

**Analog Electronic Circuits**  
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**Lecture - 25**  
**The Incremental Voltage-Controlled Voltage Source The Common-Drain**  
**Amplifier-Incremental Picture**

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Lecture 12

VCVS: Incremental VCVS

Ideally: input impedance =  $\infty$   
output " = 0

$\frac{v_o}{v_i} = 1$

$I_x = g_m(v_i - v_o)$  Vilmeter

If  $(v_i - v_o) > 0$ , means  $v_o$  is too small  
 $\Rightarrow$  must  $I_x \uparrow$

$(v_i - v_o) < 0$ , means  $v_o$  is too large  
 $\Rightarrow$  must  $I_x \downarrow$

Ideally  $g_m \rightarrow \infty$

Good morning and welcome to Analog Electronic Circuits. This is Lecture 12. So, in the last class, we basically concluded by saying that we know that, in principle, the transconductance of a MOS transistor operating in saturation. Actually, I think I have been using the notation "small v" capital  $G_s$  in principle because  $g_m$  can be, you know, as large as possible.

So, a MOS transistor operating in saturation behaves like an incremental voltage-controlled current source where, in principle, the transconductance that relates the incremental drain current to the incremental gate source voltage can be as large as possible because, in principle, we can, you know, burn arbitrarily large amounts of current in the transistor and therefore get a large  $g_m$ .

In practice, of course, as several of you pointed out, there are real problems in the sense that you know the transistor may get too hot, burn, and so on. But they are what we would call practical problems in principle; you know you can still have as much transconductance as you want. So, using this as a building block, let us now try and build the four controlled sources

that you are familiar with from basic circuit theory. The voltage-controlled voltage source, the voltage-controlled current source, the current-controlled voltage source, and the current-controlled current source

We will start with this with the voltage-controlled voltage source, and because we are talking about incremental signals here, the voltage-controlled voltage source is basically going to be an incremental.

Voltage-controlled voltage source, ok. In other words, the controlled source is a linear element, and the transistor as such is non-linear. So, we can only talk about incremental signals. So, any building block that we come up with using transistors that claims to be linear is only linear for small signals, right?

Now, let us recall: what is the input impedance of VCVS?

Student: Infinity.

Infinity. Output impedance?

Student: 0.

Is 0 and therefore, when you say we have a voltage-controlled voltage source the only number you have to specify therefore, is the?

Student: Gain.

Is the gain between the output and the input,  $v_o / v_i$ , correct? Now, let us choose the simplest case, namely  $v_o / v_i$ , which is equal to 1. We will reflect on why we chose 1 later on, but at this point, 1 is as good as any other number. So, let us try to implement a voltage-controlled voltage source with a gain of 1.

And what we would like to do is to also recognise that the transconductance, while large, is actually quite dependent on the operating point, threshold voltage, and all this other stuff.

So, what we would like to do is build an incremental voltage-controlled voltage source where the properties of the VCVS are largely independent of the properties of the transistor. In this case, the only property we are talking about is the incremental I mean, it is the transconductance of the transistor, alright?

So, in other words again let us derive this from first principles. What we are going to do is basically first come up with a plan that we verbalize. Once you know what you want you can always build an electronic circuit to do it right. So, the problem statement therefore, is we have a voltage  $v_i$  and we have some load resistance  $R_L$  and we would like the voltage across the load which is,  $v_o$  to be equal to  $v_i$ .

Student:  $v_i$ .

And that is because we wanted to shoot for an incremental gain of 1. So, let us imagine you are in a lab, and let us, for argument's sake, also assume that there is some source resistance for the input. So, this is our  $R$  source. We have a voltage of  $v_i$  with an internal resistance of  $R$ . We are in a lab, and we would like to make the voltage across a load  $R_L$  exactly equal to  $v_i$ .

Student:  $v_i$ .

Ok. So, in principle, what would we do and what equipment would we need?

Student: Volt meter.

So, let me you know let me kind of track back a little and say well you want  $v_i = v_o$  why not I just shot  $v_i$  with  $v_o$ . Yes, it is a smart idea or a stupid idea.

Student: Stupid idea.

Why? Well, that is a terrible idea because you know there is of course, a voltage drop and as you keep changing  $R_L$ . The voltage will keep changing at the output. So, that is no good.

Right. So, we can dismiss that right away. So, what we need therefore, what we need?

Student: A voltmeter.

Student: And next one we need a variable method  $v_o$ .

So, basically one way of doing this is to say well we have a variable voltage source. And what do we do?

Student: Connect voltage.

Connect which with?

Student: Circuit and joint sir.

So, basically, the idea is to say, "Well, take a voltmeter, which measures, say, the voltage between the positive terminal and the negative terminal, and now what do we do?" You read the reading on the voltmeter, correct? And what is the reading on the voltmeter? By the way, what is the impedance of the voltmeter?

If you have an ideal voltmeter, the internal resistance of a voltmeter is infinite. So, what exactly is the voltmeter actually the reading on the voltmeter therefore, represents?

Student:  $v_i$ .

Very good. So, the voltmeter therefore, reads  $v_i - v_o$ . So, if the voltmeter reading is greater than 0 what does it mean? What does it mean? Then we figure out what to do? It means that what  $v_i$  is? You cannot say it is too little or too high. It is  $v_o$ 's job to follow  $v_i$ .

Student:  $v_i$ .

So, it basically means if  $v_i - v_o$  is greater than 0 it means that?

Student:  $v_o$  is too small.

Means  $v_o$  is too small. What must I do therefore,

Student: Increase  $V_x$ .

Must increase  $V_x$  alright. Now, let me ask you a question if you want to increase the potential of a node. In this case we are taking the variable voltage source and simply yanking its potential up and down. Can you think of another way of increasing or decreasing the potential of a node without using a voltage source?

Yeah. So, there are two ways of changing the potential of a node, one is of course, use a variable voltage source to go and move the potential up and down the other way is to?

Student: Pump a current.

Pump a current, alright. And why are we interested in pumping a current? Because that transistor is a?

Student: Voltage.

It is a variable, I mean it is an electronically variable.

Student: Current source.

Current source, correct. So, therefore, we would like to use a variable current source because we are talking about eventually using transistors. So, now, if we wanted a variable current, instead of using a variable voltage source here. If you had to use a variable current source what would we do? So, basically you need to connect a current?

Student: Current pump current.

Which pumps current there, some  $I_x$  correct. So, if the voltmeter reading is greater than 0, it means that  $v_o$  is too small again, but what must we do now? So, what we must do therefore, is to increase  $I_x$ , does it make sense? Alright. Now, if on the other hand  $v_i$  minus  $v_o$  is less than 0, what does it mean?

Student: Large.

What does it mean?

Student:  $v_o$  is too large.

$v_o$  is too large and therefore, we must reduce  $I_x$ .

Student: Reduce  $I_x$ .

Does it make sense to people? Alright. So, therefore, we can see that  $I_x$  is a current source which is controlled by which voltage?

Student:  $v_i - v_o$ .

$v_i - v_o$ . So, it is controlled. So, it is therefore, proportional to  $v_i - v_o$  alright. And the constant of proportionality will therefore, the output is a current the controlling quantity is a?

Student: Voltage.

Voltage. So, the constant of proportionality will have dimensions of?

Student: Conductance.

Conductance, right. So, that is what we will simply call  $g_m$ , correct. Is a sign of gram positive or negative?

Student: Positive.

Why?

Student: Because if  $v_i$  is greater than  $v_o$ ,  $I_x$  must be positive.

So, alright. So, in other words, remember that the general notation for a current source is actually that, alright. So, now can somebody recognize the transistor, the terminals of the transistor in this picture.

Student: Yes sir.

Or by the way so, basically  $I_x$  produces a current which is proportional to  $v_i - v_o$ . And what if you want  $v_o$  to be exactly equal to  $v_i$ , what comment can you make about the transconductance  $g_m$ ?

How much do we need?

Student: Infinite.

Why? Because you ideally want  $g_m$  must tend to infinity because even if you see an infinite simile small difference between  $v_i$  and  $v_o$  you must go and kick that node  $v_o$  so hard so that its potential becomes exactly the same as that of  $v_i$ .

Student:  $v_i$ .

Is that clear alright? So, now, what comment can you make, can you now recognize the terminals of the transistor here? Stare at this picture I mean in this picture this is the gate, this is the source, this is the drain. So, stare at the two pictures and tell me which terminal is which?

Student: Gate source.

So, this gate is the input.

Student: Source is the output.

Source is the output and the other end of the current source is drain.

Student: Drain.

Drain right, because you simply recognize this as being the incremental  $V_{GS}$ , does it make sense?

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VCVS: Incremental VCVS

Ideally: input impedance =  $\infty$   
output " = 0

$\frac{v_o}{v_i} = 1$

$v_o = g_m (v_i - v_o) R_L$

Voltmeter

If  $(v_i - v_o) > 0$ , means  $v_o$  is too small  
 $\Rightarrow$  must  $I_x \uparrow$

If  $(v_i - v_o) < 0$ , means  $v_o$  is too large  
 $\Rightarrow$  must  $I_x \downarrow$

Ideally  $g_m \rightarrow \infty$

$z_{in} = \infty$   
 $z_{out} = 0$   
 $\frac{v_o}{v_i} = 1$

What is a large  $g_m$ ?

$\frac{v_o}{v_i} = \frac{g_m R_L}{1 + g_m R_L}$

And therefore, the circuit, when you recognise the transistor, becomes  $v_i R_S$ ; this is  $R$ ; this is  $v_o$  alright. Ok. So, let us tabulate the properties of the voltage-control current. This is the incremental picture, ok? It does not mean that, again, let me retrain that, it does not mean that you take a transistor connected up like this and magically you will get  $v_o$  equal to  $v_i$ ; this only works when the transistor is operating in the saturation region. So, for that, you have to act appropriately.

Student: Bias.

Biasing the transistor, you already know at least 5 or 6 ways of biasing the transistor; you can pick your favorite way to bias the transistor. Once you bias the transistor, you also know how to get rid of elements that you do not want and keep elements that you do want, and so on, by adding infinite inductors and infinite capacitors, and then you must make sure that the incremental circuit looks like this one.

So, before we actually build the real circuit, let us tabulate what we will get as far as the input impedance is concerned. What is the input impedance?

Student: Infinity.

This is infinity because the incremental gate current is 0, that does this depend on  $g_m$  being infinite or not?

Student: No.

It is independent of  $g_m$  correct. What about  $Z_{out}$ ? You know  $g_m$  is infinite. The easiest way is to figure out that well if you go and change  $R_L$ , what comment can you make about the output voltage?

Student: It remains the same.

It remains the same, alright and therefore, this basically means that the output resistance seen is 0 if  $g_m$  tends to infinity. What comment can you make about  $v_o / v_i$  this we knew already, if  $g_m$  tends to infinity the incremental gain is 1. Does it make sense to people? Alright. So, now, ideally  $g_m$  must be infinite in reality. Well, we can say we cannot get  $g_m$  is infinity after all  $g_m$  must be very large now the question is what is a large  $g_m$ ? Alright, again this is context dependent and we have to figure out what the context in this particular case is and how do you propose to figure out what it means to have a large  $g_m$ ? How do we figure it out? We know that  $g_m$  must be large.

Student: We can put the output or the  $g_m$  send it

Any ideas? Ok. So, equivalently you can say that there are multiple ways of doing this.

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Ideally  $g_m \rightarrow \infty$   
 $z_{in} = \infty$   
 $z_{out} = 0$   
 $\frac{v_o}{v_i} = 1$   
 What is a large  $g_m$ ?  
 $(v_i - v_o) < 0$ , means  $v_o$  is too low  $\Rightarrow$  must  $I_x$  down  
 NPTEL

$\frac{v_o}{v_i}$

One is to simply compute  $v_o / v_i$  when  $g_m$  is finite and stare at that expression and figure out for what values of  $g_m$  that expression will tend to 1.

Student: 1.

Alright and to do that well we go back to our circuit here this is  $g_m(v_i - v_o)$ . What are the unknowns? What is the incremental gate voltage?

Student:  $v_i$ .

$v_i$  that there is no. So, what is the only unknown?

Student:  $v_o$ .

$v_o$ . So, how will you figure out  $v_o$ ? Right KCL at the output node. So,  $v_o / R_L$  that is the current flowing downwards is nothing, but  $g_m v_o (v_i - v_o)$  and therefore,  $v_o / v_i$  is nothing, but  $g_m R_L / (1 + g_m R_L)$ , alright. So, therefore, staring at this expression, what comment can we make about what constitutes a large  $g_m$ ?

Student:  $R_L$  considered as  $g_m$ .

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$\frac{v_o}{R_L} = g_m(v_i - v_o)$   
 $\Rightarrow \frac{v_o}{v_i} = \frac{g_m R_L}{1 + g_m R_L}$   
 $g_m R_L \gg 1$   
 $\Rightarrow g_m \gg \frac{1}{R_L}$

Ideally  $g_m \rightarrow \infty$   
 $z_{in} = \infty$   
 $z_{out} = 0$   
 $\frac{v_o}{v_i} = 1$

If  $(v_i - v_o) > 0$ , means  $v_o$  is too small  
 $\Rightarrow$  must  $I_x \uparrow$   
 If  $(v_i - v_o) < 0$ , means  $v_o$  is too large  
 $\Rightarrow$  must  $I_x \downarrow$

What is a large  $g_m$ ?

$g_m R_L$  must be much much greater than 1. Alright or equivalently the meaning of  $g_m$  a large  $g_m$  is that it is much much greater than  $1/R_L$ . So, to find output impedance, this is the gain with the finite  $g_m$ . What comment can we make about the output resistance? How will we figure it out?

How will we find out the output resistance?

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$\frac{v_o}{R_L} = g_m(v_i - v_o)$   
 $\Rightarrow \frac{v_o}{v_i} = \frac{g_m R_L}{1 + g_m R_L}$   
 $g_m R_L \gg 1$   
 $\Rightarrow g_m \gg \frac{1}{R_L}$

Ideally  $g_m \rightarrow \infty$   
 $z_{in} = \infty$   
 $z_{out} = \frac{1}{g_m}$   
 $\frac{v_o}{v_i} = \frac{g_m R_L}{1 + g_m R_L}$

If  $(v_i - v_o) > 0$ , means  $v_o$  is too small  
 $\Rightarrow$  must  $I_x \uparrow$   
 If  $(v_i - v_o) < 0$ , means  $v_o$  is too large  
 $\Rightarrow$  must  $I_x \downarrow$

What is a large  $g_m$ ?

$v_x = \frac{R_L}{R_L + \frac{1}{g_m}} I_x$

Well, we de-energize all the independent sources so,  $v_i$  becomes 0 alright and so, therefore, does  $R_{SX}$  you know and we need to find  $Z_{out}$ . So, what will we do? We will replace the transistor with this incremental equivalent. So, that is our controlled source for the end right there, we will put a test voltage and measure the test current, what is that, what is the strength of that current source? What is the strength of that current source? What is that current source?

Student:  $g_m$ .

$g_m$  times is the incremental  $V_{GS}$ , what is the incremental gate voltage?

Student: 0.

0. So, that is basically  $g_m (0 - v_{test})$  right. So, that is equivalent to changing the direction of the arrow there and making this simply  $g_m v_{test}$ . So, what do we conclude therefore?

What do we conclude output resistance is therefore,  $g_m R_L / (1 + g_m R_L)$ . I mean another way of doing it without doing this is to basically see that  $v_o$  can be written as  $R_L / (R_L + (1 + g_m v_i))$  and simply staring at this expression you know does this seem familiar?

Student: Voltage divider.

So, voltage divider so, the vertical arm is  $R_L$  the horizontal arm is  $1/g_m$  and it is being driven by voltage source  $v_i$ . So, it is clear that this must be the output resistance ok. I mean if you can see it this way well and good if you cannot never mind it is not important. The fool proof way of finding output resistance is simply what you call de-energizing all independent sources which means that you shoot all the voltage sources and.

Student: Open sources.

Open it all?

Student: Current sources.

Current sources and then apply?

Student: Test voltage

Test voltage and measure the test current that is something that will always work.

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$$v_o = \frac{R_L}{R_L + \frac{1}{g_m}} v_i$$

Common-drain amplifier

So, with this you know everything that we need to figure out about the amplifier is known. So, basically let me redraw the circuit, this is  $v_i$  this is  $R_s$  ok and as you can see which terminal of the transistor is common to both the input side and that is the input source as well as the load.

Student: Drain.

The drain right. So, what would you call this? This is the common drain amplifier. And the common drain amplifier is a way of realizing an incremental voltage controlled voltage source with a gain of 1.

Student: 1.

With a gain of 1.