

Depreciation, Alternate Investment and Profitability Analysis.
Professor Dr. Bikash Mohanty.
Department of Chemical Engineering.
Indian Institute of Technology, Roorkee.
Lecture-3.
Declining Balance Method.



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Declining-Balance (Fixed Percentage) Method

When the declining-balance method is used, the annual depreciation cost is a fixed percentage of the property value at the beginning of the particular year.

The fixed-percentage (or declining-balance) factor remains constant throughout the entire service life of the property, while the annual depreciation is different each year.

Depreciation per annum = (Net Book Value) x Rate%

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Welcome to the course depreciation, alternate investment and profitability analysis, we are continuing with module one that is depreciation. The topic of today's lecture is declining-balance method, this is a depreciation method. When the declining-balance method is used, the annual depreciation cost is a fixed percentage of the property value at the beginning of the particular year.

The fixed percentage or declining-balance factor remains constant through the entire service life of the property, while the annual depreciation is different in each year. The depreciation per annum is equal to net book value into a constant percentage which is given here by rate percent.

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Under these conditions, the depreciation cost for the first year of the property's life is Vf , where f represents the fixed-percentage factor.


Depreciation for 1st year = Vf

Book value at the end of 1st year or start of 2nd year
 Book value = $V - Vf = V(1-f)$

Book Value at the end of 1st year $V_1 = V * (1 - f)$

At the end of the second year $V_2 = V * (1 - f)^2$

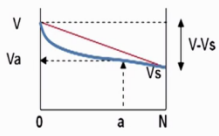
At the end of "a" years $V_a = V * (1 - f)^a$



Under these conditions, the depreciation cost for the first year of the property life is V into f , where f represents the fixed percentage factor. So, we can write down the depreciation for first year is V into f and the book value at the end of the first year or we can say the start of the second year is equal to book value is equal to $V - V$ into f . If we take V common, this is V in the brackets $1 - f$. Book Value at the end of the first year is V_1 , if we consider it to be V_1 , this is equal to V into $1 - f$, at the end of the second year if I consider it to be V_2 then it is V into $1 - f$ whole square and at the end of the 'a' th year, this is V_a is equal to V into $1 - f$ to the power a.

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At the end of N years (i.e., at the end of service life)

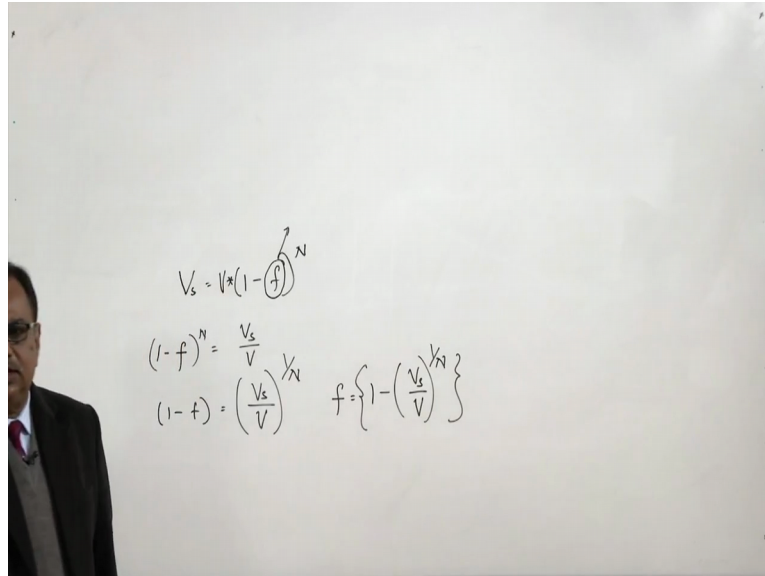


$$V_a = V * (1 - f)^a$$

$$V_s = V * (1 - f)^N$$

Therefore, $f = \left[1 - \left(\frac{V_s}{V} \right)^{\left(\frac{1}{N} \right)} \right] \dots 1$

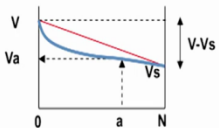




Now, at the end of the Nth year this is obviously, at the end of the Nth year the value becomes V_s that is salvage value and we can write down V_s is equal to V into 1 - f to the power N. So, we can write down here, V_s is equal to V into 1 - f to the power N. now, if this f, the fix factor is unknown. So, from this equation, we can find out this fix factor and this fix factor is f 1 - f to the power N is equal to V_s by V or 1 - f is equal to V_s by V to the power 1 by N or f is equal to 1 - V_s by V to the power 1 - N.

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At the end of N years (i.e., at the end of service life)





$$V_a = V * (1 - f)^a$$

$$V_s = V * (1 - f)^N$$

Therefore, $f = [1 - (\frac{V_s}{V})^{(1/N)}]$...1

Equation (1) represents the textbook method for determining the fixed percentage factor, and the equation is sometimes designated as the **Matheson formula**.

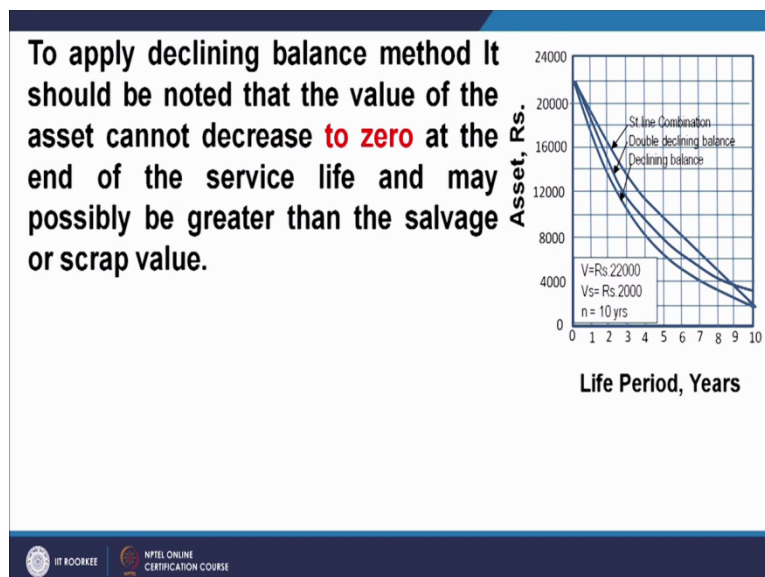
Now, this is the equation to find out, the value of the fixed factor f. Now, we will see that, the depreciation rate is not constant in this declining-balance as shown in the left hand side figure, the depreciation is more, during the, in the straight line this is something like this, and the declining-balance, this is something like this, this is declining-balance. This equation

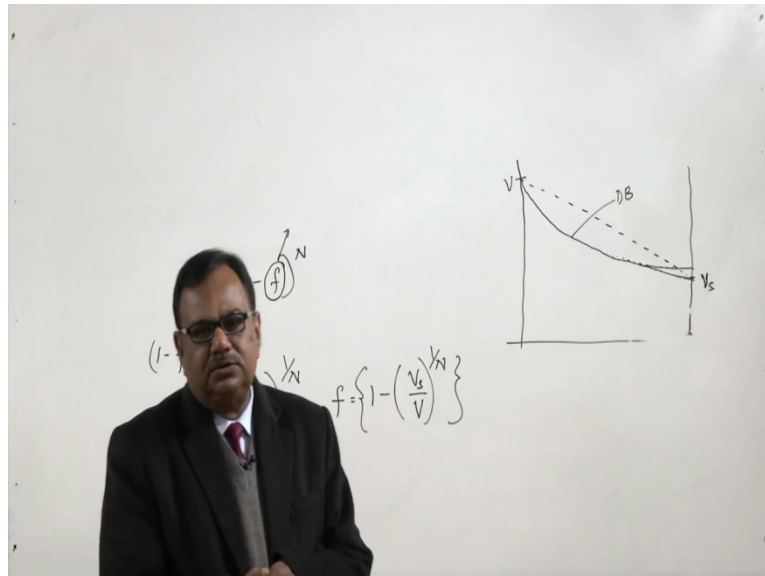
which is equation number one, represents the textbook method for determination of the fixed percentage factor and the equation is sometimes designated as the Matheson formula. Comparison with the straight line method shows that declining-balance depreciation permits the investment to be paid of more rapidly during the early years of the life.

Declining balance method is appropriate where an asset has a higher usage in the early years of its life. For instance, computers and its accessories have better usage in the early years, these also becomes absolute in a span of few years due to advent of new technologies. Use of declining-balance method to depreciate computer equipment would ensure higher depreciation in the early years of its operation.

The increased depreciation cost in the early years are very attractive to concerns just in starting phase of business, why? At the starting phase of business, the company has put a lot of money into the business and it is always short of money, but during that period at the starting phase if it pays more tax or returns the money, more money in terms of tax then it will overload the business. Because the income tax load reduced at the time when it is most necessary to keep all pay out cost at a minimum and this is why if the depreciation cost in the early ages are more than one have to pay less income tax in early ages and for this purpose, declining-balance method is good.

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To apply declining-balance method, it should be noted that the value of the asset cannot decrease to zero at the end of the service life and may possibly be greater than the salvage value or the scrap value. Let me explain this, if I am using, declining-balance method, this is my V_s point, it may reduce to a value which is greater than previous and hence, what is being done after some period of time, one switches to straight line method of depreciation to bring the salvage value to its original value.

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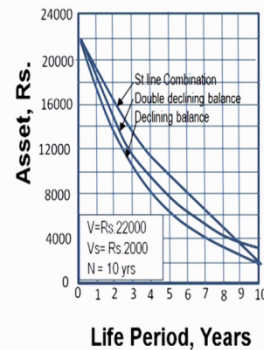
To apply declining balance method It should be noted that the value of the asset cannot decrease to zero at the end of the service life and may possibly be greater than the salvage or scrap value.

To handle this difficulty, it is sometimes desirable to switch from the declining-balance to the straight-line method after a portion of the service life has expired.

Life Period, Years

This is known as the **combination method** as shown in figure. It permits the property to be fully depreciated during the service life, yet also gives the advantage of faster early-life write-offs.

Figure also shows the effect of time on asset value when the declining-balance method of depreciation is used with an arbitrarily chosen value of f .



To handle this difficulty, it is sometimes desirable to switch from the declining-balance to a straight line method as I have done this here, I have switched declining-balance method to straight line method here, switch from the declining-balance to the straight-line method after a portion of the service has expired. This is known as the combination method, as shown in the figure, in the right hand side, it permits the property to be fully depreciated during the service life yet also gives the advantage of faster early-life write-offs.

So, the both properties are combined when I am using a combination method that means, the first recovery in the early period and then reaching to the Vs in the later period when I am using a straight-line method. The figure in the right hand side also, shows, the effect of time on asset value when the declining-balance method of depreciation is used with an arbitrarily chosen value of f .

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Examples of Declining Balance Method

Example-1: The original value of a piece of equipment is Rs 33,000, completely installed and ready for use. Its salvage value is Rs 3000 at the end of a service life estimated to be 10 years. Determine the asset (or book) value of the equipment at the end of 5 years using Declining Balance method.

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Solution of Example-1

Given:
 $V = 33,000$
 $V_s = 3000$
 $N = 10$
 $V_5 = ?$

fixed % factor = $\left[1 - \left(\frac{V_s}{V}\right)^{\frac{1}{N}}\right]$

$f = \left[1 - \left(\frac{3000}{33000}\right)^{\frac{1}{10}}\right]$ Book Value
 $= \left[1 - (0.09091)^{0.1}\right]$ Book Value at the end of
 $= \left[1 - 0.786794\right] = 0.2132$ 5th year = $V_s = V \times (1-f)^5$
i.e. 21.32% $= 33000 \times (1-0.2132)^5$
 $= \text{Rs } 9950.289$

Now, start with the examples and take the first example, the first example is the original value of a piece of equipment is rupees 33,000, completely installed and ready to use, its salvage value is RS 3000 at the end of a service life estimated to be 10 years. Determine the asset or book value of the equipment at the end of 5th year using declining-balance method.

Now, what is given, given V it is equal to 33,000 at the initial value of the asset, Vs is equal to 3000, N is equal to 10 and we need to calculate what is V5. The asset value or the book value at the end of 5th year. Now, the fixed percentage factor is equal to $1 - \left(\frac{V_s}{V}\right)^{\frac{1}{N}}$. Now, here Vs is the salvage value, V is the original value and this factor f is equal to $1 - \left(\frac{3000}{33000}\right)^{\frac{1}{10}}$. So, we can calculate this, this is equal to $1 - 0.786794 = 0.2132$.

3000 divided by 33000 comes out to be 0.09091 to the power 0.1. This is equal to 1 - 0.786794 and this equal to 0.2132 that is 21.32 percent.

Now, we have computed the f factor this comes out to be 21.32 or 21.32 percent. Now, we can calculate book value. Book value at the end of 5th year is equal to V_5 is equal to V into $1 - f$ to the power 5. This is 33000 into $1 - 0.2132$ to the power 5 and this comes about comes to be rupees 9950.289, this is our answer.

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Example-2: The original value of a piece of equipment is Rs 33,000, completely installed and ready for use. Its salvage value is Rs 3000 at the end of a service life. If the fixed % factor for depreciation is 21.33% , determine the service life of the equipment.

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Solution of Example-1

Given:
 $V = 33,000$
 $V_s = 3000$
 $N =$
 $f =$

$$f = \left[1 - \left(\frac{V_s}{V} \right)^{1/N} \right]$$

$N = 10 \text{ years}$

$$\left(\frac{V_s}{V} \right)^{1/N} = 1 - f = 1 - 0.2133 = 0.7867$$

$$\frac{V_s}{V} = \frac{3000}{33000} = 0.090909$$

$$\left(0.090909 \right)^{1/N} = 0.7867$$

$$N = \frac{\ln \left(\frac{V_s}{V} \right)}{\ln (0.7867)}$$

$$= \frac{\ln (0.0909)}{\ln (0.7867)}$$

The second example is, the original value of a piece of equipment is 33000, completely installed and ready for use. Its salvage value is rupees 3000 at the end of a service life. If the fixed percentage factor for depreciation is 21.33 percent, determine the service life of the equipment. Now, we do not know the value of N where the value of f is given, 0.2133. So,

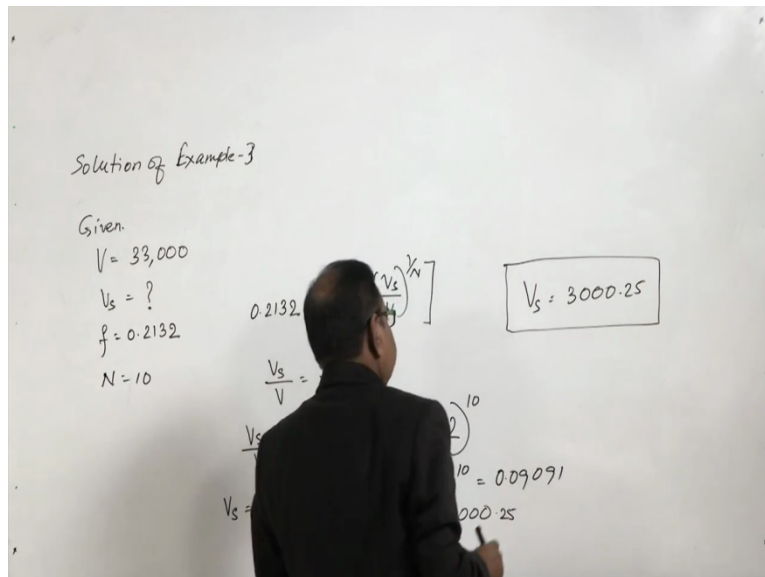
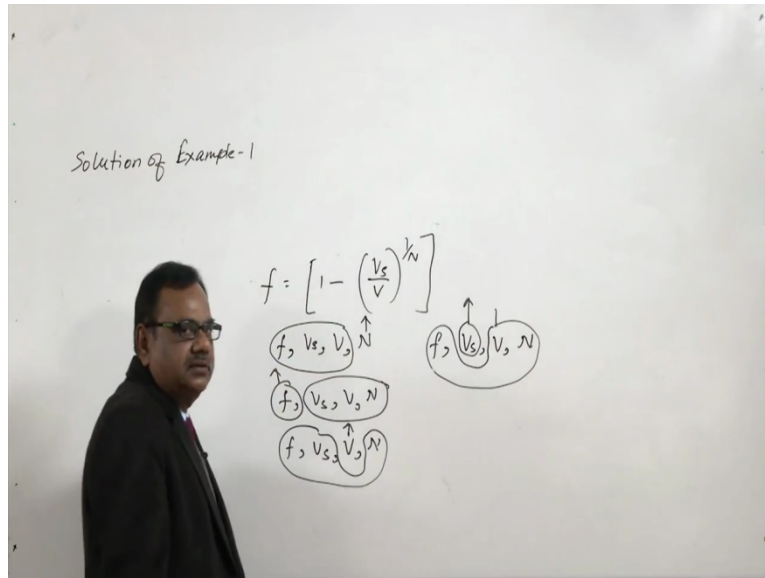
my V is given the original value of the equipment, V_s is given 3000, f is given 0.2133 but N is not given, I have to calculate the value of N .

Now, we start with our formula first, percentage factor is equal to $1 - V_s$ by V to the power 1 by N or V_s by V to the power 1 by N is equal to $1 - f$ and this is equal to $1 - 0.2133$ which is equal to 0.7867. Now, if we calculate V_s by V , this is 33000 divided by, sorry this is 3000 by 33000, and which comes out to be 0.090909. So, 0.090909 to the power 1 by N is equal to 0.7867.

Now, if I take $\log N$ is equal to $\log V_s$ by V divided by $\log 0.7867$ this is equal to $\ln 0.090909$ divided by $\ln 0.7867$ and this is equal to 9.995 or I can say 10 years. So, this is the answer of the example number two. So, N is 10 years. Let us move to example number three, again the same numerical is used but with a twist.

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Example-3: The original value of a piece of equipment is Rs 33,000, completely installed and ready for use. The service life of the equipment is 10 years. If the fixed % factor for depreciation is 21.32%, determine the salvage value of the equipment.



The original value of a piece of equipment is rupees 33000 completely installed and ready for use. The service life of the equipment is 10 years if the fixed percentage factor for depreciation is 21.32 percent, determine the salvage value of the equipment. Basically, here I would like to explain our basically equation is f is equal to $1 - V_s$ by V to the power N . This is the equation every time I am using to calculate different values.

Here, if we see in this equation the variables are f , V_s , V and N . So, there are 4 variables and this is a single equation and the single equation can only give the value of a single unknown, that means if I supply the values of these three, I can calculate out N or if I supply the value of these three, I can calculate this one or if I supply value of these three, I can calculate this or if I supply of this, then I can calculate this one.

So, this is how the questions are framed. In this case, we have to find out what is value of V_s . So, f is given, V is given and N is given. So, this is example number three, given V is given 33000, V_s is unknown, f is equal to 0.2132, N is equal to 10. So, we have 0.2132 is equal to $1 - V_s$ by V to the power one by N . Now, V_s by V is equal to 3000 divided by 33000 . Here, we do not know the value of V_s basically this is unknown, this is unknown.

So, I can write down V_s by V is equal to $1 - f$ to the power N is equal to $1 - 0.2132$ to the power 10, this comes out to be, this is 0.7868 to the power 10, to the power 10 comes out to be 0.09091 . So, V_s is equal to 33000 into 0.09091 is equal to rupees into 33000 comes to be 3000 , 25paise. So, my answer is V_s is equal to.

Now, let me summarize today's lecture. The monetary value of an asset decreases over time due to use wear and tear or obsolescence. This decrease measured as depreciation and can be used as a means of distributing the original cost of a physical asset over the life period during which the asset is in use employing many methods. The present lecture demonstrates how to use declining-balance method for depreciation computations and also shows where you should use declining-balance method and what benefits you can extract using declining-balance method in taxation. Thank you.