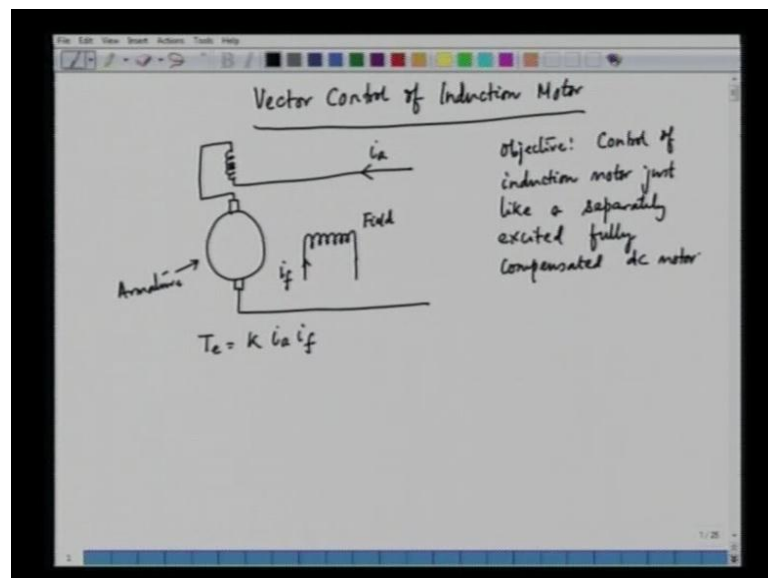


Advanced Electric Drives
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Lecture - 9

Welcome to this lecture on Advanced Electric Drives. In the last lecture, we have just started the vector control of induction motor, which is also called the field oriented control or trans vector control. This is an advanced control technique for induction motor, in which we can control the torque with high dynamic response. So, today we will start with the vector control of induction motor.

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Now, by vector we mean there has to be an amplitude and phase angle, now when we are controlling an induction motor we are controlling the stator MMF both in amplitude and phase angle. So, when you are controlling the stator MMF with amplitude and phase angle, we call that be vector control, the primary objective of vector control is to control an induction motor, similar to that of a separately excited d c motor. There has to be a control similar to separately excited d c motor, because in d c motor we have separate brush armature and field, so let us see the structure of a d c motor.

So, ((Refer Time: 01:48)) this is d c motor, we have, we have brushes here this is armature and we also have a field winding, this is the armature of the d c motor. And

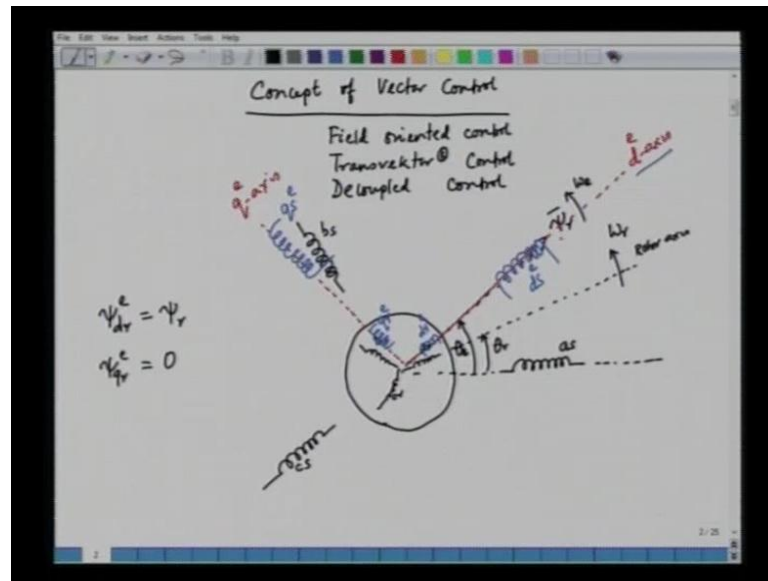
often what we have in case of large d c motor, we also have an compensating winding, the purpose of the compensating winding is to neutralize the effect of armature reaction. And the compensating winding is connected in series with the armature, and the MMF of the compensating winding is in opposition to the armature MMF, so that there is a cancelation of the armature MMF and effect on the field is reduced.

So, we can also have the compensating winding here ((Refer Time: 02:44)), and how do we connect it, we connect it in the following fashion, so we have the armature current. We can say this to be i_a and we have the field current, which you can say to be i_f and we know that the torque is equal to $K i_a i_f$ ignoring magnetic circulation, so the objective of vector control is to control an induction motor just like a d c motor. So, the objective in this case, control of induction motor just like a separately excited, fully compensated d c motor.

And we have the flexibility in this case, we can control the torque by if the controlling i_f and i_a , but controlling i_f will be accompanied by delay, so we do not control i_f we keep i_f constant and we control i_a to control the torque of the d c motor. Similarly, in case of an induction motor although apparently we do not have any field and armature, we have to identify a field current or a flux component of current, and armature current or a torque component of current. So, that we can control this independently, we can control the flux independently and we can control the torque independently by some other component of current.

So, this concept of field orientation or vector control was given by a scientist call Felix Blaskay, way back in 1969. And that time he introduced a concept of field orientation, but it was difficult to implement the field orientation for some time, because of non availability of flux digital signal processing devices. We have to have faster computer to process the signals is real time to be able to control an induction motor, just like a d c motor; so let us try to see the concept behind the vector control of induction motor.

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We can call this to be also field oriented control or trans vector control or decoupled control, now if we take a three phase induction machine, we have three phases, phase a, phase b and phase c. We can draw the three phases of the machine, this is the rotor and we can have one phase here, we can have the second phase here and we have the third phase here. And similarly, the rotor can also have three different phases phase a, phase b and phase c, so these are the status phases, and these are the rotor phases.

And rotor is rotating this is rotor axis ((Refer Time: 07:05)), and the rotor is rotating at a speed of ω_r radian per second and the stator is stationery and this angle, is the rotor angle that is θ_r . So, what we do here that we are talking about three phase symmetrical induction machine, the rotor is rotating at a speed of ω_r , we analyze a machine from a synchronously rotating reference frame. And the reference frame is so chosen that, the reference frame is attach to the rotor flux vector that is extremely imported, that we are talking about the reference frame which is attach with the rotor flux vector.

So, we can say for example, so this is the rotor flux vector and this we can say to be ψ_r which is also rotating and the rotor flux vector is basically a flux vector, that is rotating in the space with synchronous speed and the synchronous speed is ω_e . So, this is the synchronous speed which with the rotor flux vector ψ_r is rotating, it is a vector

have been amplitude phase angle. And when this is rotating the angle between the flux vector and the stationary phase a axis, this angle is θ_e .

So, what we do we take a reference frame and the reference frame is attached with the rotor flux vector, so we will choose a d-axis, so this is our d-axis ((Refer Time: 08:59)) and we can also choose a q-axis orthogonal to d-axis, so this is our q-axis. And this d-q-axis are rotating with the rotor flux vector at synchronous speed, and synchronous speed is ω_e and since, this is very special reference frame. We call this reference frame to be d_e and q_e , d^s_e and q^s_e symbolizing that, these are the reference frame attached with a rotor flux vector.

And when we are analyzing this from rotating reference frame, we can always have fictitious winding like $d_e s$ winding and $q_e s$ winding, so we can have the stator windings which are fictitious. So, we can have the windings here in the stator and this you can call to be d_s winding, but this is rotating with the rotor flux vectors, so we can call this to be d^s_e . And similarly, we can have a q_s winding and the q_s winding is also rotating winding, we can call q^s_e and similarly, in the rotor we can always have a equivalent rotor winding also, like $d_r e$ and $q_r e$.

So, we can have a rotor winding here in the rotor, this is $d_r e$ and similarly, we can have $q_r e$ as we have seen in case of Crohn's simitive machine model, we can have two windings in the stator and two windings in the rotor. But, these windings are not stationary they rotating at the speed of rotor flux vector, because the reference frame is attach with the rotor flux vector. Now, this is a very special reference frame, now if we are taking this reference frame what is the advantage, the advantage is this, that if we are orienting the d-axis of the reference frame.

This is the reference frame d-axis along with the rotor flux vector that is ψ_r , we have this following equation, the equation is this that $\psi_{d_r e}$ is equal to ψ_r . You can see that if I find out the d-axis component of the rotor flux the total rotor flux in the oriented along the d-axis. So, we can say that the d-axis flux is entirely ψ_r and if I ask this question what is $\psi_{q_r e}$, what is the component of rotor flux vector or the rotor flux along the q-axis rotor, and that will be equal to 0.

Because, the rotor flux is entirely along the d-axis there is no component of the rotor flux along the q-axis, so we can always say that $\psi_{q_r e}$ equal to 0, so this is very similar to

that of a d c machine. Now, if you take a d c machine in this case that we have the flux along d-axis, so this is our d-axis ((Refer Time: 12:32)), so we can call this to be the d-axis here and this is the q-axis. And we can always say that, the total flux is along the field, this is the flux produced by the field winding, what about the q-axis flux, the q-axis flux is 0.

Because, in the q-axis we have the armature winding no doubt, we also having compensating winding and the compensating winding is compensating for the armature flux, it is canceling the armature flux. And we are talking about a fully compensated d c motor and due to this the q-axis flux in the rotor is 0, so we can say that there is no q-axis flux, so in this case the q-axis flux does not exist. So, we are trying to have an analogy between an induction machine and d c machine in a rotating reference frame, and the reference frame rotating at a synchronous speed.

And if the reference frame is rotating at a synchronous speed, all the s c variables will appear as d c variable, actually if you see the phase a, phase b and phase c of a induction machine, the currents are ac current. But, this ac current will appear as dc current, if we view them from a synchronously rotating reference frame. We can take an example suppose two trains are moving at a same speed, if the two vehicles are moving at a same speed both the vehicles are moving, and a person is seated in one of the vehicle, he will observe the other vehicles to be stationary.

Although both the vehicles are moving the relative velocity between the 2 is equal to 0, so if we are having a moving observer, moving at the same speed, the speed of the other vehicle from the moving observer will appear to be equal to 0. Similarly, if we are house in a reference frame rotating synchronously, the variables seen from the reference frame will appear to be d c variable. Because, there is no relative velocity between the reference frame and the a c quantities in the study state.

So, if we try to see that this is our currents, ((Refer Time: 15:02)) this is i_d s e in the d-axis and this is i_q s e in the q-axis. And similarly, we can have i_d r e in the d-axis rotor and we can have i_q r e in the q-axis rotor and this current will be d c current in the steady state. So, since the currents are d c currents, we can think of a d c machine we can visualize a d c machine in phase of an induction machine, so to be able to control we

have to derive from equation, and the equations will give us the control scheme for vector control.

(Refer Slide Time: 15:56)

The image shows a whiteboard with handwritten equations for vector control. The title is "Equation for vector control".

d-axis rotor

$$U_{dr}^e = 0 = r_r i_{dr}^e + p \psi_{dr}^e - \omega_{sl} \psi_{dr}^e \rightarrow 0$$

$$0 = r_r i_{dr}^e + p \psi_{dr}^e$$

From the second equation, it is deduced that $p \psi_{dr}^e = 0$, which leads to $r_r i_{dr}^e = 0$ and $i_{dr}^e = 0$. This is labeled as equation (1).

q-axis rotor

$$U_{qr}^e = 0 = r_r i_{qr}^e + p \psi_{qr}^e + \omega_{sl} \psi_{dr}^e$$

So, what we will be doing in this case, we will be writing down the equation for d-axis rotor, so we are writing down the equation for the d-axis rotor. So, we can say that v_{dr} in the rotating reference frame that is superscript e that is 0, because the rotor is short circuited, that is equal to $r_r i_{dr} + p \psi_{dr}$. And if you see in this case, the relative velocity between the reference frame and the rotor is $\omega_e - \omega_r$, the reference frame is rotating at a speed of ω_e . And the rotor is rotating at a speed of ω_r , and the differential speed between them is $\omega_e - \omega_r$ and we call this speed to be the split speed.

So, that is written as ω_{sl} ((Refer Time: 17:10)) and ω_{sl} is call the split speed, so when we are writing down the equation of the rotor, the actual winding a rotating at ω_r , physical rotor is moving at a speed of ω_r . But, the hypothetical winding in the rotating reference frame they are moving at speed of a ω_e , the relative velocity between these two is $\omega_e - \omega_r$. And that is the speed at which the rotationally induced e_{mf} will appear in the rotor equation.

So, we can go back to our equation here ((Refer Time: 17:45)), so we have minus of ω_{sl} into ψ_{qr} , so this is the first equation which is in the d-axis. Now, we have already seen the ψ_{qr} is equal to 0, so we can cancel this, this is equal to 0, so if ψ_{qr}

is equal to 0 we will again simplify this, we can say that 0 is equal to $r_r i_{dr} + p \psi_{dr} - e_r$. Now, when we are writing down all these equations, all the variables are referred from the primary side, so although we do not show in terms of prime variable, we assume that all the variables are observe from the stator.

So, the effective number of terms have been multiplied, the parameters are also seen from the primary side, so this equations are all taking from the primary side, so this is what we have here. And if we see in this case ((Refer Time: 18:46)) that ψ_{dr} equal to ψ_r and we would like to keep the flux constant, because if we change the flux, the flux is associated with a inductance, and the flux cannot be change is synchronously, it will take some time for the flux will change.

So, if we change the flux the torque response will be delayed and to change the torque what we do, we keep the flux constant, so what we say here that ψ_r is kept constant or the rotor flux kept constant. So, if ψ_r is kept constant or ψ_{dr} kept constant, we can say here that $p \psi_{dr}$ equal to 0, and from this equation what we obtain here is that $r_r i_{dr}$ equal to 0 or $i_{dr} = 0$, so it means there is no d-axis rotor current. To achieve the d-axis rotor winding is upset or that winding is not having any effect on the machine performance.

So, this is the first equation of the vector control, there is in the d-axis we have i_{dr} equal to 0, so this we can say as number 1 ((Refer Time: 20:10)). So, similarly in the q-axis rotor, we can write down the equation for q-axis rotor v_{qr} that is short circuited that is equal to 0, that is $r_r i_{qr} + p \psi_{qr} + \omega_s \psi_{dr}$. We are again writing down this equation in the rotor flux reference frame and the reference frame is rotating at synchronous speed, and speed of the reference frame is ω_e , that is why the speed induced e m f is appearing with a factor of ω_s ω_s is the script speed. Now, in this case this is equal to 0, because we do not have any q-axis flux ((Refer Time: 21:15)) ψ_{qr} is 0 here and because of this, this quantity will be vanish. So, we can say in this case 0 is equal to $r_r i_{qr} + \omega_s \psi_{dr}$.

(Refer Slide Time: 21:43)

The whiteboard contains the following handwritten equations:

$$\omega_{sl} = - \frac{r_r i_{qr}^e}{\psi_{dr}^e}$$

$$\psi_{dr}^e = 0 = L_r i_{qr}^e + L_m i_{qs}^e$$

$$\text{or, } i_{qr}^e = - \frac{L_m}{L_r} i_{qs}^e$$

$$\omega_{sl} = \text{Slip speed} = \frac{r_r}{L_r} \cdot \frac{L_m i_{qs}^e}{\psi_{dr}^e} = \frac{L_m}{Z_r} \cdot \frac{i_{qs}^e}{\psi_{dr}^e}$$

$$\psi_{dr}^e = L_r i_{dr}^e + L_m i_{ds}^e$$

$$\psi_{dr}^e = L_m i_{ds}^e$$

$$\omega_{sl} = \frac{1}{Z_r} \cdot \frac{i_{qs}^e}{i_{ds}^e}$$

And we can find out the value of ω_{sl} here, ω_{sl} is equal to minus of $r_r i_{qr}^e$ by ψ_{dr}^e , so this is the expression for the slip speed. Now, this slip speed expression is quite interesting, the slip speed is proportional to i_{qr}^e and it is inverse proportional to ψ_{dr}^e . Now, we can substitute for i_{qr}^e because i_{qr}^e is the rotor current in the q-axis, on the rotor current are not easily acceptable, so we have to replace the rotor current by stator current.

So, we can say here, that $\psi_{dr}^e = 0$ and that is equal to $L_r i_{qr}^e$ plus $L_m i_{qs}^e$ or we can say here that i_{qr}^e is equal to minus of L_m by L_r i_{qs}^e , so what we will do here we will substitute for i_{qr}^e in this case. So, we can rewrite this equation for the slip speed that is equal to r_r by L_r into $L_m i_{qs}^e$ by ψ_{dr}^e L_r by r_r is called the inverse of the time constant. So, we can say in this case it is L_m by τ_r into i_{qs}^e by ψ_{dr}^e , so the slip speed expression will be useful when we control the induction motor with vector control.

Now, here we can also another simplification, we know that ψ_{dr}^e is equal to as we row the expression for ψ_{qr}^e similarly, we can write for ψ_{dr}^e , ψ_{dr}^e is $L_r i_{dr}^e$ plus $L_m i_{ds}^e$. And we have already seen that $i_{dr}^e = 0$ ((Refer Time: 24:01)), this is what we have already seen. So, we can substitute this $i_{dr}^e = 0$ in this expression, so this will be 0, so this vanishes in this case. So, what we have here is

that ψ_{dr} is equal to L_m into i_{ds} , now it means the rotor flux can be control only by stator current.

If we vary i_{ds} we can change the rotor flux and ψ_{dr} is same as the total rotor flux that is ψ_r , so when we change i_{ds} we can change the rotor flux. And the expression for the slip speed, we can replace ψ_{dr} by L_m into i_{ds} , so we can write the expression for the slip speed and the slip speed here is 1 by τ_r into i_{qs} by i_{dr} . So, this expression for the slip speed will be useful for us, when we control the induction motor with vector control, now let us see how it will be useful. So, we have been able to find out the slip speed and the other equations.

(Refer Slide Time: 25:37)

The image shows a handwritten derivation of the torque equation for an induction motor in a rotor flux reference frame. The equations are as follows:

$$T_e = \frac{3}{2} \frac{P}{2} L_m (i_{qs}^e i_{dr}^e - i_{ds}^e i_{qr}^e)$$

$$= \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} (i_{qs}^e \psi_{dr}^e - i_{ds}^e \psi_{qr}^e)$$

$$= \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} i_{qs}^e \psi_{dr}^e$$

Torque Component of Stator Current

$$= \frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} i_{qs}^e \cdot L_m i_{ds}^e$$

$$= \frac{3}{2} \frac{P}{2} \frac{L_m^2}{L_r} i_{qs}^e i_{ds}^e$$

On the right side of the derivation, the rotor flux components are defined as:

$$\psi_{dr}^e = \frac{\psi_r^e - L_m i_{ds}^e}{L_r}$$

$$i_{qr}^e = \frac{\psi_{qr}^e - L_m i_{qs}^e}{L_r}$$

Now, what about the torque, torque equation is given as for an induction motor, we know it is 3 by 2 into P by 2 into L_m into i_{qs} i_{dr} minus i_{ds} i_{qr} . And since, we are talking about the rotor flux reference frame will have to put a subscript here, so this is the torque equation of an induction motor. And we can further simplify this and this if we simplify this what will do here, we will replace this i_{dr} by ψ_{dr} minus, we can say here L_m into i_{ds} by L_r .

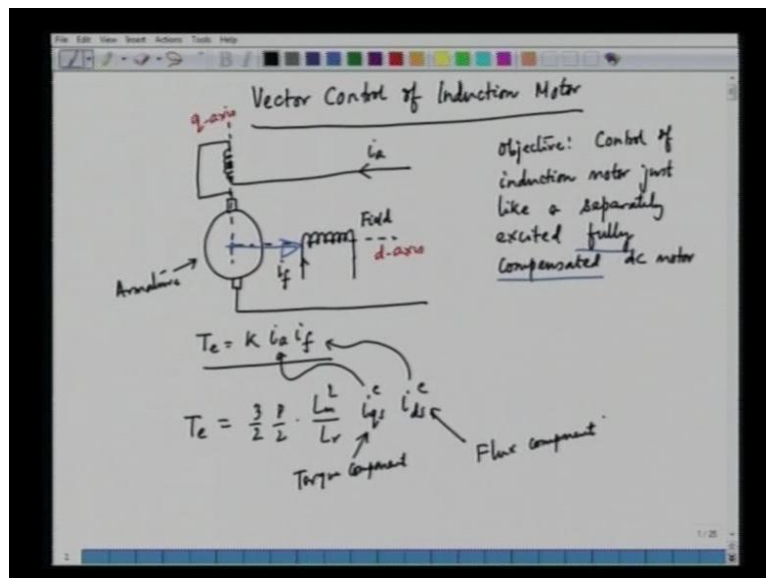
And similarly, we can substitute for i_{qr} , i_{qr} is ψ_{qr} minus L_m i_{qs} by L_r , so if we substitute for this i_{dr} and i_{qr} we can get back the torque expression in a different form. So, we can rewrite the expression for the torque, 3 by 2 into P by 2 and after simplification we will get L_m by L_r into i_{qs} into ψ_{dr} minus i_{ds} into ψ_{qr} . So,

((Refer Time: 27:23)) this is the expression for the torque of an induction motor, as a function of the stator current and the rotor flux.

And this equation will give us the equation of the torque as we have seen in case of d c machine, so what we have here is the following that we have ψ_{qr} equal to 0. Now, if ψ_{qr} equal to 0 we can make this equal to 0, and if ψ_{qr} equal to 0 we can rewrite the expression for the torque of $\frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} i_{qs} i_{dr}$. And this is a simple expression compare to a very complex equation of an induction motor and the torque can be produce by the product of two variable, and one is the flux and other is the component of stator current.

So, this is call the torque component of current and this is the flux, so we can rewrite this expression for the torque as $\frac{3}{2} \frac{P}{2} \frac{L_m}{L_r} i_{qs} i_{dr}$. And we can substitute for ψ_{dr} and ψ_{dr} is $L_m i_{ds}$, so that will give us the following expression $\frac{3}{2} \frac{P}{2} \frac{L_m^2}{L_r} i_{qs} i_{ds}$. So, we see that the equation of the torque current induction machine it just like a d c machine.

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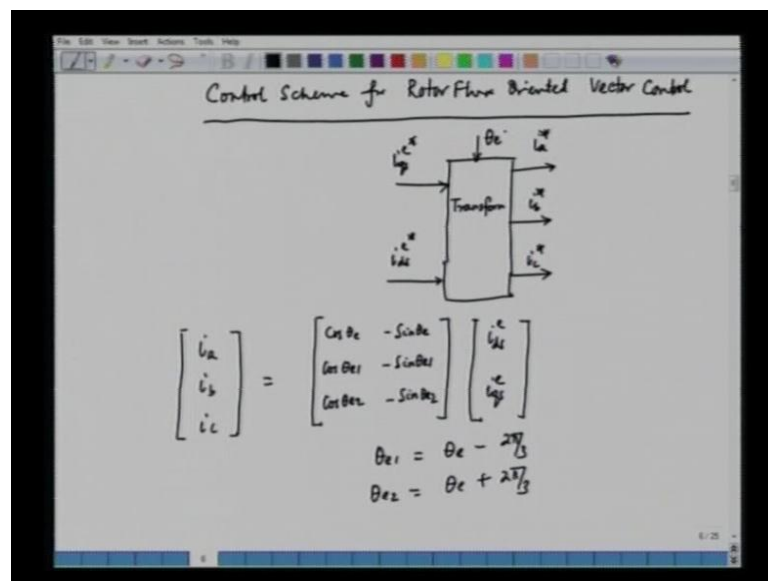


If you see the d c machine toque equation, what you have is that T_e equal to K into i_a into i_f and what we have here is something very similar, we have in case of an induction machine that we have just seen, it is $\frac{3}{2} \frac{P}{2} \frac{L_m^2}{L_r} i_{qs} i_{ds}$. So, this i_{qs} is compare able to i_a , so we can say that this is something similar to i_a and i_{ds} is something similar to the field winding current, so we have two

types of currents here, two component of current that is i_{qs} and i_{ds} ; i_{qs} is call as we have already seen this call the torque component of current and i_{ds} is call the flux component of current.

So, we have two, that is i_{qs} , the flux component of current that is i_{ds} , so if we control these two currents, we can control the torque of an induction machine just like a d c machine. So, usually what we do here is the following, we keep i_{ds} constant, so ((Refer Time: 30:49)) this we can keep constant, because if we change i_{ds} the flux will change and in the flux changes there will be delayed. So, we keep i_{ds} constant and we change i_{qs} for the torque control, so the torque is control not by i_{ds} a e primarily by controlling i_{qs} . Because, when we control i_{qs} there is no delay involve, so i_{qs} can be control quickly and the torque will response linearly to i_{qs} .

(Refer Slide Time: 31:29)



Now, let us see the control scheme, control scheme for this is call rotor flux oriented, vector control, this is call rotor flux oriented vector control, because the reference frame is oriented along the rotor flux; and hence, it is call rotor flux oriented vector control. Now, we have two currents in this case i_{ds} and i_{qs} , but this i_{ds} and i_{qs} are hypothetical current, they are the current in the rotating reference frame which is non existing and this is only in our mind this is only in the concept. Now, when we are actually controlling the machine we have to translate or we have to transform, this i_{ds}

and i_{qs} into the actual current of the machine and the actual currents are i_a , i_b and i_c .

So, we have to transform this i_{ds} and i_{qs} into i_a , i_b , i_c , so what we have to have here is the following we have to have a transformation. So, this is our i_{qs} and this is i_{ds} and we have to transform these two current components into the actual current of the machine and that is i_a , i_b , i_c . ((Refer Time: 33:13)) Let us see our original diagram here actual currents in the machines are i_a and this is phase b, i_b and this is phase c and i_c . And we have been able to evaluate what is i_{ds} and what is i_{qs} these currents we know, but these currents are hypothetical current, although we can do the control in the i_{ds} and i_{qs} , we have to actually inject i_a , i_b , i_c into the machine winding.

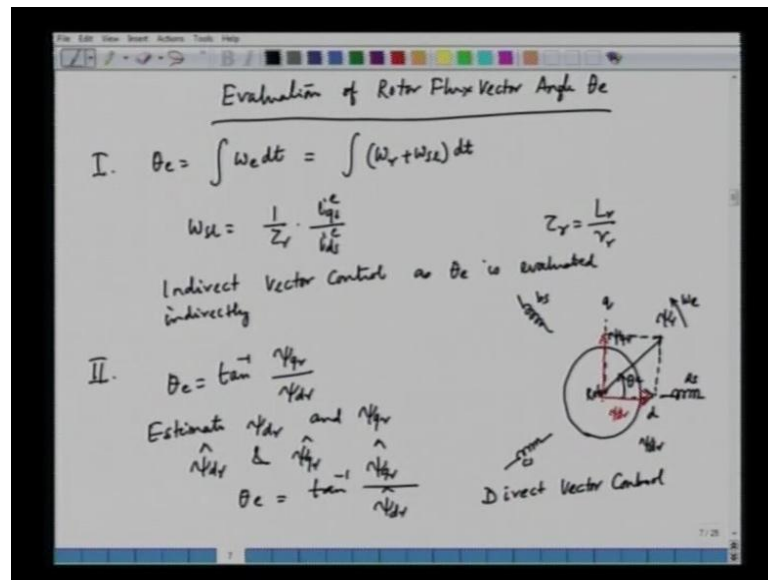
So, we have to transform this i_{ds} and i_{qs} into i_a , i_b and i_c and that involves the transformation, and if we see the this reference frame is having an angle of θ_e with a phase a. So, the transformation will involve θ_e , so the transformation that is applicable here is a transformation that is involve θ_e , so we can say here that if you want to get back i_a , i_b , i_c we have to use a transformation as follows. So, the transformation in this case is, i_a , i_b and i_c , this we have to obtain from i_{ds} and i_{qs} .

And what is the transformation here, ((Refer Time: 34:46)) this transformation we have to find out, the transformation will involve θ_e , now the transformation will be as follows, this will be $\cos \theta_e$, this is $\cos \theta_e$ 1, this is $\cos \theta_e$ 2, this is minus of $\sin \theta_e$ minus of $\sin \theta_e$ 1 minus of $\sin \theta_e$ 2. And where θ_e 1 is equal to θ_e minus of 2π by 3 and θ_e 2 is equal to θ_e plus 2π by 3, so this is the transformation that will transform i_{ds} and i_{qs} into i_a , i_b , i_c .

And when we obtain this i_a , i_b , i_c we can use a inverter to inject this current to the winding of the actual machine, so in fact these currents are the reference current. So, we can say here i_a^* , i_b^* and i_c^* , they are not the actual current, they are the reference current, so they have to impress on to the machine winding. Similarly, these currents are also i_{qs}^* and i_{ds}^* , so we can have a inverter to inject this current on to the machine winding. And this transformation as we have seeing ((Refer Time: 36:15)) this will involve θ_e and what is this θ_e , θ_e is the angle of the rotor flux vector, if we see as we have already drawn here this angle is θ_e .

Now, as we have already seen that we need θ_e for the transformation from $i_d s, i_q s$ to $i_a i_b i_c$, now there are ways to evaluate θ_e , θ_e can be evaluated indirectly, it can also be evaluated directly. And accordingly we can have an indirect vector control or a direct vector control, evaluate now rotor flux vector angle θ_e .

(Refer Slide Time: 37:01)



So, we know that θ_e is obtained by integration of ω_e , ω_e is the speed of the reference frame, and this is also the speed of the rotor flux vector. Now, if we integrate this ω_e , we get the angle that is θ_e that is one way and how do you find out this ω_e , ω_e can be evaluated as ω_r plus ω_{sl} . So, if we add the rotor speed and slip speed we get the synchronous speed that is ω_e , now slip speed can be calculated we already seen that slip speed is given by 1 by τ_r into $i_q s$ by $i_d s$.

So, if we know $i_d s$ and $i_q s$ and if we know τ_r and τ_r is the rotor time constant that is equal to L_r by r_r , we can evaluate what is the slip speed there is ω_{sl} , so slip speed can be easily calculated. And the rotor speed that is ω_r can be measured by using a deep sensor or an encoder, so we can measure the rotor speed we can calculate the slip speed and then the summation on these two will give us the speed of the rotor flux vector that is ω_e , integration of that will give us θ_e and θ_e can be use to transform $i_d s$ and $i_q s$ into $i_a i_b i_c$.

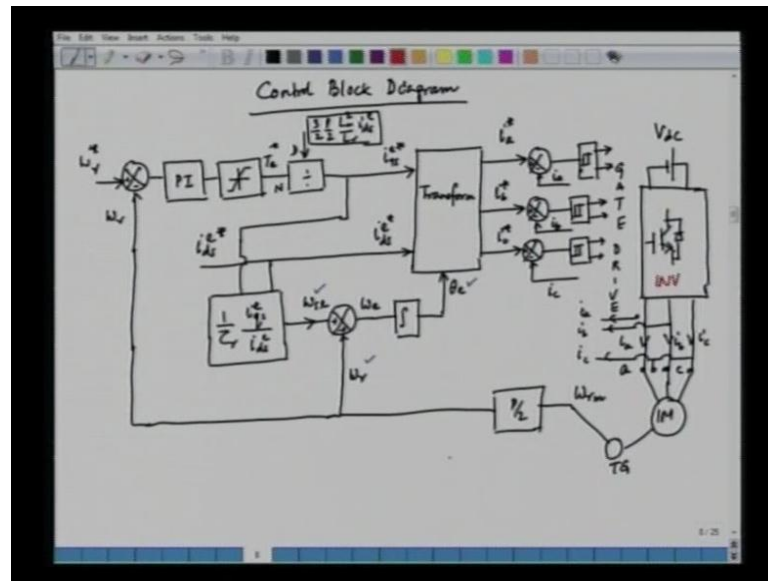
Now, this is called indirect vector control as θ_e is evaluated indirectly, this is one of the ways to evaluate θ_e , now the second method of evaluating θ_e is to change the rotor flux. If we can change the rotor flux in the d-axis and in the q-axis, stationary d-axis and q-axis, suppose we are having a machine, ((Refer Time: 39:34)) these are the machine windings the stator a_f , b_f and c_f and this is the rotor, and we want the rotor flux vector. So, we can have some sensor in the rotor and this is our stationary d-axis and this is the stationary q-axis, so we can find out what is ψ_{dr} and we can find out what is ψ_{qr} in the stationary.

So, ψ_{dr} and ψ_{qr} can give us θ_e , so we can say that θ_e is obtained by taking the tan inverse of ψ_{qr} and ψ_{dr} , these are the stationary flux component ψ_{dr} and ψ_{qr} are the stationary flux component. Now, if we have a rotating flux, actual flux is rotating at ω_e and this flux with a two component, one is ψ_{dr} this we can call to be ψ_{dr} , and this can also have component in the q-axis that ψ_{qr} . And the angle in this case is θ_e , now if we want to evaluate the angle we have right angle triangle and the perpendicular is ψ_{qr} .

And the base is ψ_{dr} , we can evaluate the angle θ_e a tan inverse of ψ_{qr} ψ_{dr} this is pretty straight forward, but the difficulty in this case is that how to sense the rotor flux. The sensing of the rotor flux is not very easy, because rotor is a moving member and housing a sensor inside the rotor is very difficult, and this cannot be used for retrofit application and hence, we cannot have rotor flux sensor inside the rotor. So, if we do not have rotor flux sensor, how to change the rotor flux, how to how to evaluate the rotor flux, that can be evaluated by using flux estimator.

So, what we can do is that we can estimate ((Refer Time: 41:54)) ψ_{dr} and ψ_{qr} and estimation of ψ_{dr} and ψ_{qr} can give us $\hat{\psi}_{dr}$ and $\hat{\psi}_{qr}$. And then we can evaluate what is θ_e from the estimate these are the estimates, and from the estimate we can calculate or we can evaluate what is rotor flux angle that is θ_e , so this is called direct vector control. Because, in this case we are able to find out θ_e directly without taking a help of slip speed, so we will now see a control block diagram of a vector control drive.

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So, we have here the transformation block and this angle is θ_e which we use for the transformation, we have reference speed in this case ω^* , then we are subtracting the actual speed. We are feeding into a PI controller and we can as well have a limiter in this case, and the limiter is used to limit the output of the PI controller, in case we do not have any limiter, some time the PI controller output can reach a very large value. So, to limit to the practical value we have to have a limiter after the PI controller.

And the output of the limiter is the reference torque T_e^* and this we can divide by $\frac{3}{2} \frac{L_m}{L_r}$ into $i_{d_s}^*$, so what we obtain here is $i_{q_s}^*$, this is what we can divide here, this is the numerator, this one is the denominator. And this is $i_{q_s}^*$ because this is the reference torque component of current and $i_{d_s}^*$ is given directly, what we have here is $i_{d_s}^*$, because we want to keep the flux constant and we are keeping i_{d_s} constant. So, this $i_{d_s}^*$ is fed directly we are not changing i_{d_s} and from i_{d_s} and $i_{q_s}^*$ we can evaluate the slip speed, the slip speed is $\frac{1}{\tau_r}$ into $i_{q_s}^*$ by $i_{d_s} \omega_s$. And we have the feedback from the two currents and then to the slip speed we are adding the rotor speed.

So, what we obtain here is ω_e , $\omega_s + \omega_r$ is equal to ω_e and that when we integrate this get θ_e , so the integration of ω_e θ_e and this θ_e will conform $i_{d_s}^*$ and $i_{q_s}^*$ into the 3 stator currents i_a^* , i_b^* and i_c^* . And then we have the comparators here, we can have the current comparator and this we

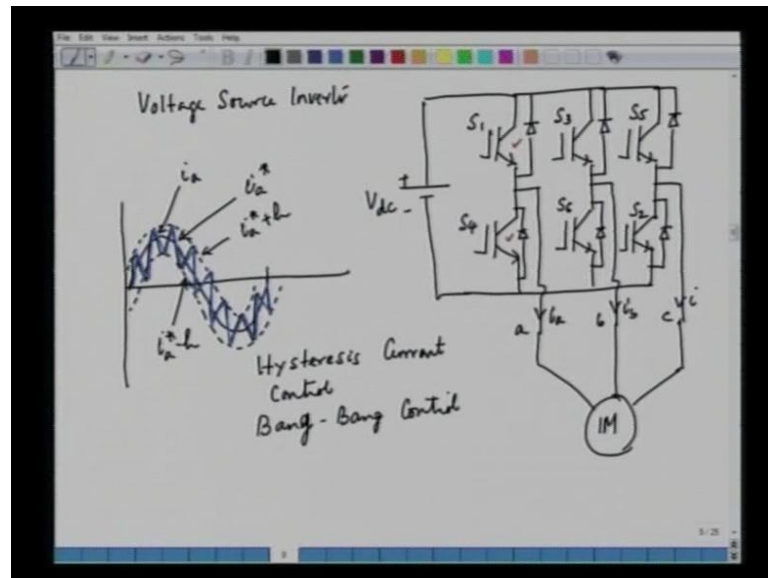
can have some sort of controller for three independent phases, this is phase a, this is phase b, phase c. Here is a inverter we have d c input of the inverter and this is an inverter may be having ((Refer Time: 48:00)), and then we have the induction motor here, the inverter will have the three phase output.

And outputs are stay to the induction motor, and we have a speed sensor or a tachogenerator here, the tachogenerator will be giving the output and then this is ω_r this will be giving us a mechanical output. So, what we can do here is that, we can multiply this by $P/2$ or $3/2$ this is $P/2$, this will be ω_{rm} the mechanical speed then we can multiply by $P/2$ to get the electrical speed. And the electrical speed is fed back here, and this what we are controlling is the electrical speed which can always the scale.

So, this ω_r here is the electrical speed, ω_{rm} is the mechanical speed and hence we have to multiply the mechanical speed by pole pair to obtain the electrical speed. So, this is the close loop control and this will be giving the gate drive signal for the inverter, so these are the gate drive signal, and this feedback will be i_a , this is the actual current that is fed back. Here we have i_b and here we have i_c , and in this case we have three different phases ((Refer Time: 49:59)) this is a, this is b and this is c, and the currents here are i_a , this is i_b and this one is i_c .

So, we can have the current sensors, we can have the current sensors in three phases to give us i_a , i_b and also for phase c we can have a another current sensor to give us these three signals. And these three signals can be fed back as the feedback signal for phase a, phase b and phase c inverter control. So, this actually is a close loop control block diagram for indirect vector control, it is call indirect vector control, because the slip speed is calculated. And we are adding the slip speed with the rotor speed to evaluate the transformation angle that is θ_e , now we will focus on the control of the inverter this is the inverter. This inverter is a voltage source inverter, so let us try to see what is the structure of this inverter? So, if you see the structure of the inverter, this inverter would be a three phase inverter something like this.

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And this is the d c voltage, and these are the three phases of the inverter, we have say for example phase a, phase b and phase c, and since this is a V f i the transistor will have anti parallel diode, so we have the diodes here to facilitate by directional flow of current. So, this is the voltage source inverter and the currents are in this case i_a , i_b and i_c and this will be feeding to the motor, so we have phase a, phase b and phase c of the machine, so the inverter fits to the induction motor.

And we have the inverter switches, we can call this to be S 1, this to be S 3, this to be S 5, this to be S 4, this to be S 6 and this to be S 2. So, we have 6 switches and when we have 6 switches we have 6 gate drive, so the 6 gate drives can be fed to the transistor 1, S 1, S 2, S 3, S 4, S 5 and S 6. The objective is this that whenever we have the phase a current the actual current should follow the phase a reference current as faithfully as possible. So, in this case what we have here is the following, we have phase a current this is i_a star and the actual current will follow the reference current within a bang.

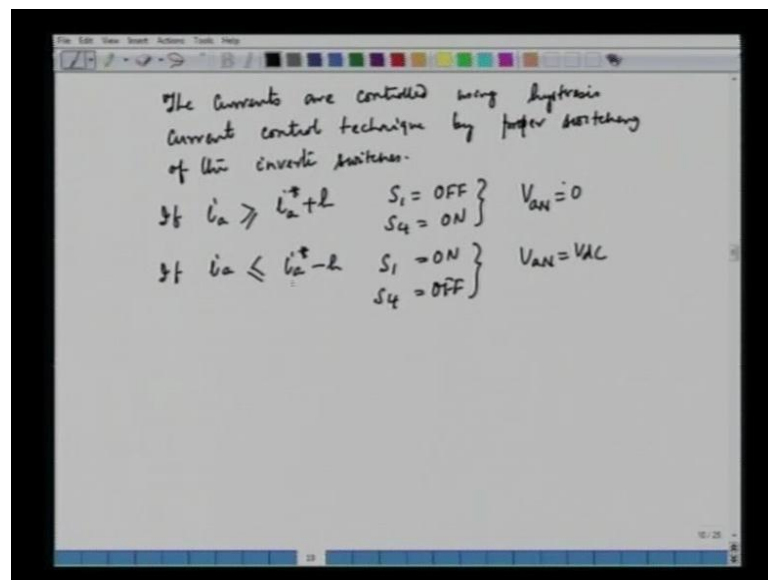
So, this is how the actual current will look like this is i_a , so what we do we have a reference current that is i_a star we define a bang around the reference current, we have upper bang and lower bang. So, this is the upper bang call i_a star plus h, star means the reference current similarly, we have a lower bang which is shown as a dotted line, so we can call this to be i_a star minus h. So, what we are trying to do here the actual current is

made to follow the reference current, within an upper band and a lower band and this is called hysteresis current control.

So, we can call this to be hysteresis current control, so if you talk about a particular phase say for example, phase a if you want to increase the phase a current, we switch on the upper switch. And if you want to decrease the phase a current we switch on the lower switch and go on doing like that and hence, the current will rise and fall, rise and fall, so it basically follows the actual current I mean the reference current within the band. So, this has got other names also we call this as bang-bang control, so we have to control the inverter in such a way that the actual current follows the reference current within the hysteresis band.

So, this is for phase a and similarly we can control phase b and phase c current and phase b is shifted from phase a by 120°, phase c is shifted from phase b by 120°. And the inverter is controlled in such a way that, the inverter will inject the actual current within a hysteresis band of the reference current on to the three phases of the machine that is phase a, phase b and phase c.

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The currents are controlled using hysteresis current control technique by proper switching of the inverter switches. So, we can just have a logic, that if i_a is higher than $i_a^* + h$ S_1 is turned off and S_4 is turned on, and if i_a is less than $i_a^* - h$ S_1 is turned on and S_4 is turned off. So, this means V_{dc} is equal to 0 or the voltage here will be

equal to 0, so it means we have V_{a-N} is equal to 0, and this means V_{a-N} equal to V_{dc} . And if we see this inverter structure we can define i_a is P, and we can define N here and these are our three phases a, b and c, so we are concentrating on phase a.

Now, if we concentrate on phase a, we can define V_{a-N} , V_{a-N} a capital N, now if the current is hitting the upper bang it means it is increasing, so we have to bring it down, now we have to bring it down by switching the lower switch, the lower switch is S 4. So, in this case, if it is hitting the upper bang greater or equal to this, we can switch off the upper switch and switch on the lower switch, it means we can make V_{a-N} equal to 0. And if i_a is less or equal to $i_a^* - h$, it means the current is hitting the lower bang, we have to switch on the upper switch, may have increase the current.

The current can be increased by switching on the upper switch and switching off the lower switch, so that is what we can do here, that if i_a is less than $i_a^* - h$, we can switch on the upper switch and switch off the switch. And S 1 and S 4 are complementary, we can see this inverter structure, ((Refer Time: 59:52)) that these two switches are complementary. The gate drive to S 1 is the inverse of gate drive to S 4, similarly the gate drive of S 3 is the inverse of gate drive of S 6, and gate drive of S 5 is the complement of gate drive to S 2.

So, these are complementary switches and this is basically the structure for one phase there is phase a, and we can similarly half for phase b and phase c. And hence, we can control the three phases as per the reference current requirement, and when we control the three phase current, the machine is automatically controlled on the vector control. So, in this particular lecture we have discussed the vector control of induction motor, we have seen how the vector control is similar to that of a d c motor control, we derived expression for the slip speed.

We have seen what is the difference between direct vector control and indirect vector control, we have also seen a control block diagram of close loop speed control of induction motor with vector control. So, in the next lecture, we will try to see that instead of keeping the flux constant, if we vary the flux how does the response change; so we will see the vector control operation under variable rotor flux.