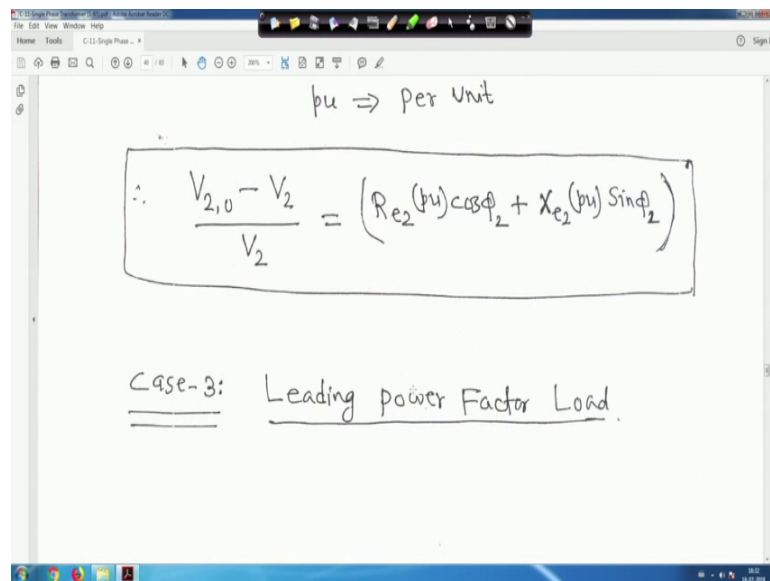


Fundamentals of Electrical Engineering
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Lecture – 57
Single Phase Transformer (Contd.)

Ok, we are back again. So, next is Leading Power Factor Load right.

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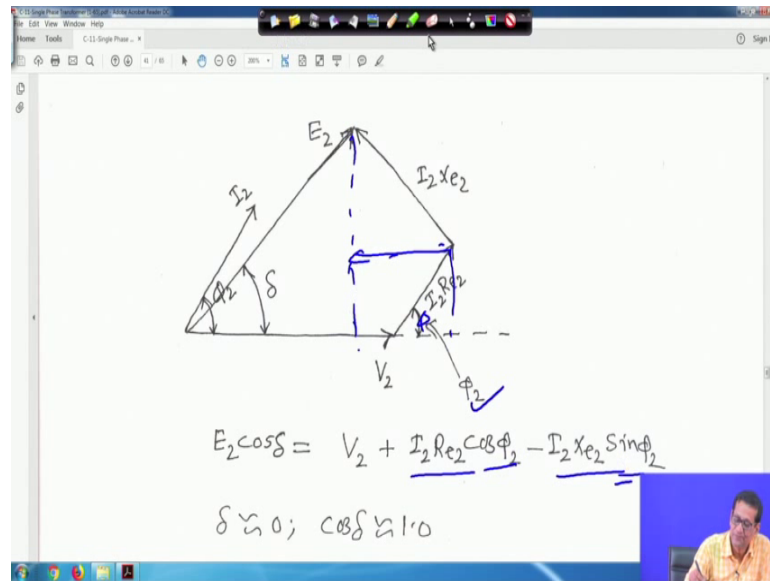
pu \Rightarrow per unit

$$\therefore \frac{V_{2,0} - V_2}{V_2} = (R_{e2}(\text{pu}) \cos \phi_2 + X_{e2}(\text{pu}) \sin \phi_2)$$

Case-3: Leading power Factor Load.

So the way, we have done Lagging Power Factor Load, same way we will do it your Leading Power Factor. In this case current is leading right.

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Look that E_2 square is equal to I_2 did not do it for you. This is your job that you please do it. I have made the approximation one right. So, this is my, I_2 current is this is my V_2 . So, I_2 current is leading. The voltage I_2 is leading voltage V_2 . So, this is my E_2 . So, this is my this angle I_2 angle ϕ_2 is between I_2 and V_2 and angle δ is between E_2 and V_2 everything is clearly marked right.

So, take your what you call the horizontal projection; therefore, $E_2 \cos \delta$ will be V_2 right. I mean it will be this $E_2 \cos \delta$ right I mean this one right, whatever this thing this one we take; so, $E_2 \cos \delta$ will be your V_2 . First you make it like this V_2 plus this one is $I_2 R_{e2} \cos \phi_2$ because this angle is marked here ϕ_2 right and this going like this. So, take its projection right.

So, that will be then you have to subtract it right. So, it will be minus $I_2 X_{e2} \sin \phi_2$ right because you what you call you have to find out $E_2 \cos \delta$. So, it will be first you make V_2 plus this one, then this one you also find out how much it is. So, it is minus $I_2 X_{e2} \sin \phi_2$ right.

So, just 1 minute. So, that and we assume δ is equal to 0; so, $\cos \delta$ is equal to 1 right.

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$$E_2 \cos \delta = V_2 + I_2 R_{e2} \cos \phi_2 - I_2 X_{e2} \sin \phi_2$$

$$\delta \approx 0; \cos \delta \approx 1.0$$

$$\therefore \frac{E_2 - V_2}{V_2} = \frac{I_2}{V_2} (R_{e2} \cos \phi_2 - X_{e2} \sin \phi_2)$$

$$\frac{V_{2,0} - V_2}{V_2} = \frac{I_2}{V_2} (R_{e2} \cos \phi_2 - X_{e2} \sin \phi_2)$$

OR

So, $E_2 - V_2$ upon V_2 is equal to same way we will do it I_2 upon V_2 $R_{e2} \cos \phi_2 - X_{e2} \sin \phi_2$.

(Refer Slide Time: 02:05)

OR

$$\frac{V_{2,0} - V_2}{V_2} = (R_{e2}(pu) \cos \phi_2 - X_{e2}(pu) \sin \phi_2)$$

$R_{e2}(pu) = \frac{R_{e2}}{Z V_2}$
 $X_{e2}(pu) = \frac{X_{e2}}{Z V_2}$

 $= R_{e2} \cos \phi_2 - X_{e2} \sin \phi_2, Ld v 20$

So, $V_{2,0} - V_2$ upon V_2 will be actually is equal to same way that $Z V_2$ is equal to V_2 upon I_2 . So, you will get R_{e2} per unit $\cos \phi_2$ minus X_{e2} per unit $\sin \phi_2$ right. So, if it is your what you call that in general that for Lagging Power Factor sign is plus for regulation; for Leading Power Factor sign is minus right and other thing if you do that your what you call that your that unity power factor let me go to that; that your

unity power factor load the regulation right. Here it is here; that means, here also here look here also you can write know this one is equal to R_e^2 divided by V_2 upon I_2 .

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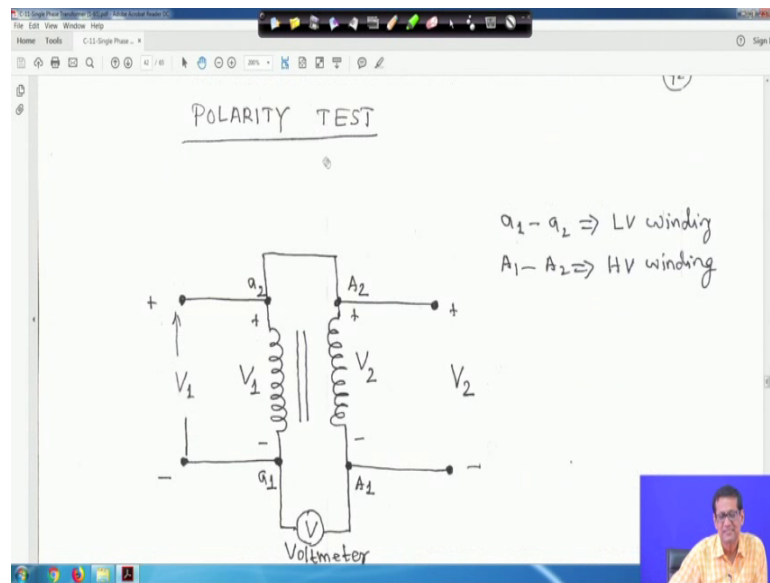
$\delta \approx 0, \therefore \cos \delta \approx 1$
 $\therefore E_2 \approx V_2 + I_2 R_{e2}$
 $\therefore \frac{E_2 - V_2}{V_2} = \frac{I_2 R_{e2}}{V_2}$
 $\therefore \frac{V_{2,0} - V_2}{V_2} = \frac{I_2 R_{e2}}{V_2}$

Case-2: Lagging Power Factor Load ($I_2 \times R_{e2} \cos \phi_2 - I_2 R_{e2} \sin \phi_2$)

So my, this is my R_e^2 divided by Z_B^2 . This is actually is equal to R_e^2 per unit right and unity power factor load so, $\cos \phi_2$ is equal to 1 right. So, that means, that means, that means, in general that formula of the regulation right formula of the voltage regulation of a transformer. So, in general, it will be I am making it here for you. It will be R_e^2 , then per unit $\cos \phi_2$; I can write plus minus X_e^2 per unit $\sin \phi_2$. If it is a lagging power factor, if it is a unity power factor your $\cos \phi_2$ is equal to 1 and $\sin \phi_2$ is equal to 0 right.

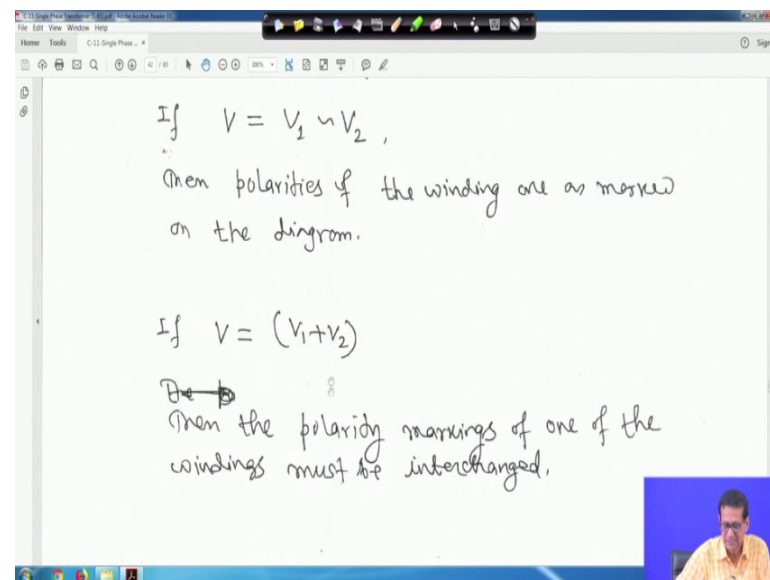
So, ϕ_2 is equal to 0. It will be simply R_e^2 per unit right or and if it is a lagging power factor, it will plus this term. If it is a leading power factor, it will be minus right. This you have to keep it in your mind in general. So, if you just if you remember this only this formula, this formula; so, unity power factor ϕ_2 is 0 right. For lagging power that sign should be your what you call plus right and for leading power factor sign should be minus right. So, this is for your this thing.

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Next is Polarity Test. Here that how we exchange test the polarity in your laboratory when you will do it, definitely you will do like this. So, suppose this is Polarity Test.

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So, a 1 a 2 Low Voltage winding and capital A 1 capital A 2 is High Voltage winding. This thing is given right. So, one thing is there a suppose this polarity is not like this a 1 a 2, it is plus minus a 2 is plus here it is minus. Here capital A 2 plus and capital A 1 minus. This voltage is V 1, V 1 and this is V 2, V 2 and on voltage Voltmeter is

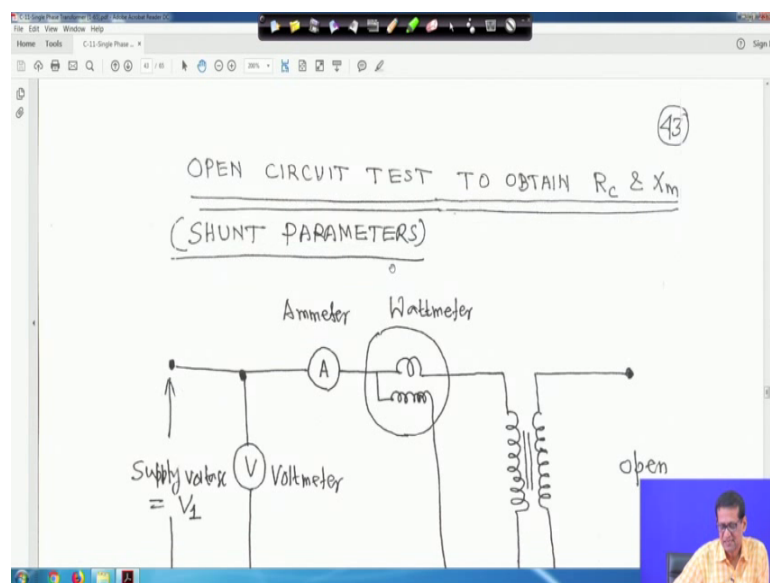
connected your across capital A 1 and small a 1 and this is the polarity now it is marked right.

Now, if V_1 it is difference operator. I am using V_1 , it is difference of course, a difference operator V_2 right; why, I have why I have made this symbol? This is I am giving you a small exercise that why I am writing V_1 difference or V_2 the difference operator. It is actually like tilde right; so, this one written as and if it is like this right. Then, the polarities of the winding are as marked in the diagram.

If you get like this, then you but why I have used difference operator right, then the polarity as it is marked you have what you call in the diagram it will remain as it is. It will not change, it is unchanged if you get the reading of the Voltmeter is like this if you get like, but I have used difference operator? It is a small your what you call exercise for you right.

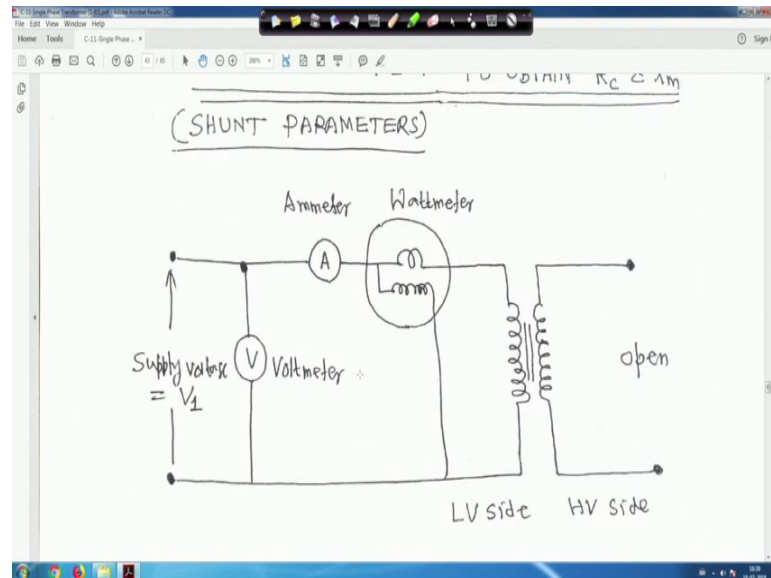
And if you get if you get your V is equal to V_1 plus V_2 right. So, everything is marked actually if you get V_1 V_1 plus V_2 , then the polarity margins of one of the winding must be interchanged either this side or this side; you just interchange right. Then, your what you call your then, if you get V is equal to V_1 plus V_2 . I mean if it is additive right. So, then the polarity markings of one of the windings must be interchanged. So, this is all for polarity test nothing is there actually alright.

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Now, Open Circuit Test to obtain R_c and X_m ; that means, for the transformer, we have to find out the your what you call the parameter right particularly R_c , X_m , R_1 , X_1 , R_2 , X_2 ; all these things you need to obtained. So, generally open circuit test we for to obtain R_c and X_m that is a shunt we call a shunt parameter because these are connected in parallel. These are shunt parameters right; we will perform actually open circuit test.

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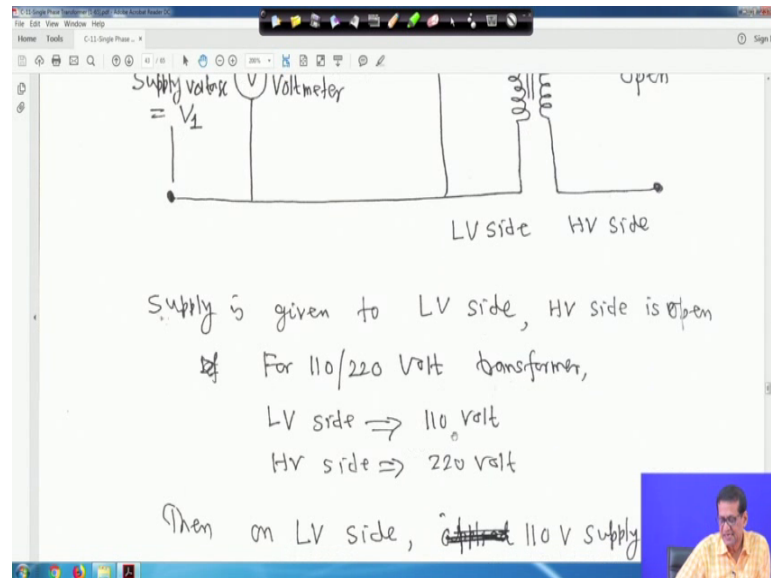
Now, for open circuit test, what we have to do is you need you have to connect 1 ammeter; 1 Voltmeter is there and secondary side that high voltage side actually remain open actually in the laboratory actually its open circuit test or short circuit test whatever it is; it can be performed on either side right.

But in the laboratory right that generally we will perform that this one on LV side your what you call the supplier that your open circuit test, you perform on the LV side and not on the high voltage side right. So, but either side, it can be done; either side, sometimes suppose that voltage level may not be available right. So, because that your what you call the high voltage may not be available in the laboratory that is why we perform your what you call open circuit is your what you call this on the your low voltage side. So, this is the low voltage side for open circuit test right.

But short circuit test in the laboratory performed on the high voltage side. But let me tell you one thing, it can be done on either side; you will get the same result right. So, this is

the Ammeter is connected 1 Wattmeter is connected and 1 Voltmeter is here. In this supply voltage is V_1 right.

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So, if you so supply is given to 1 voltage side and you have to suppose in the laboratory you have 110 by 220 volt. Suppose your transformer is 110 by 220 Volt in the laboratory say then, low voltage side is 110 Volt and high voltage side is your what you call 220 Volt.

Then, on low voltage side 110 Volt is given this side actually 110 Volt is given. Suppose for example, if this low voltage side is 110 Volt and the high voltage side suppose transformer you have 2000 Volt 2 KV. In the laboratory that 2 KV may not be available right that is because for open circuit test you need full voltage. That is why you perform open circuit test on the low voltage side in the laboratory, but either side, it is possible. I mean you will get the same result same parameters value R_c and X_m .

(Refer Slide Time: 08:42)

LV side \Rightarrow 110 volt
 HV side \Rightarrow 220 volt
 Then on LV side, ~~at~~ 110 V supply is given.
 Wattmeter reading gives \Rightarrow Core or Iron loss $\Rightarrow W_i$
 Ammeter reading gives \Rightarrow No-load current $\Rightarrow I_0$
 Voltmeter reading gives \Rightarrow LV side applied voltage $\Rightarrow V_1$
 $\therefore V_1 I_0 \cos \phi_0 = W_i$

So, your what you call that Wattmeter reading is actually in that case wattmeter, this side is open that is secondary is open. There is no load on the secondary; it is written open circuit right. So, whatever Wattmeter will give, it will basically give you the core loss right that is your it is the term because an open circuit is carries no load current right and Ammeter will give you the I_0 , the no load current and Wattmeter will give you the no load power loss right and this is the voltage you are giving 110 Volt.

So, in that case everything is written here Ammeter will give no load current I_0 and your Voltmeter will be your applied voltage is V_1 . So, this Wattmeter reading is known, Ammeter current I_0 is known, supply voltage V_1 is also known; therefore, you can get ϕ_0 . Therefore, $V_1 I_0 \cos \phi_0$ is equal to W_i .

(Refer Slide Time: 09:29)

Handwritten equations on a whiteboard:

$$\therefore \cos \phi_0 = \frac{W_i}{V_1 I_0} = \text{no-load power factor.}$$

$$\therefore I_c = I_0 \cos \phi_0$$

$$I_m = I_0 \sin \phi_0$$

The number 44 is circled in the top right corner.

That means $\cos \phi_0$ is equal to W_i upon $V_1 I_0$ that is no load power factor right and see and therefore, if you get $\cos \phi_0$. So, I_c you will get $I_0 \cos \phi_0$, we have seen before. I_m we will get $I_0 \sin \phi_0$ you will get it right. Therefore, your equivalent circuit say this is R_1 and X_1 .

(Refer Slide Time: 09:45)

Handwritten equations and circuit diagram on a whiteboard:

$$\therefore I_c = I_0 \cos \phi_0$$

$$I_m = I_0 \sin \phi_0$$

The equivalent circuit diagram shows a primary winding with resistance R_1 and reactance X_1 connected to a secondary winding with resistance R_2 and reactance X_2 . The secondary winding is open-circuited. The primary current is I_0 , and the secondary current is I_c . The primary voltage is V_1 . The secondary winding is connected to a core with permeability μ and length l . The secondary winding is connected to a core with permeability μ and length l . The secondary winding is connected to a core with permeability μ and length l .

$$\therefore R_c = \frac{V_1}{I_c} = \frac{V_1}{I_0 \cos \phi_0}$$

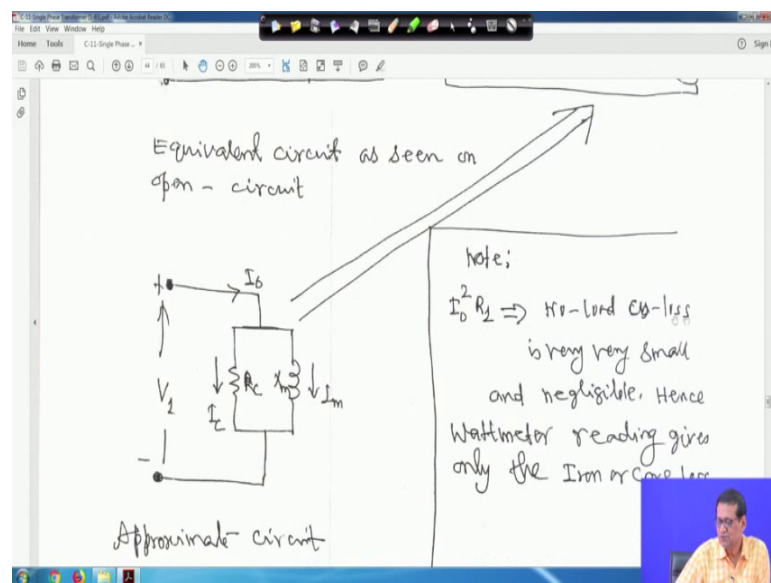
$$X_m = \frac{V_1}{I_m} = \frac{V_1}{I_0 \sin \phi_0}$$

Equivalent circuit as shown

This is the current I_0 , this side is open - your what you call the that your what you call that your secondary side is open circuited.

So, nothing is drawn after these right; nothing is drawn R_1 and X_1 put it here and this is the current I_0 . Therefore, your what you call R_c will be V_1 upon I_c and I_c you have got it because $\cos \phi_0$ you got it I_c you know I_0 you know $\cos \phi_0$. Now, therefore, R_c will be V_1 upon I_c that is V_1 upon $I_0 \cos \phi_0$. Similarly, X_m will be V_1 upon I_m . So, V_1 upon $I_0 \sin \phi_0$. Actually this I_0 current is very small and in the winding resistance of the transformer is also very small. Therefore, this loss your what you call that no at your no load, the winding loss in the transformer is negligible right.

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Therefore, this is the circuit, but equivalent circuit as seen from this when this R_1 X_1 say it is not there neglected. Therefore, this is the equivalent circuit for no load right and everything marked by an arrow right. So, that is $I_0^2 R_1$ no load copper loss is very very small, negligible right. And here, Wattmeter reading gives only iron or core loss. So, what your what you call for open circuit test?

(Refer Slide Time: 10:59)

The whiteboard shows a handwritten circuit diagram of a transformer's primary winding. It consists of a voltage source V_1 connected in series with a resistor R_1 and a reactance X_1 . The current flowing through the circuit is labeled I_m . Below the diagram, the text reads: "Approximate circuit" and "Voltage drop across $(R_1 + jX_1)$ is negligible." To the right of the diagram, there are handwritten notes: "is very very small and negligible. Hence Wattmeter reading gives only the I_m or core loss."

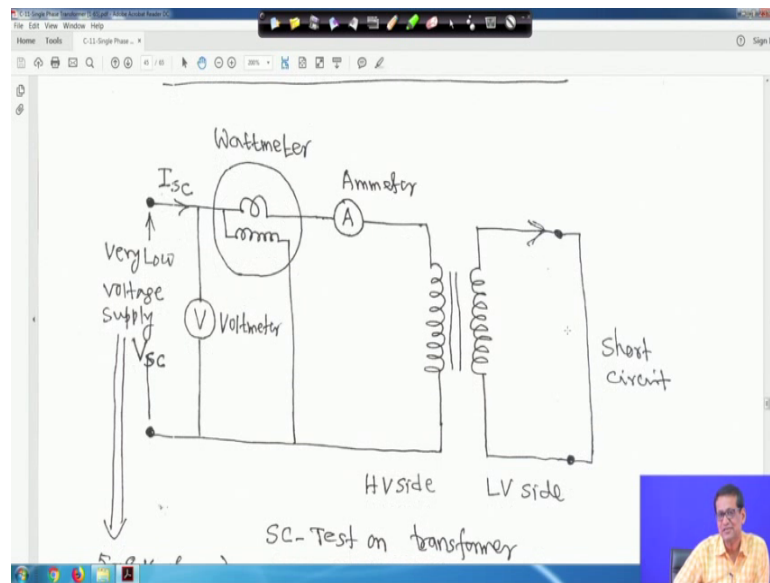
Now, so the voltage drop across R_1 plus jX_1 is negligible because I_0 is very small right. So, this is your approximate circuit.

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The whiteboard features a handwritten title: "SHORT-CIRCUIT TEST TO OBTAIN SERIES PARAMETERS (R & X)". Below the title is a circuit diagram for a short-circuit test. It shows a transformer with its secondary winding short-circuited. The primary winding is connected to a "Very Low voltage supply". A voltmeter is connected across the primary terminals, and the current is labeled I_{sc} . A wattmeter is connected in series with the primary winding, and an ammeter is connected in series with the secondary winding. The word "Short" is written at the bottom right of the diagram.

Now, Short - Circuit Test to obtain the series parameter that is your resistance and reactance.

(Refer Slide Time: 11:14)



Now, actually in a transformer there now this is the Short - Circuit Test. Short - Circuit Test is performed on the high voltage side because when we perform the Short - Circuit Test that we need hardly 5 to 8 percent of the total your voltage on the high voltage side right, to flow the your what you call the rated current or full load current say the secondary is the your what you call low voltage side is the short circuit not secondary is low voltage side is the short circuited right.

So, to allow that rate[e]- your full load current to flow or rated- current to flow, this short circuit; this low voltage side, it needs very small voltage right maybe 5 to 8 percent of the rated voltage on the high voltage side. So, it is written here very low voltage supply and this is V_{sc} . So, this supply is given for an your, what you call for an instrument called VARIAC, variable resistance supply.

Just if you just move it like this then, fuse will blow right because it will use current. So, this is as this is my short circuit current, this is the Voltmeter is connected, Wattmeter is connected and this is Ammeter and this is the your what you call that low voltage value short circuit, it is shorted right.

(Refer Slide Time: 12:20)

The image shows a whiteboard with handwritten notes. At the top, it is titled "SC-Test on transformer" and has "HV side" and "LV side" written above it. On the left side, there are two vertical arrows pointing downwards. The first arrow points to the text "5-8% of Rated Voltage". A large right-pointing arrow connects this text to the right side of the board. Below "5-8% of Rated Voltage", there is another downward arrow pointing to the text "As a result the exciting current under SC condition 0.1 to 0.5% of full-load current". On the right side, the text reads: "Transformer Resistance and Leakage reactance are very small. Hence 5-8% of rated Voltage is sufficient to circulate the full-load current." At the bottom of the whiteboard, there is a line of text: "110/220 Volt transformer, 2.2 KV". In the bottom right corner, there is a small video inset showing a man in a yellow shirt.

Now, in this case 5 to 8 percent of the rated is required to allow that your full load current or your rated current. So, as a result the exciting current your what you call current under short circuit condition 0.1 to 0.5 percent of the full load current. So, exciting current means I_0 ; so, that is negligible very very small right. And transfer resistance and leakage reactance are very small; here 5 to 8 percent of rated voltage is sufficient to circulate the full load current. Because it is short circuited, it is short circuited right and transformer resistance and leakage reactance is very very small size right.

So, Wattmeter reading actually will give you the copper loss and this Ammeter reading will that give the your what you call full load current.

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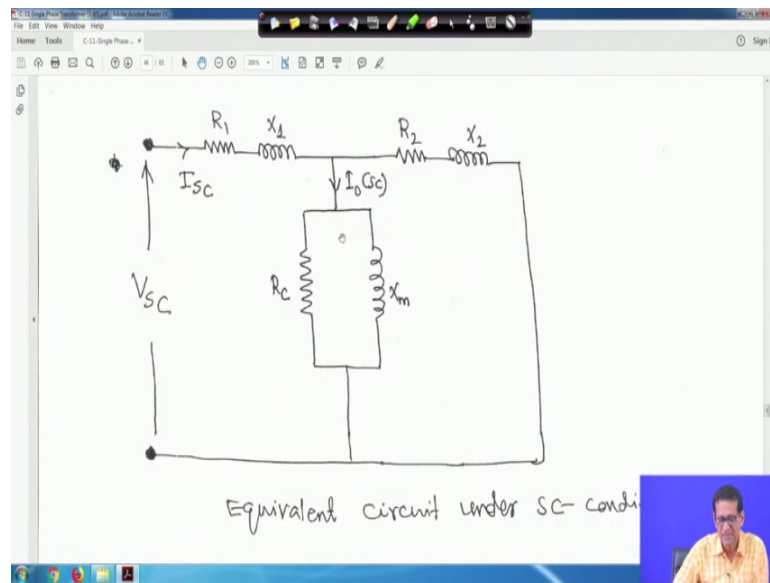
The image shows a whiteboard with handwritten notes. On the left side, it says "Under SC condition 0.2 to 0.5% of full-load currents". On the right side, it says "5-8% of rated voltage is sufficient to circulate the full-load current". In the center, it says "110/220 Volt transformer, 2.2 KVA transformer" and "HV = 220". Below that, it says "∴ V_{SC} = 5-8% of 220 Volt." and "Forexample V_{SC} = 5% of 220 Volt = 11 Volt.". On the right side, there is a calculation: $I_{SC} = I_{FL} = \frac{2.2 \times 1000}{220} = 10 \text{ Amp.}$. At the bottom right, there is a small video inset of a man speaking.

So, in this case if it is suppose 110, 220 volt. So, and say transformer for example, if it is 2.2 KVA transformer. So, high voltage side actually 220 volt. So, short circuit voltage you need 5 to 8 percent of 220 Volt; that means, your 5 to 8 percent means roughly your 5 percent of 220 Volt means hardly 11 volt.

So, if your what you call if your 11 Volt about 11 Volt you supply a rated current that is the full load current that 2.2 KVA transformer. So, 2.2 into 1000 by high voltage side voltage is 220. So, 10 Ampere; that means, you will allow that 10 Ampere current to flow right.

And five if a 5 percent is 11 volt. So, around 11, 12 or 13 Volt, you will find the 10 Ampere current is flowing. So, that VARIAC you have to move it very slowly. Suppose, if you move it very fast; then, fuse will be off. Again you have to the your what you call again you have to switch off the supply and you have to reconnect the fuse wire right.

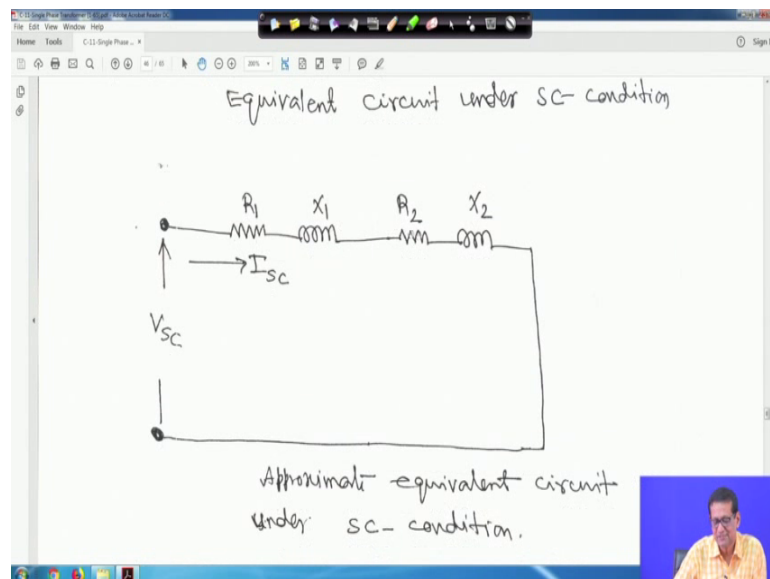
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Therefore, this is the equivalent circuit you have studied for a transformer right and this is the short circuit current and this is I_0 this thing, but this your what you call this I_0 is very small percent of the I_{SC} . So, this term we will neglect. This loss in the R_c we actually we will neglect right wattmeter in the Wattmeter reading that equivalent circuit under short circuit condition.

If you neglect this, this part because I this component this loss here will be very negligible here very negligible.

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So, that means, it will be a simple circuit right; simple series circuit. So, you will get your $R_1 \times 1$, $R_2 \times 2$ are all in series right. So, it is the approximate equivalent under short circuit condition. So, voltage is equal to V_{sc} current is equal to I_{sc} .

(Refer Slide Time: 14:38)

Approximate equivalent circuit under sc-condition.

Voltage = V_{sc}
 Current = I_{sc} } Full-load current,
 Power = W_{sc} } Copper-loss.

And power is equal to W_{sc} that is the Copper-loss. I_{sc} is the Full-load current and V_{sc} is the voltage; what I told you reconnect under short circuit condition to the low voltage side that is 5 to 8 percent right.

(Refer Slide Time: 14:49)

$Z = \frac{V_{sc}}{I_{sc}} = \sqrt{R^2 + X^2}$

$(I_{sc})^2 R = W_{sc}$

$\therefore R = \frac{W_{sc}}{(I_{sc})^2}$

$X = \sqrt{Z^2 - R^2}$

$R = R_1 + R_2$
 $X = X_1 + X_2$

These values are referred to HV side

So that means, Z is equal to now V_{sc} upon I_{sc} that is impedance of the transformer we will get, that is $\sqrt{R^2 + X^2}$ right. Actually, R is equal to $R_1 + R_2$ and X is equal to $X_1 + X_2$ right.

Another thing you know that $I_{sc}^2 R$ the copper loss is equal to Wattmeter reading because total R is $R_1 + R_2$. So, $I_{sc}^2 R$ is equal to W_{sc} the Wattmeter reading right. Therefore, R is equal to W_{sc} upon I_{sc}^2 . So, we get $R_1 + R_2$ right. These values all are referred to high voltage side because short circuit test is performed on the high voltage side right. Therefore, this is my Z we got.

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$$(I_{sc})^2 R = W_{sc}$$

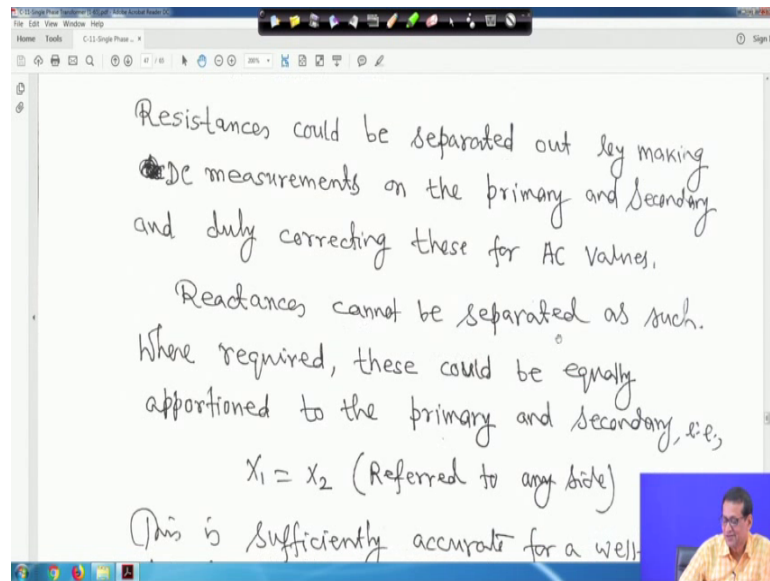
$$\therefore R = \frac{W_{sc}}{(I_{sc})^2}$$

$$X = \sqrt{Z^2 - R^2}$$

These values are referred to HV side.

So, this is X equal to then root over Z square minus R square right, but Z is a your what you call X also is equal to $X_1 + X_2$ together; R also $R_1 + R_2$ together right. But, but how we will separate this right?

(Refer Slide Time: 15:42)



So, generally resistance could be separated out by making DC measurement on the primary and secondary and duly you are correcting these for AC values. This one, I am not doing in this video course, but I am telling you that from your you try to find out that how to find out the resistance suppose if it is asked that each side of the transformer winding, you measure the resistance right. How you will do this? It that resistances could be separated out by making DC measurement right on the primary and secondary and duly correcting those for AC values. This you should try to do it now of your own right.

That and second another thing is that your reactance's cannot be separated as such right, but where you right where your you required, these could be equally your approximated to the primary and secondary side.

(Refer Slide Time: 16:32)

DC measurements on the primary and secondary and duly correcting these for AC values.
Reactances cannot be separated as such.
Where required, these could be equally apportioned to the primary and secondary, i.e.,
 $X_1 = X_2$ (Referred to any side)
This is sufficiently accurate for a well designed transformer

For a well designed transformer generally reactance is X_1 is equal to X_2 referred to any side right. This is sufficiently accurate for a well designed transformer and for $R_1 R_2$, just an exercise for you just you see you know you put the you put in on the forum that sir we are doing like this and we will we will we will give the answer whether you are correct or not right.

So, another thing numerical, we will come later.

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AUTOTRANSFORMERS
For two-winding transformers, the windings are electrically isolated. In a two winding transformer, all VA is transferred magnetically.
When the primary and secondary windings are electrically connected so that part of the winding is common to the both, the

Another thing is Autotransformer that you what you call that basically it is a your two-winding transformer right; Autotransformer and so, so far whatever I have talked know something I have said also; one example is also not means an Autotransformer, but some instrument name I have taken. So, you tell me give one example of Autotransformer right, where Autotransformer is being used right.

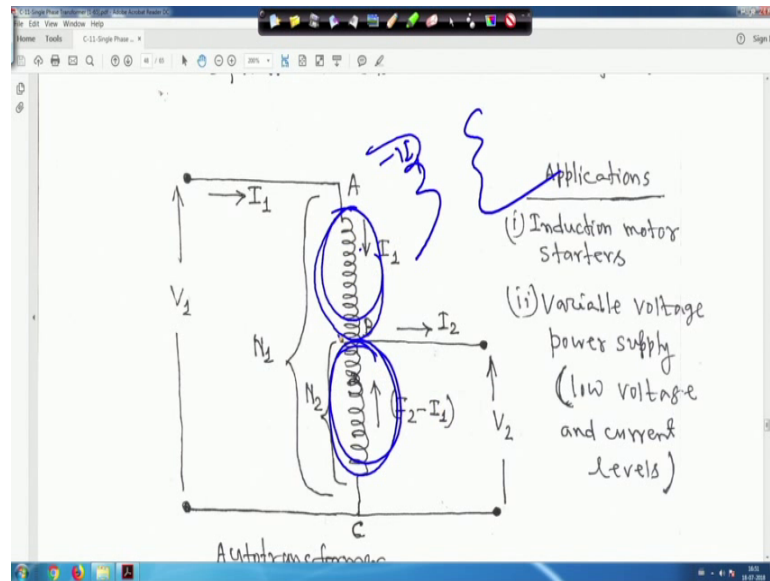
So, something I have written perhaps right for two-winding transformers, the windings are electrically isolated that you have seen right. In a two-winding transformer, all Volt ampere is transferred magnetically that also you have seen for single phase transformer.

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The image shows a digital whiteboard interface. The main content is handwritten text in black ink on a white background. The text reads: "are electrically isolated. In a two winding transformer, all VA is transferred magnetically," followed by "When the primary and secondary windings are electrically connected so that part of the winding is common to the both, the transformer is known as autotransformer." Below the text is a simple circuit diagram showing a horizontal line with a dot at the left end, an arrow pointing right labeled I_1 , and a vertical line at the right end labeled 'A'. To the right of the diagram, the word "Application" is written above a horizontal line, with "(i) Induction m" written below it. In the bottom right corner, there is a small video inset showing a person's face.

When the when the primary and secondary winding are electrically connected. So, that part of the winding is common to both, the transformer is known as Autotransformer. That means, actually primary secondary that is your, what you call windings are electrically connected to that part of the winding is common to both right. In that case, we call this as a Autotransformer.

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For example, application here something is written that induction motor starters variable voltage power supply that is VARIAC right; just I mentioned and your low voltage and current your low voltage and current levels right.

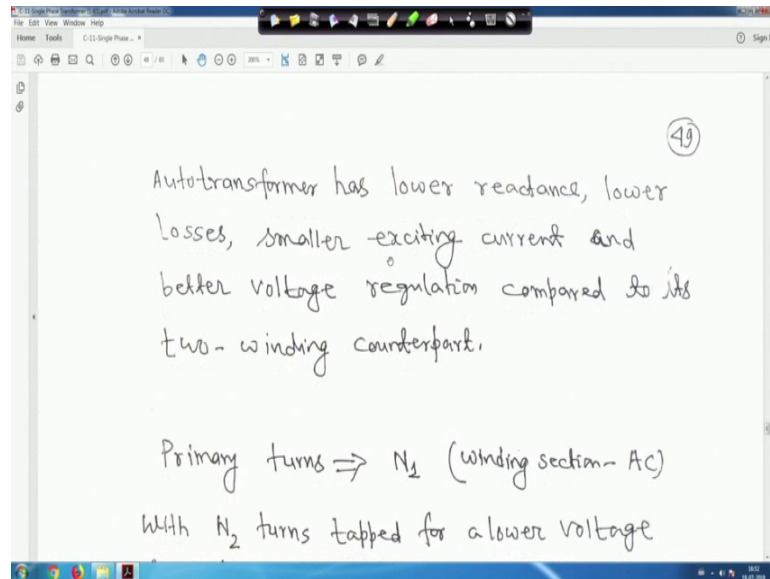
So, basically if you if you consider like this, first little bit we have to understand; there should not be any confusion. Before doing anything I am just trying to tell you suppose this is only 1-1 winding is there that you can see only 1 winding. Now for example, if I want it is a two-winding transformer, then what I will what we will do? This one we consider as 1 winding and this one, we consider another winding right. For two-winding transformer as if as if this is 1 as if this way you imagine. So, if you consider this part. So, current is flowing here is I_1 right and if you consider this part it is I_2 minus I_1 right.

This way I mean this as if this part is 1 winding and this part is 1 winding like a two-winding transformer whatever we have studied there. Just now whatever we have studied so far right; so, in that case your what you call this is the current flowing your through this is I_1 and current suppose if load is connected, this is I_2 and this if you take in this direction, current will be I_1 minus I_2 , but I have taken in this direction. So, it will be I_2 minus I_1 right. So, for from A to C, this is A and this is total winding number of turns is N_1 and for B to C number of turns is N_2 and current flowing A to B is I_1 and your C to

B in this direction is I_2 minus I_1 and this is the current I_1 and this is the voltage V_1 and this is the voltage V_2 right same as whatever.

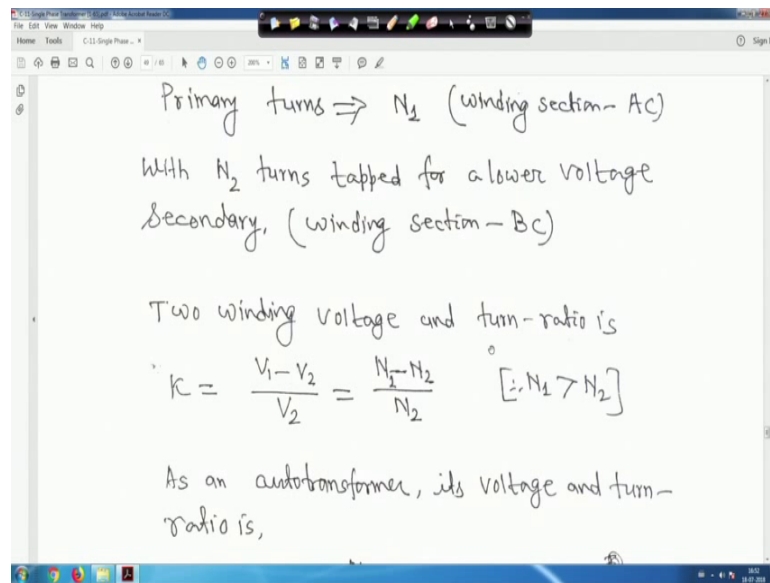
But when you consider two-winding transformer as if this is 1 winding and this is another winding, when you see the autotransformer we will make in different way right.

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So, in this case, so this is an Autotransformer, but we have to compare these 2 right. So, in this case, so Autotransformer has your what you call some lower reactance, lower losses, smaller exciting current and better voltage regulation compared to two-winding your counterpart right. So, primary turns N_1 .

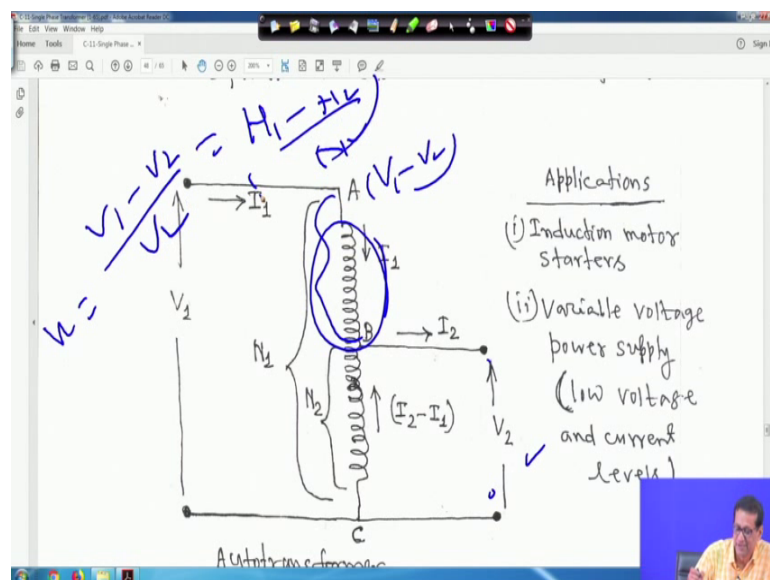
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I told you winding section AC with N_2 turns tapped for a lower voltage secondary winding section BC this I told you.

Now, two-winding voltage and turns ratio right. So, for two-winding voltage, I told you that this for two-winding transformer this is 1 winding right.

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This is 1 winding. This voltage V_1 , this voltage is V_2 . So that means, this voltage is V_1 minus V_2 . I mean here, this voltage is V_1 minus V_2 and this is my V_2 right if it is a two-winding transformer. Therefore, my K actually will be equal to V_1 minus V_2 .

2 by V_2 for two-winding transformer. That means, this one can be written as N_1 minus N_2 divided by N_2 right. This portion only this portion you have to understand here, there should not be any confusion right.

So, in this case ; so in this case, same I am writing K is equal to V_1 minus V_2 upon V_2 , N_1 minus N_2 upon N_2 ; of course, N_1 greater than N_2 .

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As an autotransformer, its voltage and turn-ratio is,

$$k' = \frac{V_1}{V_2} = \frac{N_1}{N_2} > 1 \quad \therefore k' = \frac{N_1 - N_2}{N_2} + 1$$

$$\therefore k' = \frac{(V_1 - V_2) + V_2}{V_2} = \left(\frac{V_1 - V_2}{V_2} \right) + 1$$

$\therefore k' = k + 1$

Now, when you take Autotransformer as an autotransformer its voltage and turns ratio will be V_1 upon V_2 .

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Applications

- (i) Induction motor starters
- (ii) Variable voltage power supply (low voltage and current levels)

Autotransformer

$V_1 = \frac{V_1}{V_2} = \frac{N_1}{N_2}$

For Autotransformer, the same winding we are using for both right. So, for autotransformer, this is your one turn that is your N_1 and this is another turn, same winding; something we are tapping it out right, same winding. So, voltage is V_2 right.

So, for autotransformer suppose K dash is equal to say V_1 by V_2 is equal to N_1 upon N_2 right. When we are taking as autotransformer, this full transformer and part of this we are that voltage we are tapped from this your what you call from some part say between your between A and C that is B and C right. So, in this case ; so, in this case your K dash is equal to V_1 upon V_2 is equal to N_1 upon N_2 that is greater than 1. Because N_1 greater than N_2 from the diagram. Therefore, K dash it was V_1 / V_2 that K dash can be written as you add V_2 subtract V_2 . So, K dash is equal to V_1 minus V_2 upon V_2 sorry V_1 minus V_2 plus V_2 upon V_2 right.

So, this can be written as V_1 minus V_2 upon V_2 plus 1 because V_2 / V_2 by V_2 is 1. Therefore, V_1 minus V_2 upon V_2 is equal to k . So, K dash is equal to K plus K_1 . This is the relationship between the autotransformer turns ratio and that two-winding transformer ratio, the way we have considering right.

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Let us compare VA ratings of the two.

As a two winding transformer

$$(VA)_{TW} = (V_1 - V_2) I_1 = (I_2 - I_1) V_2$$

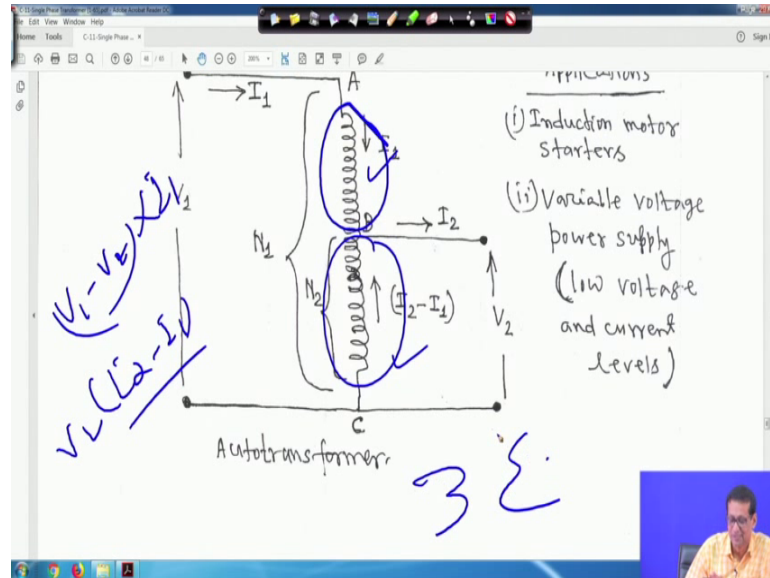
When used as an autotransformer

$$(VA)_{Auto} = V_1 I_1 = V_2 I_2$$

Now, let us compare Volt ampere rating of the 2 right as a two-winding transformer, I told you the voltage is your what T W stands for two-winding. TW stands for two-winding. So, Volt for two-winding transformer that your V_1 minus V_2 into I_1 is equal

to I_2 minus I_1 into V_2 , as if you if you if you go like this as if this is one winding, this is your one winding.

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So, as if (Refer Time: 22:51) voltage here total is V_1 , this is V_2 . So, voltage here V_1 minus V_2 and current flowing through this is I_1 . This is the Volt ampere rating for this winding as if 2 windings are separate this way you imagine and this is another winding is there voltage is V_2 into your I_2 minus I_1 right; both have to be same if the rating Volt ampere rating. As if this is one winding, as if this is another winding; I mean it is like this, it is like this and here it is voltage for this one voltage is your V_1 minus V_2 and current is your I_1 and here voltage is V_2 current is I_2 minus I_1 this way imagine right.

So, that is why that is why it is V_1 minus V_2 into I_1 is equal to I_2 minus I_1 into V_2 .

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$$(VA)_{TW} = \left(\frac{V_1 - V_2}{V_1} \right) (V_1 I_1)$$

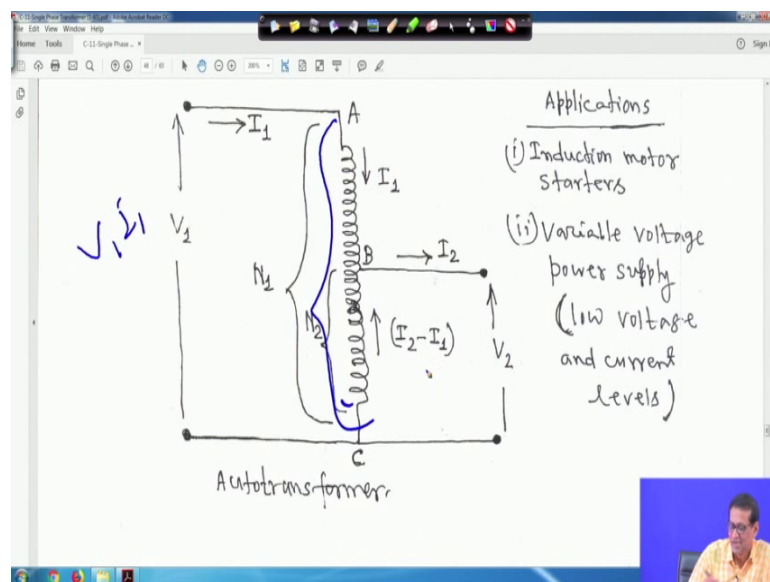
$$\therefore (VA)_{TW} = \left(1 - \frac{V_2}{V_1} \right) (V_1 I_1)$$

$$\therefore (VA)_{TW} = \left(1 - \frac{N_2}{N_1} \right) (VA)_{Auto}$$

$$\therefore (VA)_{TW} = \left(\frac{N_1 - N_2}{N_2} \right) \cdot \left(\frac{N_2}{N_1} \right) (VA)_{Auto}$$

When used as an autotransformer, so Volt ampere will be what will be V_1 into I_1 because same winding we are using. So, for autotransformer; so for autotransformer right, for autotransformer, this is the whole winding.

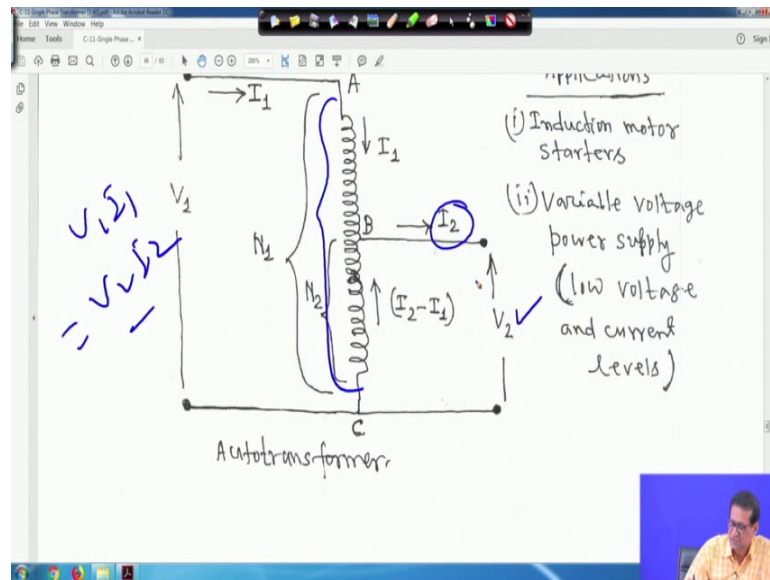
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As if this this way I think primary and secondary right. So, for autotransformer if you take, the this is the V_1 and current is I_1 say $V_1 I_1$ right and output we are taking V_2 into your what you call your this thing your I_2 minus I_1 right.

So, in this case for your for autotransformer, for autotransformer your sorry $V_1 I_1$ is equal to $V_2 I_2$ minus I sorry $V_2 I_2$ actually here hold on. For autotransformer input I have to see the input; input here this is the whole winding. Input here is $V_1 I_1$ and output here is current is I_2 .

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So, this is $V_2 I_2$ is equal to $V_2 I_2$ right because this is the current I_2 going to the load and voltage your here it is V_2 ; so, if is ideal case only. So, it is $V_2 I_2$ is equal to $V_1 I_1$ into I as an autotransformer right.

So, this is an autotransformer; therefore, we can right V_A two-winding transformer is equal to we can write your this your here if you come that V_A two-winding transformer $V_1 I_1 - V_2 I_2$ into I_1 , this one. So, divide numerator and denominator by V_1 here. Here you divide if you do. So, it will be $V_1 I_1 - V_2 I_2$ upon $V_1 I_1$ right or V_A two-winding transformer is equal to this, this bracket part you can write $1 - \frac{V_2}{V_1}$ upon $V_1 I_1$.

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$$\begin{aligned} \therefore (VA)_{TW} &= \left(1 - \frac{N_2}{N_1}\right) (VA)_{Auto} \\ \therefore (VA)_{TW} &= \left(\frac{N_1 - N_2}{N_1}\right) \cdot \left(\frac{N_2}{N_1}\right) (VA)_{Auto} \\ \therefore (VA)_{TW} &= \frac{K}{K'} (VA)_{Auto} \\ \therefore (VA)_{Auto} &= \left(\frac{K+1}{K}\right) (VA)_{TW} \\ \therefore (VA)_{Auto} &= \left(1 + \frac{1}{K}\right) (VA)_{TW} \end{aligned}$$

$(VA)_{Auto} > (VA)_{TW}$

Or you can write V_2 by V_1 is equal to N_2 by N_1 1 minus N_2 upon N_1 and $V_1 I_1$ that is Volt ampere rating of the autotransformer. This is $V A$ auto right because it is $V_1 I_1$ is equal to $V_2 I_2$. So, it is or $V A$ auto transformer.

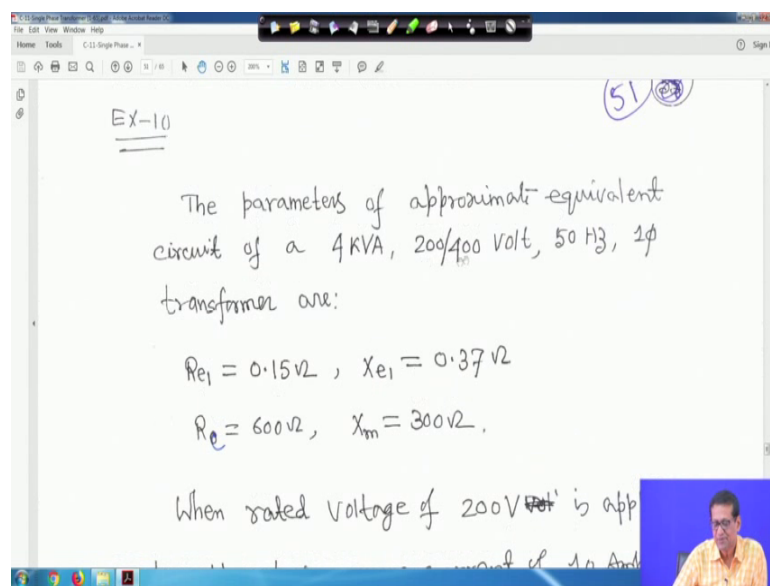
Therefore, if you simplify all these things right that $V A$ this one your what you call this N_1 minus N_2 upon N_1 . So, numerator and denominator this term you multi[ply]-numerator denominator this term you multiply by N_2 . Therefore, what will happen you can write N_1 minus N_2 upon N_2 into N_2 upon N_1 Volt ampere auto right. Therefore, this N_1 minus N_2 upon N_2 your what you call your into N_2 minus N_1 is nothing but K upon K dash $V A$ auto. These portions please do it all this thing relationship is given that K dash is equal to your K plus 1. So, there you use all this relationship. So, you will get $V A$ two-winding transformer is equal to K by K dash your what you call $V A$ auto right.

So, this your this is your K and K dash is equal to already given N_1 upon N_2 . So, it is K upon K dash $V A$ auto right or you can write $V A$ auto is equal to your K dash is equal to we have put K plus 1 because we have seen earlier K dash is equal to K plus 1 cross multiply right. But and put K dash is equal to K plus 1. So, $V A$ auto will be K plus 1 upon K into $V A$ two-winding transformer or $V A$ auto will be 1 plus K is equal to $V A$ two-winding transformer. That means, $V A$ auto is greater than your $V A$ two-winding

transformer that is that is Volt ampere rating of the autotransformer greater than your Volt ampere rating of the two-winding transformer right.

Because your K is greater your what you call K is always your what you call greater than 0 right. So, naturally V A auto what will be greater than V A of two-winding transformer. With this your single phase transformer is over and you will see few a numerical's right and this is very simple thing and nothing is there. Just there should not be any confusion of autotransformer very simple thing right. So, take one example.

(Refer Slide Time: 27:34)



The screenshot shows a digital whiteboard with handwritten text and equations. At the top left, it is labeled "EX-10". The text reads: "The parameters of approximate equivalent circuit of a 4 KVA, 200/400 Volt, 50 Hz, 1φ transformer are:". Below this, the equations are: $R_{e1} = 0.15 \Omega$, $X_{e1} = 0.37 \Omega$, $R_e = 600 \Omega$, and $X_m = 300 \Omega$. At the bottom, it says "When rated voltage of 200V is app". A small video inset in the bottom right corner shows a man speaking. The slide is part of a presentation window titled "C:11 Single Phase Transformer".

The parameters of approximate equivalent circuit of a 4 KVA, 200 by 400 Volt, 50 Hertz single phase transformer. These are the parameters given. R_e is equal to X_e and R_c is equal to given 600 Ohm. X_m is given right.

(Refer Slide Time: 27:49)

$R_e = 600\Omega$, $X_m = 300\Omega$.

When rated voltage of 200V is applied to the primary, a current of 10 Amp, 0.8 pf lagging flows in the secondary winding. Calculate

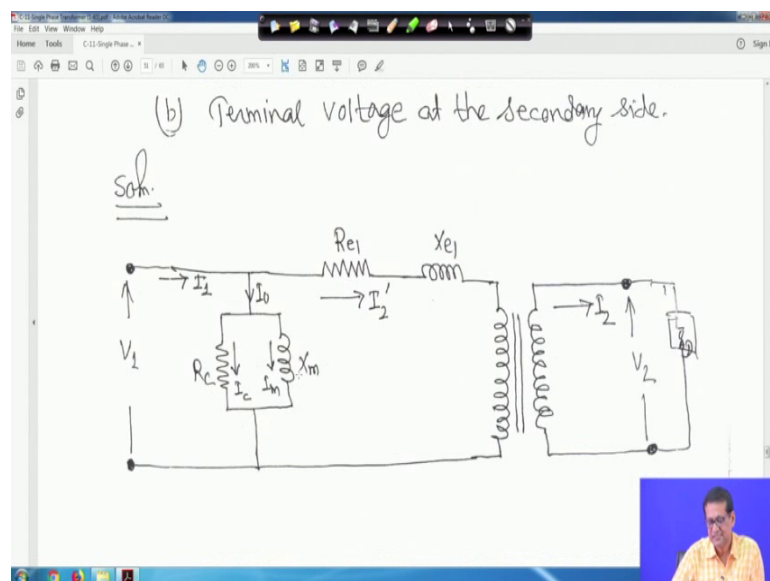
(a) Current in the primary

(b) Terminal voltage at the secondary side

Now, when rated voltage of 200 Volt is applied to the primary a current 10 Ampere 0.8 power factor lagging flows in the secondary winding, you have to calculate. So, this is your problem this is your problem right.

When rated voltage of 200 Volt is applied to the primary a current of 10 Ampere 0.8, power factor lagging your flows in the secondary winding; you have to calculate current in the primary terminal voltage at the secondary side. It is very simple. This is the circuit right.

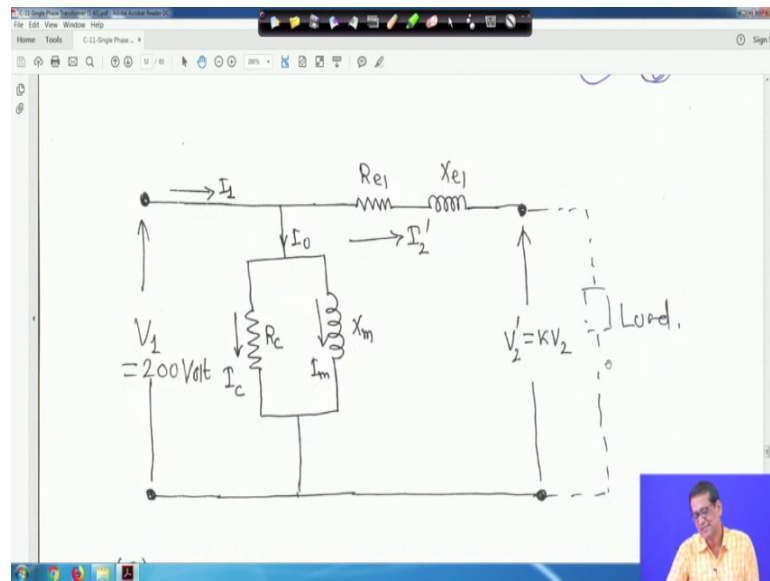
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So, this is your my equivalent circuit R_{e1} X_{e1} right. This one your what you call a this side a load is given. So, everything your in terms of primary side.

So, in that case, your now when we earlier we have seen it know when we transform this to that side, it will be coming out V_2 dash is equal to $K V_2$ and dash lines shows the load.

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Earlier, we have seen this circuit this side 2 hundred Volt parameters are given R_{e1} X_{e1} R_c X_m all are given.

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(a)

$$I_2 = 10 \text{ Amp at } 0.8 \text{ pf lagging}$$

$$\therefore I_2' = I_2 \times \frac{N_2}{N_1} = 10 \times \frac{400}{200} = 20 \text{ Amp at } 0.8 \text{ pf lagging.}$$

$$\therefore I_2' = (16 - j12) \text{ Amp.}$$

$$I_c = \frac{200}{600} = 0.33 \text{ Amp}$$

$$I_m = \frac{200}{300} = 0.67 \text{ Amp.}$$

So, I_2 is given also 10 Ampere right. I_2 is given 10 Ampere at 0.8 power factor lagging. So, I_2 is on the secondary side. So, I_2 dash you have to bring it to the referred to the primary side. So, I_2 dash will be I_2 into N_2 upon N_1 because $N_1 I_2$ dash is equal to $N_2 I_2$. So, I_2 dash is equal to this much. So, I_2 dash you will get 20 Ampere at 0.8 power factor lagging right. That is 36.87 degree lagging; that means, I_2 dash will be 16 minus j 12 Ampere. Directly now it is understandable; so, directly we are writing.

(Refer Slide Time: 29:16)

$$\therefore I_2' = I_2 \times \frac{N_2}{N_1} = 10 \times \frac{400}{200} = 20 \text{ Amp. at } 0.8 \text{ pf lagging.}$$

$$\therefore I_2' = (16 - j12) \text{ Amp.}$$

$$I_c = \frac{200}{600} = 0.33 \text{ Amp}$$

$$I_m = \frac{200}{300} = 0.67 \text{ Amp.}$$

$$\therefore I_0 = I_c - j I_m = (0.33 - j0.67) \text{ Amp.}$$

And I_c will be 200 by 600 because R_c 600 Ohm; terminal voltage is 200. So, this much and I_m is equal to 200 by 300 this much right. So, $I_c I_0$ is equal to I_c minus your $j I_m$. So, this is the current I that is no load current I_0 .

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The screenshot shows a whiteboard with the following handwritten content:

$$\therefore I_1 = I_0 + I_2' = (0.33 - j0.67) + (16 - j12)$$
$$\therefore I_1 = 20.67 \angle -37.8^\circ \text{ Amp}$$

(b)

$$V_2' = V_1 - I_2' (R_{e1} + jX_{e1})$$
$$\therefore V_2' = 200 \angle 0^\circ - (20 \angle -36.87^\circ)(0.15 + j0.37)$$
$$\therefore V_2' = 193.2 \angle -1.2^\circ \text{ Volt}$$

Therefore I_1 is equal to I_0 plus I_2 dash. You just add these two, you will get I_1 is equal to 20.67 angle minus 37.8 degree ampere right and V_2 dash, we know this earlier we have solved an problem. We have seen the derivation also. V_2 dash will be V_1 minus I_2 dash R_{e1} plus jX_{e1} right.

So, in that case you will get V_2 dash after solving you will get your 193.2 angle minus 1.2 degree.

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The screenshot shows a whiteboard with the following handwritten content:

$$\therefore V_2' = 200 \angle 0^\circ - (20 \angle -36.87^\circ)(0.15 + j0.37)$$
$$\therefore V_2' = 193.2 \angle -1.2^\circ \text{ Volt}$$
$$\therefore KV_2 = 193.2 \angle -1.2^\circ$$
$$\therefore V_2 = 386.4 \angle -1.2^\circ \text{ Volt}$$

Ex-1)

And you know that your what you call this Volt and you know V^2 dash is equal to $K V^2$ we know that. So, V^2 will be your what you call 386.4 angle minus 1.2 degree Volt because your K is equal to your half right. So, that Volt ratio is given 200 by your what you call 400 right. So, this problem is a simple problem.

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Ex-11

A transformer has its maximum efficiency of 0.98 at 15KVA at unity power factor. During the day, it is loaded as follows:

1 hr, 3kW, pf = 0.6	} Find all-day efficiency
5 hr, 10kW, pf = 0.8	
5 hr, 18kW, pf = 0.9	
4 hr, - at no load	

Now, example 11: a transformer has its maximum efficiency of 0.98 at 15 KVA at unity power factor. During the day, it is loaded as follows right it is because we have find out all day efficiency. So, for 10 hour, it was 3 Kilowatt, power factor 0.6 right. Lagging, it generally lagging; but not mentioned here right; so, 5 hour, 10 Kilowatt, power factor is 0.8 right and your 5 hour, 15 Kilowatt, power factor 0.9 and 4 hour, at no load. So, total if you add it 24 hours right and find all day efficiency. So, 10 hour, 3 kilowatt. So, basically 3 Kilowatt into 10 means 30 Kilowatt hour right.

So, similarly like this.

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Soln.

Maximum efficiency of the transformer
 $= 0.98$

Load at which maximum efficiency
occurs $= 15 \text{ KVA}$ at unity power factor

At maximum efficiency,
Iron loss $=$ cu-loss.

So, maximum efficiency of transformer is 0.98 that is given. Now load at which the maximum efficiency occurs that is 15 KVA at unity power factor that is given, that maximum efficiency of 0.98 at 15 KVA at unity power factor.

(Refer Slide Time: 31:19)

At maximum efficiency,
Iron loss $=$ cu-loss.

We know

$$\eta_{\text{max}} = \frac{x_{pf}}{x_{pf} + 2W_i} = \frac{\text{Output}}{\text{Output} + 2W_i}$$
$$\therefore \eta_{\text{max}} = \frac{15 \times 1000 \times 1}{15 \times 1000 \times 1 + 2W_i} = 0.98$$

That means, at maximum efficiency iron loss is equal to copper loss that we have derived. We know that for maximum efficiency η_{max} is equal to X_{pf} upon $X_{pf} + 2W_i$ that we have derived that is output by output plus $2W_i$ right.

(Refer Slide Time: 31:37)

Handwritten notes on a whiteboard:

$$\therefore \eta_{\text{max}} = \frac{15 \times 1000 \times 1}{15 \times 1000 \times 1 + 2W_i} = 0.98$$

$\therefore W_i = 153 \text{ W} = 0.153 \text{ kW}$
 at 15 kVA load
 $\therefore \text{Cu loss} = W_i = 153 \text{ W} = 0.153 \text{ kW}$

Interval-1: 10 hrs, ~~load~~ load = $\frac{3}{0.6} = 5.0 \text{ kVA}$
 Cu-loss at 5 kVA load
 $= \left(\frac{5}{15}\right)^2 \times 0.153 = 0.017 \text{ kW}$

Now, output is equal to 15 KVA at unity power factor. So, 15 into 1000 into 1 that is your this much of Watt because therefore, multiplied by 1000 divided by 15 into 1000 into 1 plus 2 W_i is equal to 0.98 because maximum efficiency 0.98 from which we will get W_i is equal to 153 Watt; so, 0.153 Kilowatt.

Therefore, copper loss at where your at maximum efficiency iron loss is equal to your copper loss right. So, it is your 0.153 Kilowatt right. Now interval one that is 10 hours load is 3 by 0.6 that is 5 KVA right because power factor is 0.6 and it is 3 Kilowatt; so, 5 KVA. So, copper loss, we have to find out at this load. Copper loss copper loss is proportional to the square of the load. So, this we will keep in mind your rated KVA 15 is given and at that time load is 5. So, it will be 5 by 15 square into 0.153. So, it is 0.017 Kilowatt right because copper loss varying with the load.

So, at that time, if I because this is Kilowatt divided by power factor will give you KVA right.

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$$= \left(\frac{5}{15}\right) \times 0.153 = 0.017 \text{ kW}$$

Energy Loss = $0.017 \times 10 = 0.17 \text{ kWh}$

Interval-2:
5 hrs 10

So, this similarly that that will energy loss will be 0.017 into 10. So, that is 0.17 Kilowatt hour right. So, this is your, what you call that energy loss. Similarly if you if you just look into this right; so, at 3 Kilowatt power factor is given it is 10 hour. So, if you just your, what you call that load was 3 Kilowatt. So, we converted it to your KVA and it is dependent on the square of the load. At that time, what is the your what you call in that your what you call that energy loss right.

But if it is a simple load nothing is given. So, 3 Kilowatt into 10 means it will be your, what you call 30 Kilowatt hour right. Little bit we have seen at the beginning I think right for the DC circuit analysis something you have seen; so, similarly your interval to 5 hour.

(Refer Slide Time: 33:35)

Interval-2:

$$5 \text{ hrs, Load} = \frac{10}{0.8} = 12.5 \text{ KVA}$$
$$\text{Cu-loss} = \left(\frac{12.5}{15}\right)^2 \times 0.153 = 0.1042 \text{ kW}$$
$$\text{Energy Loss} = 5 \times 0.1042 = 0.521 \text{ kWh}$$

Interval-3:

So, load is twelve point 5 KVA because 10 by 0.8; 0.8 is the power factor. So, copper loss will be 12.5 upon 15 square into 0.153; so, 0.1042 Kilowatt. So, energy loss will be 5 into 0.1042 that 0.521 Kilowatt hour right.

(Refer Slide Time: 33:53)

Interval-3:

$$5 \text{ hrs, Load} = \frac{18}{0.9} = 20 \text{ KVA}$$
$$\text{Cu-loss} = \left(\frac{20}{15}\right)^2 \times 0.153 = 0.272 \text{ kW}$$
$$\text{Energy loss} = 5 \times 0.272 = 1.36 \text{ kWh}$$

Interval-4:

Similarly, interval three, power factor is 0.9 and it is 18 Kilowatt; so, 18 upon 0.9; so, 20 Kilovolt Ampere. So, that time copper loss will be 20 upon 15; that mean, transformer is overload if rating is 15 at 20; that means transformer is overloaded right. So, 20 by 15

square into 0.153; so, 0.272 Kilowatt. So, its energy loss will be 5 into 0.272; so, 1.36 Kilowatt hour.

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Energy loss = $5 \times 0.272 = 1.36 \text{ kWh}$.

Interval - 4:

4 hrs, no-load,
cu-loss = 0.0
Energy loss = 0.0

So, interval four, 4 hours no load copper loss is 0 energy loss is 0.

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Energy loss (due to iron loss) during the whole day
 $= 0.153 \times 24 = 3.672 \text{ kWh}$.

Energy loss (due to cu-loss) during the whole day
 $= (0.17 + 0.521 + 1.36)$
 $= 2.051 \text{ kWh}$.

Now, now energy loss due to iron loss plus during the whole day; so, 0.153 because iron loss 0.153 and 24 hours multiplied, it will be 3.672 Kilowatt hour. Therefore, energy loss due to copper loss during the whole day you add 0.17 plus 0.521 plus 1.36; 2.051 Kilowatt hour.

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Energy Loss (due to cu-loss) during the whole day
 $= (0.17 + 0.521 + 1.36)$
 $= 2.051 \text{ kWh.}$

Total Energy loss $= (2.051 + 3.672) \text{ kWh.}$

Total output during the whole day
 $= (3 \times 10 + 10 \times 5 + 18 \times 5) \text{ kWh}$

So, total energy loss. So, due to copper loss and iron loss, you add you that is 2.051 plus 3.672 right. Total output during the whole day.

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$= (3 \times 10 + 10 \times 5 + 18 \times 5) \text{ kWh}$
 $= 170 \text{ kWh.}$

$\eta_{\text{watt-day}} = \frac{\text{output}}{\text{output} + \text{losses}}$
 $= \frac{170}{(170 + 2.051 + 3.672)}$
 $= 96.7\%$

So, it is your 3 into 10 that is output plus 10 into 5 plus 18 into 5. I told you that initially 10 into 30 Kilowatt hour 5 into 10 and plus 18 into 5. This is the output and this is the copper loss right. So, it is 170 Kilowatt hour. So, output your efficiency is equal to all day will be output by output plus losses.

So, this is output is 170 and this is my, your copper loss and this is my energy in terms of energy. So, it will become 96.7 percent right. So, this is your some 1 or 2 more examples are there like autotransformer and your what you call this thing; we will see in the next video lecture.

So, thank you very much.