Since we have already coded this and we have already activated this option. So, it has being shown here is solver for analysis, but maybe in your personal computers it is not available.

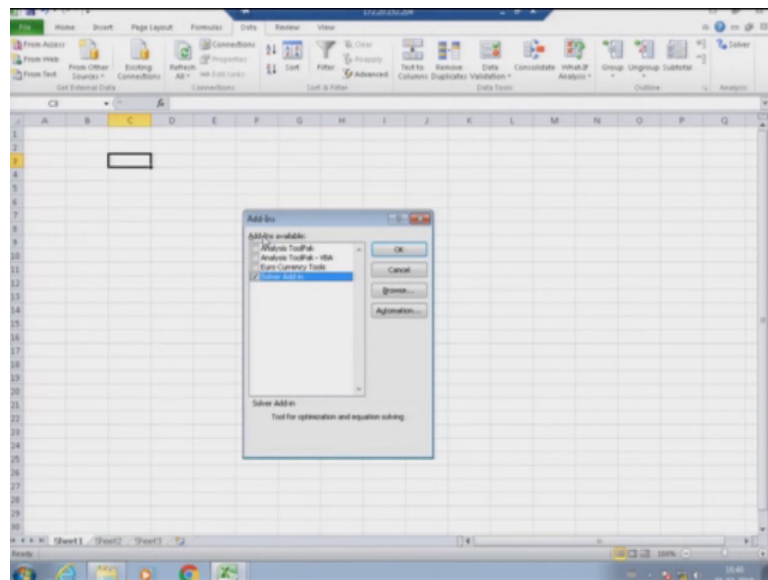
So, to get this available you first need to go to file menu and choose the options. There you will get an option of selecting add ins.

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There are various different add ins which are provided by Microsoft and we need to select excel add ins and then click on go.

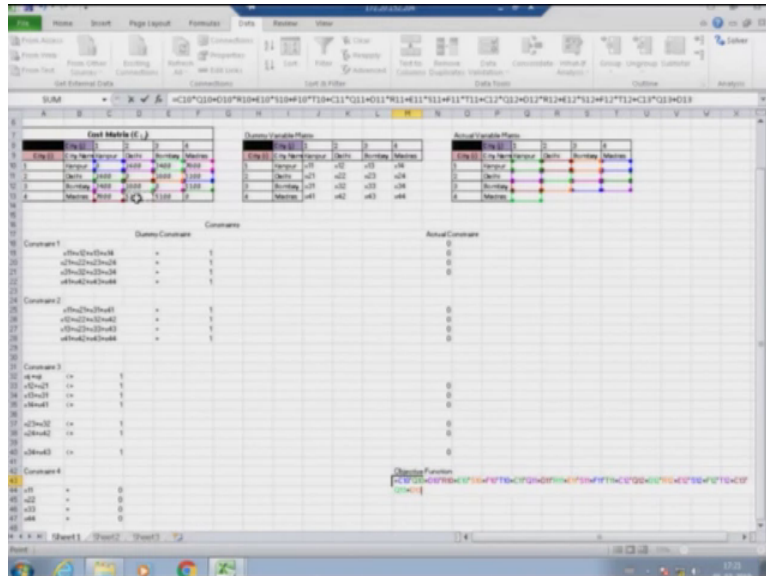
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There are four different variables as here we are as here we have, but we only need solver add in for this purpose. So, select this and click ok. In your computers it will first install and then maybe it will ask you to restart your Microsoft excel application. Then once restarted you can use solver dialogue for optimization problems. So, let us first copy the question which we need to optimize.

So, this is the question which we are talking about. And data given here is the cost matrix. So, there is nothing new in this. So, we can directly copy this.

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Now we have question and what the question is saying that we have few cities and these cities have some cost related to them for travelling from one city to another.

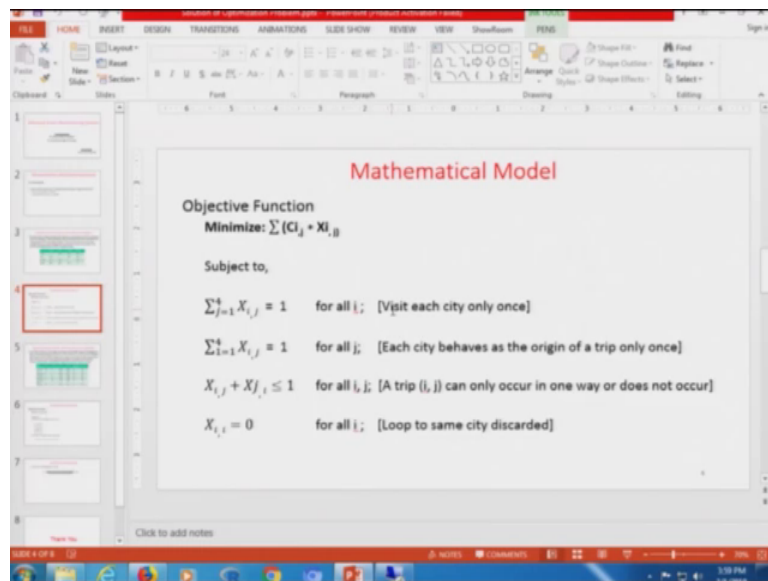
Now, the first thing which we need to do in solving an optimization problem is to first select the variables. So, here we have already discussed that the cities are the variables. And the i denotes the origin city and j denotes the destination city. So, we have created this matrix. And now create dummy variable matrix. Now if you see that how these values have been filled up. The curiosity will be like how can we code all the mathematical constraints which we have created in our mathematical model. And then get the solution from this solver excel. So, as we are doing it manually analogously we will first create the variable.

So, actually if you can see we have created x_{ij} variables here. So, just to demonstrate that the variables are created these cells are actually the variables which the follower will use. So, let say this is x_{11} then this is x_{12} to this is x_{13} this is x_{14} . Same way all the values can be filled in and these values will be used to optimize the objective function in the optimization problem using the solver. Now this is just for the demonstration purpose that is why I have written this is a dummy variable matrix, but to actually use this metrics for the purpose of optimization, we will create this matrix again, but we will

keep these values these cells unfilled so, that the solver can change the values in the cells to get the optimized result.

So, let us create the actual variable matrix and just reset all these cells in the variable matrix to null so, that the solver can use it. Now we have initialised all our variables. Now let us start with defining the constraints for the problem.

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So, let us see what is the first constraint. The first constraint says that the $\sum_{j=1}^n x_{ij}$ for all i should be equal to 1; that means, each city should only be visited once. So, let us encode this into our excel. So, you have already seen that if we are giving the basic input in any cell, then we can directly write into it and this is function where we can see what are the value of this cell.

So, you can see this is the basic string, but when you are going to encode anything which is having an expression. We need to first start with equal to sign. So, let us start putting the expressions for this mathematical model by using the equal to sign with start. Now we need to give this constraint as $x_{11} + x_{12} + x_{13} + x_{14} = 1$. So, let us write the dummy constraints first so that we can stay clear what we are going to encode in mathematical model. The first instance of the first constraint will be $x_{11} + x_{12} + x_{13} + x_{14}$.

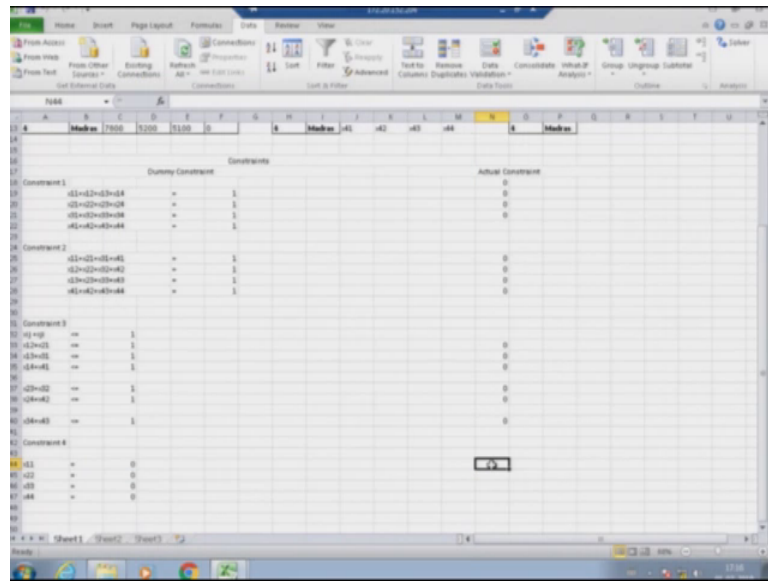
The next will be x_{21} plus x_{22} plus x_{23} plus x_{24} . The next will be x_{31} plus x_{32} plus x_{33} plus x_{34} . The last constraint of this first constraint will be x_{41} plus x_{42} plus x_{43} plus x_{44} . So, these all instances of the first constraint will be equal to 1. This will constraint the value to make anyone of the origin city to be equal to 1. Otherwise there will be loops in the solution. Similarly let us first see what is the second constraint.

So, the second constraint talks about that each city behaves as the origin of a trip only once therefore, we can see that we are changing the value of i here from one to 4 for all the j s. Means first the j will remain constant for first instance then the second instance the j will change. So, similarly let us define constraint 2. So, the first constraint would be x_{11} plus x_{21} plus x_{31} plus x_{41} . The next will be x_{12} plus x_{22} plus x_{32} plus x_{42} . The third constraint would be x_{13} plus x_{23} plus x_{33} plus x_{43} . The last would be x_{14} plus x_{24} plus x_{34} plus x_{44} .

these will also be constrained with the same equal to 1. Now the next constraint is that we should not get that loops in the trips. So, this was defined in the lecture like x_{ij} plus x_{ji} should be less than equal to 1. So, we will put this now. So, this constraint is important because otherwise the loops give the objective function minimum, but that minimum value will not be accurate. So, this x_{ij} plus x_{ji} less than equal to 1 should be for all i comma j .

So, we write all the instances because we are going to encode this. So, x_{12} plus x_{21} less than equal to 1 x_{13} plus x_{31} x_{14} plus x_{41} x_{23} plus x_{32} x_{24} plus x_{42} x_{34} plus x_{43} . So, these are all the instances of constraint 3 and we can verify this yes.

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Now, this is the last constraint. And this is required because there are no such thing as city i to city i . Means we are not going to travel from the city in which we are in.

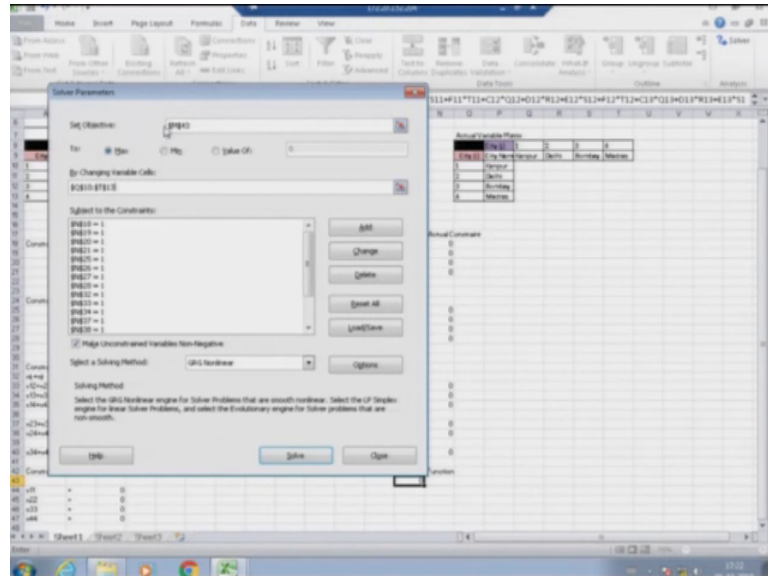
So, this is constraint $4 \times 1 \ 1 \times 2 \ 2 \times 3 \ 3 \times 4 \ 4$. Now these are all the dummy constraints here we are going to actually encode these constraints. Because now we have clear picture about what do we need to do next. So, as I have told you that we have actual variable matrix here. And each blank cell is a variable. So, to select x_{11} we are going to use this cell to select x_{12} we are going to use this cell. So, let us start writing the left hand side of this equation first.

So, start with equal to and using the control button on your keyboard start picking up the blank cells or the variables which we have mentioned here in the dummy constraints. So, x_{11} is. So, click on this. Now write plus because we are going to add all these constraint. So, and by pressing the control button, we are going to select the next variable. And the next variable here is x_{12} . So, this is how we are going to select multiple variables. Now select the third variable x_{13} and x_{14} . So, you have encoded the left hand side of the first instance of the first constraint.

Similarly, we are going to do it for all the instances of the first constraint. So, we have encoded the left hand side and you can see that these are showing the value 0s. Because we have written an expression here and the variables in expression are all null. So, it is

calculating it to 0 currently, but when we will run our solver. It will give some values to these constraints and only one of the variable will get the value one as per the constraint.

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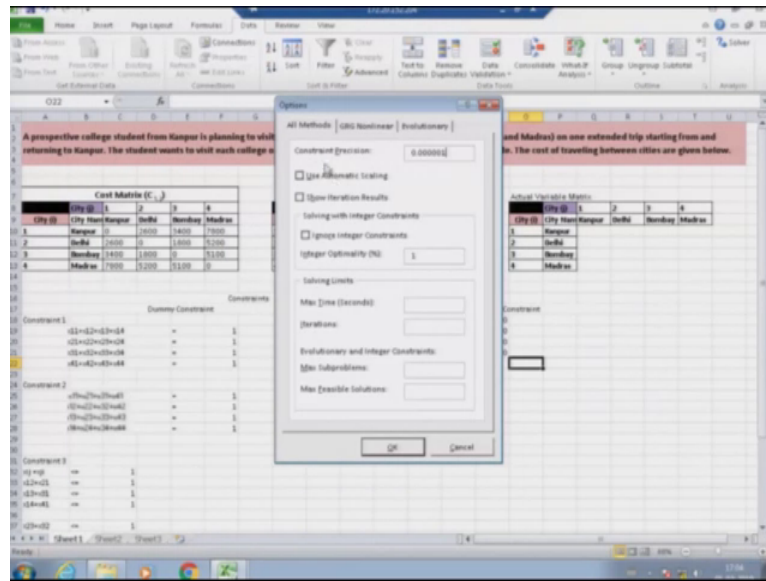


Now, let us encode this into solver. So, go to your data tab and choose solver button. Here I would like to tell you that the set objective is the value which contains the cell having the objective as being encoded.

So, currently we have only encoded the first instance offer for constraint. So, we have not yet encoded the objective value. So, let us skip this for now. And by changing variables ask for all the variables which needs to be changed by the solver. So, solver parameters include all the variables. And the objective function will try to maximize or minimize as per the given value and then the final value will get generated in to a report. And the subject to constraint types include all constraints which we are going to encode.

So, be using the add button we can add a constraint we can also edit constraint which have already added. We can delete the constraint. We can also reset all constraint and also we can load or save the constraints.

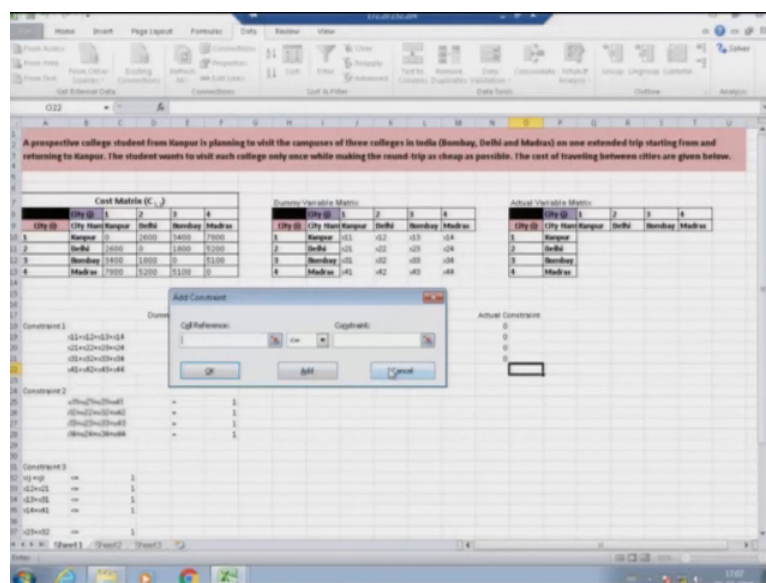
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The option tab includes the different options for the solver. So, there are many different types of solvers and their parameters we are going to use a very basic simple linear programming solver, but there are various methods which can be used to get to the solution for complex problems. And evolutionary techniques are also one of the solution methodology which can be used by the excel solver, but it has limited capabilities.

So, let us start adding the constraints which we have created.

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So, after pressing the add button, this new dialogue box will appear and the cell reference will ask for left hand side of cell and the values in the right hand side can be given here. This button can be used to select the cells or if you want to write the actual address of the cell, then you can see the row or column. Like if you want to give the value of this cell then we need to write n of 18. So, n 18 if you write here it will select the cell or you can directly click on this cell. So, just click on this and now it is asking for the cell which you want to write here.

So, I will click here and then again I will click on this button. Next is what type of constraint is this. So, as we have already seen this is an equal to type of constraint. So, use the drop down menu and select the equal to and then write the rhs value which one for if. Just click on add now it is asking for another constraint. So, again select the cell by following the same steps third one and the last instance.

Now, we have encoded our first constraint of the mathematical model which has 4 instance. And also here you can see that it is showing n 18 n 19 n 20 n 21 these are the address of the cell and dollar sign here represents that the value will remain fixed. Means it will only see this cell in the whole worksheet. Now close this for the time being and let us add another constraint. We will follow the same step here also and here we will add $x_1 + x_2 + x_3 + x_4 = 1$. The next instance is $x_1 + 2x_2 + 3x_3 + 4x_4 = 1$.

Similarly, $x_1 + 3x_2 + 3x_3 + 4x_4 = 1$ and the last one is $x_1 + 4x_2 + 4x_3 + 4x_4 = 1$. Now the last constraint and here we need to add $x_1 + 2x_2 + x_3 = 1$. So, just select $x_1 + 2x_2 + x_3 = 1$ here $x_1 + 2x_2 + x_3 = 1$ next is $x_1 + 3x_2 + x_3 = 1$ $x_1 + 3x_2 + x_3 = 1$ third one is $x_1 + 4x_2 + x_3 = 1$ $x_1 + 4x_2 + x_3 = 1$ $x_1 + 4x_2 + x_3 = 1$. Again we will open the dialogue box for solver and add all these constraints.

So, we have encoded the second constraint. Now we will encode the third constraint. So now, we are going to add the constraints 3 in us model. So, click on the solver tab and start adding the third constraint. So, the first instance of the third constraint is in this cell. So, let us select this and this is the less than equal to constraint and the value of RHS is 1.

Similarly, add the next instance. So, let us check we have given an 18 19 20 21 then from 25 to 28 25 26 27 28 next is from 32 33 34 35 32 33 34. So, we have missed one constraints here 35. This is x_{14} plus x_{41} .

So, you can also check whether the values which you have encoded is correct or not by double clicking on the cells which you have encoded like we just encoded x_{14} plus x_{41} . So, this is x_{12} plus x_{21} x_{13} plus x_{31} x_{14} plus x_{41} . This is x_{23} plus 632 this is x_{24} plus x_{42} this is x_{34} plus x_{43} .

Now, the last constraint first encode this x_{11} is equal to 0. So, we can directly include this into solver tab and we do not need to encode because there is no expression involved in these constraints. So, we can directly go to solver. And at so, the first constraint is x_{11} is equal to 0. So, just click on x_{11} mu is equal to i 0 at x_{22} equal to 0 at x_{33} equal to 0 at x_{44} equal to 0 at.

So now, we have created all our constraints and just to verify the last ones are p_{13} means t and this is 13 so, this is the x_{44} equal to 0 constraints. And we should not miss any constraint here or we should not use different cells because then the solver will get misinterpreted. And it will wrong value or it may not generate the result. So, the next step is to define the objective function.

Now, we know that the objective is to minimize the cost of the whole trip. And the cost can be calculated by multiplying the cost of each travel from i to j with the variable and since we are talking about a binary variable modelling. So, the variables can only take one or 0 as the value. So, if x_{23} is equal to 1, then only the x_{23} value which means 1800 will get added into the trip otherwise it will not.

So, there will only be 4 values from this matrix which will get added by changing the ones and 0s in this metrics. So, let us write this objective function by encoding. So, first select the cost matrix the value from cost matrix of c_{ij} and then multiply it with the variable matrix x_{ij} . And then we will add all these values one by one. So, the first is c_{11} into x_{11} plus c_{12} into x_{12} plus c_{13} into x_{13} plus c_{14} into x_{14} .

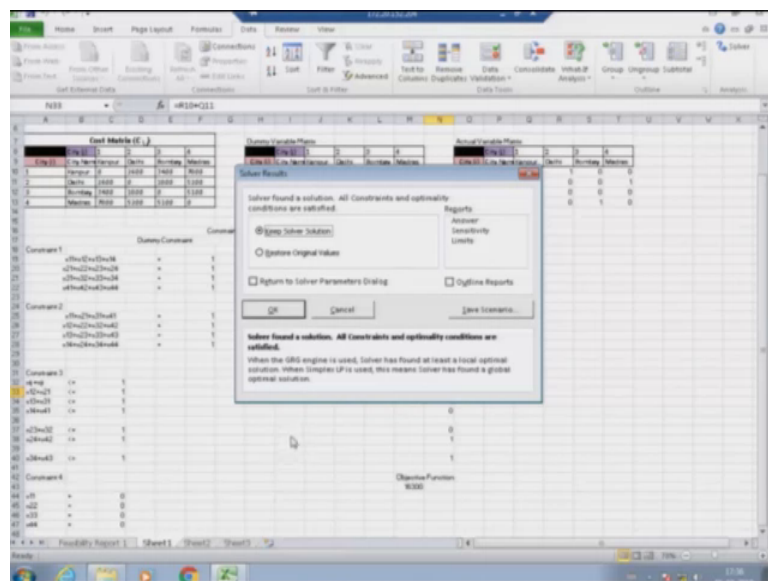
Similarly, on the second row, c_{21} into x_{21} plus c_{22} into x_{22} plus c_{23} into x_{23} plus c_{24} into x_{24} plus, c_{31} into x_{31} plus c_{32} into x_{32} plus c_{33} into x_{33} , plus c_{34} into x_{34} plus c_{41} into x_{41} plus c_{42} into x_{42} plus c_{43} into x_{43} .

4 3 and the last c 4 4 into x 4 4. Thus we have created the objective function here. And now we need to add this into the solver.

So, set objective will ask you for the cell where you encoded your objective function. And we can give this and it is also asking for where you have defined your variables. So, we can select all these columns. Now our model is complete we have defined the objective function in a cell. We have selected all the cells, where we have r variables which are yet undefined with any values and then all the constraints. These constraints will constraint the value of the objective function. And now we also need to select whether we are going to minimize the objective function or maximize. Since here the cost of the travel needs to be minimised just select minimize.

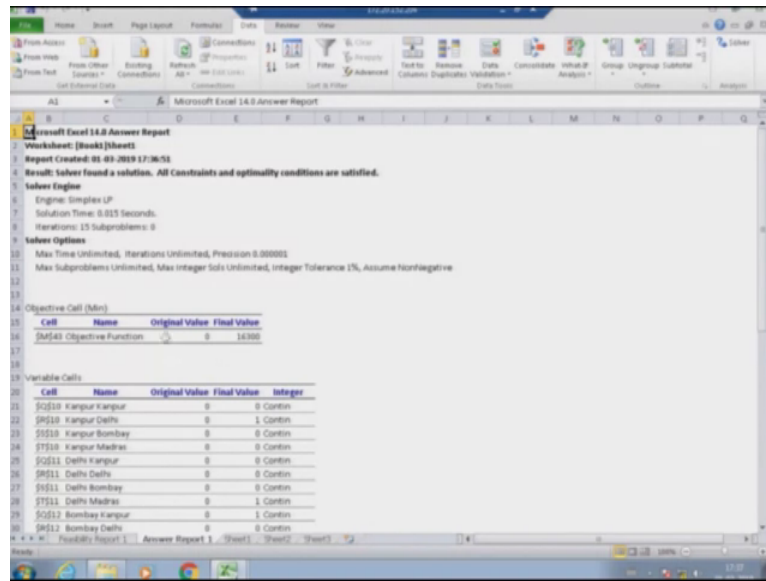
The solving method needs to be chosen also and here we are going to simple excel p and just press the solve button. Then it will ask you whether to generate a report or not. So, we have created the complete model and we have defined object function.

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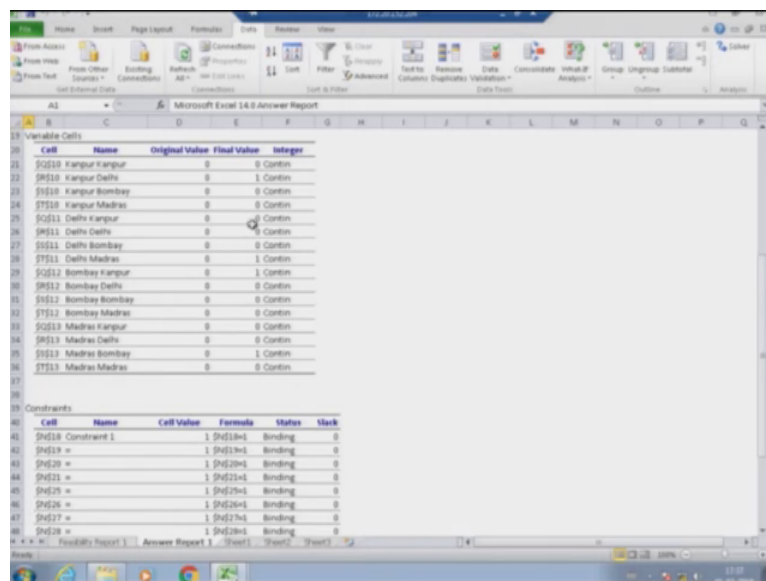


So, let us solve this problem by clicking on solve button. And here if the solver is saying solver formula solution. Now you can choose different things here like you can also do sensitivity analysis which is an advanced part of automation problem. And you can also see the answer. So, just click on ok. And it will create a new spreadsheet answer report one.

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So, it is showing that the objective function is having the value 16300. And it has only given the value of one to only some of the variables in the whole variable matrix. Like you can see that the final answer is showing that the student will travel from Kanpur to Delhi. Then from Delhi to madras because the i comma j which means 2 comma 4 value is 1. Then the student will travel from madras to Bombay and the last trip will be from Bombay to Kanpur. So, he is going to come back to Kanpur by following all the four cities in the minimum cost and the cost will be 16300.

So, this is the whole process of creating a spreadsheet for evaluating an optimization problem by encoding it using a solver tab. To analyse and to make decisions whether which variables need to be given what value you. So, I believe this is the problem which you can use to encode any type of different optimization problem which has only binary constraints.

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Optimization Problem with Continuous Variables

- A fertilizer factory is planning to produce bio-fertilizer bags of 50 kilograms (kg) containing between 0.5% and 1.25% Carbon (C), 0.3% to 0.5% Nitrogen (N), no more than 0.05% Sulphur (S), and no more than 0.04% phosphorus (Ph). There are seven raw materials available to produce the fertilizer whose composition, availability (in kg) and cost (Rs.) is given below.

Raw material	% of C	% of N	% of S	% of Ph	Availability (in kg)	Cost (Rs.)
Lime stone	3.0	0	0.013	0.015	40	200
Pyrite	2.5	0	0.008	0.001	30	250
Worm meal	0	0	0.011	0.05	60	150
Bone meal	1.2	0	0.002	0.008	50	220
Neem cake	0	90	0.004	0.002	20	300
Groundnut cake	0	96	0.012	0.003	30	310
Charcoal	90	0	0.002	0.01	25	165

So, let us start with the second problem. So, this is the second problem which was discussed in lecture 7 by the course instructor. And in this problem the difference from the previous problem is that, this problem includes the continuous variables which means that the variables can take any real value as it is value for maximising or minimizing the objective function.

So, let us first recap what was the problem. So, in this fertilizers factories planning to produce bio fertiliser bags of 50 kilo grams containing between 0.5 percent and 1.25 percent carbon 0.3 percent 2.05 percent nitrogen, no more than 0.05 percent sulphur and no more than 0.04 percent phosphorous. There are 7 raw materials available to produce the fertilizers whose composition availability and cost is given below.

So, this is the matrix which will be using in our excel for various different operations.

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Mathematical Model

Objective Function
Minimize: $\sum (C_i + X_i)$

Subject to,
Constraint 1: Availability constraint

$0 \leq X_1 \leq 40$
 $0 \leq X_2 \leq 30$
 $0 \leq X_3 \leq 60$
 $0 \leq X_4 \leq 50$
 $0 \leq X_5 \leq 20$
 $0 \leq X_6 \leq 30$
 $0 \leq X_7 \leq 25$

Constraint 2: Bag Quantity constraint

$X_1 + X_2 + X_3 + X_4 + X_5 + X_6 + X_7 \geq 50$

Now, let us recap what was the mathematical model. Here also we are going to minimize the cost of the bag. And the c_i are the cost matrix and x_i are the variable matrix. So, we are going to multiply each c_i with its own x_i . And here the x_i is not a binary variable rather a continuous variable. And it is subjected to constraints of availability like the variables x_1 amount of limestone, x_2 amount of pyrite, x_3 amount of worm meal, x_4 amount bone meal, x_5 amount of neem cake, x_6 is groundnut cake and x_7 is charcoal.

So, the first constraint is that the x_1 should be greater than equal to 0 and all x_i are greater than equal to 0 which means we need to have some quantity. And the quantity cannot be negative. And we have also been given the availability of these materials. So, x_1 is limited to only 40. The next is 30 60 50 20 30 and 25 which was given in a mathematical model as shown here. The next contain was the bag quantity constraint which shows that the each bag should contain this much amount and the bag quantity should be greater than or equal to 50 kg.

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Mathematical Model

Constraint 3: Quantity constraint [Carbon]

$$0.5 \leq \frac{3.0 \cdot X_1 + 2.5 \cdot X_2 + 1.2 \cdot X_4 + 90 \cdot X_7}{X_1 + X_2 + X_3 + X_4 + X_5 + X_6 + X_7} \leq 1.25$$

So, the last constraint is the quality constraint and we are showing here the quality constraint for the carbon. So, this is here as defined in the lecture. This ratio is how we are going to constrained the quantity in the final objective and the mathematical model. Now as discussed earlier we should not have ratios in the mathematical model. Thus when are going to encode this into our excel file we are going to rearrange this equation and take the quantity of the bag to the lhs and rhs of this equation.

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The screenshot shows an Excel spreadsheet with the following sections:

- Raw Material Data Table:**

Raw material	% of C	% of N	% of P	% of S	% of K	Availability (in kg)	Cost (Rs.)
Lime stone	0	0	0.012	0.011	0	40	100
Pyrite	2.5	0	0.009	0.001	0	30	150
Worm manure	0	0	0.011	0.01	0	40	110
Rock phosphate	1.2	0	0.002	0.009	0	10	120
Basic slag	0	90	0.009	0.002	0	20	100
Superphosphate	0	90	0.012	0.002	0	30	110
Charcoal	0	0	0.002	0.01	0	20	105
- Solution Table:**

Variable assignment	Raw material	% of C	% of N	% of P	% of S	% of K	Availability (in kg)	Cost (Rs.)	Lower Bound of raw material	Upper Bound of raw material
x1	Lime stone	0	0	0.012	0.011	0	40	100	0	40
x2	Pyrite	2.5	0	0.009	0.001	0	30	150	0	30
x3	Worm manure	0	0	0.011	0.01	0	40	110	0	40
x4	Rock phosphate	1.2	0	0.002	0.009	0	10	120	0	10
x5	Basic slag	0	90	0.009	0.002	0	20	100	0	20
x6	Superphosphate	0	90	0.012	0.002	0	30	110	0	30
x7	Charcoal	0	0	0.002	0.01	0	20	105	0	20
- Quantity of Each chemical required:**

Quantity of Each chemical required	43.0	10	0.0240	0
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- Constraint on each chemical quantity:**

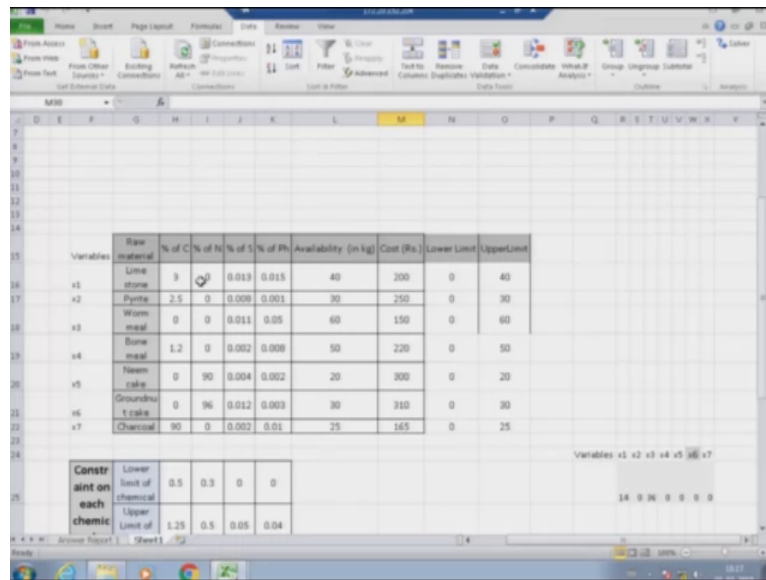
Lower limit of chemical	0.5	0.5	0	0
Upper limit of chemical	1.25	0.5	0.05	0.04
- Variables:**

Cell	\$D\$10	\$E\$10	\$F\$10	\$G\$10	\$H\$10	\$I\$10
Variable	0	0	0	0	0	0
- Objective Function:**

Cell	\$J\$10
Objective Function	0.117791222

So, let us start with encoding the model. We have already created the complete solution file here. And you can see that this is the way which you can create your own spreadsheet for any type of problem. And now let us create the same mathematical model in a spreadsheet from scratch.

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So, this is the new spreadsheet with only the data from the question. And now let us first start by creating the variables.

So, let us take this matrix and we know that we have defined x 1 as the quantity of the raw material of lime stone. So, we will write here x 1 x 2 x 3 x 4 x 5 x 6 and the last x 7. These are the dummy variables and we are not going to use these variables in our modelling, but for demonstration purpose we are going to write it. So, that we do not get confused while we are modelling the equation in the solver tab.

Next is we know the availability in kgs. So, let us define the lower limit and upper limit of this availability. So, the lower limit of all the raw materials is 0. And the upper limit is provided here 40 30 60 50 20 30 and 25.

So, as we have discussed in the previous problem that we are going to give empty cells to the variables. So, let us define the variables here, x 1 x 2 x 3 x 4 x 5 x 6 x 7. And these cells will have the values after we have completed our modelling. So, we can re arrange this. Then we are going to get the quantity of each material.

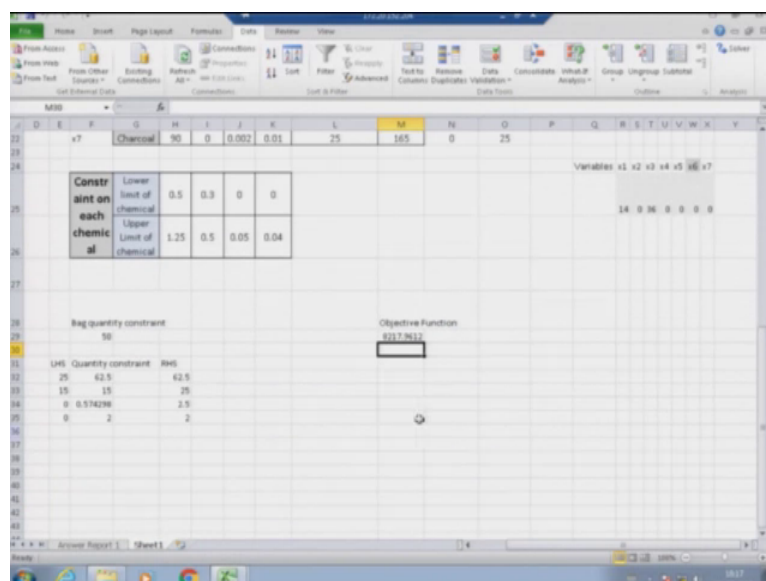
So, this is the data which has given in the question. And we can directly ticket from the question. And you can rearrange this just below all the materials. So, thus as per the question the lower limit of chemical carbon is 0.5 the upper limit is 1.25 the nitrogen has 0.3 as the lower limit 0.5 as the upper limit and so on next let us first see the constraints.

So, the first is the availability constraint, and since we know that if there are no expressions in the constraint we can directly model it into a solver tab. So, we switch to our solver from the data tab and start encoding constraint for the availability. So, first encode the lower limit of the availability.

This is variable x_1 . It should be greater than or equal to 0, x_2 should be greater than or equal to 0, x_3 greater than or equal to 0, x_4 greater than or equal to 0, x_5 greater than or equal to 0, x_6 greater than or equal to 0, and the last x_7 is greater than equal to 0. Now we will encode the upper limit of the availability constraint.

So, again starting from x_1 this is less than equal to 40. So, again x_1 less than equal to 40, x_2 less than equal to 30, x_3 less than equal to 60, x_4 less than equal to 50, x_5 less than equal to 20, x_6 less than equal to 30 and x_7 is less than equal to 25. So, the first constraint has been encoded. Now let us see the second constraint the second constraint is the bag quantity constraint and since it is an expression we first need to encode it into a cell.

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So, close the solver tab and choose a cell of your liking and start encoding the bag quantity constraint.

So, it is the sum of all x_i 's. So, start from x_1 plus x_2 plus x_3 plus x_4 plus x_5 plus x_6 plus x_7 . And now put this into the solver. This should be greater than equal to 50. So, we have encoded the second constraint also. Now is the third constraint and here what we are saying is that the 3 into x_1 here 3 is the percentage of that particular chemical. So, let us see how we are going to encode this first. We will encode the expression in the numerator and as we have already encoded the expression in the denominator we will use the same value from the previous cell.

So, these are the values of the content of carbon in each different raw material. So, let us write the quantity constant here. So, let us start encoding the quantity constraint for the carbon. So, as shown in the constraint it is 3 into x_1 plus 2.05 into x_2 plus 0 into x_3 plus 1.2 into x_4 , plus 0 into x_5 , plus 0 into x_6 plus 90 into x_7 .

So, we have encoded the numerator of the first instance of this quantity constraint. Similarly, we can encode the constraints for nitrogen sulphur and phosphorus and it will be like the same procedure with different column. 0 into x_1 plus 0 into x_2 plus 0 to x_3 plus 0 into x_4 90 plus 96 into x_6 plus 0 into x_7 .

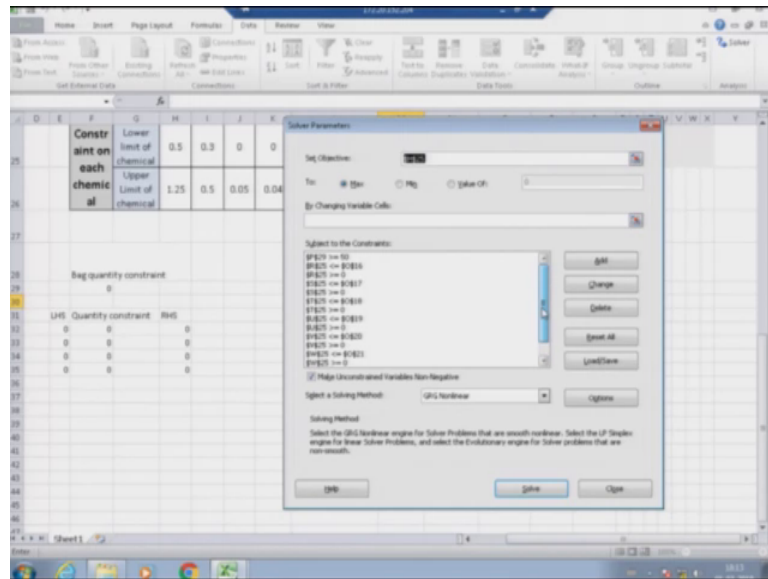
For sulphur it is 0.013 into x_1 and all the following are with similar procedure. So, this is the last percentage of phosphorus and all the following are with similar procedure. And now we need to encode the lower and upper limit as shown in the constraint. So, here we are going to rearrange this equation. Therefore, we need to multiply 0.5 with the total value of the bag.

This is the LHS this is the RHS. So, this is 0.5 into we have encoded the sum of the bag in this cell. So, we will multiply this. Similarly, the lower limit of chemical nitrogen and by following the same procedure we can define the rhs value also.

So, we have encoded all the constraints. And now we are going to encode the objective function. So, let us review what was the objective function. It is the calculation of cost. So, c_i into x_i . So, our cost data is in this column for each raw material and our x_i s are this.

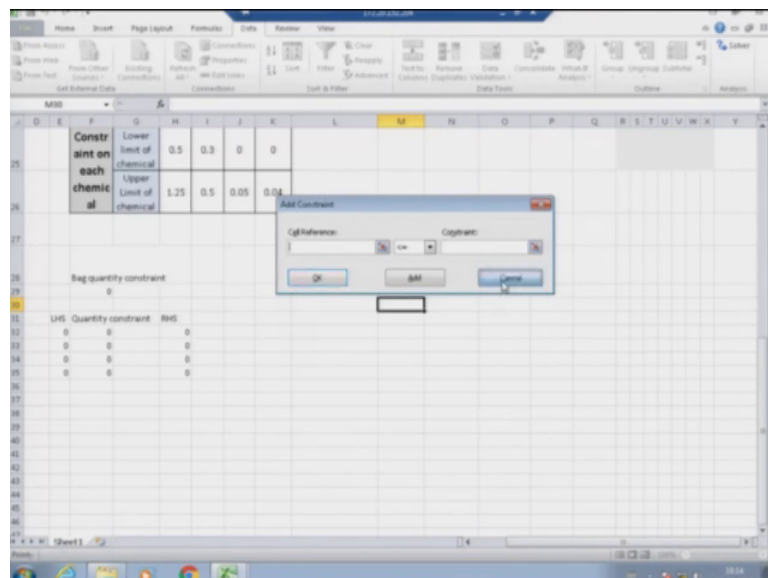
So, let us encode this.

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Now, we need to fill all these new constraints in to our solver tab. So, we have filled the constraints in the solver tab till back quantity constraint. The next we are going to fill is the quantity constraint of each chemical.

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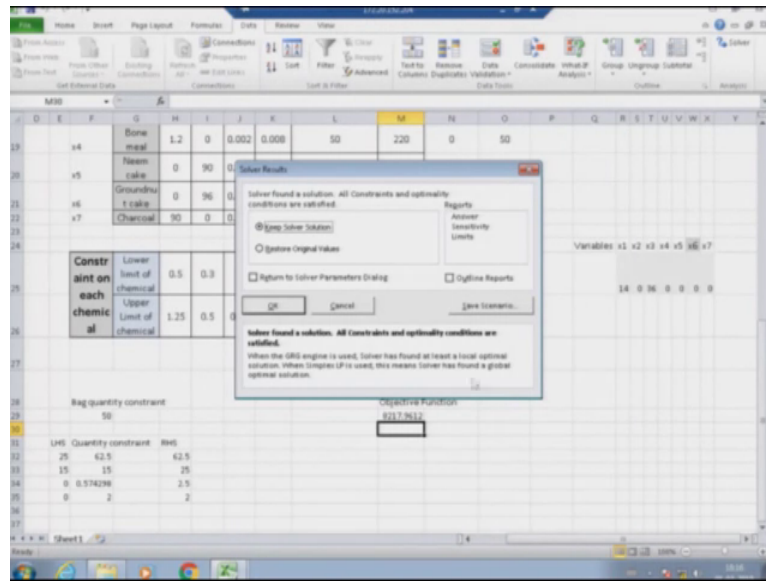


So, by clicking on add let us select this is the cell in which we have encoded the numerator of this constraint. So, select this this should be greater than equal to the lhs.

And similarly this should be greater than equal to lhs. And for the rhs part the same numerator less than equal to rhs.

And finally, the objective function this should be minimised and r variables are in these tabs. So, after creating the constraints which showed crosscheck those constraints every time. So, that there should be no discrepancy. Now we will use simple excel p and solve this.

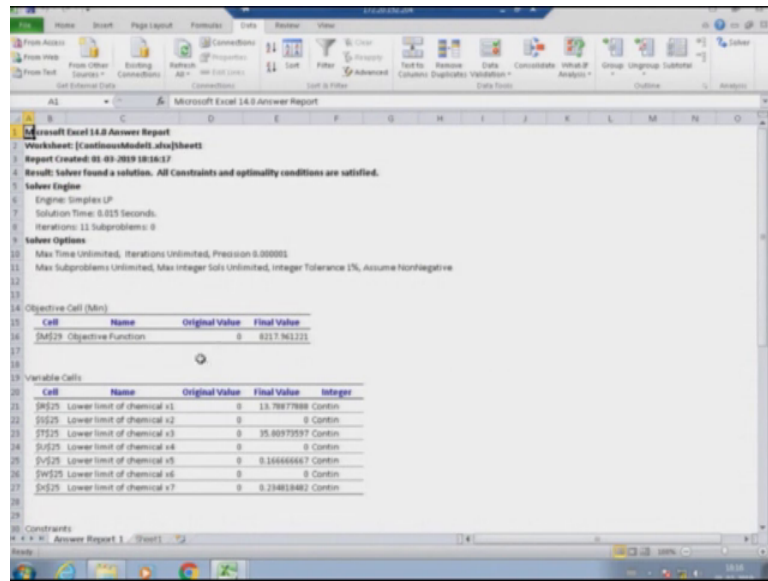
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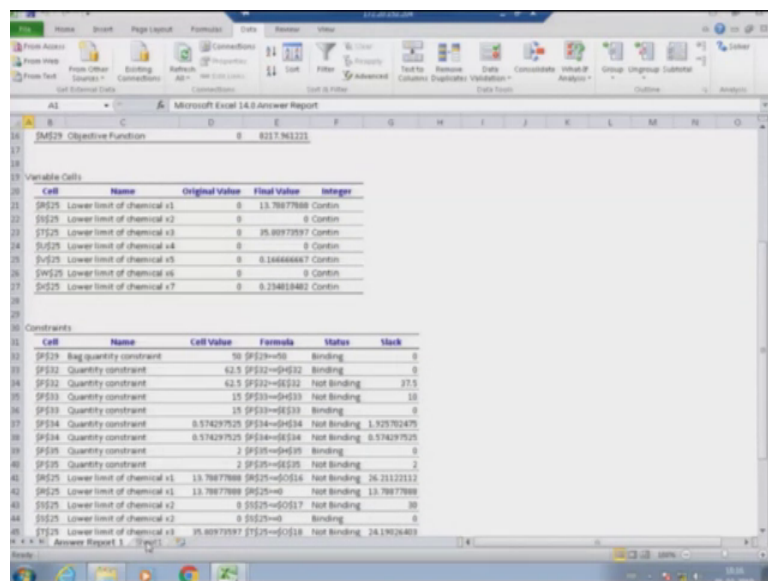
And here the solver is saying that it has found a solution.

Again as previous we can use the answer report to analyse.

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And this will be generated in another spreadsheet and it is showing that the final value is 8 2 1 7 and all the variables will be given some values. You may be wondering why we were using all these 0 values while encoding in the solver tab. Because these type of spreadsheets are future proof.

So, if your values of these nitrogen content or any other value like cost or anything will change. You just need to give the different values in these cells and just solve with the button given in the solver. And it will evaluate all the different values. You do not need to

create these type of spreadsheet from scratch you have to create the new spreadsheet when your problem changes, but for the same problem with different data you just need to enter the new data.

So, this is how we develop these spreadsheet and we create the models so that we can get the optimal solution. And this is it for. Now hope you have got the idea of how to encode a spreadsheet from scratch. We will share these spreadsheet and also please be more active in the forums and discuss any problems which you may have in these spreadsheets.

Thank you.