

Integrated Circuits, MOSFETs, OP-Amps and their Applications
Prof. Hardik J Pandya
Department of Electronic Systems Engineering
Indian Institute of Science, Bangalore

Lecture - 13
Operation of Depletion type MOSFET

Welcome; to this particular module and this is a continuation of our last lecture in which we have seen the MOSFET. We have seen how the MOSFET can be fabricated using the process flow. Then, we have seen how the enhancement MOSFET works; we have seen some transfer characteristics. In this module we will concentrate on depletion type MOSFET.

So, in the case of enhancement type MOSFET, the channel was the channel was not there between source and drain. If I say that my index finger; then, this one is source and this one is drain; then, the channel which is this pen was not there. That means, channel is not there.

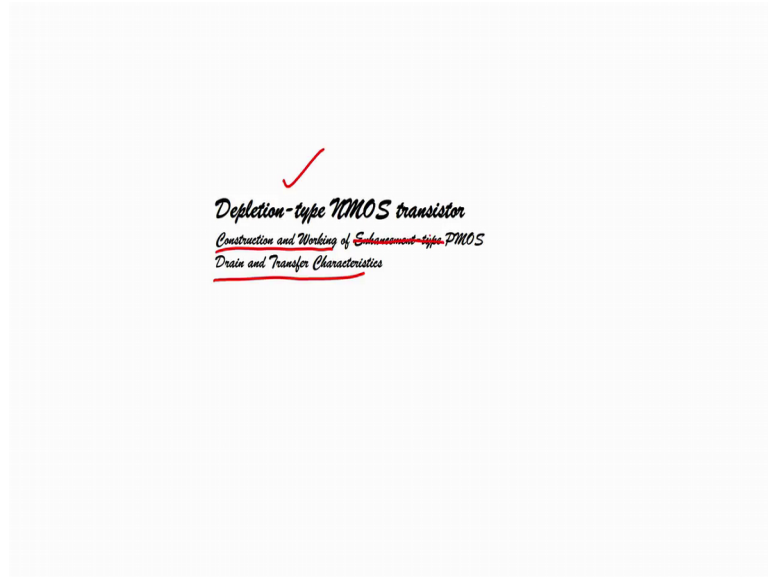
So, this channel can be generated when we apply a negative gate voltage compared to the source, positive gate voltage compared to source of V_{GS} gate is positive compared to source. And then because of the positive voltage at the gate, the electrons will get attract from the base and there will be formation of channel.

Duty formation of this channel as we go on increasing V_{GS} , our current starts increasing for particular value of V_{DS} . For constant V_{GS} when we increase V_{DS} , it will reach to a saturation region; when it starts saturating, the constant voltage or V_{DS} saturation, it also called the Pinc- off region.

And then when we keep on increasing suddenly it shoots up after or continuously increase in the V_{DS} and that is your MOSFET may get breakdown or it is a breakdown region or the MOSFET may get affected it may get destroyed. So, we should not exceed V_{DS} more than a particular value.

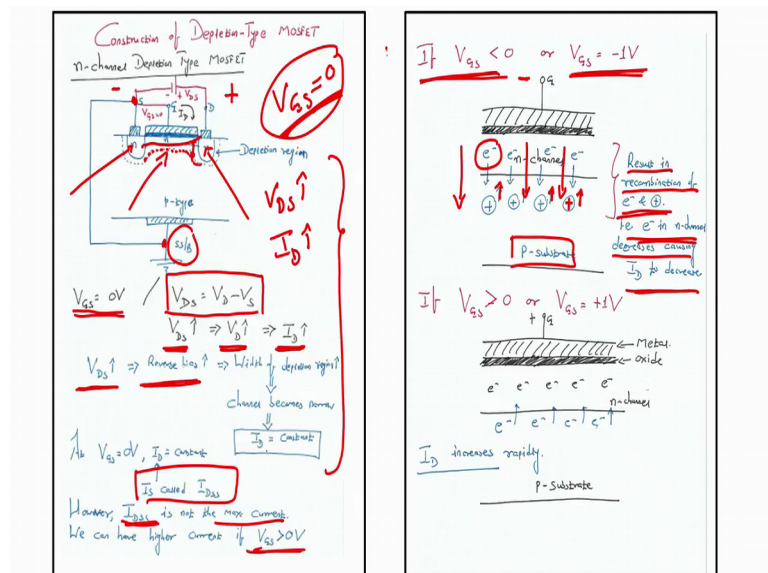
We have also seen that the gates to source voltage should be greater than equal to threshold voltage to see the flow of current, to see the flow of I_D which is drain current. So, in this particular module, let us see how the depletion type MOSFET is there, how we can operate it and what is the construction of depletion type MOSFET?

(Refer Slide Time: 02:34)



So, if you see the screen; today, we will be discussing about depletion-type nmos transistor; its construction and working as well as its drain and transfer characteristics. We will see the drain and transfer characteristics, we will see the construction and Working of the depletion type MOSFET not Enhancement type, Depletion type MOSFET.

(Refer Slide Time: 02:55)



So, you see this slide, we will see or you can see what is here. This particular figure if you see, there is a substrate which is SS slash B; this is internally connected to the source

over here. We are applying V_{DS} , where drain is more positive compared to source. And then, right now in this particular condition, the gate is directly connected to source; gate is directly connected to source; that means, that V_{GS} , V_{GS} is 0; V_{GS} is 0.

Now, in this condition you can see, source is here, drain is here and there does already channel exist in between source and drain; there is already channel existing between source and drain. Now; that means, that when my V_{GS} is 0 volt, what is my V_{DS} ? V_{DS} is nothing but voltage at the drain minus voltage at the source.

So, if I increase V_{DS} , my V_D will increase and correspondingly my I_D will increase. Why? Because I already have this channel present between source and drain; so, in particular condition when you have V_{GS} equals to 0, when you have V_{GS} equals to 0 on increasing V_{DS} , on increasing V_{DS} ; we can see increase in drain current, we can see increase in drain current.

But in case of enhancement type when V_{GS} equals to 0, even on increasing V_{DS} we were not able to find any drain current because there was no channel between source and drain easy. So, now, in case of depletion type MOSFET, what we see? That when we apply no gate to source voltage gate to source voltage is 0. In this case when we apply, when we increase V_{DS} we can see correspondingly, increase in current I_D .

So, what is that? Let us see next one V_{DS} if I keep on increasing then the reverse bias will keep on increasing, width of depletion will keep on increasing and channels becomes narrower and I_D becomes constant, I_D becomes constant. How? So, if I keep on increasing V_{DS} , if I keep on increasing V_{DS} ; then, channel will start getting narrowed like this which you can see from the figure, right over here and because the channel is getting narrow, what will happen, what will happen? The width of depletion region, this width of depletion region is increasing. Now beta depletion region will be see, it is like this. So, the width is increasing, the width of depletion region is increasing.

Now, if the width of depletion region is increasing; that means, channel is becoming narrower; if channel becomes narrower, my current I_D will be constant. And in this particular case when V_{GS} equals to 0, V_{GS} equals to 0, when my I_D that is my drain current which is a constant value; then it is called I_D Saturation or I_{DSS} . It is called I_D Saturation or I_{DSS} .

However, note that the I_{DSS} is not the maximum current; it is not the maximum current. We can have higher current if you increase V_{GS} greater than 0. So, that is not that I_D is I_D constant i_d saturation; that means, that we cannot have more than I_{DSS} , it's not a maximum current. We can have more than I_{DSS} , if we start increasing V_{GS} greater than 0 volts. This was a condition, when we have V_{GS} equals to 0 volt, but if I increase V_{GS} greater than 0 volt, I will see the increase in the I_{DSS} or degrade in current I_D easy.

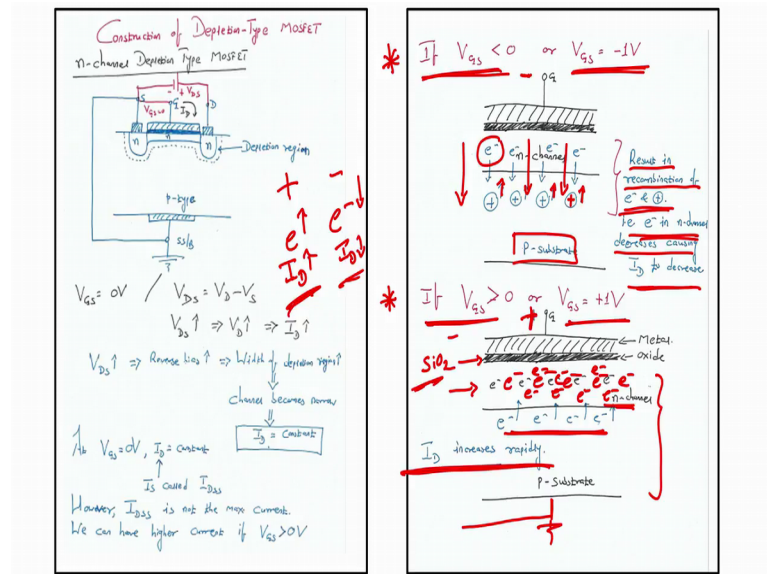
Now, if you see the right slide, right side of the slide, what you see; if V_{GS} is less than 0, if V_{GS} is less than 0 or let us say V_{GS} is minus 1 volt; V_{GS} is minus 1 volt. Now what will happen? That means; that V_{GS} ; that means, the gate is negative. So, what will happen? The electrons, the electrons will be post down because electron is negatively charged; we applied negative to the gate terminal.

So, negative-negative will cause repulsion. This repulsion will effect in the pushing the electrons down into the substrate. You can see there is a substrate. So, electrons will come down, it will be pushed down like this and because of a negative charge is there holes will have positive charge that we know. So, holes will be pushed up, it will be pulled up; you see holes will be pulled up, electrons will be pushed down.

So, this will result in recombination of electrons and holes that is electron in n-channel decreases causes I_D to decrease. So, you get it. So, if I have this particular condition where my V_{GS} is less than 0, when my V_{GS} is less than 0, what will happen? My electrons from the channel will be pushed down the holes will be pulled up and there will be recombination of holes and electrons and ultimately, what I see is decrease in the channel and the current I_D will also simultaneously decreased. Now current I_D will also decrease.

So, let us consider another condition.

(Refer Slide Time: 09:02)

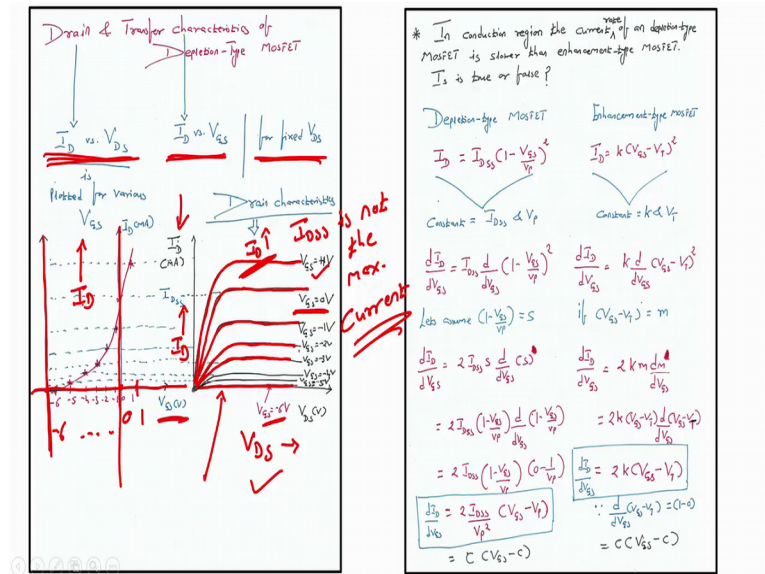


That is in this case my V G S is greater than 0 volt, V G S is greater than 0 volt; see if my V G S is greater than 0 volt, let us assume it is plus 1 volt. You can see here plus at gate terminal; you have substrate, you have substrate which is connected to the ground or it connected to the ground and also internally the connected to the source that we know. So, here if I have gate which is positive compared to source.

Then, what will happen the electrons, the electrons here, in the substrate; in the substrate, this will be pulled up. This already n-channel is there. You see here, n-channel. This is electrons within n-channels. This forms a channel between source and drain. This is your oxide layer S i O 2, thin layer of gate oxide, we already have seen. How can we go gate oxide? We can go grow gate oxide using thermal oxidation; thermal oxidation.

Now, if I apply positive with respect to the substrate. Then, what will happen? The electron that minority carriers from the P-substrate will be pulled up and there will be more number of electrons in the channel, there will be more number of electrons in the channel that will cause, that will cause my I D to increase rapidly, that will cause my I D to increase rapidly, very easy right; see we have to just understand positive apply electron will be attracted negative apply, electron will be pushed down if electrons are push down, the channel will be narrowed and my I D will be decreasing, if my electrons are pushed up I can see my I D increasing. Depletion type MOSFET very easy; very easy.

(Refer Slide Time: 10:52)



So, in this case if I want to draw a drain transfer characteristics, drain and transfer characteristics for depletion type MOSFET. How can I draw it? Now you see here, see this case here you see at V_{GS} equals to 0 volt I already have on increasing V_{DS} , on increasing V_{DS} , I will see increase in I_D . You see here let us consider V_{GS} equals to 0 volt; that means, we have to consider this line and you see here there is a current already flowing right in case when V_{GS} is 0 volt.

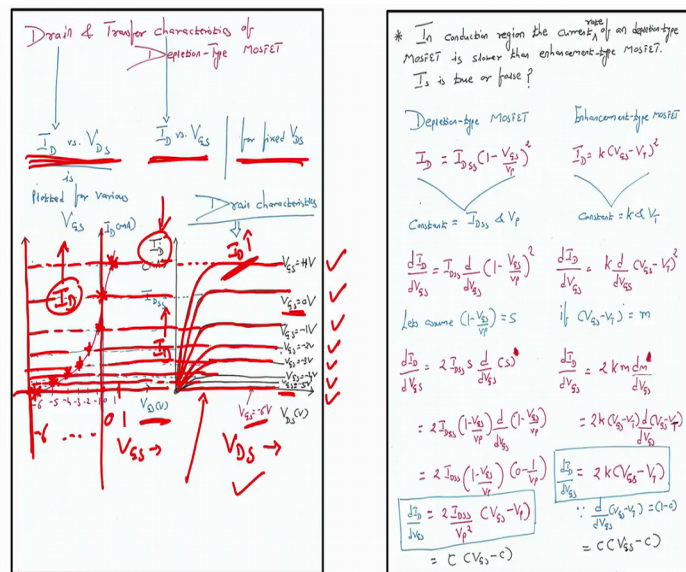
So, if I have if I have V_{GS} less than 0 volt, in this case my current will start decreasing; my current start decreasing, you can see. You can see the saturation I_{DSS} is reaching early and at V_{GS} equals to minus 6 volt, you can see here is all almost call, but what if I increase V_{GS} greater than 0 volt? If I increase V_{GS} greater than 0 volt like we discussed, we can see the current still increasing, you can still see the current increasing. The I_D is still increasing; that means, my I_{DSS} is not the maximum current, my I_{DSS} is not maximum current, because if I increase my V_{GS} greater than 0 volt, I can still see that the current I_D is increasing.

So, what we see here, the drain characteristics is I_D versus V_{DS} . Here, I_D versus V_{DS} while transfer characteristics would be i_d versus V_{GS} for fixed V_{DS} ; for fixed V_{DS} , let us draw the transfer characteristics. Now in this case what I will do is, I will draw an x and y; x y plot like this. And what I will do? I will write down my value for if this is 0 volt, this is 1 and then so on in this direction. This is minus 6. What is this? V_{GS} .

What is here? Here is I D. So, what I will write? Minus 6, minus 5, minus 4 until 1 because I have applied the similar voltages, I have applied similar V G S in my this plot, this plot.

So, you see these all the voltage is we are writing here in the x axis. Now, you see what we have to do? We have to, we have to just draw because this is I D, this is ID. So, you get and this is also I D, you see this is also I D this is also I D.

(Refer Slide Time: 14:10)



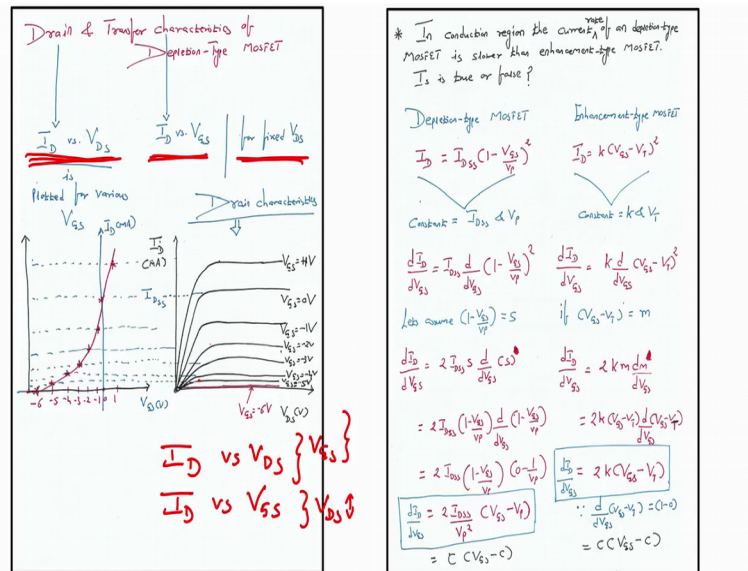
So, what we had to do? We have to just connect this I D values like this, like this, like this.

Now, what we have to do? We have to see. What we have to see? That what is the value here for current for V D S constant, let us say V D S is constant. Now let us consider minus 6, for minus 6 current is 0. So, I will have 0, minus 5; for minus 5 my current is let us say 1. So, I will put a star here. Then 2, then 3 then let's say current is 4 current becomes higher, still higher for 0.

For 1, I can see here my current is somewhere here and let say this value is 8 and 8 milliamperes. Then, what I see is I have points on this axis, on this axis just by understanding, what is the current value for particular V G S value. So, here my plot is I D versus V G S; I D versus V G S.

So again, I can draw the transfer characteristics, draw the transfer characteristics if I have or if I know the drain characteristics that is I_D versus V_{DS} . If I know I_D versus V_{DS} , what we are saying. If we know, what is, how the plot for I_D versus V_{DS} looks like for different value of V_{GS} is very easy to plot I_D versus V_{GS} .

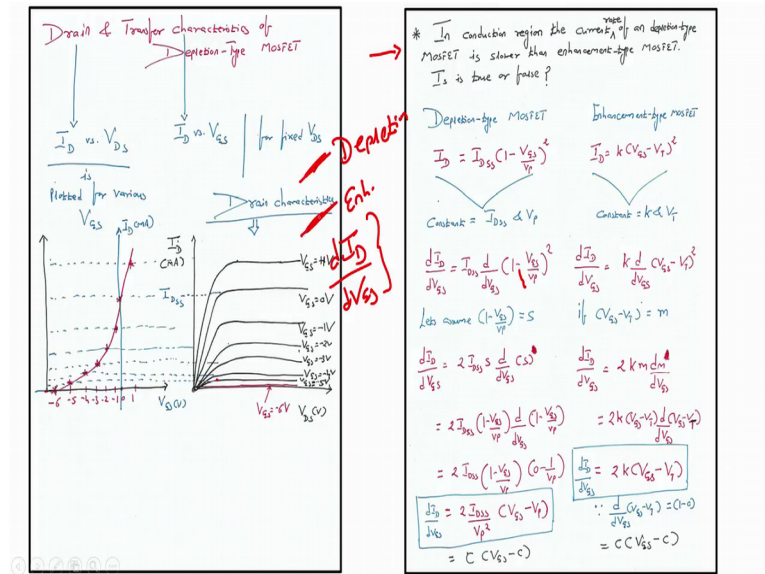
(Refer Slide Time: 16:13)



What I am saying is if I know the plot I_D versus V_{DS} , how it looks like. It is for different value of V_{GS} ; for V_{GS} different values. Then it is extremely easy to plot I_D versus V_{GS} for same V_{DS} ; for same V_{DS} , very easy is not it; extremely easy.

So, now if I have a problem; if I have a problem which you can see here.

(Refer Slide Time: 16:57)



Here, the problem is in the conduction region; in the conduction region the rate of current, the current rate of an depletion type MOSFET; the current rate of an Depletion type MOSFET is slower than Enhancement type MOSFET. What is written? The sentence written is let us read it together in the conduction region, the current rate of an depletion or of a depletion type MOSFET is slower than the current rate in enhancement type MOSFET, is this statement true or false that is a question.

So, let us we have to find out whether the statement is true or false. The statement is if I use my MOSFET, 1 is my depletion MOSFET; 1 is my enhancement MOSFET and what it says that in conduction region triode, in conduction region my rate of change of current that is my I_D that is my rate of change. So, dI_D by dV_{GS} , rate of change of current is slower when, I use depletion compared to when I use enhancement; is it true or is it false.

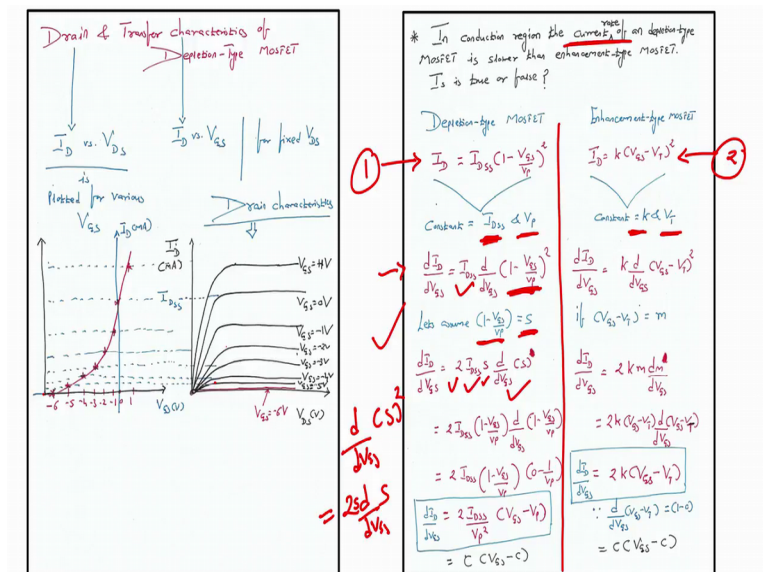
So, let us solve it; let us solve it. Now we all know that the I_D formula for the depletion type MOSFET is nothing, but I_D equals to $I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$ and if I want to understand enhancement type MOSFET then, my current formula I_D will be I_D equals to K times $V_{GS} - V_T$ whole square.

We will see derivation of one this, rest you have to do by yourself; try to do by yourself as well. So, one, once I know the formula I_D equals to $I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$ and I_D equals to K times $V_{GS} - V_T$ whole square. Then, what is the constant here? Here my constant is I_{DSS} and V_p here my constant is K and V_T .

Because here I_{DSS} is constant; we know it. Here Pinch-off voltage is constant; I know it. Here K is constant, I know it. Here threshold voltage is constant, I know it.

So, in this case if I do the derivation because I want to see the rate of change or rate of change that is why I had to do derivation. So, $\frac{dI_D}{dV_{GS}}$ this particular equation, equation 1 here is also equation.

(Refer Slide Time: 19:54)



Let's say make it to, let us say this equation number 2. So, we are deriving from 1. So, 1, if you see further $\frac{dI_D}{dV_{GS}}$ right to I_{DSS} ; I_{DSS} is constant; $\frac{d}{dV_{GS}}$ of $\left(1 - \frac{V_{GS}}{V_p}\right)^2$ this side first, left side, this side first.

So, let us assume here that $1 - \frac{V_{GS}}{V_p} = S$; $1 - \frac{V_{GS}}{V_p}$ is nothing but my constant S in that case $\frac{dI_D}{dV_{GS}}$ equals to 2 times I_{DSS} $\frac{d}{dV_{GS}}$ of S ; because $\frac{d}{dV_{GS}}$ of S^2 equals to 2 $S \frac{dS}{dV_{GS}}$ because we have considered this value, $1 - \frac{V_{GS}}{V_p} = S$. So, we can have $\frac{dV_{GS}}{dV_{GS}}$ of S square that can be nothing but 2 times $\frac{d}{dV_{GS}}$ of S . There was we written see 2 times $\frac{d}{dV_{GS}}$ of S and 2 times S , $2S \frac{d}{dV_{GS}}$ of S .

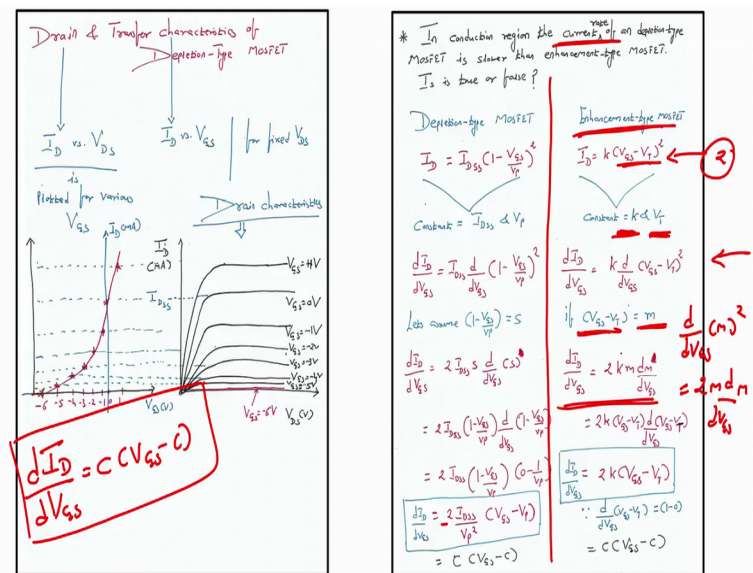
So, 2 times $S \frac{d}{dV_{GS}}$ of S . And then, we have your I_{DSS} . We have your I_{DSS} ; 2 times when you have this derivation of S^2 is 2 times $S \frac{dI_D}{dV_{GS}}$ of S . So, that is only a simple derivation by which we can get this formula, which is right in front

of you is nothing but $d I_D$ by $d V_{GS}$ is nothing but 2 times I_{DSS} into S into D by $d V_{GS}$ into S .

So, with this formula if I substitute the value of S , my S is nothing, but $1 - V_{GS}$ by V_p . So, if I substitute value of $1 - V_{GS}$ by V_p then, I get this particular formula. So, if I further understand $2 I_D$, $1 - V_{GS}$ by V_p . Now derivation of 1 is 0 and my d by $d V_{GS}$ of V_{GS} by V_p will be -1 by V_p . So, if I further solve this equation, what I have d by $d I_D$ by $d V_{GS}$; d by $d I_D$ by $d V_{GS}$ is 2 times I_{DSS} . Now you multiply this and this or you get V_p square $V_{GS} - V_p$; $V_{GS} - V_p$.

Now, what is constant here? We know see I_{DSS} is constant and V_p is constant, we know. So, let us put the constant value. So, this main set, this particular value is constant; 2 is constant, I_{DSS} by V_p whole square will be constant, $V_{GS} - V_p$, V_p is again constant. So, I will write C as a constant, $V_{GS} - C$ which is again a constant. So, my role or my equation for the depletion region.

(Refer Slide Time: 23:18)



For the depletion MOSFET is $C V_{GS} - C$. This is my equation. For what? Depletion type MOSFET and the 2 in conduction region, the great of change of current.

Now, I had to see how the rate of change of current or the current change occurs in the enhancement type MOSFET? I will see how the change of current occurs in

enhancement type MOSFET. So, let us consider the right side of the slide and second half that is the equation number 2.

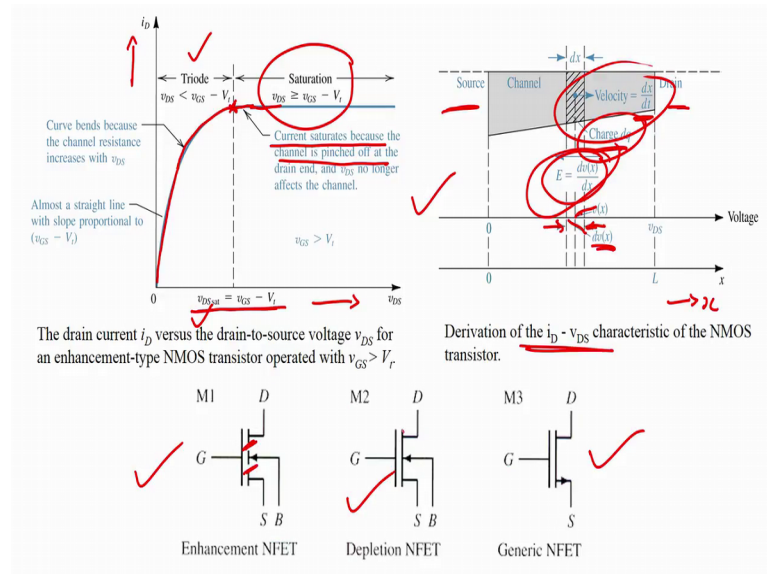
So, now we will just consider this particular side. So, let's start. So, now, we know that enhancement type MOSFET, your current i_D is $K (V_{GS} - V_T)^2$. Here K is constant and V_T is constant; K is constant V_T is constant. So, if I start derivative my $d I_D$ by $d V_{GS}$ is multiply K times d by $d V_{GS}$ of $V_{GS} - V_T$ whole square.

Now, if I assume $V_{GS} - V_T$ is equal to m . Then I will have $d I_D$ by $d V_{GS}$ equals to $2 K m$ dm by V_{GS} . Again which is similar thing, what we have is d by $d V_{GS}$ of m^2 this is nothing but 2 times m d by $d V_{GS}$ of m . This is what we are written here, this what we are written here. K is there so, we have substituted K also.

Now, once I have this, I will again substitute value of m . So, when I substitute value of m , I will had $2 K$; m is what? $V_{GS} - V_T$. So, $2 K$ into $V_{GS} - V_T$; d by V_{GS} of $V_{GS} - V_T$; when I solve this. I will get $2K (V_{GS} - V_T)$; $2K (V_{GS} - V_T)$.

Now, d by $d V_{GS}$ of $V_{GS} - V_T$ is nothing but see $V_{GS} - V_T$; so, 1 . And V_T is constant. So, my $1 - 0$ is 1 . So, here my value is nothing but this is constant. This is constant and V_T is constant. So, it will be constant into it is writing like constant because K is constant 2 is constant $V_{GS} - V_T$; V_T is constant.

(Refer Slide Time: 27:23)



So, if I see the characteristics, it is just to help you out once again. You see V_{DS} saturation is V_{GS} minus V_t ; you just understand this plot. I_D you can see almost a straight line and then, the curve bends as the channel resistance increases with V_{DS} . This is your nothing but V_{DS} saturation which is here. This region is your triode region; once you saturate current saturates because the channel is pinched off. So, this is the pinched off voltage and here in saturation region V_{DS} is greater than V_{GS} minus V_t .

So, if I see this particular plot, but I see there is a source; there is a channel, there is a drain. Here there is a drain, here there is a source. And there is a formation of charge, the velocity is nothing but dx by dt . This is my x ; my x , velocity is dx by dt . My E will be nothing but $dv(x)$ by dx ; where, this is my voltage $v(x)$, this one and this will be my $dv(x)$; you see here this one will be my $dv(x)$.

So, if I want to draw voltage plot and I am to see how the channel is formed; I can find the velocity, I can see the charge, I can see what is electric field and that's how we can derive the I_D versus V_{DS} characteristics of a MOSFET. You can again see the symbol of enhancement type MOSFET; you can see that depletion type n-channel MOSFET generic and general m MOSFET.

But you here and you see enhancement type there is a break between the drain and source and the reason is that there is no channel at the starting of the MOSFET; when

you take a MOSFET enhancement type there is no channel, but in case of depletion type there is a formation of channel and in the starting and that's why we can see this particular line; easy; very easy, very easy.

(Refer Slide Time: 29:43)

* Determine V_T for $K = 0.4 \times 10^{-3} \text{ A/V}^2$ and $I_{D(on)} = 3.5 \text{ mA}$ with $V_{GS(on)} = 4 \text{ V}$.

Ans: Enhancement-type MOSFET

For Triode Region: $I_D = 2K \left[\frac{V_{GS} - V_T}{2} \right]^2 V_{DS}$ --- (1)

For Saturation Region: $V_{DS} = V_{GS} - V_T$ --- (2)

Substituting (2) in (1)

$$I_D = K (V_{GS} - V_T)^2$$

$$\Rightarrow 3.5 \text{ mA} = 0.4 \times 10^{-3} \frac{\text{A}}{\text{V}^2} (4\text{V} - V_T)^2$$

$$\Rightarrow \frac{3.5 \text{ mA}}{0.4 \times 10^{-3} \frac{\text{A}}{\text{V}^2}} = (4\text{V} - V_T)^2$$

$$\Rightarrow \sqrt{8.75 \text{ V}^2} = \sqrt{(4\text{V} - V_T)^2}$$

$$\Rightarrow 2.95 \text{ V} = 4\text{V} - V_T$$

By adding eq. (1) & (2)

$$\Rightarrow V_T = 1.05 \text{ V}$$

Summary of given values:

- $3.5 \text{ mA} = I_D$
- $V_{GS} = 4 \text{ V}$
- $V_T = ?$
- $K = 0.4 \times 10^{-3} \text{ A/V}^2$

So, let us do one more example and then, we will finish this particular module and we continue in a next module of the same lecture. So, if you are given, determine V_T , that is threshold voltage for K of some value, I_D on for some value with V_{GS} on for some value. So, first is we should understand that V_{GS} on its 4 volts, I_D on its 3.5 milliamperes; that means, this is nothing but my enhancement type MOSFET.

For enhancement type MOSFET, my for triode region, I know the equation for triode region I_D equals to 2 times K into bracket V_{GS} minus V_T into V_{DS} minus V_{DS} square by two bracket over; this is my equation for triode region.

For saturation region, I know V_{DS} equals to V_{GS} minus V_T . So, I will substitute this value of V_{DS} into this particular equation, what will I have? Substituting 2 in 1 and I_D equals to K times V_{GS} minus V_T whole square.

Now, I already have I_D , what is I_D ? 3.5 milliamperes. This is already given here. I have V_{GS} 4 volts, V_T I do find it out. K is also given 0.4×10^{-3} ampere per Whole Square, this everything is given.

So, if I substitute the value, what I find is if I substitute the value 3.5 equals to this value then, I will have here this particular equation. So, this particular value, I will put it here and I will solve it; I will solve. So, I will have $8.75 V^2$ equals to nothing but $4 V$ minus V_T whole square. Now, this - this gone.

So, 2.95 equals to $4 V$ minus V_T . So, we can have by taking square root; by taking square root of this particular equation, if I take square root of this particular equation. Then what will happen? I had 2.95 volts equals to $4 V$ minus V_T . Then I have V_T equals to 1.05 volts, easy very easy.

So, if I know what kind of MOSFET I have, I can find out V_T because I know that in saturation region V_{DS} equals to V_{GS} minus V_T , triode region; this is the equation. I substitute this equation, I will have a equation for drain current; in the equation of the drain current everything is given. I_D is given, V_{DS} , K is given, V_{GS} is given; I have to just find out threshold voltage V_T .

So, we this is the last slide for this particular module and we will continue in the next module and see the further application of the MOSFET. So, I hope that you guys understood, what is a depletion MOSFET; you understood quickly what are the Drain characteristics. We have seen an example of whether the change in the rate of change of current in the conduction region in depletion type and enhancement type is same or different; we found that both is same. Then we have seen an example of determining the threshold voltage.

So, in the next slides, in the next modules, what we will be looking at? We will looking at the derivation of MOSFET current to voltage characteristics, derivation of MOSFET current to voltage characteristics. We will quickly see, what is channel length modulation? And then, we will move to the important application of this MOSFET which is your current mirror.

So, till then, you just go through the lecture, read it once again how the depletion MOSFET can be used compared to enhancement type MOSFET. The application is very simple in enhancement type; there is no channel. In depletion type, there is a channel. When there is no channel, if I want to attract electron; I have to apply positive gate that is why gate is positive; that means, when I increase V_{GS} my current will start increasing. In this case but, there is already channel.

So, even at V_{GS} equals to 0 that is in depletion type that is a channel between source and drain. So, V_{GS} equals to 0 still I see some current I_D and if I decrease this V_{GS} then, I will see a change decrease in the change in the current I_D , but if I increase the V_{GS} then it can be more than I_{DSS} because I_{DSS} is not the maximum current. So these much things we have understood till now.

Now let us see, what we can learn in the next class. So, I will see you in the next class; till then you take care. Bye.