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Lecture – 58 Three phase Induction Motors

So next we will be you know in another example other 3 or 4 examples and with that we will close the single phase transformer right.

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EX-12 : Ø A 100 KVA, 440/220 VOLL, 19, 50 H3 core type transformer has an efficiency of 98.5%, when supplying full-load at 0.8 bf lagging and an efficiency of 99%, when supplying half-load at unity power factor. Find the iron losses and capper losses at full-lond.

So, it is given that a look at the point a 100 KVA 442 220 volt single phase 50 hertz core type transformer has an efficiency of 98.5 percent when supplying full load at 0.8 power factor lagging an efficiency of 99 percent when analysis of supplying half load at unity power factor. Find the iron losses and copper losses at full load right. So, this is the problem.

So, now I iron loss is equal to W i and full load copper loss say W c full load means that x is equal to 1 right, I mean your it is meaning is something like this right meaning is some suppose, x is equal to you write KVA by KVA full load right. This way if you write, there is suppose transformer is rated some KVA right and the KVA at which KVA it operates.

So, ratio of these thing will give you the your x right the loading factor say. So, if it is KVA is equal to KVA fl then x is equal to 1. So, that is why it is written here x is equal to 1 right.

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00000 14 🖸 | = + 244 + | H 🗄 Sam. Iron Loss = Wi Full-lord cu-loss = WG :, X21 $0 - 985_{0} = \frac{100 \times 10^{3} \times 0.8}{100 \times 10^{3} \times 0.8 + W_{1} + W_{2}}$: 0.985 Wit + 0.985 We = 1200 -- (1) transformer at half-load with Unity

So, therefore, we know these we know derive this formulas efficiency is 98.5 percent. So, 0.985 is equal to your this is the 100 KVA transformer right. So, 100 that is your into 1000 into 0.8 power factor and x is 1, so it is not shown in here, but multiplied by 1 right, they are divided by the same value plus iron loss plus your copper loss W i plus W c. So, if you after simplification, if you simplify this then it will be 0.85 W i plus 0.985 W c is equal to 1200 this is equation 1. (Refer Slide Time: 02:18)

************ $2. \quad 0-985 = \frac{100 \times 10^3 \times 0.8}{100 \times 10^3 \times 0.8 + W_1 + W_2}$ $\therefore 0.985 \text{ With 0.965 Wc} = 1200 --(i)$ Orthout of transformer at half-load with Unity $\text{Pf} = \frac{1}{2} \times 100 \times 10^3 \times 10 = 50 \times 10^3 \text{ WV}.$

Now, when output of transferred half load with unity power factor half load means KVA by 2 right into your of unity power factor 1. This one is unity power factor as 100 KVA transfer half load the half into 100 into 1000 into 1, so 50 10 to the power 3 watt right. Therefore, at that time efficiency was 99 percent.

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***** ⊖ ⊡ | ⊕ © ₽ **|**₀ **|**₀ B $\therefore 0.99 = \frac{50 \times 10^3}{50 \times 10^3 + W_1 + (\frac{1}{2})^2 W_2}$:. 0199W; + 0.2475 Wc = 500 - - (11) Solving equality & (ii), we get, $W_i = 267.3 W$ Ans. $W_c = 950.9 W$

So, 0.99 is equal to then 50 into 10 to the power 3 divided by 50 into 10 to the power 3 plus W i and your copper loss will be half square, because we know that your copper loss is equal to your x square W c and x is a half load, so x is equal to half, so half square W c

right. Therefore, let me clear it. Therefore, 0.99 W i plus 0.2475 W c is equal to 500 that is 2, equation 2. So, solving equation 1 and 2, we get W i is equal to 267.3 watt and W c is equal to 950.9 watt. So, this is the iron loss and this is copper loss this is the answer. Here next is you will solve it, I am make double does double dash that this is this is not example is an exercise for you.

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We = 950.9W EX-13" Calculate the voltage regulation of a transformen having cu-loss of 2%. of the output and the readance drop of 5% when power factor is (a) 0.8 lagging (b) 0.8 leading

You have to calculate the voltage regulation of a transformer having copper loss of 2 percent of the output and the reactance drop of 5 percent, when power factor is 0.8 lagging and 0.8 leading. You will use that formula regulation formula, accordingly you will do it this answer is not given, but this will solve it.

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EX-13 : A single-phase step-down transformer has a turn ratio of 3. The resistance and reactance of the primary winding are 1.20 and 602 and those of the Secondary winding are 0.0512 and 0.0312 respectively. If the high voltage winding is supplied at 230 volt with low-voltage winding short-circuited, find 1 in the Low voltage winding 1: 1

Now, next one is that this is the example 13. Here a single phase step down transformer has its turns ratio of 3; that is k is equal to 3, the resistance and reactance of the primary winding are 1.2 ohm and 6 ohm. And, those are the secondary winding at 0.05 ohm and 0.03 ohm respectively.

If the high voltage winding is supplied at 230 volt with low voltage winding short circuited right, find the current in the low voltage winding, copper loss in the transformer and power factor. It is given that is the high voltage winding is supplied at 230 volt with low voltage winding short circuited. You have to find out the current in the low voltage winding, copper loss in the transformer and the power factor. Already we have studied open circuit test and short circuit right.

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• • * * • 4 = *1 \$ 0* + 4 = 8 (i) current in the Low voltage winding (i) current in the Low voltage winding (ii) copper loss in the transformer (iii) power factor. Sdm. turn rotion k = 3. $R_1 = 1.2 v_2; \quad X_1 = 6 v_2$ $R_2 = 0.05 v_2; \quad X_2 = \begin{pmatrix} 0.3 & v_2 \\ 0.0 & 2 \end{pmatrix}$ HV Side - primary LV Side - Secondary

So, in this case trans ratio is equal to k is equal to 3. High voltage side is primary say low voltage side will define as secondary, here it is look at the curser right. So, R 1 is 1.2 ohm x 1 is 6 ohm. R 2 is 0.0 ohm, x 2 is 0.05 ohm x 2 is this is corrected x 2 is equal to your here it is 0.03 ohm right. So, here it is your point here you here it is not 0.3 just hold on. So, it is 0.03 ohm right 0.03 ohm.

Now, so in this case, so preferred to high voltage side your Re 1 is equal Re 1 is equal to R 1 plus K square R 2 it is referred to high voltage side. Now we will have seen. so R 1 1 0.2k is 3. So, 3 square into 0.05, 1.65 ohm and this one Xe 1 x 1 plus K square x 2 will 6 plus 3 square. This is actually 0.03 right. So, all corrections have been made, so 6.27 ohm right.

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Referred to HV side, $Re_1 = R_1 + K^2 R_2 = 1.2 + (3)^2 \times 0.05 = 1.65 v_2$ Xe1 = X1+ K2X2 = 6 + (3)2X 013 = 623 12 $Z_{e_1} = \sqrt{R_{e_1}^2 + x_{e_1}^2} = \sqrt{(1.65)^2 + (8.2)^2}$ - Zei = 8:855 12.

So, impedance is equal to root over Re 1 square plus Xe 1 square. So, it is becoming actually 6.48 ohm right. So, now the circuit in the high voltage winding to sorry current in the high voltage winding while low voltage winding is short circuited.

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******** Current in the high-voltage coinding when low - voltage winding is short-circuited, $I_{sc} = \frac{V_{sc}}{Z_{el}} = \frac{230}{\frac{8-855}{C.48}} = \frac{25.97}{35.47} \text{ Amp},$ Negleching Io, $I_{1} = I'_{2} = \frac{35.47}{26.97} \text{ Amp},$ Current in low-voltage winding

That mean short circuit current I S C is equal to V S C upon Ze 1. It is given 230 volt divided by 6.48. So, it is actually 35.47 ampere. Now we are neglecting I 0 right. So, if you neglect the I 0 then from the transformer you have seen I 1 is equal to I 2 dash is equal to same current 35.47 ampere.

Now, current in low voltage winding is a transformation ratio will use I 2 is equal to K into I 2 dash I 2 is equal to right. So, K is 3. So, it will become 106.4 ampere.

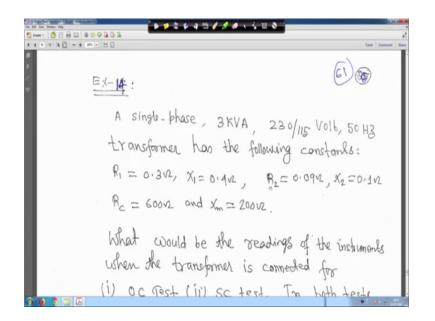
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AD - + MI HO AN $I_2 = KI_2 = 35.47 \times 3 = 77.93 \text{ Amp.} 166.4$ (ii) Total cu-loss $W_{sc_{o}} = I_{1}^{2} Re_{1} = \left(\frac{25.97}{25.97}\right)^{2} \times 1.65 = 1112.8 Hall.$ 2876H (iii) Vsc Isc Cosqsc = Wsc 230x 25 97 cos 95 = 420 2076

So, now total copper loss if you see W S C will be I 1 square R e 1. So, it is 35.47 square into 1.65. So, it is coming 2076 watt right. And here it is your what you call another thing we know the V S C I S C cos phi sc is equal to WSC. I mean Vi cos phi is equal to W same relationship. So, V is 230 volt, current is 35.47 ampere. We have to find out cos and is equal to 2076. So, it is coming actually 0.254 the power factor. This is very simple thing. Only thing is that if you look into that current in the low voltage winding it is actually 106.4 ampere quite high right.

So, if you look into the problem, if you look into the problem that a single phase step down transform this is the resistance and reactance of the primary winding all these given. And if the high voltage winding is supplied at 230 volt with low voltage winding short circuited find the current in the low voltage winding. So, look at that in the current in the low voltage winding. So, look at that in the current in the low voltage winding. So, look at that in the current in the low voltage winding. This intentionally I took this problem it is coming 106 ampere. So, in your laboratory you may not have that ammeter to measure this value of current right. So, but intentionally we took it right so, anyway.

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So, next is your a single phase 3 KVA transformer, 230 by 115 volt 50 hertz transformer has the following constant R 1 given X is given R 2 X 2 also given and R C that coal loss component resistance is given and magnetising component your reactance is given right; everything is given. Now what would be the readings of the instrument when the transformer is connected for open circuit test, then short circuit tests. In both the tests supply is given to high voltage side right, supply is given both the cases to high voltage side.

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TVX (i) OC Test (ii) SC test. In both tests Supply is given to high-voltage side. Solver, (i) or Test $V_1 = 230$ volt, $K = \frac{230}{115} = 2$. $I_c = \frac{V_1}{R_c} = \frac{230}{600} = 0.383 \text{ Amp}$ $T_m = \frac{V_1}{x_m} = \frac{230}{200} = 1.15 \text{ Amp}.$

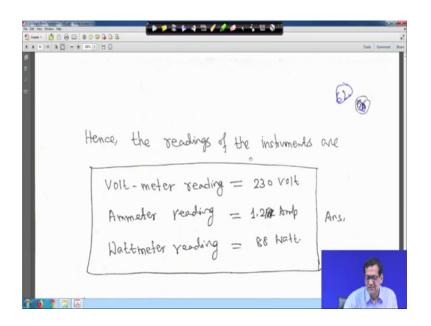
The open circuit test V 1 is equal to 230 volt, K is equal to the trans ratio 230 or voltage ratio 2 by 150 is equal to 2. So, directly can write all these problems we have solve like is like your single phase circuit. So, I c is equal to your V1 upon R c, so 0.383 ampere. Circuit is not the near because, it is understandable and I m is equal to 1 upon X m. So, 1.15 ampere therefore, I 0 is equal to under root IC square plus I m square. So, it is coming 1.212 ampere.

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$$\frac{1}{1} = \frac{1}{1} = \frac{1}{1} = \frac{1}{200} = \frac{1}{1} + \frac{1}{15} + \frac{1}{10} = \frac$$

Now input on no load to high voltage winding will be V1 into I c. That is the input at no load condition. So, it will be 230 into 0.383. So, it is basically 88.09 watt approximately your 88 watt right.

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Now, hence the readings of the instrument are volt meter reading 230 volt, ammeter reading 2 ampere and wattmeter meter reading will be 88 watt right. Now, short circuit test, here K is equal to 2.

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So, R e 1 is equal to R 1 plus K square R 2. So, compute all the thing right So, you will get 0.66 ohm and here it is Xe 1 is equal to X 1 plus k square X 2 you come to it will get 0.8 ohm. Now Z e1 you compute, you will get 1.037 ohm. Full load current in the high

your high voltage winding; this 3 KVA transformer, so I 1 is equal to 3 into 1000 mm by 230 is equal to 13.04 ampere.

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Full-load cubrent in the high voltage winding,

$$I_{1} = \frac{3 \times 1000}{230} = 13.04 \text{ darp},$$

$$\therefore V_{sc} = I_{2}Z_{e_{1}} = 13.04 \times 1.037 = 13.5 \text{ volt},$$

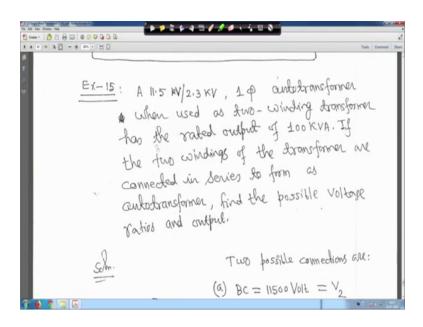
$$W_{sc} = I_{1}^{2}Re_{1} = (13.04)^{2} \times 0.66 = 112 \text{ Walt}.$$

Now, V S C under short circuit condition voltage I 1 into Z e1, you will get it is 13. high volt because, short circuit test it require very low voltage right. So, V S C will be 13.5 volt. So, and your WSC that under short circuit condition the copper loss I 1 square Re 1 it is coming 112 watt.

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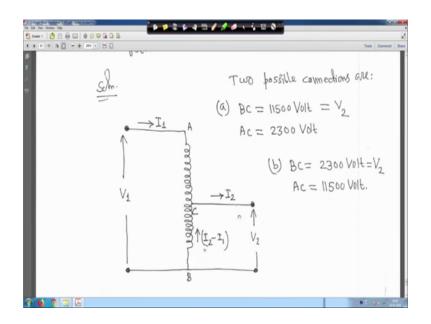
So, therefore, the reading of the instrumental are voltmeter reading will be 13.5 volt, ammeter reading will be 13 ampere and watt metre reading will be 112 watt right. So, your the this is the last problem I think for the transformer. It is an auto transformer now these are very simple thing.

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So, 11.5 KVA up on 2.3 KVA single phase auto transformer when used as 2 winding transformer has the rated output of 100 KVA. Now if the 2 windings of the transformer are connected in series to form as auto transformer find the possible voltage ratio and output right. So, this is the problem. So, how we will do it?

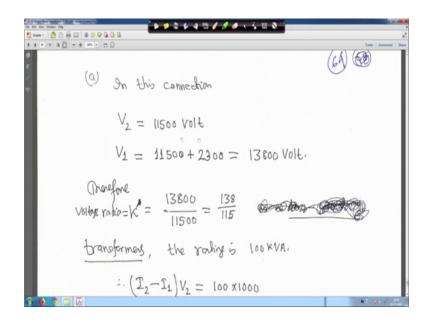
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How we will do it that two possible connections are possible. The here it is, here it is the auto transformer it is A this part is B and this here some part is C right. So, same as before this current is I 1 the upward direction is I 2 minus I 1 and this is the current going to the lord say I 2. The BC portion BC portion, so if it is 11500 volt, say this is my V 2, this is the BC portion look at the cursor point here. BC is equal to your B that is if it is so it is 2300 volt V 2 and AC that is A to C it is 11500 volt right. If we think it as a you are what you call to any transformer. So, BC is this in this much 11500 volt and Ac you are what you call you have taken 2300 volt.

Now, another 1 case is BC is equal to your 11500 volts, in that case this is V 2, this is 1 possible connection. Another you can take AC 2300 volt, another is BC, BC 2300 volt and AC will be 11500 volt, just I you are what you call just 2 possible connection possible right with these.

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So, now in suppose for the first case, in this connection where V 2 is equal to 11500 that is first case mean this one here this one this one, BC 11500 that is equal to V 2 and AC 2300 volt. So, now in this case is equal to 11500 volt therefore, V 1 you add it up right, that is your I mean add it up that is your A to B right. So, in this case it will be 11500 plus 2300 1300 13800 volt. Now, therefore, the voltage ratio your K will be 13800 upon 11500 138 by 115 right.

And you are what you call the transformer the rating is 100 KVA it is given therefore, I 2 minus I 1 into V 2 is equal to 100 into 1000 right because, it is KVA we are your are converting it to volt ampere. Therefore, I 2 minus I 1 you will get 8.7 ampere. Again V 1 minus V 2 into I 1 is equal to again 100 into 1000.

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So, from which we will get I 1 is equal to 43.5 ampere. Just see the theory for auto transformer whatever had been done right. So, now in the therefore, you can get I 2 is equal to 8.7 right from here from this equation 8 I 1 you got 43.5. So, I 2 is equal to 8.7 plus this I 1, so it is coming 52.7 ampere. KVA rating of the auto transformer is given by V 1 I 1. So, substitute all this value you will get six hundred your KVA right. So, this is 13800 into your 43.5, this is 13800, this is 43.5 divided by 1000, you will get 600 KVA or V 2 I if you make 11500 into 52.7 by 1000, here also you will give get 600 KVA right.

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Now, similarly the volume of auto transformer you know 1 minus 1 upon K dash volume of 2 winding transformer, but K dash is equal to V 1 upon V 2 right, that is 138 by 115.

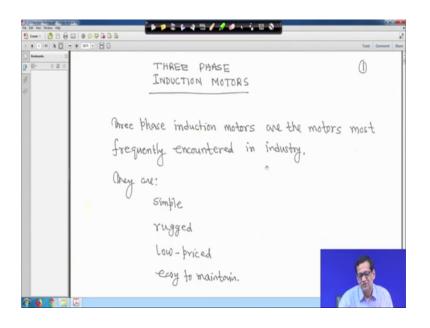
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Therefore, volume of auto transformer probably, 1 minus 115 by 138 into volume of 2 winding transformer; therefore, volume of auto when volume of 2 winding transformer will be 0.17 right, there that is your that is a answer. So, with this you are what you call, with this single phase transformer we have concluded. Things are very simple. Only thing what portion we have to your concentrate that is open circuit test, short circuit test, then your auto transformer right composition of the value of 2 winding transformer and autotransformer right and equivalent circuit and transformation and the efficiency as well as the all day efficiency and the voltage regulation for at unity power factor lagging power factor and leading power factor right.

So, thing for thing also a transformer is very simple. So, next we will start for your what you call that 3 phase induction machine. It will be very I mean only at first year level. So, it is just a basic portion right.

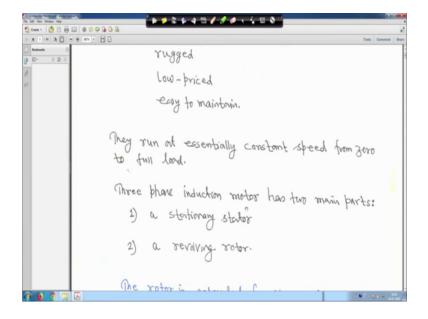
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So, so 3 phase induction motor will start. So, it is actually what particularly as at the basic level only little bit will be covered right. And just see how is it and before making this you are what you call 3 phase induction motor, I will tell at the beginning that whenever you will study this in your college, see the your laboratory that an open induction machine wound rotor induction machine as well as squirrel cage induction motor both wound rotor as well as squirrel cage induction motor it is open things see that stator part see the you are what you call the rotor part because, from here with diagram you may perhaps visualization will be slightly you know based on your imagination. But, in the laboratory definitely you have that your stator open starter open rotor separately such that, you can see on your eyes that exactly what it is right.

So, this is the thing, we will go for single phase transformer. So, hopefully that basic principle of that your induction machine a hope it will not create any problem for you. Things are things are not difficult one, but only basic purpose at first year level. So, 3 phase induction motors are the motor most frequency encountered in industry. They are simple low price, easy to maintain. I mean that is the thing in the you will find in industry all industries right you will find the induction motors are there right because, this is that this without that you without that nothing will move in the industry industrial motors are there.

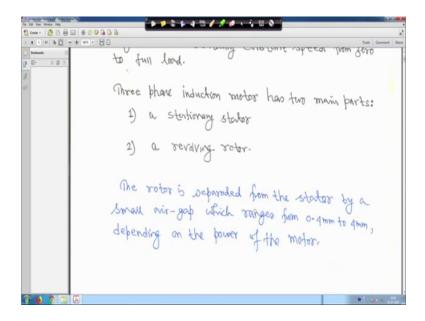
So, there are at essentially constant speed from 0 to full load. Sometimes constant speed means we call sometimes we make it as you know meaning is synchronous speed. So, sometimes we call it has a constant speed right.



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So, the 3 phase induction motor has 2 main parts. 1 is stationeries part that is called stator another is rotating part or revolving part, we call it as rotor right.

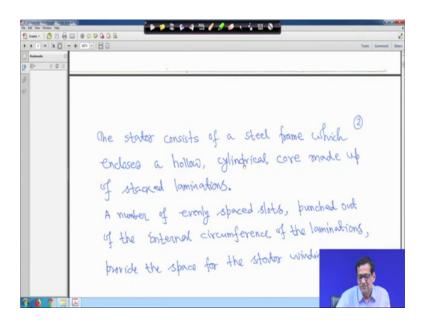
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So, the rotor actually separated from the stator by a small air gas which ranges from 0.4 millimetre to 4 millimetre depending on the power of the motor. So, there is a there is a

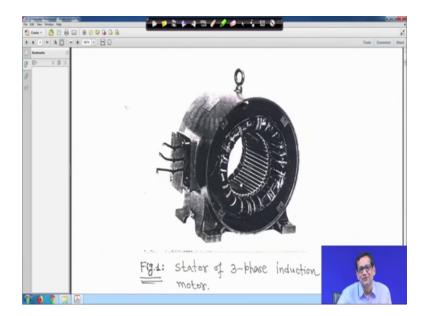
gap in between the stator and rotor and that we call air gap right. So, later we will see the power is transmitted from the stator or to rotor through air gap

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So, now, the stator actually consist of a steel frame which encloses a hollow cylindrical code made above stack lamination I mean this photograph I have I have taken from a book and this is a photocopy looks very you know looks very little bit black because, of this photocopy and these are terminals taken out.

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So, this is actually your steel part and inside that will be steel laminated right and when you will go inside these are the slots where 3 phase windings are there. You I said I said that seen your what you call in your laboratory just to see have a we just see how the stator is or the rotor is in a you are what you call similarly, for your power plant you use synchronous generator. There if you to see your what you call the design of this synchronous generator I mean, when the repair is or something you will find it look so beautiful that you are what you call that is a in first synchronous generator in the power plant right.

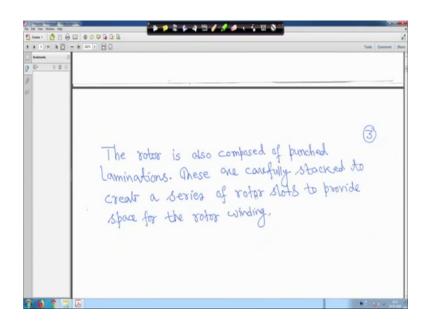
But anyways this is induction motor is a smaller size. Synchronous generator may have a very long rotor right. In any way, so this winding place how it is place, these are the slots all this thing that you will just I suggest that see your what you call your laboratory that your stator that when machine is open definitely some machine will kept you open for your what you call for your realization of this construction.

So, though stator consist of a steel frame; I told which encloses the hollow cylindrical code made up of stacked laminations right, here it is here it is and this is your steel part right. So, a number of evenly spaced lots punch out of the your what you call internal circumference of the lamination provide the space of the for the stator winding. So, stator windings are here. So, I repeat again, see in the laboratory just to see this thing and before saying anything that you have a this is a 3 phase stator know in the transformer the flux was a time varying right. The difference is transforming the static device it is a will be a rotating device.

But in the case of transformer the flux was your time varying right. In this case that in the your stator 3 phasing if you supply the power, we have studied 3 phase surface, so 3 phase windings are there. So, it will create a 3 phase your what you call rotating magnetic field. But rotor not here, rotor will I will show you separately right.

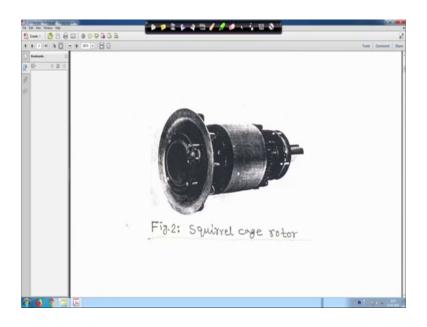
So, 3 phase magnetic field as soon as it is create the because of this your you are what you call that, we if you if we neglect the leakage resistance and reactance like transformer then the a voltage also will be induced in the stator winding in each space right. So, this is starter of 3 phase induction motor.

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So, in this case, the rotor is also composed of punched lamination these are carefully you are stuck to create a series of rotor slots to provide space for the rotor winding.

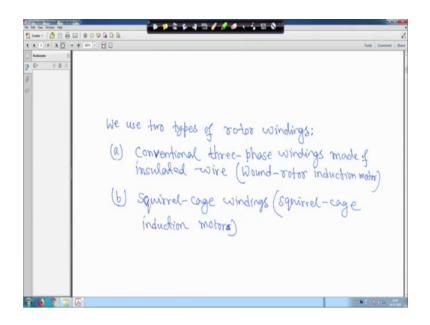
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So, here also I have taken from a book, this pick a looks black because of the photocopy. So, this is actually squirrel cage motor. So, this is the squirrel cage rotor rather right and here whatever see some kind of bar kind of things it is squirrel cage rotor, the slots are there and bars actually are placed into that. And for each a and both a end of this rotor actually you are what you call it is welded by at copper this because, this is made of your what you call cropper.

So, both sides are you are you are what you call you punch together and welded such that, it is short circuit is itself. So, why we will see later, so this is squirrel cage rotor. I suggest in your laboratory see the open induction machine, definitely it will be there right. There thus that you can have a better visualisation.

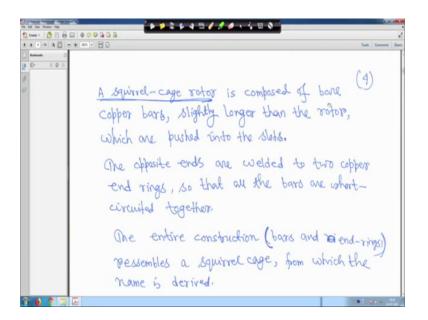
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So, we use 2 types of rotor winding, one is that conventional 3 phase winding made of insulated wire, that that we call in the wound rotor induction motor some circuit diagram will show it later. Another is the squirrel cage winding that is squirrel case induction motor right.

So, ultimately operating principle of both the things are same, final operating principle is same, but wound rotor case we will see through sleeping. You are later I will show circuit diagram that resistance can be connected and at the time of your what you call at the and finally, when it slowly and slowly resistance will be cut down and all these things will be short circuit at together. So, rotor actually for induction machine right rotor are short circuited right. This is a self starting.

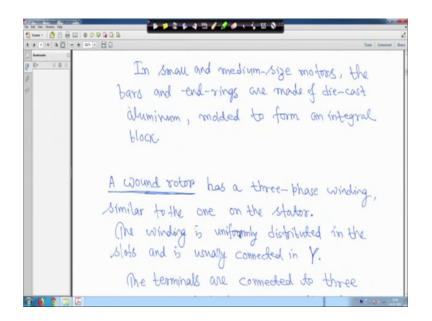
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So, how so a squirrel cage rotor is composed of your what you call bare copper bars. There the bar was showing in the diagram right, slightly larger than the rotor which are pushed into the slot. I suggest you seen that you are what you call in the college that this thing you are open machine, then you will easily understand.

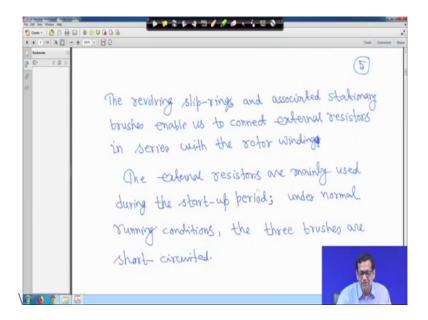
The opposite ends are welded of two copper end ring, so that all the bars are short circuited together right. It is a short circuit. The entire construction bars and end ring your resembles squirrel cage from which the name is derived, later we will see this right. In small and medium size motors, the bars and end rings are made of die cast aluminium moulded to form an in your what you call an integral block.

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Now and wound rotor case, we will see the circuit diagram later has a 3 phase winding similar to the similar one of on the stator. The winding is uniformly distributed in the slots and is usually connected in start right. The terminals are connected to 3 sleeping which turn with the rotor. With that that circuit diagram I will show you that circuit diagram I will show you later right.

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So, the revolving slip ring and you are associated stationary brushes enables us to connect external resistance in series with the rotor winding right. So, the external resistors are actually mainly used during the start up period under normal running condition the three brushes are short circuited right. Under normal running condition the 3 brushes are short circuited.

So, when you do experiment particularly in your second or third year induction machine experiment, at that time wound rotor machine definitely we will see. So, when we will do the laboratory experiment at that time you can see this, but I am not sure whether you will do the same experiment of first year or not right. So, but these are the thing, but if your pure electrical engineer, then you will definitely see it in your second year or third year electrical machine laboratory.

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-----H 3 0 0 0 HS - 8 0 power factor our the 101 operates at full-load is low - about 0.8. At light load (Small I'_2) the machine power factor is much lower. This is the inherent problem of the induction motor because of the presence of the air gap- in the magnetic circuit and the fact that the excitation current must be drawn from the mains (stater side)

Right with this; thank you very much, we will be back again.