

Integrated Circuits, MOSFETs, OP-Amps and their Applications
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Lecture – 19
Operational Amplifier Configurations

Welcome to this module and here we will see the application of operational amplifiers. So, until what we were learning in the previous lecture were the characteristics of an operational amplifier. So, when you talk about the characteristics; we have seen several characteristics operational amplifier including its input impedance it is out impedance high gain.

And then we have seen how offset voltages comes into play? What is input bias current? And then we have seen how CMRR comes into play? And what exactly CMRR is? And how the CMRR should be if it is very high? How it is useful to get the actual output voltage of our desired value and we can reduce the common mode voltage if the CMRR is extremely high; we have seen that example as well.

We have also seen how can we use the operational amplifier? And what kind of circuits we can use to nullify the effect of the offset? How can be offset the output voltage such that our output would be nullify? Or output should be 0; that means, that when we apply ground to both the terminals our output should be 0; so, what we can do?

So, we have seen that circuit that we can connect between terminal 1 and terminal 5; a potentiometer and by changing the value of the potentiometer, we will be able to see the output voltage equal to 0. Then we have also seen the input effect of input bias current, input offset current and how we can determine given the values of input offset and input bias current? Or input currents when you are given then how can you determine those values? So, once we have understood and we have also seen about the virtual ground.

Very important concept of virtual ground we have also seen; now using all these things that is our basic how we can implement the different operation on the five circuits? That is the idea that is today's lecture. So, this lecture is our class 10 and our lecture 10 and it is divided into several modules; so, to help you out to understand how the Op-amp circuits can be designed.

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Op-Amp Circuits

Typical Op-amp circuit configurations include the:

- Unity Gain Buffer (Voltage Follower)
- Inverting Amplifier
- Noninverting Amplifier
- Summing Amplifier
- Integrator
- Differentiator

Note: the integrator and differentiator are considered active filters

So, when you talk about operational amplifier circuits; what we see? We see that the operational amplifier circuits configuration includes several different applications starting from the unity gain amplifier or unity gain buffer; then we have seen inverting amplifier, then we will see inverting amplifier non inverting amplifier, then we will see summing amplifier, we will see integrator, we will see differentiator and not only that we will also see filters.

So, that is would be this filters would be our next lecture, for this particular lecture we will see the following amplifiers, we will take few problems and we will try to solve it. So, we understand how we can design operation amplifier based circuits.

So, like we have seen there are several kind of circuits we should start understanding the first one; which is the voltage follower circuits.

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Voltage Follower

The voltage follower

- Unity-gain buffer based on noninverting configuration
- Equivalent voltage amplifier model:
 - Input resistance of the voltage follower $R_i = \infty$
 - Output resistance of the voltage follower $R_o = 0$
 - Voltage gain of the voltage follower $A_{vo} = 1$
- The closed-loop gain is unity regardless of source and load
- It is typically used as a buffer voltage amplifier to connect a source with a high impedance to a low-impedance load

*↑
High Z_i
Low Z_o*

High Z_i *Low Z_o*

So, if you can see on the screen; what we see is a unity gain buffer based on non inverting configuration; what does that mean? That if I apply a voltage at the non inverting input and I have a feedback to the inverting; the output is feedback to inverting here. This becomes our unity gain buffer based on non inverting configuration because we are applying voltage to the non inverting amplifier.

We have seen this application earlier also equivalent voltage amplifier model. So, if I make a equivalent voltage amplifier model; how can I use it? You can see that the input resistance of the voltage follower; input resistance is infinite; output resistance is 0.

Voltage gain of the indicate amplifier that is why this is called unity gain. Unity gain means what? Gain is 1; so, to have gain equal to 1, we have A_{vo} voltage gain equal to 1; the closed loop gain is unity regardless of source or load.

So, this is our indicate amplifier; it is also used as a buffer voltage amplifier to connect a source with high input impedance to a low input impedance load; why? Because the indicate amplifier has a high input impedance and it has a low output impedance; that means, it can be connected to a source. Suppose the source Z_i is this one, which has extremely high input impedance; then we can connect the unity gain amplifier. And the load will have extremely low output impedance.

Then we can connect the unity gain amplifier, unity gain amplifier is also used as a last stage of most of the amplifying circuit because it is a voltage follower and will it can be connected to any load which will draw lot of current, but the voltage at the input will be same at the output.

The voltage will follow; whatever voltage is at input it will follow at the output. So, output voltage follows the input voltage that is why it is also called voltage follower; the gain is 1 that is why is it is also called unity gain amplifier. So, these are the characteristics of operational amplifier particular as a voltage follower; this is how we can use operational amplifier as a voltage follower.

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Inverting Amplifier

The inverting close-loop configuration

- External components R_1 and R_2 form a close loop
- Output is fed back to the inverting input terminal
- Input signal is applied from the inverting terminal

Inverting-configuration using ideal op amp

- The required conditions to apply **virtual short** for op-amp circuit:
 - Negative feedback configuration
 - Infinite open-loop gain
- Closed-loop gain: $G \equiv v_O/v_I = -R_2/R_1$
 - Infinite differential gain: $v_2 - v_1 = v_O/A = 0$
 - Infinite input impedance: $i_2 = i_1 = 0$
 - Zero output impedance: $v_O = v_1 - i_1 R_2 = -v_1 R_2/R_1$
- Voltage gain is negative
 - Input and output signals are out of phase
- Closed-loop gain depends entirely on external passive components (independent of op-amp gain)
- Close-loop amplifier trades gain (high open-loop gain) for accuracy (finite but accurate closed-loop gain)

Now, let us see further; the inverting amplifier; so, how we can design a circuit of an inverting amplifier using a Op-amp? So, the inverting close loop configuration external components R_1 and R_2 form a close loop; here you can see R_1 and R_2 , this forms a closed loop because you are feeding back a R_2 here and input signal is applied from the inverting terminal. So, we are applying the input to the inverting terminal.

So, three things we have to understand external components R_1 and R_2 that forms closed loop, second output is fed back to the inverting input and third is that input signal is applied to the inverting terminal. Now, the required condition to apply virtual shot up on circuit is negative feedback and infinite open loop gain; these are the requirements is

not it? So, what if there is a closed loop gain? So, close loop gain G equals to v_o by v_i which is nothing, but minus R_2 by R_1 .

See if I see here; you see at this point it will be virtual ground; we have seen the concept of virtual ground because this terminal is grounded, our inverting terminal is grounded that is why the point at non inverting terminal will also be considered as ground; the virtual ground. So, if I have register R_1 ; I apply voltage V_1 then the current flowing through my register R_1 would be nothing, but i equals to v_1 ; by R_1 .

Similarly if I want to measure the current flowing through R_2 ; it will be nothing, but i_2 equals to i_1 equals to v_1 by R_1 . So, what will be my output voltage? It is 0 here; here voltage is 0 because nothing will flow here it is a infinite input impedance and a very high input impedance and the difference voltage is also 0 volt. So, if I want to measure v_o ; v_o is nothing, but 0 minus v_1 by R_1 into R_2 . So, what will be v_o ? v_o will be nothing, but minus R_2 by R_1 .

Now if you see infinite differential gain; infinite differential gain is v_2 minus v_1 is nothing, but v_o by A is nothing, but 0; infinite differential gain would be 0. Because the infinite differential gain, the value here is 0 infinite input impedance we know that it has infinite input impedance; that means, my i_1 equals to i_2 equals to 0, then you have 0 output impedance; that means, my output voltage will be nothing, but v_o equals to v_1 minus i_1 ; R_2 that is correct, v_o equals to what? v_1 minus i_1 into R_2 because you see here is same this R_2 . So, I have v_o equals to nothing, but v_o equals to V_1 minus i_1 ; R_2

So, if I substitute the value what will I have? Output equals to minus V_1 ; R_2 by R_1 . Now if I take voltage gain is negative because my inverting amplifier my voltage gain is minus R_2 by R_1 ; my gain is minus R_2 by R_1 , voltage gain then we can multiply by input. So, voltage gain is what? Negative.

Input and output signals are out of phase; this is another concept and we have seen this concept. Let us see when you talk about out of phase; out of phase is nothing, but when we apply the input to the inverting terminal which is over here.

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Inverting Amplifier

The inverting close-loop configuration

- External components R_1 and R_2 form a close loop
- Output is fed back to the inverting input terminal
- Input signal is applied from the inverting terminal

Inverting-configuration using ideal op amp

- The required conditions to apply **virtual short** for op-amp circuit:
 - Negative feedback configuration
 - Infinite open-loop gain
- Closed-loop gain: $G \equiv v_O/v_I = -R_2/R_1$
 - Infinite differential gain: $v_+ - v_- = v_O/A = 0$
 - Infinite input impedance: $i_2 = i_1 = 0$
 - Zero output impedance: $v_O = v_- - i_1 R_2 = -v_I R_2/R_1$
 - Voltage gain is negative
 - Input and output signals are out of phase
 - Closed-loop gain depends entirely on external passive components (independent of op-amp gain)
 - Close-loop amplifier trades gain (high open-loop gain) for accuracy (finite but accurate closed-loop gain)

It is applied to the inverting terminal input is signal like this, output will be multiplied or amplified version of the input. Output would be amplified version of the input and that amplification depends on the value of R_2 by R_1 .

But is it in phase or out of phase? This is in phase signal, but in case of inverting; you will see that the output would be amplified, but out of phase; it will be magnified, but generally 180 degree out of phase; if this is 0 degree, it is 180 degree out of phase. So, that is what is written here that input signals and output signals are out of phase.

Next closed loop gain depends entirely on external passive components; why? Because we have R_2 and R_1 ; so, this is external passive component, R_1 is resistor, R_2 is resistor; these are externally connected to the Op-amp that is why they are external passive; passive components. And our gain, this is a closed loop if you see this amplifier it is in close loop configuration. Now closed loop gain depends on the value of R_2 and R_1 and that is why we can say that the close loop gain depends entirely on external passive components.

Close loop amplifier trades gain for accuracy; that means, that here we do not have extremely high gain, but we can change the gain and we can have finite, but accurate closed loop gain. So, accuracy is better here, but we have finite closed loop gain, but in case of no feedback you will have infinite gain, this is the inverting amplifier.

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• Inverting Amplifier const. ...

- Equivalent circuit model for the inverting configuration
 - Input impedance: $R_i \equiv v_i / i_i = v_i / (v_i / R_1) = R_1$
 - For high input closed-loop impedance, R_1 should be large, but is limited to provide sufficient G
 - In general, the inverting configuration suffers from a low input impedance
 - Output impedance: $R_o = 0$
 - Voltage gain: $A_{v_o} = -R_2 / R_1$

$1 / (1/R_1) = R_1$

$V_o = \left(\frac{-R_2}{R_1} \right) \times V_i$ $V_o = - \times V_i$

Now, if I draw equivalent circuit model of inverting configuration; what will I have? I have R_1 , my gain is minus R_2 by R_1 into v_i ; I have output voltage v_o , input voltage v_i . So, input impedance is nothing, but R_i equals to v_i by i or v_i by i equals to v_i divided by v_i by R_1 that is correct; which is nothing, but v cancel or this value will be cancelled. So, it is nothing, but 1 divided by 1 by R_1 which is equal to R_1 ; that means, my input impedance will depend on the value of register R_1 .

For high input close loop impedance; R_1 should be large, but is limited to provide sufficient G; what does that mean? That if I have A_v equals to what is my gain here? R_2 by R_1 ; isn't it? And if I say output voltage; v_o is nothing, but R_2 by R_1 into input voltage v_i . Now what we are saying here? That for high input closed loop impedance, what we should have? We should have R_1 extremely high; R_1 value should be extremely high. So, if I put R_1 extremely high; what will happen? My output would be similar to my input.

Let us say if R_1 is infinite or closed infinite; this R_2 value R_2 by R_1 will be extremely small into v_i into v_i . So, I cannot do that R_1 can be extremely high, this is not possible otherwise this will not work properly. So, what is written? But is limited to provide sufficient gain, we have to use very high value of R_1 , but we have to also understand what is the gain of our amplifier? For example, if I want to have gain of amplifier to be 100; then I can have R_2 which is 100, but R_1 ; I cannot have 100, I can only have 1.

So, if I have gain of; so, I can have R 2 equal to 100 K; R 1 equal to 1 K; you see. So, it is limited by this gain; even we want higher. If I put like 10 K here, my gain will not be 100; my gain will become 10 because gain is nothing, but minus R 2 by R 1. So, it is limited to provide sufficient gain; this is an example which we have seen.

Now in general, the inverting configuration suffers from low input impedance; you see her why? Because you see here only R 2 by R 1; if I want to have gain of 100; my R 1 would be 1 K; if I select R 2 equal to 100; a 1 K is extremely small, but in reality we should have R 1 or in input impedance extremely high.

So, in case of inverting amplifier the low input impedance is a problem or in another terms inverting amplifier configuration suffers from a low input impedance. Output impedance is 0; voltage gain is nothing, but minus R 2 by R 1 easy? Super easy right?

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Example 1: Inverting op-amp

Find the closed loop gain of the following inverting amplifier circuit

• **Solution**

Given $R_f = 100 \text{ k}\Omega$ and $R_{in} = 10 \text{ k}\Omega$

The gain of the inverting op-amp

$$A_v = V_{out}/V_{in} = -R_f/R_{in}$$

$$A_v = 100 \text{ k}/10 \text{ k} = 10$$

Therefore, the closed loop gain of the inverting amplifier circuit is 10 or 20 dB ($20\log(10)$)

Handwritten calculation:

$$A_v = V_{out}/V_{in} = \left| -\frac{R_f}{R_{in}} \right| = \frac{-100}{10} = -10 = 10$$

So, let us solve an example. So find the closed loop gain of following inverting amplifier circuit. You are given a circuit and you are asked to find the closed loop gain; now we are already given R in 10; R F 100, then what is our A v? A v is nothing, but V out by V in or we can write minus R F by R in 100 by 10 both is kilo ohms; so I do not write itm that is fine. So, what I have? Minus 10, but gain cannot be minus, so we always write is equal to 10; gain is equal to 10.

So, if I want to understand the closed loop gain; my closed loop gain of the inverting amplifier circuit is 10 or 20 dB or 20 log 10. So, this is how I can understand my inverting amplifier.

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Example 2: Inverting op-amp

The gain of the original circuit is to be increased to 40 (32dB), find the new values of the resistors required

Solution

Given $A_v = 40$

Since, the gain of the inverting op-amp is

$$A_v = R_f / R_{in}$$

$$A_v = 40 = R_f / R_{in}$$

Let us assume input resistance $R_{in} = 10 \text{ k}\Omega$

$$R_f = A_v * R_{in} = 40 * 10 \text{ k}\Omega = 400 \text{ k}\Omega$$

$A_v = 40 = \frac{R_f}{R_{in}} \Rightarrow R_f = 40 \times R_{in}$
 $R_f = 400 \text{ k}\Omega$

Let us see one more example; so, the inverting amplifier, the gain of the original circuit is to be increased by 40 dB. Find the values of resistors; see we are not given the values of register. Now, what is given? That we have to increase the gain to 40 dB or 40 or 32 dB; so, what will be value of resistors? That is the question.

So, given A_v equals to 40; it is already given, gain is 40. Now since it is an inverting Op-amp; is it inverting Op-amp? Yes because we are providing input to the inverting terminal. So, what will be my A_v ? A_v will nothing, but A_v would be R_f by R_{in} . So, 40 equals to R_f by R_{in} ; so, if I assume that my R_{in} ; let us say it is 10 kilo ohm; then my R_f would be what? See I have this formula, I have A_v equals to 40, equals to R_f by R_{in} implies R_f equals to 40 into R_{in} .

If I assume R_{in} to be 10 kilo ohm, my R_f would be 400 kilo ohms; very easy super easy. If I consider R_{in} as 1 kilo ohm; then my R_f would be 40 kilo ohms, if I assume my R_{in} equal to 10 kilo ohm; R_f would be 100 kilo ohms. So, this is how we can solve the question for the inverting amplifier.

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Example 3: Inverting op-amp

Find V_N , V_1 and V_o for the circuit shown in the figure

Solution

Apply KCL at Node N,

$$I_3 + I_4 = 0$$

$$\frac{V_N}{10k} + \frac{(V_N - V_o)}{20} = 0$$

$$2V_N + V_N = V_o$$

$$V_N = V_o/3$$

Now, $V_o - V_1 = 6$ and $V_N = V_1$ as per virtual ground

Therefore, $V_o - V_N = 6$

$$V_o = V_N + 6$$

$$V_o = V_o/3 + 6$$

$$V_o = 9V$$

and $V_N = V_1 = 3V$

Handwritten notes:

$$V_N = \frac{V_1}{R_3} = \frac{V_1}{10k}$$

$$I_3 = \frac{V_1 - V_N}{R_3} = \frac{V_1 - V_1}{10k} = 0$$

$$I_4 = \frac{V_N - V_o}{R_4} = \frac{3 - 9}{20k} = -\frac{6}{20k}$$

$$V_N = V_o/3 = 9/3 = 3V$$

Let us see one more example; I am giving you more example, so that you can understand when you are given a circuit; how can you solve the problem? So, find V_N ; V_1 , V_o for the circuits shown here; for this particular circuit, we have to find lot of things; so, let us see. So, if I use the circuit first at node N; I have to here, I have to find. So, I will use Kirchhoff current flow at node N and what will I have? I will have I_3 and I have I_4 here. So, that will be I_3 plus I_4 equal to 0; according to Kirchhoff current this will be I_3 plus I_4 equals to 0.

Now, what is I_3 ? I_3 is nothing, but V by R ; what is V ? V is my V_N ; what is R ? R is my 10 kilo ohm; V_N 10 kilo ohm. So, I substitute these value correct; plus I_4 what is I_4 ? I_4 is here, I_4 is nothing, but you see here, you see here. So, it is like V_N minus V_o divided by R_4 correct V_N ; so, from here I_3 is what? I_3 will be my V_N by 10 kilo ohm, which is my R_3 ; I_3 will be V_N by R_3 which is V_N by 10 kilo ohm. And I_4 equals to V_N minus V_o by R_4 equals to V_N minus V_o divided by 20 kilo ohms.

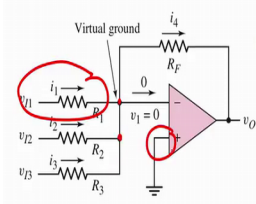
This is what I have written here, so from here when you solve it; you will find that V_N equals to V_o by 3. Now V_o minus V_1 equals to 6 and V_N equals to V_1 ; as per virtual ground, V_o minus V_1 equals to 6. Because here see; what is the bias voltage? 6 volt; that is applied across the 3 and V_o ; so, if I say V_o minus V_1 ; V_o this voltage minus this voltage is nothing, but 6 volts.

And V_N ; this V_N this voltage V_N should be equal to this voltage V_1 ; why? Because by the concept of virtual ground. So, what we have? V_o minus V_1 equals to 6 and V_N equals to V_1 ; so, therefore, V_o minus V_N equals to 6. So, V_o will be V_N plus 6; so, V_o would be V_N plus 6; V_N is what? V_N is V_o by 3. So, I will put V_o by 3 plus 6; so, V_o would be nothing, but 9 volts.

Now, I know that V_N equals to V_1 equals to 3 volts; how? Because I know V_N equals to V_o by 3 equals to 9 by 3; equals to 3 volts. V_N equals to V_o by 3; this is 3 equals to what is V_o ? V_o is 9 volts; so, 9 Volts by 3 which is nothing, but my 3 volts. So, this is how I can find; what is the V_N , V_1 and V_o for a given circuit; when you are given a circuit of an inverting amplifier.

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Summing Amplifier



Example:
Design a summing amplifier as shown in figure to produce a specific output signal, such that $v_o = 1.25 - 2.5 \cos \omega t$ volt. Assume the input signals are $v_{i1} = -1.0$ V, $v_{i2} = 0.5 \cos \omega t$ volt. Assume the feedback resistance $R_F = 10$ k Ω

Solution: output voltage

$$v_o = -R_F \left(\frac{v_{i1}}{R_1} + \frac{v_{i2}}{R_2} + \frac{v_{i3}}{R_3} \right) = -R_F \left[\frac{(-1)}{R_1} + \frac{0.5 \cos \omega t}{R_2} \right]$$

Or, $1.25 - 2.5 \cos \omega t = R_F \left[\frac{1}{R_1} - \frac{0.5 \cos \omega t}{R_2} \right]$

Or, $1.25 - 2.5 \cos \omega t = \frac{R_F}{R_1} - \left(\frac{R_F}{R_2} \right) (0.5 \cos \omega t)$

So, the DC input line contains the resistance R_1 can be calculated as

$$\frac{R_F}{R_1} = 1.25 \quad \text{Or,} \quad R_1 = \frac{R_F}{1.25} = \frac{10}{1.25} = 8 \text{ k}\Omega$$

Similarly the time varying signal input line contains the resistance R_2 as

$$\left(\frac{R_F}{R_2} \right) (0.5 \cos \omega t) = 2.5 \cos \omega t \quad \text{Or,} \quad R_2 = R_F \times \frac{0.5 \cos \omega t}{2.5 \cos \omega t} = 10 \times \frac{0.5}{2.5} = 2 \text{ k}\Omega$$

Using KCL at the input node
 $i_1 + i_2 + i_3 - i_4 - 0 = 0$

Output voltage
 $V_o = -R_F \left(\frac{V_{i1}}{R_1} + \frac{V_{i2}}{R_2} + \frac{V_{i3}}{R_3} \right)$

Now, let us see an example of a summing amplifier. So, what is summing amplifier? Let us see the circuit; so, when you see the circuit; what do you find is that when you use inverting amplifier; if you come back on the screen, you will see that we are using a inverting amplifier, we have a feedback register, but instead of one input register; you have three; you can have n input registers. So, n inputs and the output will be summation of all the inputs. So, how can you do that? It is written over here, if you are given this circuit; then using Kirchhoff current law what we can find? We can find, i_1 these values i_1 , i_2 , i_3 three values I get. So, i_1 plus i_2 plus i_3 minus i_4 ; here and here you see this configuration minus 0 equals to 0

So, output voltage would be what? V_o equals to minus R_F ; am I right? Why? Because it is inverting amplifier; this is the inverting amplifier. So, inverting amplifier our formula is R_F by input resistance R_{in} ; here first is V_1 by R_1 ; why? Because R_F into V_1 here' V_1 by R_1 plus V_2 by R_2 plus V_3 by R_3 ; that means, output voltage is the summation of the input voltage and you can change the gain with the help of R_F and input registers.

That means, it is not only providing a summation; it is also providing the amplification, and that is why; what we say is this is an; summing amplifier. Now here you can see very easily that the concept about virtual ground will come here, here and here this is nothing, but because the non inverting terminal is grounded; the voltage at the inverting terminal is also considered as 0 which is your virtual ground.

Now, if you are given an example which is over here in front of you; this example a design a summing amplifier as shown in figure to produce a specific voltage such that v_o equals to this; assume that v_1 is this, v_2 is this and feedback register R_F is of 10 kilo ohm value.

Now, if you see closely; you are given v_{in1} ; you are given this voltage which is your v_{in1} here; you are given v_{in2} , but you are not given anything about v_{in3} here; are you given anything about v_{in3} . So, we do not have to assume there is v_{in3} or v_{in3} equals to 0. Now we can just; we know this formula which is similar to here; this formula for summing amplifier, we will substitute the value; so, minus R_F remains as it is here.

What is V_{i1} ? V_{i1} is minus 1 volt divided by R_1 plus what is V_{i2} ? V_{i2} is nothing, but $0.5 \cos \omega t$ by R_2 ; now what is V_o ? V_o is given as 1.25 minus $2.5 \cos \omega t$; equals to R_F into this value.

So, if I further solve it; what will I have? 1.25 minus $2.5 \cos \omega t$ equals to R_F by R_1 ; minus R_F by R_2 into $0.5 \cos \omega t$. So, the DC input line contains resistance R_1 and that can be calculated as nothing, but R_F by R_1 equals to 1.25 ; this is very easy; here you see this value R_F by R_1 or R_1 equals to R_F by 2.5 ; what is R_F ? R_F is given 10 kilo ohm; so, R_1 equals to 8 kilo ohm.

Similarly, time varying signal input line contains R_2 ; you can see here, you see the point here you have to understand is; when you are considering DC input line, then you can

see DC input line; it contains this value, but point varying signal; this contains this value; point varying signal which is this one; it will have $2.5 \cos \omega t$. So, I can write R_F by R_2 into $0.5 \cos \omega t$ is nothing, but this particular equation or R_2 is nothing, but this value or further if I solve it; R_2 would be 2 kilo ohms.

Thus I have found the value of R_1 , I have found the value of R_2 and now I can put this value and design a summing amplifier; it is very easy; let us quickly once again see what we have done with summing amplifier. Summing amplifier is nothing, but an inverting amplifier connected in a way that you have a lot of input voltages; more than one input voltage.

So, here you can see; so, this is you can take a summation of those input voltages; it can be N numbers; like this it can be until N, this is R_N ; i_N ; V_{iN} ; N times. So, point is that the formula is very easy v_o equals to; feedback register R_F since this is inverting. So, minus R_F by R_1 we have seen.

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Summing Amplifier

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Design a summing amplifier as shown in figure to produce a specific output signal, such that $v_o = 1.25 - 2.5 \cos \omega t$ volt. Assume the input signals are $v_{i1} = -1.0$ V, $v_{i2} = 0.5 \cos \omega t$ volt. Assume the feedback resistance $R_F = 10 \text{ k}\Omega$

Solution: output voltage

$$v_o = -R_F \left(\frac{v_{i1}}{R_1} + \frac{v_{i2}}{R_2} + \frac{v_{i3}}{R_3} \right) = -R_F \left[\frac{(-1)}{R_1} + \frac{0.5 \cos \omega t}{R_2} \right]$$

Using KCL at the input node

$$i_1 + i_2 + i_3 - i_4 - 0 = 0$$

Output voltage

$$v_o = -R_F \left(\frac{V_{i1}}{R_1} + \frac{V_{i2}}{R_2} + \frac{V_{i3}}{R_3} \right)$$

So, the DC input line contains the resistance R_1 can be calculated as

$$\frac{R_F}{R_1} = 1.25 \quad \text{Or,} \quad R_1 = \frac{R_F}{2.5} = \frac{10}{2.5} = 8 \text{ k}\Omega$$

Similarly the time varying signal input line contains the resistance R_2 as

$$\left(\frac{R_F}{R_2} \right) (0.5 \cos \omega t) = 2.5 \cos \omega t \quad \text{Or,} \quad R_2 = R_F \times \frac{0.5 \cos \omega t}{2.5 \cos \omega t} = 10 \times \frac{0.5}{2.5} = 2 \text{ k}\Omega$$

v_o equals to minus R_F by R_1 into V_1 ; this is inverting amplifier. Now here we have minus R_F by R_1 into V_1 plus we have or minus plus we can also write minus R_F by R_1 into V_2 plus; again we have minus R_F by R_3 ; this is R_2 into V_3 .

So, if I solve this; I will have this equation once I know this equation, if I am given a problem which is shown here; that for the given output voltage, if you have two signals;

input signals and you have feedback registers, then we can solve the value of R 1 and R 2 because there are only two because there are only two voltages V 1 and V 2.

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Summing Amplifier

Example:
Design a summing amplifier as shown in figure to produce a specific output signal, such that $v_0 = 1.25 - 2.5 \cos \omega t$ volt. Assume the input signals are $v_{i1} = -1.0$ V, $v_{i2} = 0.5 \cos \omega t$ volt. Assume the feedback resistance $R_F = 10$ k Ω

Solution: output voltage

$$v_0 = -R_F \left(\frac{v_{i1}}{R_1} + \frac{v_{i2}}{R_2} + \frac{v_{i3}}{R_3} \right) = -R_F \left[\frac{(-1)}{R_1} + \frac{0.5 \cos \omega t}{R_2} \right]$$

Or, $1.25 - 2.5 \cos \omega t = R_F \left[\frac{1}{R_1} - \frac{0.5 \cos \omega t}{R_2} \right]$

Or, $1.25 - 2.5 \cos \omega t = \frac{R_F}{R_1} - \left(\frac{R_F}{R_2} \right) (0.5 \cos \omega t)$

So, the DC input line contains the resistance R_1 can be calculated as

$$\frac{R_F}{R_1} = 1.25 \quad \text{Or,} \quad R_1 = \frac{R_F}{1.25} = \frac{10}{1.25} = 8 \text{ k}\Omega$$

Similarly the time varying signal input line contains the resistance R_2 as

$$\left(\frac{R_F}{R_2} \right) (0.5 \cos \omega t) = 2.5 \cos \omega t \quad \text{Or,} \quad R_2 = R_F \times \frac{0.5 \cos \omega t}{2.5 \cos \omega t} = 10 \times \frac{0.5}{2.5} = 2 \text{ k}\Omega$$

Output voltage

$$V_0 = -R_F \left(\frac{V_{i1}}{R_1} + \frac{V_{i2}}{R_2} + \frac{V_{i3}}{R_3} \right)$$

Using KCL at the input node

$$i_1 + i_2 + i_3 - i_4 - 0 = 0$$

So, we have to find R 1 and R 2; we are given the value of R F, we are given the value of v o. We are given the value of v 1 and v 2; everything is given. So, this becomes; life becomes very easy because we have to just substitute the value and solve it and then we know that this is the DC input line, this is the resistance R 1; that is the feed would line contains. And then we see the time bearing signal, this is the time bearing signal and it is rated with this particular signal; so, then you can find the value of R 2. Thus R 1 and R 2 is very easy to find.

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Example 2: Summing Amplifier

What will be the output voltage of an Op-amp inverting adder for the input voltages $V_1 = -10V$, $V_2 = +10V$, $V_3 = +5V$ and resistances $R_1 = 600K\ \Omega$, $R_2 = 3000K\ \Omega$ & $R_3 = 2M\ \Omega$ if the feedback resistance is considered to be $2M\ \Omega$?

Solution

Given data:

$$V_1 = -10V, R_1 = 600k$$

$$V_2 = 10V, R_2 = 300K$$

$$V_3 = 5V, R_3 = R_f = 2M$$

The output voltage of an inverting adder or summer circuit is evaluated by,

$$V_o = -(K_1V_1 + K_2V_2 + K_3V_3)$$

where, 'K' represents the constant gain factor.

So, let us see one more example of summing amplifier. So, what will be output voltage of Op-amp inverting adder; it is also called inverting adder; for the input voltage is V_1 is given V_2 is given, V_3 is given. R_1 is given, R_2 is given, R_3 is given and feedback resistance considered to be 2 mega ohms; R_f is also given; you see life is so, easy it is; so, easy question; everything is given V_1 , R_1 , V_2 , R_2 , V_3 , R_3 , R_f ; everything is given.

Now, output voltage is what? Output voltage is V_o equals to minus K. So, K is nothing, but this is nothing, but gain factor; R_f by R_1 that is the K, R_f by R_2 ; K_2 ; R_f by R_3 K_3 ; so, minus bracket K_1 , V_1 plus K_2 ; V_2 plus K_3 ; V_3 .

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Example 2: Summing Amplifier

What will be the output voltage of an Op-amp inverting adder for the input voltages $V_1 = -10V$, $V_2 = +10V$, $V_3 = +5V$ and resistances $R_1 = 600K \Omega$, $R_2 = 300K \Omega$ & $R_3 = 2M \Omega$ if the feedback resistance is considered to be $2M \Omega$?

Solution Contd..

$$K_1 = R_f / R_1 = 2M / 600K = 2000K / 600K = 3.33$$

$$K_2 = R_f / R_2 = 2M / 300K = 2000K / 300K = 6.66$$

$$K_3 = R_f / R_3 = 2M / 2M = 1$$

Therefore, $V_o = -(K_1V_1 + K_2V_2 + K_3V_3)$

$$= -[3.33 \times (-10) + 6.66 \times (10) + 1 \times 5]$$

$$= -[-33.3 + 66.6 + 5]$$

$$= -38.3 V$$

Hence, the final output value of voltage of an inverting amplifier is nothing but summation of all input voltages estimated to be in terms of negative voltage of about $-38.3 V$

So, if I substitute the values then what will happen? K_1 is nothing, but R_f by R_1 . So, if I substitute values; 2 mega ohm via 600 kilo ohm, I will have 3.33 which is my R_f by R_1 or K_1 . Same way if I substitute value for K_2 ; that is R_f by R_2 ; 2 mega ohm divided by 300 kilo ohm; I will have 6.66. And then finally, for K_3 ; R_f by R_3 ; 2 mega ohm by 2 mega ohm is 1. ;

So, I have now 3 values if I substitute those values in this equation what will I have? V_o equals to minus 38.3. Hence the final output voltage of a inverting amplifier is nothing, but the summation of all the input voltages estimated to be in terms of negative voltage of about 38.3 volts; about minus 38.3 volts; negative voltage is minus so 38.3 Volts; very easy, this is how the summing amplifier can be solved.

So, what we have seen in this particular module is that we have seen that we can use the operation amplifier; as an inverting amplifier and then we have solved few problems. Then we have also seen, the operational amplifier as a summing amplifier and we have seen a problem, how it can be used as an adder or as a summer or the summing amplifier?

Now, in the next module; let us see how you can use operation amplifier as the non inverting amplifier? Say there are several applications like we have seen the slide 1; that the Op-amp can be used as an inverting, non inverting, differentiator, integrator, summer. So, we will see few other circuits in the next module. Till then you just look at what I

have thought, in this particular module and I will see you in the next module bye take care.