

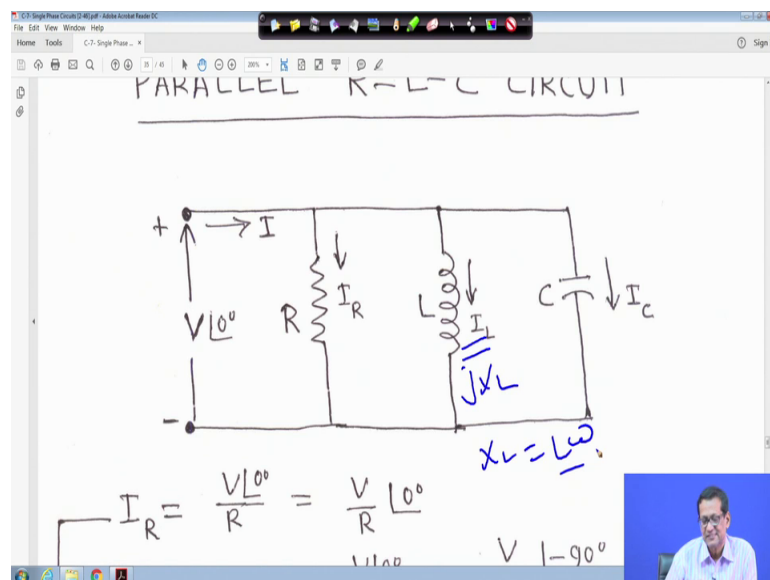
Fundamentals of Electrical Engineering
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Lecture – 44
Resonance and Maximum Power Transfer Theorem

So next we are back again, so, next parallel RLC circuit right, look whenever making it trying to cover each and everything, it will be helpful for you right. And just you I mean things are very simple and as it has been taken from the different books. Books are given in that your what you call all the list of the book, that is and something it is something in my class notes right.

So, something I have tried something of my own also, for our understanding. So, any good book you should follow, the books which I have referred there in your this thing your 4-5 books referred just see those books right. All these books are available right in your library also all these books will be available.

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So, now this is a simple parallel circuit right RLC circuit, voltage source V is given, R, L and C, all these things are parallel. So, current flowing through this R is I_R, through L, I_L and through I_C right. So, what we have to do is that is a parallel circuit. So, let us see I_R, I_L, I_C and I, this total current is I, I is equal to I_R plus I_L plus I_C right kcl if you apply here.

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Handwritten equations for current in a parallel RLC circuit:

$$I_R = \frac{V \angle 0^\circ}{R} = \frac{V}{R} \angle 0^\circ$$

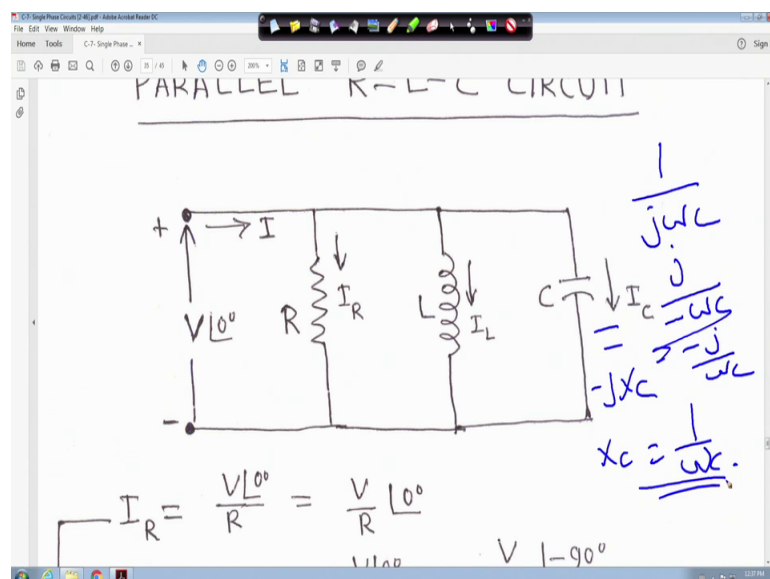
$$I_L = \frac{V \angle 0^\circ}{jX_L} = \frac{V \angle 0^\circ}{X_L \angle 90^\circ} = \frac{V}{X_L} \angle -90^\circ$$

$$I_C = \frac{V \angle 0^\circ}{-jX_C} = \frac{V \angle 0^\circ}{X_C \angle -90^\circ} = \frac{V}{X_C} \angle 90^\circ$$

$$I = I_R + I_L + I_C$$

So, I_R is equal to we are taking this V angle 0 degree, this is reference voltage is given. So, parallel circuit so, V angle 0 upon R so, V/R angle 0 right, this is the I_R . I_L is equal to V angle 0 upon jX_L , this is your whenever it will be given like these this is your this thing. So, it is actually will take jX_L right, X_L is equal to $L\omega$ right, this is your what we call that your X_L is equal to $L\omega$. So, this is jX_L we take so, we take jX_L similarly, for the capacitor when will take actually it is your what you call.

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We will take minus jX_C and X_C is equal to $1/\omega C$ right, this way we will take, generally $1/\omega C$ this will be this thing. If you multiplying numerator and denominator it will be j by j square j square is minus. So, minus ωC is equal to minus j by ωC right.

So, that is why we write minus jX_C and X_C is equal to $1/\omega C$ right. So; that means, your this one; that means, $V \angle 0$ upon jX_L is equal to $V \angle 0 / X_L \angle 90^\circ$. So, V upon X_L angle minus we have seen in the pure inductive circuit your what you call current lag we have seen it.

Similarly, for capacitor we see the currently it is the voltage, $V \angle 0$ minus jX_C . So, it is $V \angle 0 / X_C \angle -90^\circ$ because, of j minus j it is minus 90° . Here because of j it is plus 90° so it will be V upon X_C 90° . So, I is equal to I_R Plus I_L plus I_C right.

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$$I = I_R + I_L + I_C$$

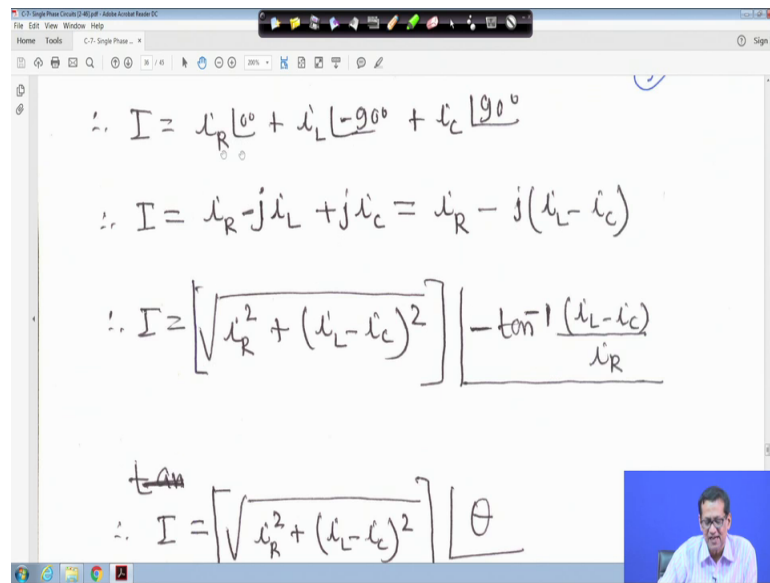
$$I_R = I_R \angle 0^\circ, \text{ i.e., } I_R = \frac{V}{R}$$

$$I_L = I_L \angle -90^\circ, \text{ i.e., } I_L = \frac{V}{X_L}$$

$$I_C = I_C \angle 90^\circ, \text{ i.e., } I_C = \frac{V}{X_C}$$

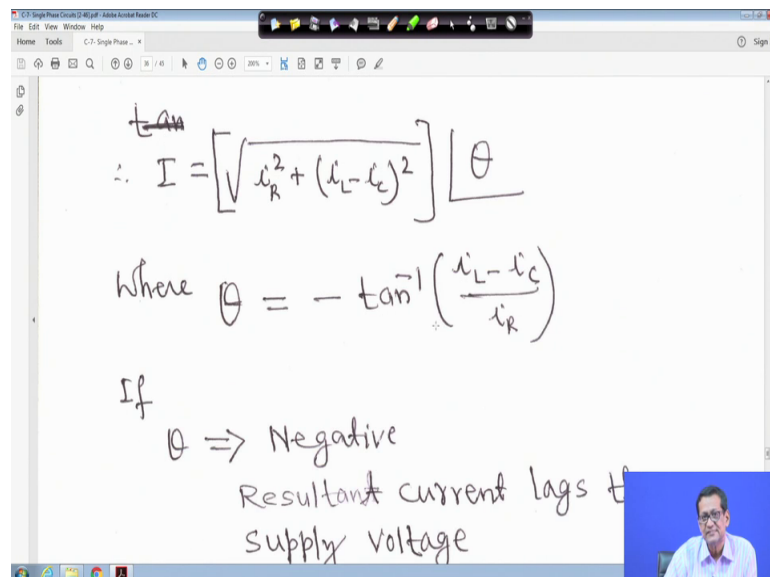
So, I_R is equal so, $I_R \angle 0$ because, your resistive circuit this is your circuit and this is your this is your what we call V upon R angle 0 . So, I_R is equal to your $I_R \angle 0$ that is I_R is equal to V upon R , I_L is equal to I_L angle minus 90° . This I_L is nothing, but V upon X_L this is the magnitude. Similarly, I_C is equal to I_C angle 90° degree, I_C is nothing, but V upon X_C right.

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$$\therefore I = I_R \angle 0^\circ + I_L \angle -90^\circ + I_C \angle 90^\circ$$
$$\therefore I = I_R - jI_L + jI_C = I_R - j(I_L - I_C)$$
$$\therefore I = \left[\sqrt{I_R^2 + (I_L - I_C)^2} \right] \angle \left[-\tan^{-1} \left(\frac{I_L - I_C}{I_R} \right) \right]$$
$$\therefore I = \left[\sqrt{I_R^2 + (I_L - I_C)^2} \right] \angle \theta$$

So, now if you add the total current I will be IR angle 0 plus i L angle minus 90 degree plus i L angle 90 degree. So, its magnitude will be root over IR square plus i L minus i C whole square and angle is minus tan inverse i L minus i C upon R.

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$$\therefore I = \left[\sqrt{I_R^2 + (I_L - I_C)^2} \right] \angle \theta$$

Where $\theta = -\tan^{-1} \left(\frac{I_L - I_C}{I_R} \right)$

If $\theta \Rightarrow$ Negative
Resultant current lags the supply voltage

This is now, understandable to you therefore, you can write this is the magnitude of the current I into angle theta and theta is equal to minus tan inverse i L minus i C by R right.

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If $\theta \Rightarrow$ Negative
Resultant current lags the supply voltage

$\theta \Rightarrow$ Positive
Resultant current leads the supply voltage.

Theta negative then resultant current lags the supply voltage if theta is negative and if it is positive resultant current reach the supply voltage right.

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$I_1 = \frac{V}{Z_1} = Y_1 V$
 $I_2 = \frac{V}{Z_2} = Y_2 V$
 $I_3 = \frac{V}{Z_3} = Y_3 V$

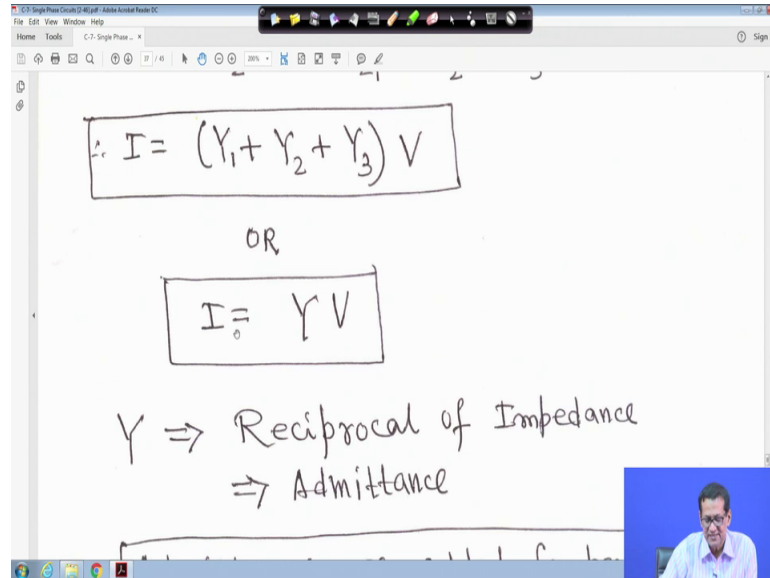
$I = I_1 + I_2 + I_3 = \frac{V}{Z_1} + \frac{V}{Z_2} + \frac{V}{Z_3}$

$I = (Y_1 + Y_2 + Y_3) V$

So, in general this is the circuit here in general. So, here suppose in general if it is Z_1, Z_2, Z_3 . So, it is not pure R it may be some impedance, some impedance, some Z_1, Z_2, Z_3 . So, I_1 will be V upon Z_1 parallel circuit will be $Y_1 V$, I_2 will be V upon Z_2 , it will be $Y_2 V$ and I_3 is equal to V upon Z_3 , it is $Y_3 V$ right therefore, I is equal to I_1 plus I_2 plus I_3 right.

So, it will be V upon Z_1 plus V upon Z_2 plus V upon Z_3 right therefore, I is equal to Y_1 plus Y_2 plus Y_3 V .

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$$I = (Y_1 + Y_2 + Y_3) V$$

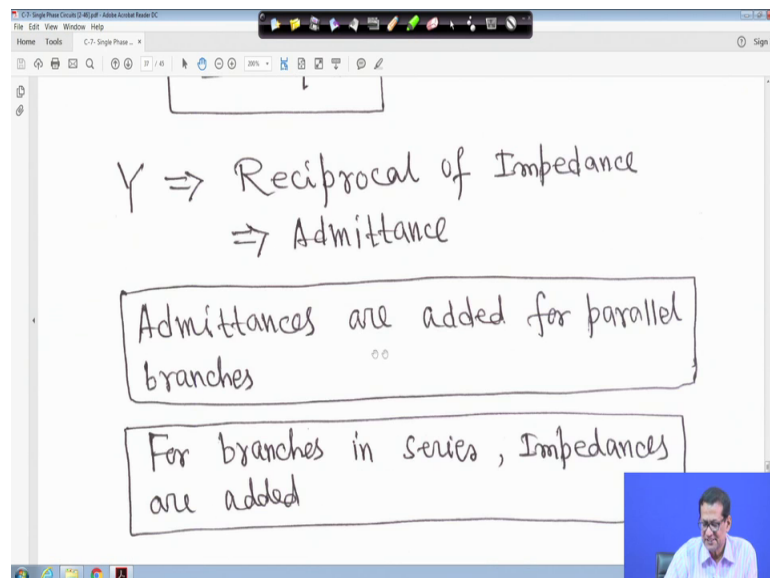
OR

$$I = Y V$$

$Y \Rightarrow$ Reciprocal of Impedance
 \Rightarrow Admittance

Or I is equal to YV or Y is equal to reciprocal of impedance that is called admittance just now we have seen right.

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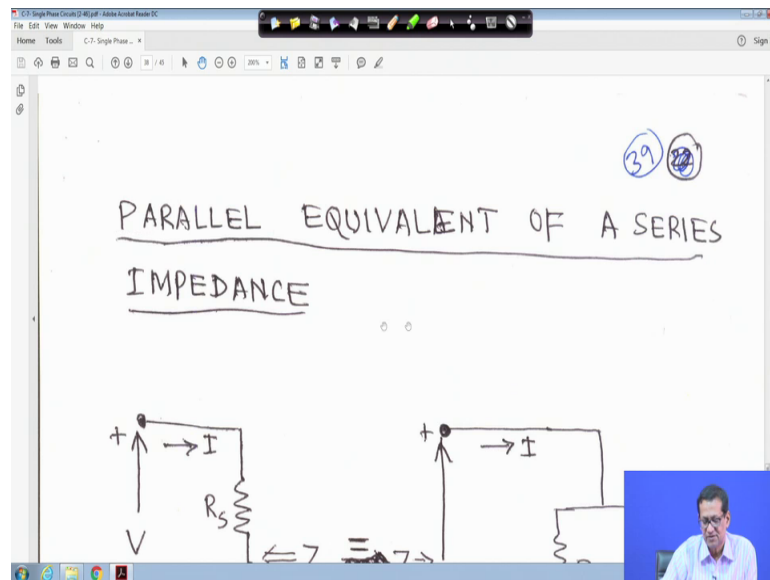
$Y \Rightarrow$ Reciprocal of Impedance
 \Rightarrow Admittance

Admittances are added for parallel branches

For branches in series, Impedances are added

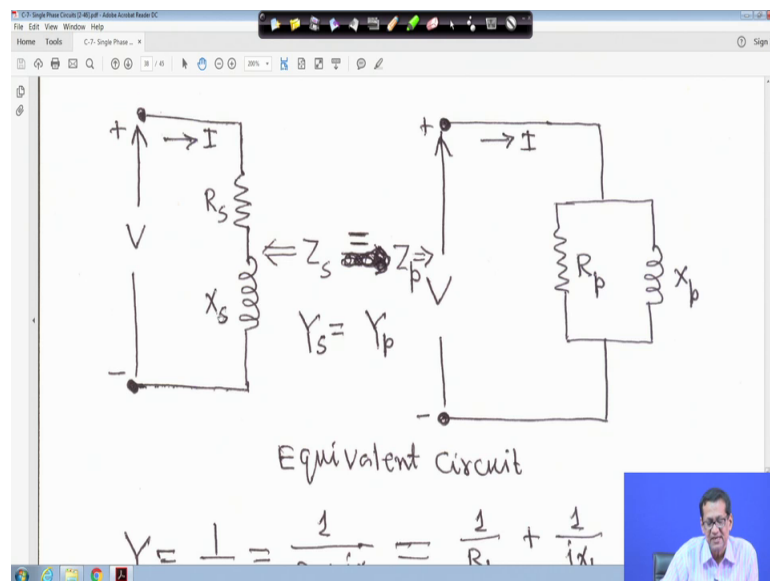
So, admittance are added for parallel branches, for branches in series impedance are added and for branches in parallel right admittance are added right. So, now, parallel equivalent, next is this is the simple thing right this is the simple example will do.

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Now, next is that parallel equivalent of a series impedance right.

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For example this is my series impedance R_s and X_s and this is my supply voltage V . Now, question is that we want this one is equivalent R_p and X_p these 2 circuits are equivalent to each other right. That means, Y_s is equal to Y_p ; that means, series admittance is equal to parallel admittance and this branch is R_p and X_p .

We have to obtain R_p and X_p in terms of R_s and X_s this is eh here what we call that parallel equivalent of a series impedance. So, this is series, what we want is parallel

equivalent right. So, in this case we know Y is equal to 1 upon Z. So, 1 upon Z means for C is equal to 1 upon R S plus jX S this we define Y S. And this is my parallel equivalent is equal to we can write 1 upon R P plus 1 upon jX p because this is inductive so, 1 upon plus jX p.

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Equivalent Circuit

$$Y = \frac{1}{Z} = \frac{1}{R_s + jX_s} = \frac{1}{R_p} + \frac{1}{jX_p}$$

\Downarrow Y_s \Downarrow Y_p

$$\therefore \frac{R_s}{R_s^2 + X_s^2} - j \frac{X_s}{R_s^2 + X_s^2} = \frac{1}{R_p} - j \frac{1}{X_p} = g - jb$$

$$\therefore g = \text{conductance} = \frac{1}{R_p} = \frac{R_s}{(R_s^2 + X_s^2)}$$

This is equals to Y P right or this R S plus jX S you multiply numerator and denominator by R S minus jX S you multiply and then we will get R S upon R S square plus X S square minus jX S upon R S square plus X S square is equal to it is 1 upon R p minus j 1 upon X P. This one, this term you multiply numerator and denominator by j. So, 1 upon R p minus j upon X p that is equal to g minus j b say.

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$$Y_s = \frac{R_s}{R_s^2 + X_s^2} - j \frac{X_s}{R_s^2 + X_s^2} = \frac{1}{R_p} - j \frac{1}{X_p} = g - jb$$

$$\therefore g = \text{conductance} = \frac{1}{R_p} = \frac{R_s}{(R_s^2 + X_s^2)}$$

$$b = \text{susceptance} = \frac{1}{X_p} = \frac{X_s}{(R_s^2 + X_s^2)}$$

G is equal to conductance is equal to 1 upon R p. So, 1 upon R p is equal to separate real and imaginary part, 1 upon R p is equal to R S upon R S square plus X S square this one right. And similarly your 1 upon X p is equal to X S upon R S square plus X S square this is 1 upon X or just go right, R p is equal to R S square plus X S square upon R S, X p is equal to R S square plus X S square upon your X S right.

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Also

$$R_p = \frac{(R_s^2 + X_s^2)}{R_s}$$

$$X_p = \frac{(R_s^2 + X_s^2)}{X_s}$$

Now

$$\frac{V}{I} = Z_s = R_s + jX_s$$

So; that means, this is that parallel your series one series impedance R S plus jX S can be represented by 2 parallel connecting a or what we call impedance. One is of course, is

fairly resistive R_p is equal to this one and X_p is equal to this one. This is called your parallel, this is called your what you call that your series parallel equivalent of a series impedance, this is also possible right.

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The screenshot shows a presentation slide with the following content:

Now

$$\frac{V}{I} = Z_s = R_s + jX_s$$
$$\therefore V = IR_s + jIX_s$$

Below the equations is a phasor diagram. It shows a vector V at the top right. A vector IR_s is drawn from the origin to the tip of V . A vector jIX_s is drawn from the tip of IR_s to the tip of V . The angle between IR_s and V is labeled θ . The angle between IR_s and jIX_s is labeled 90° .

And we know V by I is equal to say Z_s for the series circuit, it is R_s plus jX_s therefore, V is equal to IR_s plus jIX_s . So, V is my reference thing and what we call this is the current I say R in it is inductive circuit. So, I is lagging by an angle θ . So, this one my IR_s and this is my jIX_s right and this angle is 90 degree not marking again by blue ink, but this is 90 degree. So, this is understandable.

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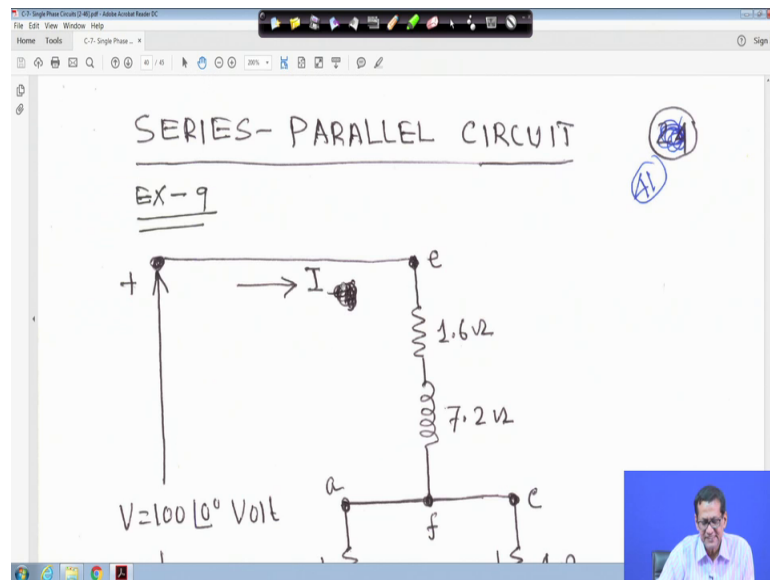
$$\frac{I}{V} = Y_p = \frac{1}{R_p} - j \frac{1}{X_p} = g - jb$$
$$\boxed{I = Vg - jVb}$$

Below the equations is a phasor diagram. A horizontal vector labeled V is shown. A vertical vector labeled Vb points downwards from the tip of V . A diagonal vector labeled I points downwards and to the left from the tip of V . The angle between V and I is labeled θ . A horizontal vector labeled Vg points to the right from the tip of V . A small inset video of a speaker is visible in the bottom right corner of the slide.

Similarly, for parallel equivalent I by V is equal to I_P because, it is admittance that is why I by V and is equal to 1 upon R_P minus j 1 upon X_p is equal to g minus jb right. Therefore, my I is equal to you multiply I by V is equal to g minus jb therefore, I is equal to Vg minus jVb .

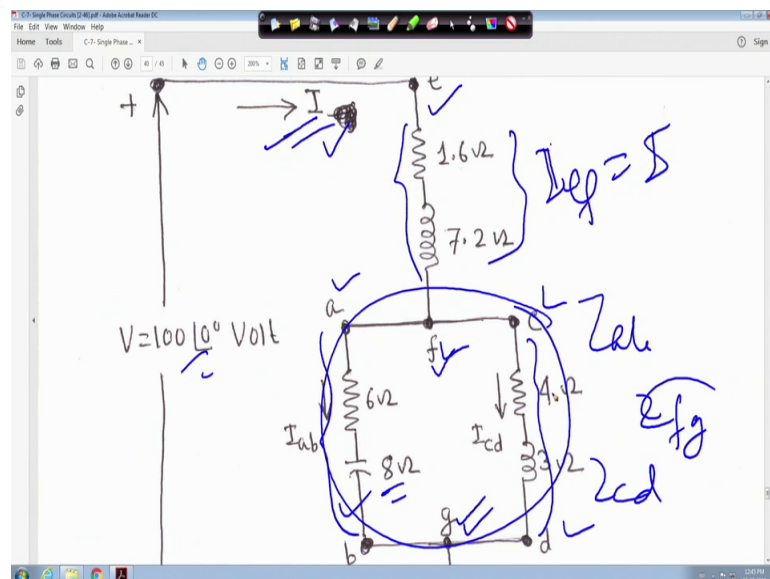
In that case also V is that reference thing, current anyway lagging by θ . So, this is my Vg so, this portion is Vg and this is my imaginary part Vb so, this is my Vb . So, both admittance and both impedance this figure diagram when you call IR_S plus I this thing jIX_S right that is V and when you when you consider admittance it will Vg minus jVb both have been shown right. So, now, series parallel circuit so.

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Suppose take this example that is one series parallel circuit.

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So, this circuit actually it is your this point you have to find out this is the current I and this point is a, this is b, this is c, this is d, this point is e, this is f and this point is g right.

So, this is a see this is series part and this 2 are parallel part. So, everywhere a, b, c, d, e, f, g it is marked right and first thing is this 2 are parallel 4 plus j 3 and 6 minus j 8 it is in parallel right make their equivalent series first; make their equivalent series first with that you add this one right.

After that you divide V by Z you will get the I right so, this is my fg. So, this way it has been it has been marked right your I your I ef is equal to I, this is I right and your Z your what you call this Z fg right this, this is your f point and this is g point. So, you find out that this 2 are in parallel this 4 plus j 3 and are in parallel you find out say equivalent.

So, again and again I will not come to the circuit, but everything is marked. So, this is my this part impedance is Z ab, this part impedance is Z cd right and equivalent is will be Z fg when this 2 parallelly be taken right. Similarly for reciprocal will be your admittance. Again and again I will not come to the circuit.

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Determine I_{ef} , I_{ab} , I_{cd} , power and Power Factor.

Soln.

$$Y_{ab} = \frac{1}{Z_{ab}} = \frac{1}{6-j8} = (0.06 + j0.08) \text{ mho}$$

$$Y_{cd} = \frac{1}{4+j3} = (0.16 - j0.12) \text{ mho}$$

So, you have to find out I ef, I ab, I cd, power and power factor.

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Soln.

$$Y_{ab} = \frac{1}{Z_{ab}} = \frac{1}{6-j8} = (0.06 + j0.08) \text{ mho}$$
$$Y_{cd} = \frac{1}{4+j3} = (0.16 - j0.12) \text{ mho}$$
$$Y_{fg} = Y_{ab} + Y_{cd} = (0.22 - j0.04) \text{ mho}$$

So, Y_{ab} is equal to when you will do this please draw the circuit first right. So, 1 upon Z_{ab} is 1 upon 6 minus j 8 it comes this per value. Similarly, Y_{cd} you do it, it will be 0.16 minus j 0.12 mho right. So, Y_{fg} admittance, Y_{ab} plus Y_{cd} this much is coming.

Now, Z_{fg} is equal to 1 upon Y_{fg} so, it is coming 4.4 plus j 0.8 ohm right. So, Z_{eg} now you add Z_{ef} plus Z_{fg} first what you do, first we compute the admittance of a parallelly parallel circuit is easy for calculation.

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$$Z_{fg} = \frac{1}{Y_{fg}} = \frac{1}{(0.22 - j0.04)} = (4.4 + j0.8) \text{ } \Omega$$
$$Z_{eg} = Z_{ef} + Z_{fg} = (1.6 + j7.2) + (4.4 + j0.8)$$
$$\therefore Z_{eg} = (6 + j8) \text{ } \Omega$$
$$\therefore I = \frac{V}{Z_{eg}} = \frac{100 \angle 0^\circ}{61.8} = 1.618 \text{ A}$$

And then we add and then we are converting finding out the Z fg 1 upon Y fg. So, this much we got, now Z eg the total impedance will be your Z ef plus your this much Z ef is given in the circuit 1.6 plus j 7.2 and this one you add. So, it is coming 6 plus your Z e your what you call 6 plus j 8 ohm.

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$$\therefore Z_{eg} = (6 + j8) \Omega$$

$$\therefore I = \frac{V_s}{Z_{eg}} = \frac{100 \angle 0^\circ}{6 + j8} = 10 \angle -53.2^\circ \text{ Amp}$$

$$\text{Power Factor} = \cos \theta = \cos(53.2^\circ) = 0.60$$

$$P = VI \cos \theta = 100 \times 10 \cos(53.2^\circ)$$

$$\therefore P = 600 \text{ Watt}$$

$$V_{er} = I \cdot Z_{ef} = I_{ef} Z_{ef} = (6 - j8)(1.6 + j7.2)$$

Therefore, current I should be is equal to V upon Z eg. So, this is coming 10 angle minus 53.2 degree ampere. So, power factor is equal to cos theta. So, angle between the voltage as current is 53.2 degree lagging. So, it is 0.60 right and P is equal to VI cos theta.

So, 100 into 10 cosine 53.2 degree so, P is equal to 600 watt right. So, next is V ef is equal to I into Z ef. So, the I is equal to I ef I told you at the beginning so, it is 6 minus j 8 into 1.6 plus j 7.2.

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The screenshot shows a whiteboard with the following handwritten calculations:

$$V_{ef} = I \cdot Z_{ef} = I_{ef} Z_{ef} = (6-j8)(1.6+j7.2)$$
$$\therefore V_{ef} = 73.8 \angle 24.4^\circ \text{ Volt}$$
$$\therefore V_{fg} = V - V_{ef} = 100 \angle 0^\circ - 73.8 \angle 24.4^\circ$$
$$\therefore V_{fg} = 44.7 \angle -42.8^\circ \text{ Volt}$$

A small video inset in the bottom right corner shows a man speaking.

So, this is your 73.8 and angle 24.4 degree volt. Similarly, V_{fg} is equal to v minus V_{ef} if you apply kvl here right, then you will get 0 here what we call V_{fg} we apply the kvl in the circuit. So, am not going to the circuit again and again just you draw and look it you have done this circuit everything, only consider instantaneous polarity and solve it. So, it will be $100 \angle 0^\circ$ ohm minus $73.8 \angle 24.4^\circ$. So, this is coming actually 44.7 and angle minus 42.8 degree volt right.

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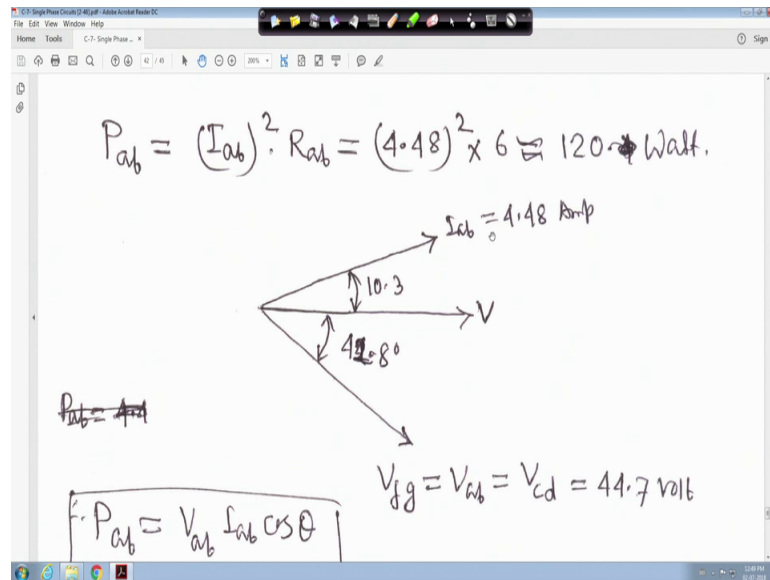
The screenshot shows a whiteboard with the following handwritten calculations:

$$I_{ab} = Y_{ab} V_{fg} = (0.06 + j0.08) \times 44.7 \angle -42.8^\circ$$
$$\therefore I_{ab} = 4.48 \angle 10.3^\circ \text{ Amp}$$
$$I_{cd} = V_{fg} \cdot Y_{cd} = 44.7 \angle -42.8^\circ \times (0.16 - j0.12)$$
$$\therefore I_{cd} = 8.95 \angle -79.7^\circ \text{ Amp.}$$

There are some circled annotations in blue ink at the top right of the whiteboard. A small video inset in the bottom right corner shows a man speaking.

Now, I_{ab} is equal to $Y_{ab} V_{fg}$. So, it is your Y_{ab} you got and V_{fg} now we have we computed here V_{fg} . So, I_{ab} will be this one, 4.48 angle 10.3 degree ampere. Similarly, I_{cd} will be V_{fg} in to Y_{cd} . So, it will get 44.7 angle this one into your Y_{cd} , it is coming 8.95 angle minus 79.7 degree ampere right.

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So, at P_{ab} power loss is equal to $I_{ab}^2 R_{ab}$. So, it is I_{ab} is equal to 4.48 square and R_{ab} is equal to 6 so, it is 120 watt right.

So, again and again I have not come to the circuit then it will consume lot of time, I will suggest please draw this when you look into this video link lecture, you please you please draw the circuit faster. And all these calculations other things if you find any error, you just let me know that whether let me know such that I can rectify myself. Even when am telling with many things 1 or 2 places because, so, many things are there. So, 1 or 2 places am making small error somehow, but I have rectified right immediately.

So, if you have any doubt you can put all that questions in the forum I will give you the answer right. So, whenever you I tell again and again whenever look in to this video lecture first you draw the circuits, then you look what has been done.

So, this is my present diagram this is V is the reference one right angle 0 degree and I_{ab} actually leading voltage 10.3 degree. So, that is why it is leading and your I and other current that your this one your V_{fg} that is 44 point V I mean if you come to that V_{fg}

come to this, it is V_{ab} that is your what you call this is leading and if you come to your V_{fg} it is lagging from this reference voltage V . So, minus 42.8 degree that is why this voltage is 42.8 degree, it is lagging, this all voltages are same 44.7 degree.

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$$P_{ab} = \cancel{44.7}$$

$$V_{fg} = V_{ab} = V_{cd} = 44.7 \text{ volt}$$

$$P_{ab} = V_{ab} I_{ab} \cos \theta$$

$$= 44.7 \times 4.48 \cos(42.8^\circ + 10.3^\circ)$$

$$= 120 \text{ Watt}$$

Now, if you think in terms of power factor P_{ab} is equal to $V_{ab} I_{ab} \cos \theta$ V_{ab} 44.7 into 4.48 cosine of this one. Because, $\cos \theta$ means angle between your this I_{ab} and this your V_{ab} . This is V_{fg} is equal to V_{ab} angle between I_{ab} and V_{ab} . So, 42.8 plus 10.3, this is the power factor angle right, that is why it is taken 42.8 plus 10.3 degree right.

So, it is 120 watt similarly, we saw $I_{ab}^2 R_{ab}$ is equal to 122 W; that means, it is matching if it is not; that means, how much calculate some if it is not somewhere calculation has gone wrong somewhere right so, this is 1.

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Similarly

$$P_{cd} = (I_{cd})^2 R_{cd} = (8.95)^2 \times 4 = 320 \text{ Watt.}$$
$$P_{ef} = (I_{ef})^2 R_{ef}$$
$$= (10)^2 R_{ef} = (10)^2 \times 1.6 = 160 \text{ Watt.}$$
$$P = P_{ef} + P_{ab} + P_{cd} = (160 + 320 + 120)$$

Similarly, your P_{cd} is equal to I_{cd} square R_{cd} , it is 320 watt right and P_{ef} , I_{ef} square R_{ef} square R_{ef} so, it is coming out 160 watt. So, total P is equal to P_{ef} plus P_{ab} plus P_{cd} it is 600 watt right.

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$$P = P_{ef} + P_{ab} + P_{cd} = (160 + 320 + 120)$$
$$P = 600 \text{ Watt}$$
$$PF_{(ab)} = \frac{6}{\sqrt{6^2 + 8^2}} = 0.6 \text{ (leading)}$$
$$PF_{(cd)} = \frac{4}{\sqrt{4^2 + 3^2}} = 0.8 \text{ (lagging)}$$

And power factor your for ab 6 upon root over 6 square plus 8 square, it is 0.6 leading. Power factor for cd part it is 4 upon root over 4 square plus 3 square 0.8 lagging. This one you do it of your own right and if you given that draw phasor diagram.

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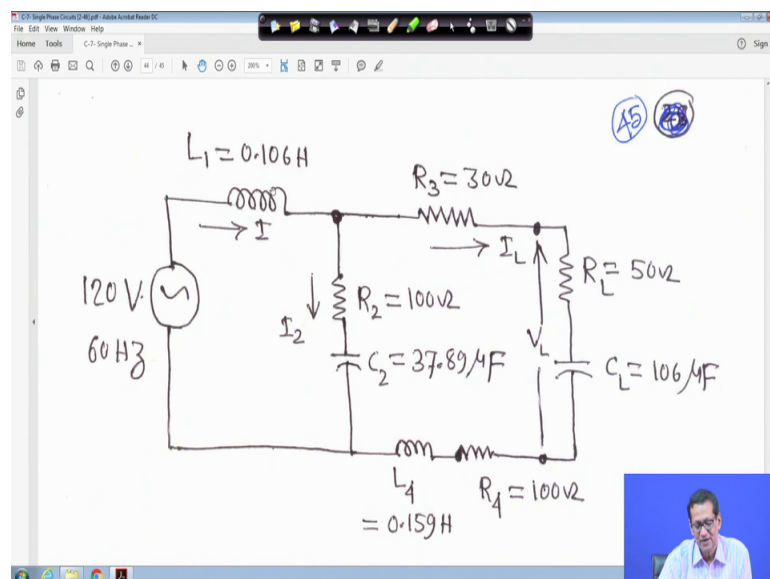
Handwritten calculations on a whiteboard:

$$PF_{(al)} = \frac{6}{\sqrt{6^2 + 8^2}} = 0.6 \text{ (leading)}$$
$$PF_{(cd)} = \frac{4}{\sqrt{4^2 + 3^2}} = 0.8 \text{ (lagging)}$$

DRAW PHASOR DIAGRAM.

You please draw the complete phasor diagram, I have not drawn for you right. So, this is your what you call your this is the way few examples we have taken this you solve your purpose right.

(Refer Slide Time: 15:58)

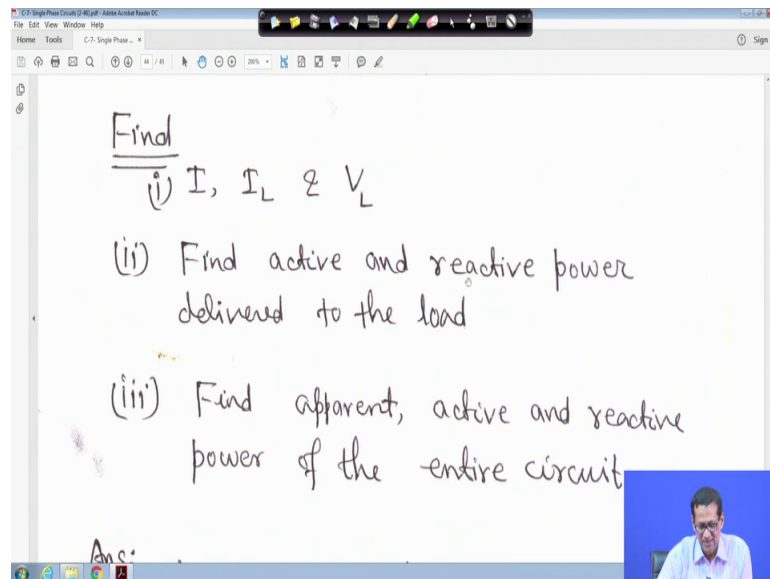


So, now another one is this problem your what you call is given to you L_1 , I your what you call L_2 , your L_1 is given 0.106 and C_2 is given 37.89 micro farad. C_L is your 106 micro farad, L_2 is not there, and R_3 is there 30 ohm, R_L is 50 ohm right and this is V_L .

In this problem you have to find solve for I, I 2, I L, voltage is 120 volt rms, that means you take the reference 120 angle 0 degree and frequency at this 60 hertz. You take f is equal to 60 hertz, this problem we will solve and as standard circuit kcl, kbl this is one thing.

Second thing you will find out suppose you will find out I L using (Refer Time: 16:44) theorem right that will do using (Refer Time: 16:47) theorem you will do this right. And also using this what we call and in say your simply kcl, kbl. You should find out all this thing and answers are given.

(Refer Slide Time: 16:59)



The image shows a screenshot of a whiteboard interface. The whiteboard contains the following handwritten text:

Find

(i) $I, I_L \text{ \& } V_L$

(ii) Find active and reactive power delivered to the load

(iii) Find apparent, active and reactive power of the entire circuit

Ans:

In the bottom right corner, there is a small video feed showing a man in a light blue shirt speaking.

All these things had been asked what you have to do is and answers are given right.

(Refer Slide Time: 17:04)

(ii) Find apparent, active and reactive power of the entire circuit.

Ans:

(i) $I = 1.5426 \angle -12.614^\circ$ Amp
 $I_L = 0.6672 \angle -40.48^\circ$ Amp
 $V_L = 37.3 \angle -67.05^\circ$ Volt

The screenshot shows a whiteboard with handwritten text. At the top, it says '(ii) Find apparent, active and reactive power of the entire circuit.' Below that, under the heading 'Ans:', it lists three equations: (i) $I = 1.5426 \angle -12.614^\circ$ Amp, $I_L = 0.6672 \angle -40.48^\circ$ Amp, and $V_L = 37.3 \angle -67.05^\circ$ Volt. A small video inset of a man is visible in the bottom right corner of the whiteboard window.

These are the answers, but here frequency 60 hertz by mistake do not take 50 hertz then this answer will not come. So, frequency f is your 60 hertz right.

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(i) $P_L = 22.25$ Watt
 $Q_L = -11.126$ VAR (Capacitive)

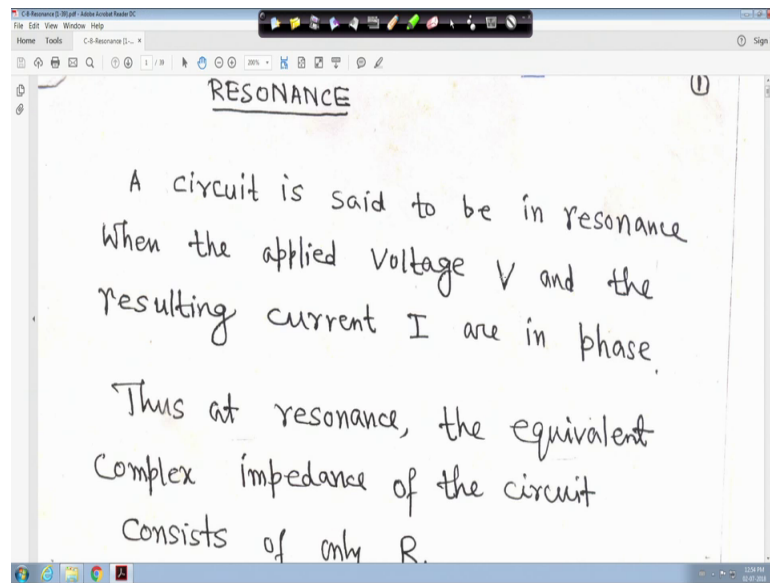
(ii) Apparent Power = 185.112
 ~~122.554 VA~~

$P =$ ~~100.4 Watt~~ 180.64 Watt
 $Q =$ ~~70.27 VAR (capacitive)~~
 40.425 VAR (Inductive)

The screenshot shows a whiteboard with handwritten calculations. Part (i) shows $P_L = 22.25$ Watt and $Q_L = -11.126$ VAR (Capacitive). Part (ii) shows Apparent Power = 185.112 , with ~~122.554 VA~~ crossed out. Below that, $P =$ ~~100.4 Watt~~ 180.64 Watt and $Q =$ ~~70.27 VAR (capacitive)~~ 40.425 VAR (Inductive). A small video inset of a man is visible in the bottom right corner of the whiteboard window.

So, and all these your what we call all these answers are answers are given so, all these answers are given. So, with this right our single phase AC circuit at least this part is over right. So, at least single phase ac circuit is over and you will solve many problems take any book and you please do it.

(Refer Slide Time: 17:37)



So, a circuit now we will go to the resonance circuit then we will see the maximum power factor theorem for single phase this is circuit. A circuit is said to be in resonance right, in resonance when the applied voltage V and the resulting current I are in phase. When V and I both are in phase a circuit can be said that is in resonance right.

So, now, in that case what will happen? If circuit is a resonance so, in V and I in what you call in phase; that means, that circuit will become a as you it is a something like an equivalent your resist resistive circuit right. So, thus at resonance the equivalent complex impedance of the circuit consists of only resistance right.

(Refer Slide Time: 18:26)

Thus at resonance, the equivalent complex impedance of the circuit consists of only R .
Since V & I are in phase, the power factor of a resonant circuit is unity.

The image shows a whiteboard with handwritten text. At the top, there is a small diagram of a series RLC circuit with a voltage source V and current I in phase. The text explains that at resonance, the equivalent complex impedance is purely resistive (R), and because voltage and current are in phase, the power factor is unity. A small video inset of a man is visible in the bottom right corner of the whiteboard frame.

Since later will see this, since V and I are in phase the power factor of a resonant circuit is unity right. Suppose you have a series RLC circuit, R Plus jX_L minus X_C , when X_L is equal to X_C that is resonance of condition occur right, will come to that.

(Refer Slide Time: 18:43)

Whenever the natural frequency of oscillation of a system (could be electrical, mechanical or a civil structure or a hydraulic) coincides with the frequency of the driving force (a voltage source in an electric circuit or a wind force in civil structure etc.), the two system resonate with respect

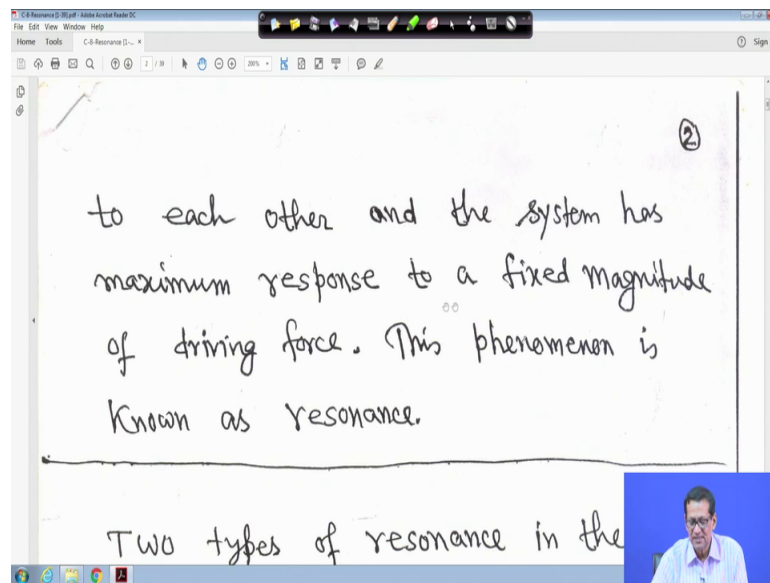
The image shows a whiteboard with handwritten text defining resonance. It states that resonance occurs when the natural frequency of oscillation of a system (which could be electrical, mechanical, civil structure, or hydraulic) coincides with the frequency of the driving force (such as a voltage source in an electric circuit or a wind force in a civil structure). The text is underlined for emphasis. A small video inset of a man is visible in the bottom right corner of the whiteboard frame.

Whenever; now, this is one general thing, whenever the natural frequency; whenever the natural frequency of oscillation of a system could be electrical, mechanical or a civil structure or a hydraulic right coincides with the frequency of the driving force a voltage

source in an electric circuit or a wind force in civil structure etc, the 2 system resonant with respect to each other right.

So, whenever if the natural frequency of the oscillation of a system right if it coincide with the frequency of the driving force right then the 2 system resonance with respect to each other. Resonance is very it is not good for this system right.

(Refer Slide Time: 19:27)



So, in that case your and maximum and in that case has a maximum response to a fixed magnitude of driving force. So, this phenomena is known as a resonance. Similarly, for electrical circuit particular series RLC circuit when it is a resonance condition the current is maximum right, we will come to that. Generally 2 types of resonance in the electric circuits.

(Refer Slide Time: 19:47)

TWO types of resonance in the electric circuits,

- Series Resonance
- Parallel Resonance

SERIES RESONANCE

Circuit diagram showing a resistor R , an inductor $jL\omega$, and a capacitor $-j/\omega c$ connected in series.

One is the series resonance, another is the parallel resonance right. So, first we will see the series resonance.

(Refer Slide Time: 19:55)

SERIES RESONANCE

Circuit diagram showing a resistor R , an inductor $jL\omega$, and a capacitor $-j/\omega c$ connected in series.

$$Z = R + j\left(L\omega - \frac{1}{\omega c}\right) = (R + jX)$$

The circuit is in resonance when $X=0$, i.e., when $L\omega = \frac{1}{\omega c}$

So, in the case of series your simple RLC circuit are $jL\omega$ minus j upon ωC right. So, Z is equal to impedance Z is equal to R Plus $jL\omega$ minus ωC is equal to you can right say R Plus jX in this form right.

(Refer Slide Time: 20:11)

The screenshot shows a whiteboard with the following content:

$$| R \quad jL\omega \quad -j/\omega C |$$
$$Z = R + j(L\omega - \frac{1}{\omega C}) = (R + jX)$$

The circuit is in resonance
When $X=0$, i.e., when $L\omega = \frac{1}{\omega C}$

$$\therefore \omega = \frac{1}{\sqrt{LC}} = \omega_0$$

A small video inset in the bottom right corner shows a man in a white shirt speaking.

The circuit is in resonance when X is equal to 0 that is when X is equal to 0 means that $L\omega - \frac{1}{\omega C}$ is equal to 0 means that $L\omega$ is equal to $\frac{1}{\omega C}$; that means, ω is equal to $\frac{1}{\sqrt{LC}}$ is equal to ω_0 . This ω_0 we will call that your what we will call that is the resonance frequency ω_0 right.

(Refer Slide Time: 20:35)

The screenshot shows a whiteboard with the following content:

Then, since $\omega = 2\pi f$, the resonant frequency is given by,

$$f_0 = \frac{1}{2\pi\sqrt{LC}} \text{ Hz.}$$

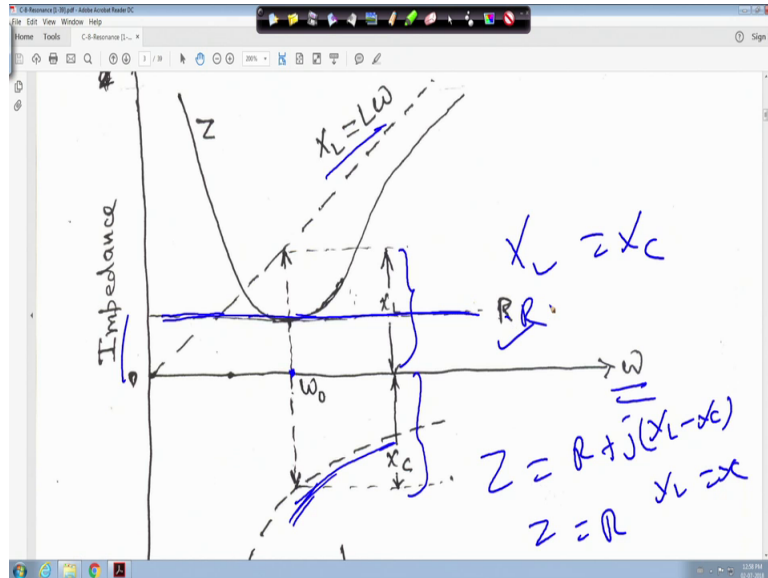
At the bottom, there is a diagram showing a vertical axis labeled Z and a dashed line labeled $X_L = L\omega$.

A small video inset in the bottom right corner shows a man in a white shirt speaking.

So, since ω is equal to $2\pi f$, the resonance frequency is given by f_0 is equal to $\frac{1}{2\pi\sqrt{LC}}$ because, ω is equal to $2\pi f$ is equal to this thing.

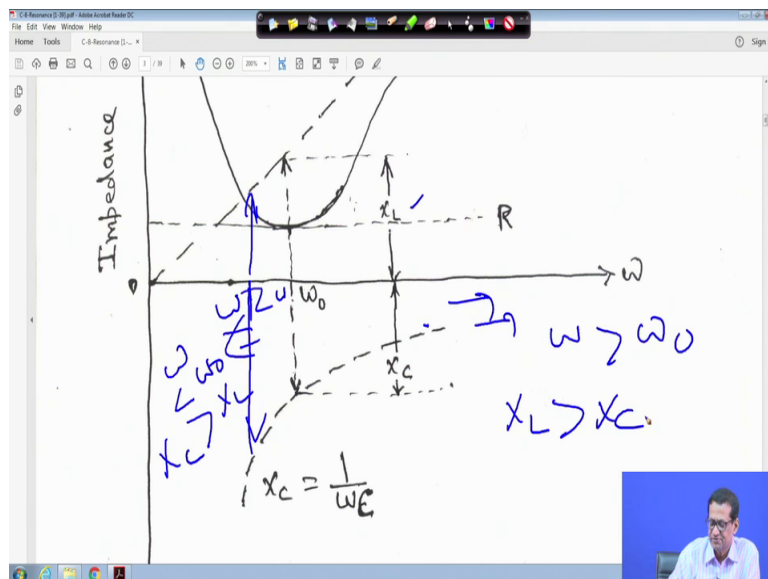
So, it will be f is equal to 1 upon 2π root over LC . So, f_0 is equal to 1 upon 2π root over LC hertz, this is the resonance frequency.

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Now, if you plot suppose this is my impedance; if this is my impedance if we plot. So, X_L is equal to this is my Z plot, this is my Z plot right. Now, this dash line that your this line it is X_L is equal to $L\omega$ because it is a straight line passing through the origin right. Similarly, this side X_C is equal to 1 upon ωC right, this side is ω and this side is an impedance. This impedance means Z , X_L , X_C everything right.

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So, X_C is equal to $1/\omega C$ looks like a rectangular hyperbola right. So, that this dash line is plot right. So, this thing from here to here, from here to here right, from here to here this is my X_L and from here to here this is an X_C . And at X_L is equal to X_C that is frequency is equal to this $1/\omega_0 C$ right.

So, this is that simple plot for impedance verses your ω , this is ω , this is impedance right. This is my this is my X_L is equal to $1/\omega C$ plot and this line this X_C is equal to this curve X_C inverse or what we call X_C is equal to $1/\omega C$ plot and this dash line is the resistance R right.

Because, at when X_L is equal to X_C at that time ω is equal to ω_0 at the time Z is equal R . Because, $R + jX_L - X_C$ so, X_L is equal to X_C at resonance. So, Z is equal to R , this dash line is R right. So, at ω is equal to ω_0 I told you X is equal to X_0 .

(Refer Slide Time: 22:26)

$$X_C = \frac{1}{\omega C}$$

At $\omega = \omega_0$, $X_L = X_C$; $X = 0$

\therefore Thus, $Z = \sqrt{R^2 + X^2} = R$

Thus at resonance, the impedance Z is a minimum. Since $I = \frac{V}{Z}$, the current is maximum

So, impedance Z is equal to X is equal to 0. So, it will be R , thus at the resonance impedance Z is minimum. Since, I is equal to minimum means it is R because X_L minus $X_C = 0$ impedance is minimum R . So, since I is equal to V by Z as the Z is minimum that resonance that current is maximum right so, now, angle.

(Refer Slide Time: 22:49)

$$Z = R + j\left(L\omega - \frac{1}{\omega C}\right)$$

$$\theta = \tan^{-1}\left(\frac{L\omega - \frac{1}{\omega C}}{R}\right)$$

$$L\omega - \frac{1}{\omega C} < 0 \quad \left| \begin{array}{l} \omega < \frac{1}{\sqrt{LC}} \\ \omega < \omega_0 \end{array} \right.$$

At frequencies below ω_0 ($\omega < \omega_0$), the capacitive reactance is greater than the inductive reactance ($\frac{1}{\omega C} > L\omega$) and θ is negative.

Now, theta is equal to tan inverse L omega minus 1 upon omega C R because, Z is equal to R plus j it is X L minus your X C right. So, tan inverse tan theta is equal to L omega minus 1 upon omega C upon R. Therefore, theta is equal to tan inverse L omega minus 1 upon omega C R right. Therefore, for example suppose, when you are at frequency is below omega 0 that is when omega less than omega 0 right.

So, in that case if omega less than omega 0, let me come to this diagram. When omega less than omega 0 this side if you come if omega less than omega 0; that means, this region, this region right it. When omega less than omega 0, the capacitive reactance is more than your inductive side right. And in other side capacitance reactance is less, but this one will be X L will be more.

So, this side if you take omega less than X 0 omega here what we call less than omega 0 right, this side omega less than omega 0; that means, your capacitance inductance your reactance X C right it is greater than your X L this side.

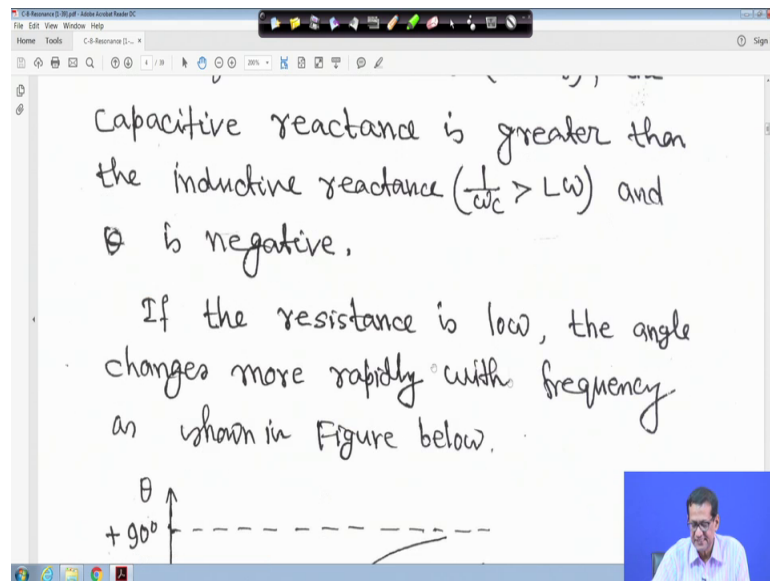
And this side your what you call when your omega greater than omega 0 I mean this side right at that time what will happen that X turns to opposite X L greater than X C right. So, if you take any value from here, you will find X L greater than X C.

So, in that; that is why in this case that if omega less than omega 0; that means, that L omega minus omega 1 upon omega C less than 0 that is omega 1 1 upon omega C greater

than $L\omega$, that is X_C greater $L\omega$. So, from this condition you get ω your less than 1 upon it is root over 1 less than 1 upon root over LC that is your ω less than ω_0 .

So, all frequencies below ω_0 that capacitive reactance is greater than the inductive reactance right and this is negative θ therefore, θ is negative. So, in that case θ is negative right.

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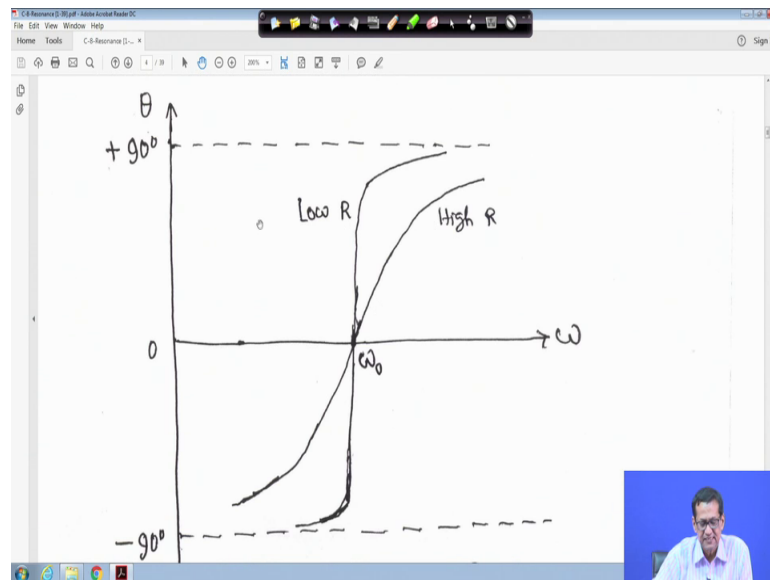
Capacitive reactance is greater than the inductive reactance ($\frac{1}{\omega C} > L\omega$) and θ is negative.

If the resistance is low, the angle changes more rapidly with frequency as shown in Figure below.

The figure shows a graph with the vertical axis labeled θ and a tick mark for $+90^\circ$. A horizontal dashed line is drawn across the graph. A solid curve starts from the left, crosses the dashed line, and continues to the right, illustrating the change in angle with frequency.

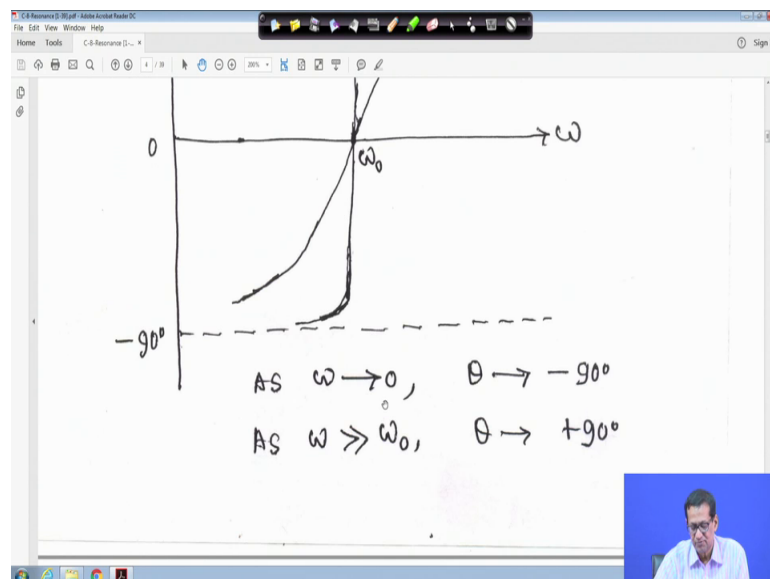
So, if the resistance is low suppose if the resistance is low the angle changes more rapidly with the frequency as shown in figure below suppose this resistance is very small.

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So, for very small resistance this is your omega and this is theta. Theta versus omega curve for small resistance the plot is very sharp look at that and for high resistance this is the plot and this is my omega 0. This side is plus 90 degree, this side is minus 90 degree right.

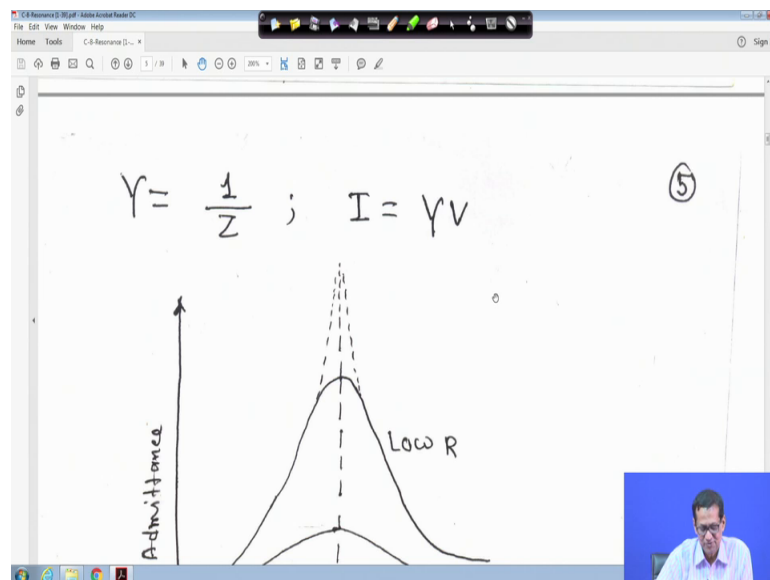
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So, as omega tends to 0 theta tends to minus 90 degree, if you come to that if omega tends to 0 this term will be tends to 0, but as omega tends to 0 this term will tends to minus infinity right.

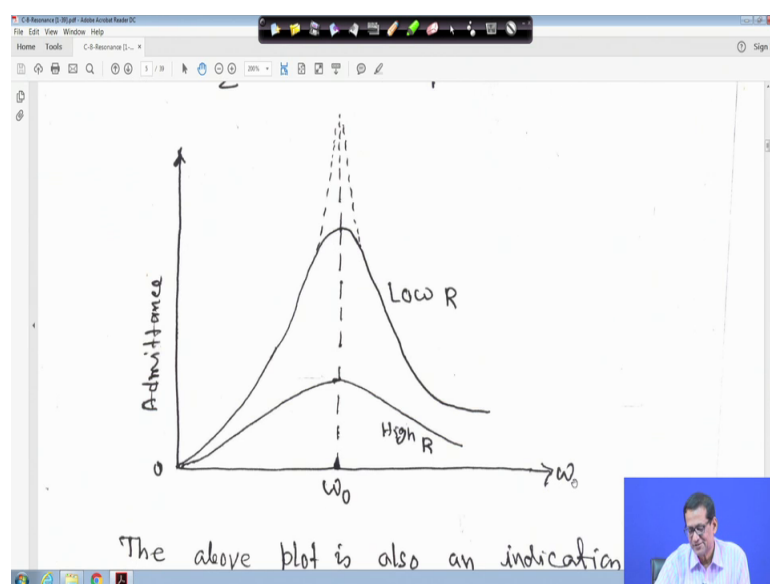
So, in this case 3 term will tends to minus 90 degree, similarly here omega is much higher than omega 0; that means, with this omega is very large this omega upon omega C term is what we call is negligible it will it is very small. But, theta tends to your what we call that plus 90 degree right. So, based on that this your diagram has been drawn right.

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So, now we know that Y is equal to 1 upon Z right that is my I is equal to YV right. So, because we know admittance earlier we have seen.

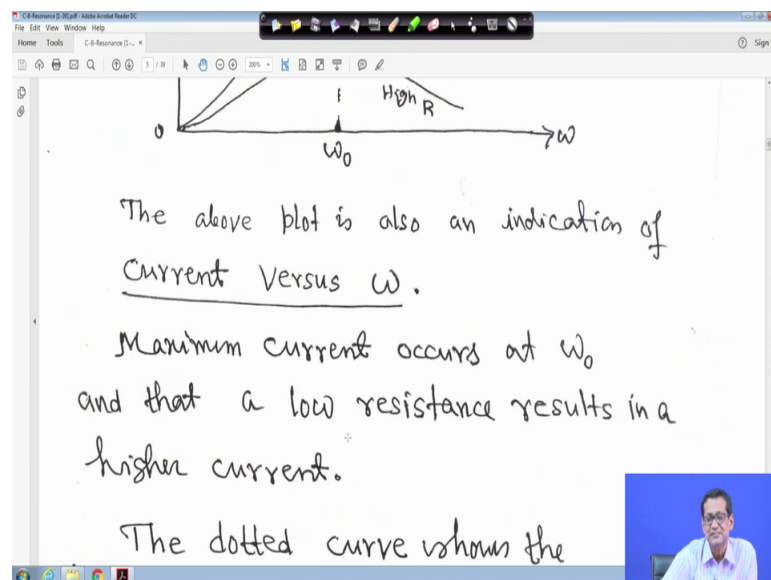
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So, if you plot admittance versus omega right. So, if you what you call if your this is this is omega 0, this plot is for the higher value of R and this plot is for the lower value of R. Finally, this dash line when R is very low it is tending to your what you call to infinity right tending to infinity.

So, now, this is your omega admittance versus omega plot, other one we saw this impedance versus omega plot this is admittance versus and this is your omega 0 right. So, if ha high R means admittance is low, low R means admittance is high. This is the plot and if R is very low it tends to infinity right.

(Refer Slide Time: 26:56)



So, the above plot is also an indication of the current versus omega plot. Now, maximum current occurs at omega 0 because, that is at resonance frequency right, a low resistance results in a higher current.

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Maximum current occurs at ω_0
and that a low resistance results in a
higher current.

The dotted curve shows the
limiting case where $R \rightarrow 0$

So, that dotted curves shows in the your limiting case the R tends to 0; that means, this one when R tends to 0 this is the dot dash line right or dotted line.

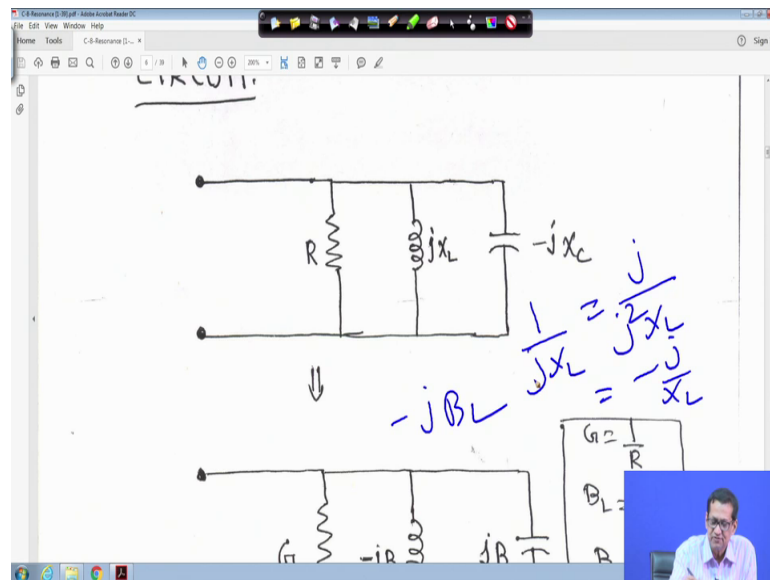
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PARALLEL RESONANCE, PURE RLC
CIRCUIT.

R jX_L $-jX_C$

So, now parallel next is the parallel resonance that is pure RLC circuit. So, in this case this is my R, this is my jX_L and this is my minus jX_C , it is capacitive.

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Now, here this R we can get it is a conductance this 2 can be represented minus jB_L jB_C that is your susceptance right so, it is in susceptance. So, it will become minus jB_L here G is equal to 1 upon R , B_L is equal to 1 upon X_L and B_C is equal to 1 upon X_C . I mean if you take; I mean if you take your what you call the reciprocal of this 1 upon jX_L , numerator and denominator you multiply by j . So, j upon $j^2 X_L$ j^2 is minus 1. So, that is minus j upon X_L .

We will take B_L is equal to 1 upon X_L that is why it is minus jB_L right. So, let me clear it so, that is why here we are writing minus jB_L . Similarly, capacitor will become jB_C it is plus right jB_C equal to 1 upon X_C .

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The slide shows a parallel circuit with three branches: a resistor with conductance G , an inductor with susceptance $-jB_L$, and a capacitor with susceptance jB_C . To the right, a box contains the definitions $B_L = \frac{1}{X_L}$ and $B_C = \frac{1}{X_C}$. Below the diagram, the following equations are written:

$$G = \frac{1}{R} ; \quad \frac{1}{jX_L} = \frac{-j}{X_L} = -jB_L$$

$$\frac{1}{-jX_C} = \frac{j}{X_C} = jB_C$$

At the bottom, the admittance equation is partially visible: $Y = G + j(B_C - B_L) = G + j\left(\frac{1}{X_C} - \frac{1}{X_L}\right)$

So, G is equal to 1 upon R here for you I have done it for 1 upon jX_L is equal to minus j upon X_L is equal to minus jB_L and similarly, 1 upon minus jB_L X is equal to j upon X_C numerator and denominator you multiply by j that all it is jB_C .

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The slide shows the same equations as the previous slide, but with the final admittance equation boxed:

$$Y = G + j(B_C - B_L) = G + j\left(\frac{1}{X_C} - \frac{1}{X_L}\right)$$

$$Y = G + j\left(\omega C - \frac{1}{\omega L}\right)$$

So, admittance Y is equal to G plus $j B_C$ minus B_L right is equal to G plus j 1 upon X_C minus 1 upon X_L right. So; that means, Y is equal to G plus j ωC minus 1 upon $L\omega$.

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A screenshot of a whiteboard with handwritten mathematical notes. At the top right, there is a circled plus sign. The notes are as follows:

$$Y = G + jB$$

where $B = (B_C - B_L)$

The circuit is in resonance when $B = 0$, i.e.,

$$\omega C = \frac{1}{L\omega}$$
$$\therefore \omega = \frac{1}{\sqrt{LC}} = \omega_0$$

In the bottom right corner, there is a small video inset showing a man in a white shirt and glasses speaking.

So, in this case we write Y is equal to G plus jB . So, where B is equal to B_C minus B_L right, this is my B_C and this is my B_L just opposite like your series one, but we have made it like this considering admittance. So, this is my B_C and this is my B_L right.

So, this is my B_C and this is my B_L , B is equal to 0, now circuit is in resonance when B is equal to 0. When this part will be 0, the circuit will be in resonance right. Therefore, ωC is equal to 1 upon $L\omega$ therefore, ω is equal to 1 upon root over your LC , that is equal to ω_0 same as before same as series circuit right.

(Refer Slide Time: 29:33)

A screenshot of a whiteboard with handwritten mathematical notes. The notes are as follows:

$$\omega C = \frac{1}{L\omega}$$
$$\therefore \omega = \frac{1}{\sqrt{LC}} = \omega_0$$

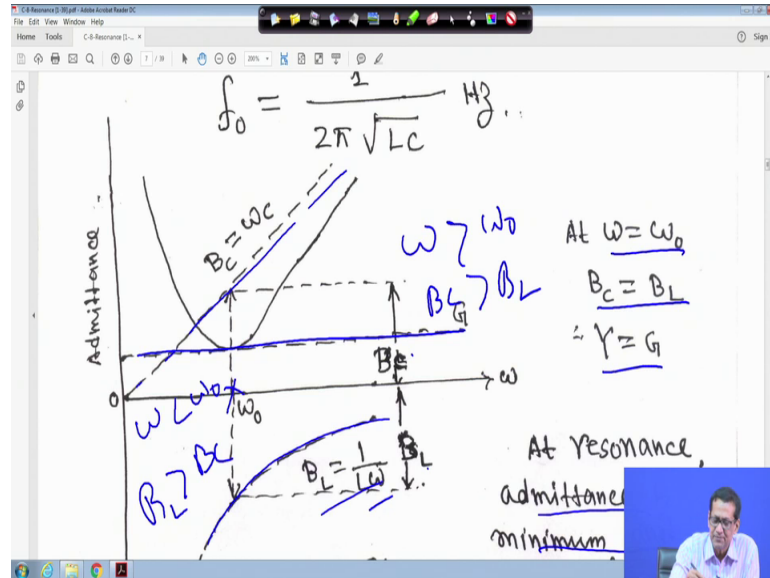
As in the series RLC circuit, the resonant frequency is

$$f_0 = \frac{1}{2\pi\sqrt{LC}} \text{ Hz}$$

In the bottom right corner, there is a small video inset showing a man in a white shirt and glasses speaking.

As in the series RL C circuit resonant frequency is f_0 is equal to $\frac{1}{2\pi\sqrt{LC}}$ Hertz.

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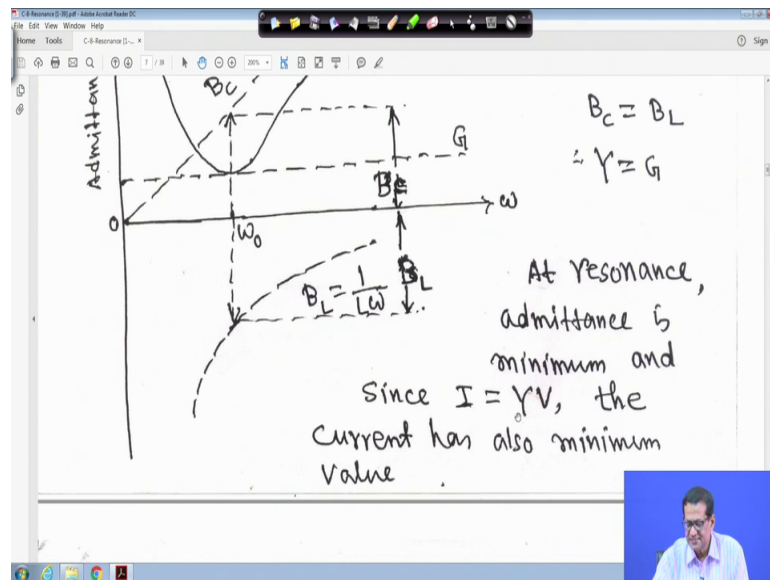


So, if you plot now admittance versus omega same as your what you call now I will do impedance versus omega for series admittance circuit. For parallel, we are plotting admittance versus omega.

So, in this case your, this is my your constant this is my constant G line. Because, B C is equal to B L right then B C omega and this is my B C is equal to omega this is dash line and this is your B L is equal to omega. It is a rectangular hyperbola, one upon 1 omega and this is my your what we you call omega 0, that is resonance frequency.

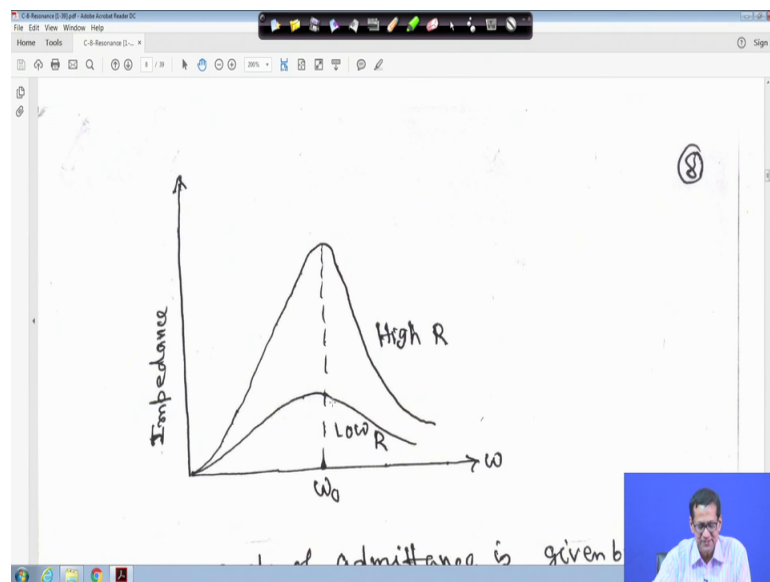
So, at this point your B C is equal to B L right and from the this side you can make out when omega less than omega 0 this side that B L will be greater than B C right. When you will come to this side when omega greater than omega 0 right this side; if you come to this side it will be your B C your greater than your B L right just opposite. So, at omega is equal to omega 0, B C is equal to B L, Y is equal to G right. So, at resonance, admittance is minimum right that resonance parallel circuit and resonance admittance is your what you call minimum.

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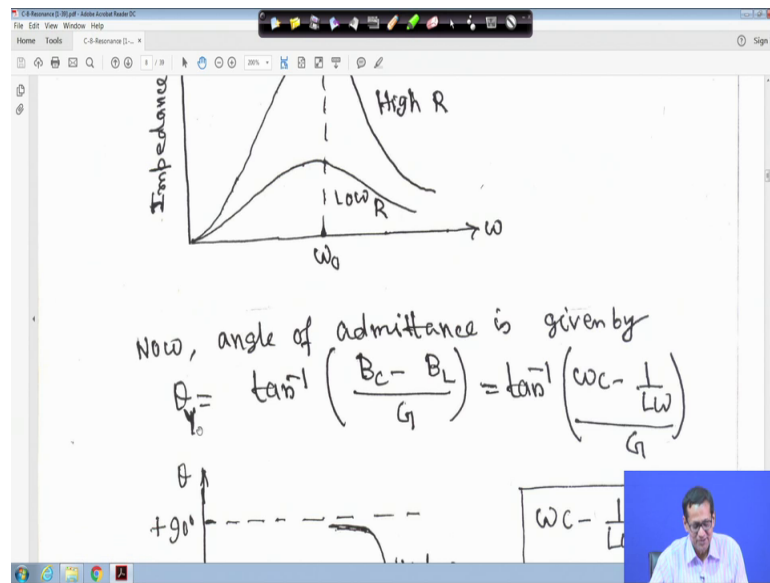
So, in this case and since I is equal to YV so, Y is that admittance the current has also minimum value for the parallel circuit right.

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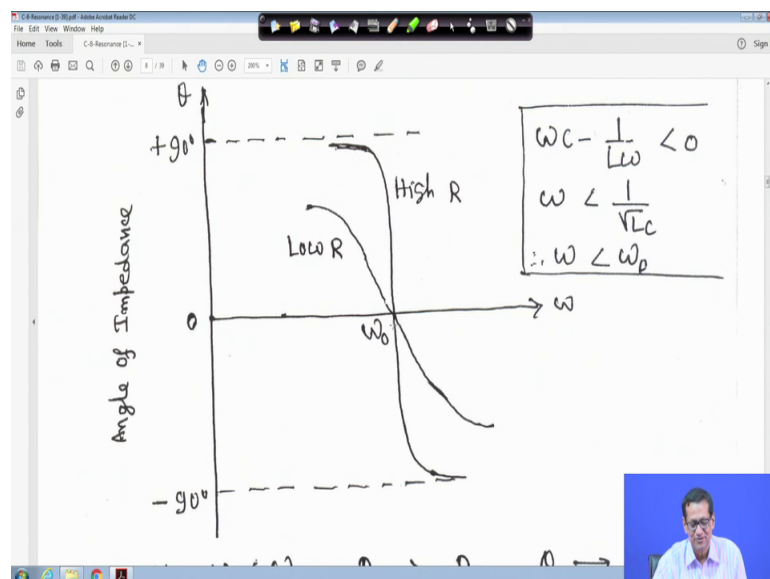
So, now if you plot now just opposite for parallel circuit impedance by ω . So, this is at ω_0 so, this is at low R and this is at higher R . Just you know it is something like your what you call that you complement to each other series and parallel right.

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Now, angle of admittance is given by theta what we call this is theta Y Suffix is y capital Y is equal to tan inverse B C minus B L upon G right. Therefore, tan inverse omega C minus 1 upon l omega by G.

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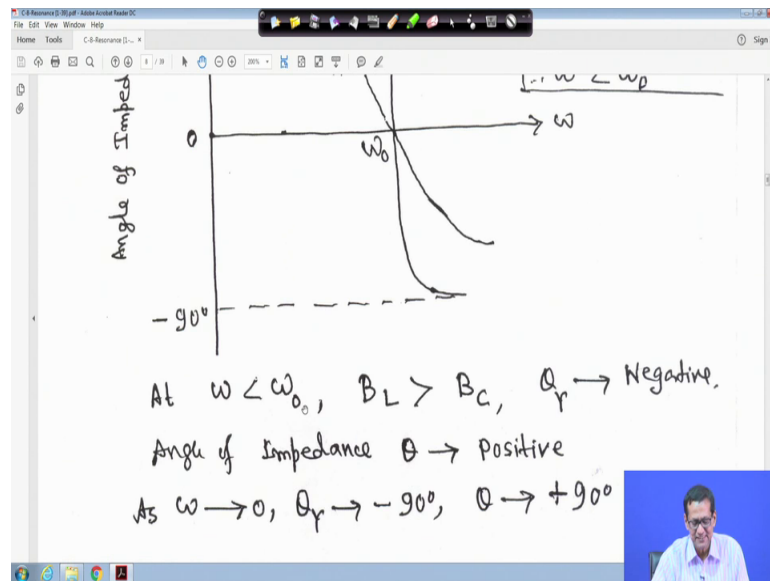


Now, if you plot this one, this is same as before this is angle of a impedance plus 90 degree, this is minus 90 degree right. So, this is very high value of R this is the plot and for low R this is the plot and this is my omega 0. The way we explain the previous one

series one it is same, but in this case it is ampere your what we call it is that we has already it is angle of impedance right.

So, if you plot like this it will be and an omega C minus 1 upon L omega less than 0. So, omega less than 0 your omega less than 0 and this is your what we call plot.

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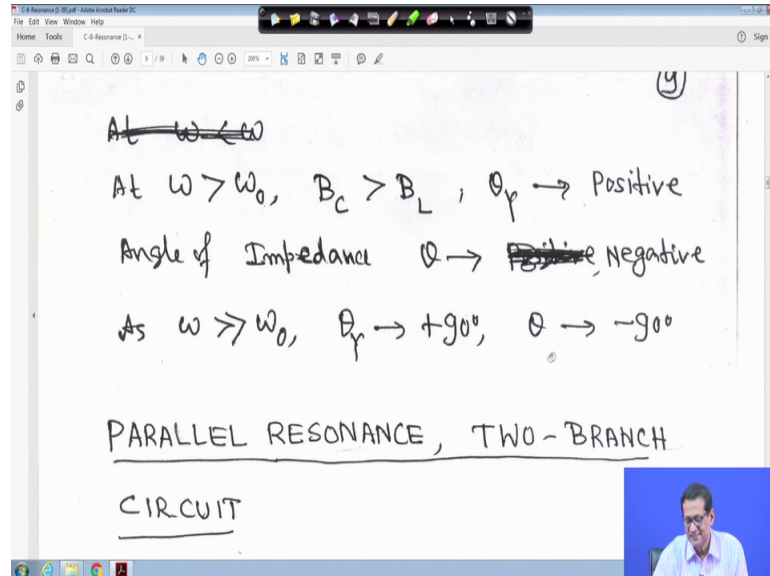
Now, if you see omega less than equal to omega less than omega 0 that is my B L greater than B C. So, theta Y is negative right. So, if you come to this here, your this thing your this one right, it will be G plus j omega C minus L omega this is my B C minus B L right. So, from this condition I see that if you are your what we call if B C minus your B C greater than B L or less than B L accordingly negative and positive angle will come right.

So, same thing is explained here that your what we call when omega less than omega 0 B L greater than B C theta Y will be negative right. And angle of impedance; that means, theta is positive because it is theta Y angle of admittance; if angle of admittance become negative then angle of impedance theta will become positive right.

Similarly, if omega tends to 0 the theta Y angle of admittance becoming minus 90 degree and therefore, the angle of impedance theta will be plus 90 degree right. So, when B L greater than B C that angle of admittance is negative; that means, angle of admittance

theta is positive. Because, this is theta Y, similarly at when omega tends to 0 right angle of admittance is minus 90 degree; that means angle of impedance is plus 90 degree right.

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So; that means, at omega greater than omega 0 B C greater than B L that is theta Y that is positive right and angle of impedance theta will be negative. This is just put in that your what we call in that expression very simple thing it is and omega is much much greater than omega 0, at that time you will see theta Y is plus 90 degree. That is angle of impedance will be minus 90 degree.

When omega great omega greater than much much greater than your omega 0; that means, if you come to this; that means, if you come to this that when omega is much much greater than omega 0, much much greater than omega 0 right, then this part is negligible compared to this part right. That means, in that case angle of admittance is your positive right. So, in that case angle of admittance is your what we call that is positive that is 90 degree and therefore, theta is equal to minus 90 degree right so, with this.

Thank you very much we will be back again.