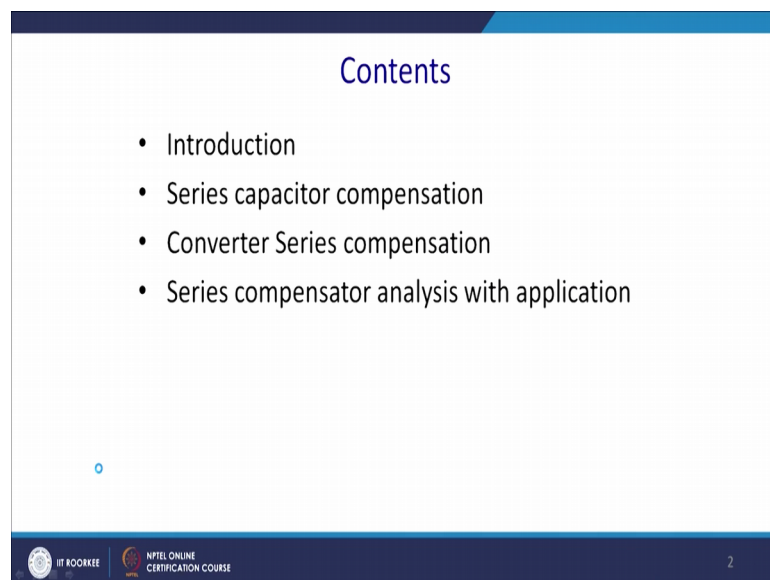


Flexible AC Transmission Systems (FACTS) Devices
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Lecture – 21
Series Compensator

Welcome to our NPTEL lectures series of Flexible AC Transmission System. We have already discussed shunt compensation. Now, we are going to discuss today the series compensation. So, Series Compensation is another important aspect of the shunt compensation. So, our presentation layout of the discussions will be on the following talk with introduction of the series compensation.

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They are the different type of the series compensation that is series capacitor compensation, converter series compensation and series compensator analysis and with its applications. Now, why you require a series compensation, the we should start with the we should start with the actually the limitation of the shunt compensation.

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Introduction

- The shunt compensation is in-effective in controlling the actual transmitted power, at a defined transmission voltage, is ultimately determined by the series line impedance and the angle between the end voltages of line.
- It was recognized that AC power transmission over long lines was primarily limited by the series reactive impedance of the line.
- Series capacitive compensation was introduced decades ago to cancel a portion of the reactive line impedance and thereby increase the transmittable power.

$P = \frac{V_s V_r}{X} \sin \delta$

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Shunt compensation is an ineffective in controlling the actual transmitted power real power, it can actually control over the reactive power, as well as it can maintain the voltage regulation of the receiving end, but it cannot control the flow of the real power into the system.

At a definite at a define transmission voltage, it is ultimately determined by the series impedance. Because P equal to V I sending end voltage receiving end voltage by X into $\sin \delta$ this is the equation. So, ultimately depends on the X and, the angle between the angle between the sending and receiving voltage that is δ . So, that is the power transmission and, shunt impedance does not starch either this or this ok.

It was recognized that the AC power transmission over the long line, primarily limited to the series reactive impedance of the line. So, ultimately it is depending on the X , if you can control the X the you can also control the flow of the real power with the transmission system. So, what it is been introduced you know, we have discussed in a will power in our first or second lectures, that is series capacitive compensation was introduced a decade ago, to cancel a portion of the reactive impedance and thereby increasing the power handling capability of the power line.

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Introduction(Cont...)

- The FACTS initiative, it has been demonstrated that variable series compensation is highly effective in both controlling power flow in the line and in improving stability.
- It can be applied to achieve full utilization of transmission assets by controlling the power flow in the lines, preventing loop flows and, with the use of fast controls, minimizing the effect of system disturbances, thereby reducing traditional stability margin requirements.
- The effect of series compensation on the basic factors, determining attainable maximal power transmission, steady-state power transmission limit, transient stability, voltage stability and power oscillation damping, will be examined.

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But it has got some limitations the facts initiative, because you know it will insert the capacitive volt impedance, in casually and with the mechanical switches and that mostly most of the cases it leads to the sub harmonic oscillation.

The facts initiatives has been demonstrated that a variable series compensator, is highly effective in both controlling the flow of the power flow in the line and improving the stability. We shall discussed and we shall prove it, more over it can be applied to achieve the full utilization of the transition asset, by controlling the power flow in the lines preventing the loop flow and with the use of the fast control minimizing the effect of the system disturbance and thus reducing he traditional stability margin requirement.

So, in a in a nutshell or in a one sentence, we can say that it is possible to enhance the stability limit with the series compensation. And, the effect of the series compensation on this two basic factor determining the attainable maximum power transmission. So, we can see that there are we have discussed there is a thermal limit there is a isolation limit. So, we required to check those aspects.

So, we can use the thermal limited optimally by using this actually optimally using the value of the impedance and, the steady state power transmission limit, transient stability, voltage stability, and power oscillation damping also will be examined with the series injection.

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Series Capacitive Compensation

- The basic idea behind series capacitive compensation is to decrease the overall effective series transmission impedance from the sending end to the receiving end, i.e., X
- The $P = (V^2/X) \sin(\delta)$ relationship characterizing the power transmission over a single line.
- Consider the simple two-machine model, analogous to that shown for shunt compensation but with a series capacitor compensated line

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Now, the basic idea is to control the impedance, the basic idea behind the series capacitive a compensation is to decrease the overall effective series transmission impedance, from the sending end to receiving end that mean the impedance X , they P the V square by \sin delta relationship characterizing the transmission line of a single line system.

And now let us consider a simple two machine model, which are already discussed in case of the shunt compensation analogous to that shown for the shunt compensation, but they will be a series capacitor compensation in the line itself. So, there is a little change what we have discussed in case of the shunt compensation. So, what happened see the circuit this is the same to machine model, we will insert the extra capacitance here.

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Series Capacitive Compensation(Cont...)

- Note that for the same end voltages the magnitude of the total voltage across the series line inductance, $V_x = 2V_{x/2}$ and V_c developed across the series capacitor this results from an increase in the line current.
- The effective transmission impedance X_{eff} with the series capacitive compensations given by

$$X_{eff} = X - X_c$$

$$X_{eff} = X(1 - k)$$
 where $k = X_c/X$, $0 \leq k < 1$

And we will split this inductance by 2 and this is V_c and this value is V_m and this value is V_r . So, thus note that the same sending end voltage and the magnitude of V_s equal to V_r equal to V_m . So, this is our assumption so, we can state that note that the same end voltage that we receiving, end voltage. And the magnitude of the total voltage across the line inductance is V_x and V_x is given by from this trigonometry, we can find out what is the value of the V_x . So, this value essentially is the V_x . So, V_x is basically $2 V_{x/2}$ and V_c develops V_c developed across the series capacitor this results from an increased in the line current.

So, what happen overall impedance decreases, since a overall impedance is decreased so, current will increase. The effective transmission impedance e effective with the series capacitive compensation will be given by X the previous with the uncompensated impedance. Most of the cases will be minus it will minus X_c and thus e effective will be you can take X common this is $1 - k$ per k is X_c by X and k can be ranges to $0 \leq k < 1$.

And ultimately we whatever same compensation, we have seen it will be there this is V_s and this is V_r and you can add up here, or you can add up here and ultimately it will be stretching. So, power angle on the new actually V_s , V_r will be this and, that it will also increases the sometime the angle between these 2 sending and receiving end voltage. And that is what we said little bit earlier that V_s equal to V_r that may be equal to $\text{mod } V$.

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Series Capacitive Compensation(Cont...)

- Assuming $v_s=v_r=v$ then the current and corresponding real power transmitted, can be
$$I = \frac{V\angle\delta - V\angle 0}{X(1-k)}$$
$$\therefore I = \frac{2V\sin(\delta/2)}{X(1-k)}$$
- Sending end power
$$P_s + jQ_s = v_s I_s^* \Rightarrow V\angle\delta \left(\frac{V\angle\delta - V\angle 0}{X(1-k)} \right)^*$$
$$\therefore P = \frac{V^2 \sin(\delta)}{X(1-k)} \text{ and } Q = \frac{V^2 (1 - \cos(\delta))}{X(1-k)}$$

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And the current corresponding to the real power transmitted by actually i that is V minus δ by V_0 by X . Now, it is been changed to 1 minus k that is you know current changes to $2V \sin \delta$ by $2Xk$ minus 1 . And the we can write the sending end power. So, it is actually V s into I s star so, you have to multiply this V dealt with this quantity.

Ultimately this quantity becomes for the real power become V square $\sin \delta$ by X and, we you have to equate the real and imaginary term, segregating the real and imaginary term, we can be see that this value of the real power becomes V square by $\sin \delta$ by X 1 minus k . And similarly the reactive power becomes V square 1 minus $\cos \delta$ by X by 1 minus k .

So, if k is 0.5 state away you have actually 24 increase of your real and the reactive power. So, same way whatever power has been send that will be received.

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Series Capacitive Compensation(Cont...)

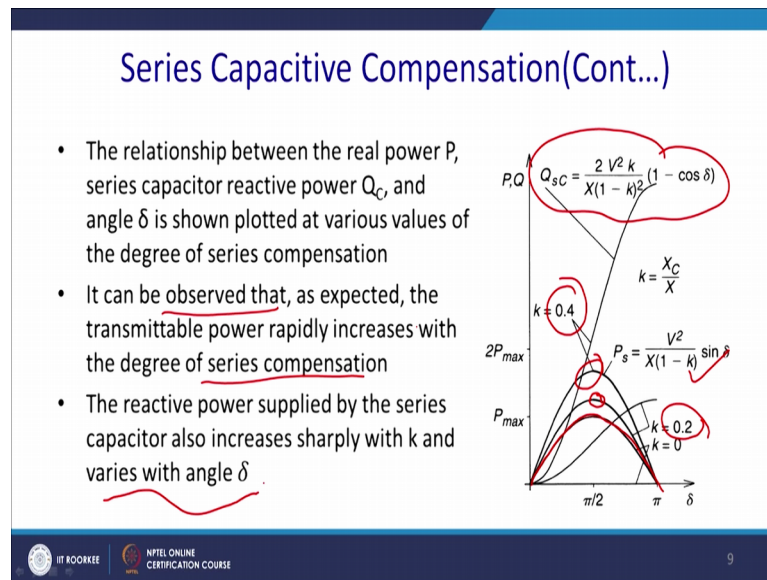
- Receiving end apparent power is
$$P_r + jQ_r = V_r I_s^* \Rightarrow V \angle 0 \left(\frac{V \angle \delta - V \angle 0}{X(1-k)} \right)^*$$
- $\therefore P = (V^2 \sin(\delta)) / X(1-k)$ and
- $Q = (V^2 (1 - \cos(\delta))) / X(1-k)$
- The reactive power supplied by the series capacitor can be expressed as
$$Q_c = \frac{2V^2 k(1 - \cos(\delta))}{X(1-k)^2}$$

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So, that is you know we can write receiving end power P_r and Q_r it is will be given by V_r into I_s , because I_s will be same because it is knows shunt compensation is there, current through the all the element would be equal. So, same value will get and ultimately you get this $V^2 \sin \delta$ by $X(1-k)$ similarly this 1.

That is what we can say you know the reactive power supplied by the series capacitor will be this reference of the sending end power and receiving end power and so, the reactive power supply by this series capacitor will be $2V^2 k(1 - \cos \delta) / X(1-k)^2$.

(Refer Slide Time: 11:11)



So, let us see what is the implication of this expression now, this is the actually X axis we have plotted phase angle delta and P and Q are plotted. So, this value corresponds to k equal to 0.4. So, you can see that for k equal to 0 corresponds to this graph with no compensation. If you make k equal to 0.2 you can have this graph.

And if you makes k equal to 0.4, you have this graph and same way k equal to 0.4, you have this is the power handled by this series capacitors so, it will be Q_c . Thus, what we can state the relation between the real power and the series capacitor reactive power Q_c and the angle delta, is shown plotted at a various values of the series compensation starting from value equal to k equal to 0, 0.2 and 0.4.

It can be observed that has express the transmitted power rapidly increases, with the degree of the series compensation of course, you know and if you can if you make this k theoretical. If it is possible 0.9 so, you have a 10 hold increase in this transmission of the real power. The reactive power supply by the series capacitor also increases sharply, with k and k and the vary k and variation of the angle delta.

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Converter Type Series Compensators (Cont...)

- An alternate compensating circuit element may be envisioned as an ac voltage source which directly injects the desired compensating voltage in series with the line.
- The function of the series capacitor is simply to produce an appropriate voltage at the fundamental ac system frequency in quadrature with the transmission line current in order to increase the voltage across the inductive line impedance, and
- There by increase the line current and the transmitted power.

The converter will injects directly appropriate voltage at the fundamental ac system frequency in quadrature with the transmission line current is converter type series compensator (SSSC)

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Now, converter type series compensator this type of compensation is called actually it is analogues to the (Refer Time: 13:12) in case of the in case of the shunt compensation. So, what you generally do, you will generally minimize the value of the impedance and, thus you get the enhance power handling capability real as well as the reactive power handling capability of the line, at the cost of the reduced impedance. So, current will be high and the thermal (Refer Time: 13:36) will be high these are the few issues will be there.

Let us see another type of the series compensation. So, this is called converter series type compensation and, alternate compensation compensating circuit element may be investigated as an ac source voltage, which directly injects the desired compensating voltage in series with the line. So, it will inject the voltage. So, same way it will manipulate the actually the a converter and, it will inject the voltage may be in series with the quadrature with the sending end voltage. And ultimately what will happen you know that the power is given by V_1, V_2 by X so, these value or these value may change depending on the position of the converter.

The function of the series capacitor is to simply produce, an appropriate voltage at the fundamental ac system frequency in quadrature in the transmission line in order to increase the voltage across the inductive line impedance. So, this is the function of this capacitor.

And thereby it increases the line current of the transmitted power. So, ultimately it reduces the value of X and this current increases ultimately extra current is the cause of extra transmitting power. So, if you are transporting ten times more that mean you are sending 10 times more current. So, you would be touching the thermal limit very soon, for this is this is not effective solution because, your because of the high current flows through the system.

Converter will inject directly the appropriate voltage at the fundamental ac system frequency in quadrature with the transmission line current, converter type series compensation for triple SC. So, this is the case here for triple SC it will inject the voltage in quadrature. Now, what happened?

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Converter Type Series Compensators (Cont...)

- The basic operating principles can be explained with reference to the conventional series compensation with the related voltage phasor diagram.
- The phasor diagram clearly shows that at a given line current the voltage across the series capacitor forces the opposite polarity voltage across the series line reactance to increase by the magnitude of the capacitor voltage

$P = \frac{V^2}{X_L - X_C} \sin \delta$

$V_s = V_r = V$

11

Let us see this is the actually the system background of this capacitor compensation. So, you have a X_C ultimately there we have voltage V_C and, ultimately you got the power $V^2 \sin \delta / (X_L - X_C)$. So, basic operation principle can be explained with the reference to the conventional series compensation with the related voltage phasor diagram.

So, what happen you know this is the angle delta this is V_S and this is V_L and, ultimately what will happen V_C will be in this direction and, V_L will be in this direction. So, what we can infer from this actually this phasor diagram. The phasor diagram clearly shows that at a given line current, the voltage across the series capacitor

forces the opposite polarity voltage, across the series line reactance to increase reactance to increase by the magnitude of the capacitor voltage. So, this one was V_L and this one was V_C that is ultimately this became V_L minus V_C this voltage.



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Converter Type Series Compensators (Cont...)

- While it may be convenient to consider series capacitive compensation as a means of reducing the line impedance, in reality, as explained previously,
- It is really a means of increasing the voltage across the given impedance of the physical line.
- Therefore that the same steady-state power transmission can be established if the series compensation is provided by a synchronous ac voltage source,
- whose output precisely matches the voltage of the series capacitor

$$V_q = V_c = -jIX_c - jkXI$$

- Where V_c is the injected compensating voltage phasor, I is the line current, X_c is the reactance of the series capacitor, X is the line reactance, $k = X_c/X$ is the degree of series compensation



12

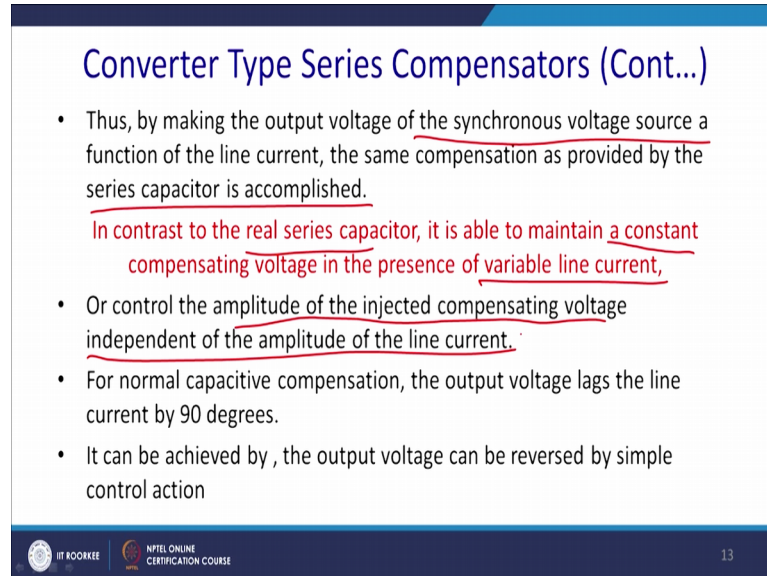
So, what we can conclude for this phasor, while it may be convenient to consider series capacitance compensation as a means of reducing the line impedance. As we have explained previously, it is really means to increase the voltage across the across the given importance of the physical line.

So, because you know voltage increases and, that is you know you make touch the insulation level. Therefore, what happened the same steady state power transmission can be established, if the series compensation is provided by the synchronous ac voltage source. So, we can we had a STATCOM, that is had a synchronous condenser and, it can be actually replaced by a series injecting a voltage source, but facts is a static solution mind it and we would not talk about any rotational solution, that was previously used for the putting long time.

Thus whose output precisely matches with the voltage of the series capacitor so, V_q equal to V_c equal to jIX_c , ultimately we can write that value equal to minus jK into XI , because you know that k equal to X_c by X . Where the V_c is the injected compensating voltage phasor and, I is a line current X is the reference of the series X is the reactance of

the series capacitor X is a line reactance and where k is x_c by x and, it is a degree of compensation.

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Converter Type Series Compensators (Cont...)

- Thus, by making the output voltage of the synchronous voltage source a function of the line current, the same compensation as provided by the series capacitor is accomplished.
In contrast to the real series capacitor, it is able to maintain a constant compensating voltage in the presence of variable line current,
- Or control the amplitude of the injected compensating voltage independent of the amplitude of the line current.
- For normal capacitive compensation, the output voltage lags the line current by 90 degrees.
- It can be achieved by , the output voltage can be reversed by simple control action

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So, thus by making the output voltage of the series, output voltage of the synchronous, voltage source a function of the line current the same compensation as provided by the series capacitor is accomplished; In contrast to the real series capacitor so, this is a converter type capacitor, you can have a control over it.

It is able to maintain a cost and compensating voltage. So, we can control its voltage across a capacitor by the converters. And in the presence of the variable line current, this is an advantage of this actually instead of the passive device we have a converter control voltage source, or control the amplitude of the injected compensating voltage independent of the amplitude of the line current.

So, that something depends on the load. So, you can vary the value of the V_q by the converter control technique. And for normal capacitive compensation the output voltage lags a line voltage current by 90 degrees and, it can be achieved by the voltage and that can reverse simply by the local control action. So, converter type series compensations have the following characteristics.

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Converter Type Series Compensators (Cont...)

- In this case, the injected voltage decreases the voltage across the inductive line impedance and thus the series compensation has the same effect as if the reactive line impedance was increased.
- With the above observations, a generalized expression for the injected voltage, V_q can simply be written:
$$V_q = \pm v_q(\vartheta) \frac{i}{I_m}$$
- Where $v_q(\vartheta)$ is the magnitude of the injected compensating voltage ($0 \leq v_q(\vartheta) \leq v_{qmax}$) and ϑ is a chosen control parameter

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In this case the injected voltage decreases the voltage across the inductive line impedance. So, ultimately net a voltage become V_l minus V_c so, V_l decreases. And thus the series compensation has the same effect of the reactive line impedance compensation, but you got an advantage that you are not changing the value of the current value of the current and the V_q are the independent to each other.

With the above observation it generalize expressions for the injected voltage V_q can be simply written as actually v plus minus depending on the kind of compensation you are doing. If you use to reduce the voltage you can also reduce the voltage i by I_m why it is called unit vector compensation, where V_q is the magnitude of the voltage injected the compensating voltage and this one is a chosen control parameter and, this is the basically gives you the direction of it.

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Converter Type Series Compensators (Cont...)

Transmitting power

Consider the sending end voltage is $V \angle \delta$, receiving end voltage $V \angle 0$ and effective reactance of transmission system is X_{eq}

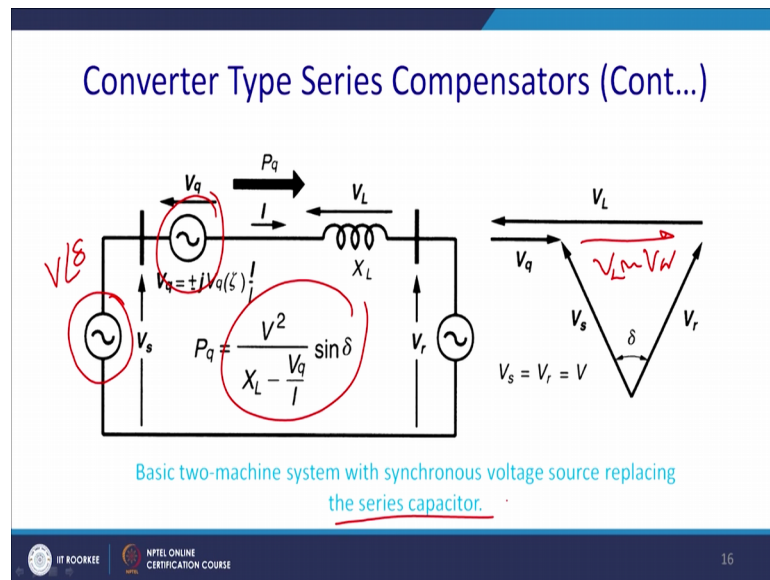
$$p = \frac{V^2}{X_{eq}} \sin(\delta)$$
$$\therefore p = \frac{V^2}{X(1 - \frac{X_C}{X})} \sin(\delta)$$
$$\therefore p = \frac{V^2}{X(1 - \frac{V_q}{I})} \sin(\delta)$$

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So, what happened with this type of compensation, with their power transmission. Considering that sending end voltage is a V angle 0 and the receiving angle is actually V angle 0 and the effect in inductance is effective. So, V squared equal to $e X q$ into $\sin \delta$ and thus you know it is V square by X 1 by 1 by $x C$ $\sin \delta$. And here we will be actually replacing because $V X$ is a function of actually $V q$ here. So, we can write the V square by X 1 minus $V q$ by 1 into $\sin \delta$. So, thus you can see that you know this quantity plays an important role to control the sending end and receiving end power.

So, ultimately and $V q$ is an variable quantity and you can control and, thus you can control the power flow in the transmission line. And you are not touching the value of the current.

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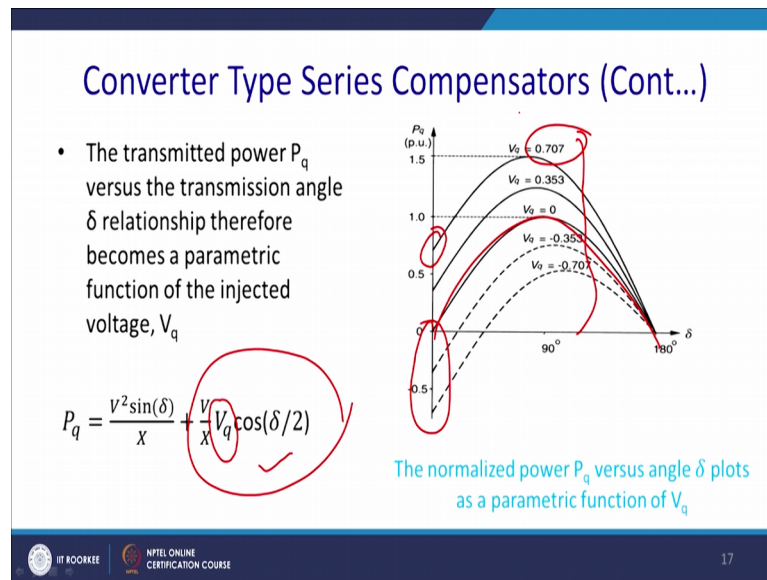


So, this is the converter type series compensation circuit diagram. So, you have to this similar two machine model, you are sending end voltage V angle δ . So, there after you can assume that you have placed a series compensator V_q as a voltage source added in series. So, far this is series capacitor and, it will have a property of plus minus $j V_q I$ by I by mod I that is the unit vector.

And that is the real power transmitted in this case is $V^2 X_L - V_q I \sin \delta$. And ultimately this will be the phasor so, effectively this voltage become V_L difference V_q . So, this is a basic two machine system of the synchronous voltage source replacing a series capacitor. So, you can have the same control with a voltage source instead of having inject instead in actually reduce the value of the impedance.

Now, what happened here so, let us draw the analysis what we have done little bit earlier for the impedance type series compensator. Now, it has advantage.

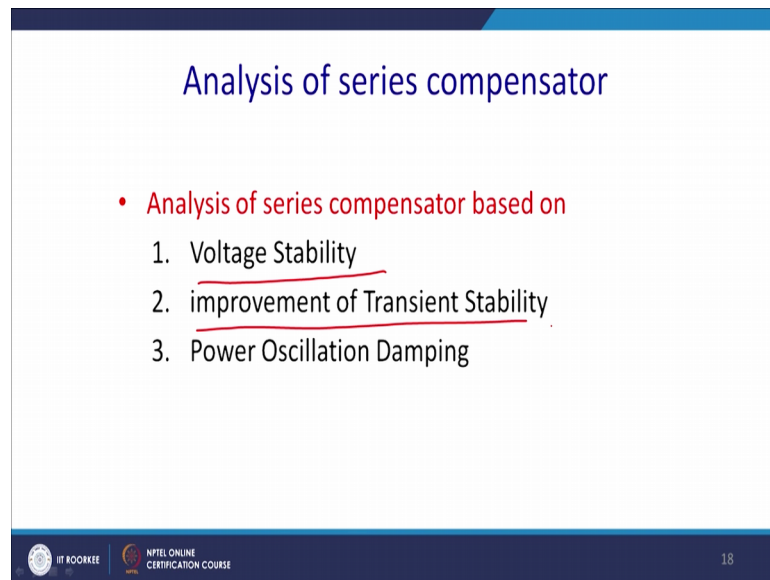
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So, value of this V_q you can make it positive and negative and, it is actually delta by 2 for this reason. This is the expression of the power, you have an a term added to it. So, assuming so that value of the V_q 0.5 or 0.707 so, what happen, you can see that. Even it has a 0 phase angle, you can transmit actually 0.7 root 1 by root 2 amount of power. And thus it will increase to the at 90 degree close to 90 degree almost 1.5 unit of power. And gradually it will come to 0 at 180 degree.

So, straight away you get around 50 percent more power for 0.707 compensation and, also you can go to the negative variation. So, it has a huge power handling capabilities so of minus 0.52 almost minus 0.707 to 1.5. So, what we can conclude the transmitted power an a transmitted power V_q , verses the transmission line angle delta relationship. And we have this following equation and this will be the changed power dimension, what was initially just this value for V_q equal to 0 ultimately, it can go up and down with the help of this series compensation. And it is a very superior competition compare to the impedance change of impedance.

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Analysis of series compensator

- Analysis of series compensator based on
 1. Voltage Stability
 2. improvement of Transient Stability
 3. Power Oscillation Damping

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Now, next course of action will be the stability. So, these are the we will see that how the series compensation will actually enhances the few desirable features of the of this transmission line, that is voltage stability improvement of the transient stability and, the power oscillation damping. We shall continue to our discussions actually with those topics in our next class thank you for attention.

Thank you.