

VLSI Design Flow: RTL to GDS

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Lecture 37 Power Analysis

Hello everybody, welcome to the course VLSI design flow RTL to GDS. This is the 29th lecture. In this lecture, we will be discussing power analysis. In the earlier lectures, we have discussed various design tasks and these tasks were related primarily to the area and the timing of the circuit. However, a third figure of merit is power is also very important for our circuit and we need to consider that in VLSI design flow. So, the tasks that we carried out in VLSI design flow that are related to power can be broadly classified into two categories.

The first one is related to power analysis and the second one is related to power optimization. So, in this lecture, we will be discussing power analysis and in the next lecture, we will be discussing power optimization. Specifically, in this lecture, we will be discussing various components of power dissipation, power models which are there in the technology libraries and the techniques to estimate power dissipation. So, the power dissipation in a CMOS circuit can be broadly classified into two types.

The first one is dynamic power dissipation. So, dynamic power dissipation occurs when a circuit performs computation actively, meaning that in a circuit the signals are basically changing. So, it may be say a signal or a net whose value is changing from 0 to 1 or 1 to 0 or there is some gate a logic gate and its output is toggling may be from 0 to 1 or 1 to 0. So, whenever there are changes in the signal values or the output of the gate is changing, then we say that our circuit is performing computation actively and the power that is dissipated during this active computation is known as dynamic power dissipation. The second type of power dissipation is known as static power dissipation and static power dissipation occurs when the circuit is powered on means that the circuit is connected to VDD and ground rails, but it does not perform active computation meaning that the value of the signal is not changing.

For example, suppose there is an inverter. Now, this inverter is connected to the VDD line and the ground line. So, we are connecting this inverter to the power supply, but

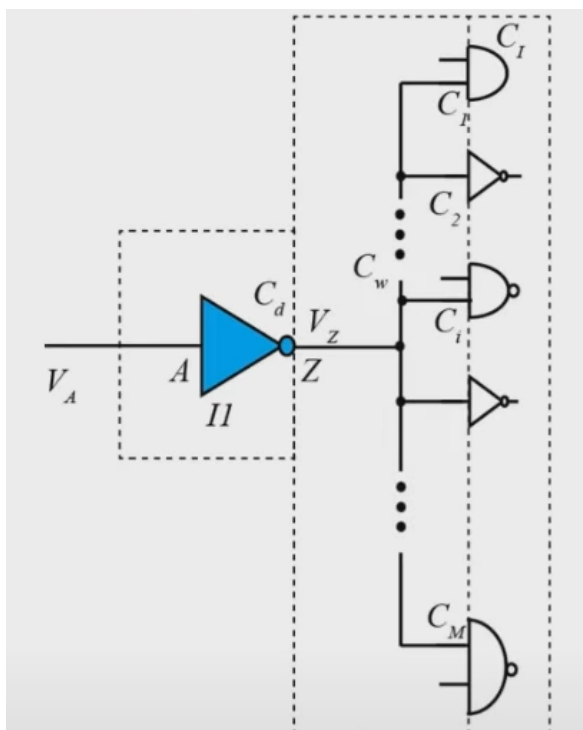
suppose the value of the input net and the output net these are not toggling it was held constant suppose the input was held constant at 0 and the output was held was the inverter will produce an output 1 in this case and these signals are not changing the input and the output values are not changing. Then the power which will be dissipated by this inverter is the static power dissipation while if there is an inverter it is of course connected to VDD and ground and suppose the input is making a transition from 0 to 1. So, if the input is changing the output will change input is changing from 0 to 1 output will change from 1 to 0.

So, the power which will be dissipated in this case will be known as the dynamic power. Dynamic power dissipation. Now, let us discuss this or let us look into this dynamic power dissipation and static power dissipation in more detail.

So, let us consider an inverter. This is an inverter which is a CMOS inverter which is driving say M loads right. So, we have the loads defined as C. This load is another load pin and so on and there are M load pins and each load pin is showing an input capacitance as C_i .

So, this is C_1 this is C_2 these are input capacitances of the pins right which are driven by this inverter right. And suppose that it is driving these loads through a wire and wire also has a capacitance, a ground capacitance which is we say that C_w is the ground capacitance. Similarly let us assume that this inverter, the CMOS inverter that is here right, has also got some internal capacitances for example, drain diffusion capacitances which can be considered as connected to the output node Z right. So, that is represented

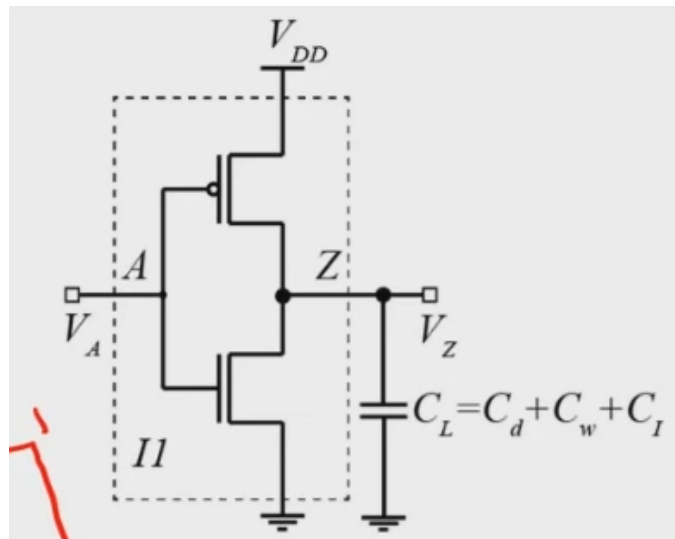
as C_d right. So, these are the various components of the capacitances which will be charged and discharged as the input of the inverter is changing.



Suppose say the input changes from 0 to 1 right then the output will change from 1 to 0 right the output at this point will change to 1 to 0. And while this 1 to this transition is happening the capacitance C_1 C_2 C_i to C_m all these capacitances will be getting discharged right because when it was 1 it was charged to V_{dd} now it is coming to 0 so it will be discharged. Similarly C_w will be discharged and C_d

will be discharged right. And if the transition is from say input at the input the transition is from 1 to 0 then the output will transition from 0 to 1 right. So in this case all these capacitance C_d C_w and all the pin loads right pin load capacitances will be charged from charged to V_{DD} right.

So when the inverter is this blue inverter which is shown here if it is making a transition all the capacitors will be charged and discharged. And during this charging discharging there will be some power dissipation which will be dissipated by the by in this process and that power dissipation is known as switching power dissipation right. Now let us understand how to quantify this switching power dissipation. Now to quantify this switching power dissipation we need to consider the internal details of this inverter right.



So if it is a CMOS inverter, this CMOS inverter will internally consist of a p MOSFET which is shown here and an n MOSFET right.

And these are the pMOS and nMOS acts as a switch right. So whenever the input is say 0 right then the p MOS will be turned on and this one will be the n MOS will be switched off. Similarly if the input is held at 1 right the p MOS will be turned off while the n MOS will be turned on right. So if we consider all the load capacitances right so there are three components one is C_d then C_w and all the pins load right. So we let us assume that the combined effect of all these pin loads is C_i .

So let us define C_i is equal to summation of C_{i_i} , i is equal to 1 to m there are m m m loads so i to m let us define this. Then we can say that C_L is equal to C_d that is internal capacitance drain diffusion capacitances or capacitances associated at with the output node z right C_d plus C_w that is a wire capacitance or interconnect capacitance and C_i

that is the combined effect of all the pin loads. So we can represent this circuit using this transistor level circuit right. So we have replaced this inverter with the pMOS and nMOS implementation and we have replaced all the load capacitances with a load capacitance C_L which is the sum of C_D plus C_W and C_i right. Now in this circuit that we are considering, whenever a transition happens, say from 0 to 1 right, suppose the transition happens from 0 to 1 or 1 to 0 the C_L will be charged and discharged right.

$$E_{sw} = C_L V_{DD}^2$$

So suppose if the transition was happening from 1 to 0 at the input right in 1 to 0 at the input the transition at the output z will be from 0 to 1 right 0 to 1. So whenever a 0 to 1 transition happens this node v z that will be charging to V_{DD} right through this path right this through this through this through this this transition whenever the input v is equal to 0 this p MOS will be turned on and that will charge it to that will charge the C_L to V_{DD} right. So in this process when the current is drawn through the p MOS this p MOS there are some resistances associated with the transistors and the interconnects and those will be basically responsible for the power dissipation. So remember that a capacitor stand alone can never dissipate power; it can only be charged or discharged but the resistances associated with this circuit are actually dissipating power. So when a charge when when when when this C_L is being charged then the then then the energy the so this capacitor C_L will store some energy while storing that energy while storing this energy that energy some power will be dissipated by this n MOS and the power lines and the internal resistances of the battery and so on and that will lead to a power dissipation of half C_L

V_{DD} square right.

And in the next cycle when the transition happens from from 0 to 1 this stored energy in the C_L in the load C_L that gets dissipated through the n MOS. So whenever a transition happens from 0 to 1 1 is the input is 1 the n MOS gets switched on right. So there is a path from V_Z to the ground and through that path whatever the charge is on C_L that will be dissipated. So whenever and in this way the half the in a half $C_L V_{DD}$ square which was stored in the capacitor that will get discharged in the second half of the cycle. So whenever a transition happens from 0 to 1 2 1 to 0 one complete cycle in this for this inverter then a total of half $C_L V_{DD}$ square plus half $C_L V_{DD}$ square that is $C_L V_{DD}$ square that much energy is dissipated right.

So this is the amount of energy that will be dissipated in the process of making a transition from 0 to 1 and 1 to 0 at the input of the transistor right. Now from this and from this energy how do we compute the power right. So we know that the energy and power are related by the power is energy energy divided by time right. So to get the power dissipation we need to understand that in what time this switching happens right

in what time the switching from or complete cycle of switching from 0 to 1 and 1 to 0 happen. If it happens very quickly then power dissipation will be higher.

If it happens slowly over a long period of time right from 0 stays long for 0 and then switches again from 0 to 1 in the after a long time then the power dissipation will be lesser though the energy dissipation will be thus will be equal to $C_L V_{DD}^2$ square in one cycle of the transition. Now how do we quantify power? To quantify power typically in a synchronous circuit what we do is that we compute power as $C_L V_{DD}^2$ square alpha times f_{CLK} . Now we multiply it by a factor alpha f_{CLK} to denote that in what time duration this energy was dissipated in and what is f_{CLK} ? f_{CLK} is the frequency of the clock in the circuit and alpha is known as the activity of the signal.

$$P_{sw} = C_L V_{DD}^2 a f_{clk}$$

f_{clk} = frequency of the clock in the circuit

a = activity of the signal

Now we have defined alpha such that the time is the time needed for this energy dissipation or the time interval in this energy dissipation is captured correctly by the suitable definition of alpha. And how do we define alpha? We define alpha is equal to 1 when the output completes one cycle of transition in one clock period right meaning that suppose let us say that the this power dissipation was happening in one clock cycle right which in this f suppose there is a clock signal right there is a clock signal whose time period is t right and the f_{CLK} is equal to $1/t$ right.

And let us assume that in this time interval this much energy SW was dissipated. So, what will be the power in this case? The power in this case will be P is equal to energy dissipated that is $C_L V_{DD}^2$ square right divided by the time interval that is t right. Now $1/t$ is f_{CLK} right. So, C_L is times V_{DD}^2 square into f_{CLK} that is what the power dissipation is if the transition if the output node z was transitioning or doing a complete transition from 0 to 1 and 1 to 0 in one clock period right. Now what happens in a synchronous circuit is that the output node for example, this node z will not toggle every clock cycle right it will make toggle say 1 once in 5 clock cycles right.

So, if that happens then this alpha will scale that right. If say this 0 to 1 and 1 to 0 transition happens once every 5 clock cycle then alpha will be taken as 1 divided by 5 that is 0.2 right. So alpha is a way of capturing what is the activity of the node z , meaning how quickly it is transitioning or how frequently it is transitioning within a

clock period right. So, this formula P_{sw} is equal to $CL \cdot V_{DD}^2 \cdot \alpha \cdot f_{CLK}$ is known as the switching power that is it quantifies the switching power of the inverter. For other types of circuit for example, the other type of logic gates for example, AND gate, OR gate and so on a similar formula can be considered where the CL can change alpha can change and f_{CLK} will be based on your based on the circuit right.

So, this is the general formula for a for a node that in this case z transitioning with an activity of alpha. Now there is another type of power dissipation which is known as short circuit power dissipation and what is short circuit power dissipation? So, short circuit power dissipation occurs if the input is transitioning at a slower rate right which is if it if the input is say rising at say from 0 to 1 at a slower rate then what will happen is that for some small amount of time this transistor PMOS and this NMOS both will be switched on and there will be some there is a path from VDD to the ground through this switched on transistor though this time interval will be very very small still there is some time small time intervals when there is a direct path from VDD to the ground and when this kind of path becomes more frequent which becomes more frequent if the if this if the transition of this if the transition or at the input is slow if we decrease the transition if we increase the slew right then it means that the transition is happening slowly and in that case the time interval for which the there will be a direct path from VDD to ground that will be increasing and during this time whenever there is a direct path between VDD to ground that during that time the power that is dissipated that is known as short circuit power right. So, we can quantify short circuit power as $V_{DD} \cdot I_{SC}$ into V_{DD} is the supply voltage and I_{SC} is the short circuit current right whatever the short circuit current which is flowing from VDD to ground right. So, now if we look into the dynamic power dissipation there are two components one that we saw in the previous slide that was related to switching and the charging and discharging of the load capacitances right and the other one due to the due to the short circuit of or short circuit path from the VDD to the ground line and therefore, the total dynamic power dissipated by a circuit is the sum of these two components. Now let us look into the static power dissipation.

$$P_{sc} = V_{DD} I_{SC} \text{ (Short Circuit Power Dissipation).}$$

$$P_{dyn} = P_{sw} + P_{sc}$$

So, static power dissipation occurs when the inputs and when the signal is held constant for example, suppose this signal input was held at constant 0 and the output will be in for an inverter the output will be 1 right. So, whenever this input is 0 right we say that the way the p MOS will get turned on this will be switched on right and there will be a direct

path from V there will be a low resistance path from this point to this point and this transistor will get charged to CL. Once that transition the the charging of this trans this load capacitance CL has happened when the CL is completely charged then no more current is drawn from this from this VDD right the from from the from the power source and this the the current should ideally become 0 and whenever the input is 0 this n MOS will be turned switched off right. So, in ideally if this is switched off and this current also dies down after charging then what we expect that in the stable state in the meaning that whenever the the input value is not changing in that case the the there is there will be no current flowing through the through the through the through the these transistors and no power dissipation will happen. But in reality what happens is that whenever we say that for example, whenever the input is 0 this transistor which we assumed it to be completely switched off they do not get it completely switched off they leak some current between say this point to this point because of various reasons.

So, what are the reasons why there can be some current from this path to this path right and and so whenever this is leaking current right this for example, when the input is 0 this transistor this transistor will be leaking current and its value is say I_{leak} right. So, whenever the input is 0 this p MOS is already turned on right. So, there is a path from VDD to node Z through a low resistance right. So, the current that will be decided I_{leak} will be decided by this switched off transistor right. If this switched off transistor was an ideal one in that case I_{leak} would have been 0 and power static power dissipation would have been 0.

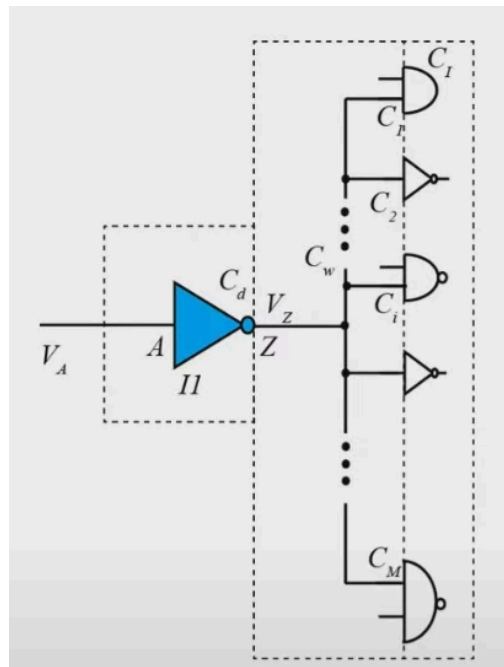
But because of various reasons this leak is appreciable at advanced technology nodes this has become significantly larger and why this I_{leak} exists there are a few reasons the first one is sub threshold current right. So, when we say that when the transistor is when we put the gate voltage of a transistor below say threshold voltage ideally we expect that the transistor is completely switched off right for an nMOS case right. But however, whenever the transistor is, whenever the gate voltage of a transistor is below threshold voltage there are some electrons which are high and have high energy and they can go from the drain to the source right from this drain to the source. So, those high energies and electrons contribute to this sub threshold current. Additionally there can be some gate leakage through the tunneling path right there can be some gate leakage.

So, between the gate and the source and drain there is an insulator and there is a capacitor. Ideally no current should flow through that. But because of the small size of the gate oxide some tunneling current can flow from the gate to the source and drain and they also contribute to the leakage current. And the third reason is the junction leak. So, there are in that within the transistor there are junctions which are reverse bias junctions and ideally the current in a reverse bias junction should be 0 right. But in real p n p n

junction those are those whose reverse bias current is appreciable maybe in pico amperes or say in nano amperes, but they exist right and they also contribute to the leakage current.

Typically in advanced technology nodes the leakage current is dominated by the sub threshold current. And how can we quantify this power dissipation which is dissipated when the signals are held constant to 0 or 1? We can simply multiply the leakage current I_{leak} with the V_{DD} right. V_{DD} is the power supply voltage right. So, we can get the static power dissipation. So now if we want to come get the complete view of the power dissipation in a CMOS circuit.

So, there are two types of power dissipation: the first is the dynamic power dissipation and the static power dissipation. And dynamic power dissipation is again of two types the switching power and the short circuit power dissipation right. So, using those from the formulas that we discussed we can compute the total power dissipated in a CMOS circuit. Now let us look into the library models which exist in the technology libraries for modeling the power. So, first let us look into the dynamic power dissipation.



Let us again consider that there is an inverter right, this inverter which is driving M loads C and their pin loads are C_1 to C_M right. And we have already computed what is the power energy dissipated in one cycle from 0 to 1 and 1 to 0. So, that was CL into V_{DD} square where CL was we have seen that we had defined CL is equal to CD that is the drain diffusion capacitance plus C_W that is the wire capacitance right the capacitance related to the wires or interconnects plus C_I which is the combined effect of all the pin

loads right. And we all and the second part of the dynamic power dissipation is the short circuit power. So, let us assume that since the formula that we derived in the last previous slide was V_{DD} into ISC that is the power dissipation.

So, this is the short circuit power dissipation right V_{DD} into ISC. Now if you want to get the energy we have to multiply it with time. So, let us assume that the the the inverter this inverter was in the short circuit condition for the time τ_{SC} and during that time interval that average current that was drawn was the short circuit current that was drawn was I_S . So, this formula E_{dyn} is equal to $C_L V_{DD}^2$ plus $V_{DD} I_S \tau_{SC}$. So, τ_{SC} is the time for which the short circuit is happening right.

So, this gives us the total energy consumed in 0 to 1 and 1 to 0 transition for this CMOS inverter right. Now if we put the value of C_L right we get this equation right that this part remains the same and instead of C_L we write C_D plus C_W plus C_I . Now in this is the total dynamic power dissipation in this formula we can identify two different sections. The first one says that the components which are dissipated within this cell are right. So, there are two components of this power. We can identify two components of the power: the power which is dissipated within the cell that is within this blue cell and the one which is dissipated outside right.

$$E_{dyn} = C_d V_{DD}^2 + V_{DD} I_{SC} \tau_{sc} + (C_W + C_I) V_{DD}^2 = E_{int} + E_{ext}$$

So, we can segregate two components depending on this capacitance as well right. So, we combine the we come we say that the the the energy dissipated in charging and discharging C_D that is the drain diffusion capacitance which is lying inside the inverter that is the internal component and also the short circuit power dissipation that is also contained completely inside the the the inverter right inside the PMOS and the NMOS of the inverter and therefore that is an internal component. So, these two are the component of energy dissipation which are which is dissipated within the cell right and the other component C_W plus C_I that is in charging this internal current capacitances and the charging of this pin load C_1, C_2 to C_m those are external to the external to the to the to the inverter and we say that it is E_{ext} . So, we can write E_{dyn} is E_{int} plus E_{ext} where E_{int} is these two components and E_{ext} is the third this code right. Now when we try to model a library which kind of power should be modeled in our library.

So, the power which is dissipated inside the cell right inside the cell means that inside this inverter that can be modeled in the library right because that is the property of that cell right and that is that can be computed at the time of power of library characterization right. So, the energy dissipated inside a cell is the property of the cell and is modeled in

the library and the energy dissipated outside a cell that is E_{external} depends on the environment or the external loads right it depends on the external loads and the capacitance sorry the the interconnect capacitance C_{C} C_{C} C_{W} and these can be computed based on the instantiation of C of the inverter right. So, the energy dissipated outside the cell can be computed by the tool based on the activity and the power supply and the capacitances external capacitances at the time of power power estimation right or power computation. However, the power mod the component of power which is lying inside the cell that is modeled inside the library because that is the property of the of the of the of the of the cell that we are characterized. So, power can be estimated using energy per transition so these are energy numbers right.

So, using these energy numbers we can compute the power by multiplying with the activity and the clock frequency right. So, now let us look into how this internal power is modeled if mod is modeled in a library. So, this internal power is modeled similar to the NLDM that we discussed earlier and the power model that we have for this is known as non-linear power model. So, the internal power dissipation depends on the output load and the input slew and therefore, it is modeled as a two dimensional table as we did for say NLDM for the delay right. In the delay also it was that the delay was dependent on output load and input slew.

Similarly, the dynamic power dissipation inside a cell depends on the output load and the input load slew. And how do we model it? We model it using an attribute which is known as internal power right. We have an attribute internal power in the technology library which captures the internal power dissipated inside our cell and this model is known as non-linear power model or NLP. So, let us have a look at how NLP looks right. So, similar to the timing arc we have a power arc we have a start pin right and an end pin.

So, the power arc is defined at the end pin and the and the related pin is the start point right. And then we have an index. We are sorry the first attribute is internal power and then we have values which can be different for rise case and the fall case and therefore, those are captured using rise underscore power. Similarly there will be rise fall underscore power and this rise underscore power is a 2D table which depends on the input net transition or input slew and the total output net capacitance or the output flow right. So, this is how the NLP model looks like and the numbers that are represented in this table are the energy numbers right. So, the values that are shown here represent energy dissipated per transition.

Now to get the power dissipation we have to multiply with the clock frequency and the activity. And how is a static power dissipation model in the library? Now the static

power dissipation depends on what is the static value at the pin. For example, if there is a NAND gate right, suppose there is a NAND gate then for the case when the input is 0 0 or the case when the input is say 0 1 the power dissipated will be different the static power dissipated will be different.

```
cell (NAND2) { ...  
    cell_leakage_power : 125;  
    leakage_power () {  
        when : "!A & !B"; value : 20; }  
    leakage_power () {  
        when : "A & !B"; value : 150; }  
    leakage_power () {  
        when : "!A & B"; value : 200; }  
    leakage_power () {  
        when : "A & B"; value : 300; } ...
```

So, we model this using a Venn condition. So, what do we mean by the Venn condition? Let us understand with an example. So, suppose if there is a NAND gate so we will define leakage power as a value say 20 when not A and not B what it means is that when A takes a value of 0 and B takes a value of 0 for let us assume that these are the pins. So, for the 0 0 case the power dissipated is 20. Similarly, we say if A is equal to 1 right if it is A and this is B right A is equal to 1 and B is equal to 0 the power dissipated in this case is 150 right. Now in addition to the leakage power based on the Venn condition an average value can be defined for a cell also.

So, if the tool needs to compute it does not know the probability of a signal being 0 or 1 in that case an average value of power dissipated by a cell is also defined by the library and that can be used by the tools. Now we have seen how to compute the power right. So, P total is equal to the switching power right and the short circuit power and the leakage power or static power static power dissipation these are three components right. Now how do we estimate the so given a design or given our circuit how does a tool will

compute this total power dissipation right. So, computing power dissipation is a challenging problem. The first of all the challenge is because of this CL.

$$P_{tot} = C_L V_{DD}^2 \alpha f_{clk} + V_{DD} I_{SC} + V_{DD} I_{leak}$$

where,

- V_{DD} = supply voltage
- C_L = load capacitance
- f_{clk} = frequency of the clock in the circuit
- α = activity of the signal

Now what is the value of this load capacitance right? So, when we say for example, we are writing an RTL at that time we do not have any interconnect right. So, and we also do not know the load capacitance of any of the pins or the signals which will be driven right. So, in that case the CL values cannot be estimated accurately even though we have done our say technology mapping in that after technology mapping we know the pin loads, but we still do not know the interconnect capacitance right. So, in that case again the CL value that we are getting is not very accurate. So, what it means is that as the design flow progresses the value of CL becomes more and more accurate as the abstraction decreases and details increases.

For example, CL can be computed very accurately once we have done the routing we have and if we have done the final routing then CL can be estimated very very accurately right. The other difficulty is related to the activity right. So, accounting for the activity of the signal is very very difficult or very tricky. Why it is difficult or tricky because the activity of the signal depends upon the application being run right. For example, let us assume that there is a processor that we are designing right.

Now depending on what application is running on this with the help of this processor right the switching activity can be higher or lower. For example, if we are doing, say, video rendering right in that case the activity can be much higher, but if we are just editing a document in that case the activity may be lower right. So, for a given chip or an integrated circuit estimating the activity is very difficult because it depends on the application and we need to understand the details and the loads that the application will need to apply on our circuit to estimate the activity of the signal. Another thing is that

even if we know the activity right we know that ok this program will run on our integrated circuit right. Even in that case the logical structure and the circuit topology will decide the activity of the signal right and then accounting for those logical structures and the circuit topology that may also be tricky right.

So, how does the tool estimate the activity and compute the power dissipation right. So, there are two types of techniques: the first one is simulation based techniques or vector based techniques. So, in this technique what we do is that we perform the simulation using the test bench right. So, we have seen that when we designed our RTL we did functional verification and for functional verification we wrote our test bench and ran the simulator right. So, we can use the same test bench to run the simulation simulation and then using the simulation result we can record the output response and save them in say VCD file right.

So, we have discussed earlier that there is a value-changed dump file or VCD file in which the values can be written right. So, in some sense this VCD file will be recording the activity of the signals right. Now using the VCD file we can convert into a format from which activity measures can be easily extracted by the tool and what is that format? That format is typically switching activity interchange format or safe format right. So, we did simulation and after simulation we got VCD file and from VCD file we get a safe file which which is in a format from which the activity can be easily extracted by power analysis tool and using these activities the tool will compute the compute the compute the power dissipation or in our circuit right. And for some signals or sometimes we may not have the activity file in that case the power analysis tool will typically assume some default activity for example, 0.

2 for the signals and based on that the computation power estimation can be done right. So, this is this technique which is based on say simulation is known as simulation based technique or vector based techniques. The other type of technique to estimate power dissipation is probabilistic technique and those techniques are also known as vectorless technique. In probabilistic technique what we do is that we propagate the activity through the circuit by considering the logic function of the gate encountered in the path. We assume certain activity at the inputs of our design or circuit and propagate that activity throughout our circuit using the logical structure of our design right.

So, let us assume for example, to illustrate this let us assume that there is a there are two signals A and B there are two signals A and B and the probability of being 1 is 0.5 for A. So, there is a signal A whose probability of being 1 is 0.5 and there is another signal P a P B whose probability of being 1 is 0.

3 right. Now, if these two signals were going to an AND gate right. So, AND gate. So, what will be the probability of being 1 at this output right. So, we can easily compute in this case that the output will be 1 only when both the inputs are 1 right.

So, therefore, if we multiply 0.5 and 0.3 we get 0.15 right, that is the probability of being 1 at the output of the AND gate right. So, this is so if we know the probability of the signal at the input we can use the logical structure we can compute the probability of being 1 at the output of the output of the gate right. Now, if these two same signals were propagating or going to an OR gate for example, there is an OR gate. Now, what will be the probability of being 1 in this case. So, in this case it will be easy to compute the probability of being 0 right and then from there if we subtract that probability from 1 then we get the probability of being 1 right right.

So, for the signal a the probability of being 1 is 0.5 so probability of being 0 is also 0.5 right that is probability of being 0 probability of being 0 right for the signal a. Now, what is the probability of being 0 for the signal B it is the probability of being 1 was 0.

3 so the probability of being 0 for signal B will be 0.7 right. Now, output of an OR gate will have a value 0 only if both the inputs are 0 right. So, what will be the probability of being 0 at the output output of the OR gate probability of 0 at the output of OR gate will be 0.

5 into 0.7 that is 0.35 right. Now, we can compute the probability of being 1 at the output of A plus B as 1 minus 0.35 that is 0.65 right that is what is shown right. So, in this case it was easy to compute because we are assuming that A and B are totally uncorrelated signals right, those are independent signals right. But in real designs what happens is that the signals diverge and they converge and therefore there are correlations right there can be correlations and then computing the probabilities and other things will not be that easy right.

So, the exact computation of the or estimation of the power dissipation is not the part of this course. However, if you want to look into more detail you can refer to this book. Now, to summarize what we have done in this lecture we have looked into power analysis of a CMOS circuit and then we looked into various components of power analysis and we also looked into the library models which are used for power analysis and how activities can be estimated correctly. So, in the next lecture we will be looking into how we can change our design or how we can make modifications in our design to reduce the power dissipation. Thank you very much. .