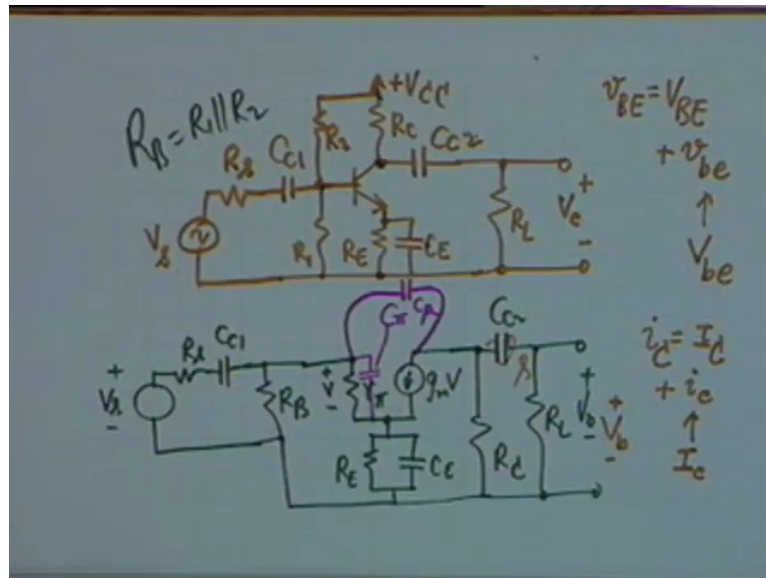


Introduction to Electronic Circuit
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Lecture 35
Small signal Amplifiers (Contd.)

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35th lecture and the topic is small signal amplifiers, as I have drawn last time a typical BJT amplifier, a complete BJT amplifier looks like this, let me draw it once at least RE and CE, there is an RC and this voltage is class VCC. The load is coupled to the transistor by means of a capacitor called CC2 coupling capacitor number 2 and this is RL, the actual load the signal voltage is taken from here and obviously this voltage shall be purely incremental voltage of the AC voltage.

Now we have adopted the notation that if I say V_{BE} this is the total base emitter voltage this is equal to the DC base emitter voltage capital V sub capital BE plus small v sub small b small e this is the AC input voltage. Now we shall adopt the notation we have already done that. That was the single part root mean square value shall be denoted by the RMS value of v_{be} if it is sinusoidal shall be denoted by capital V subscript small b small e.

For example if we are concerned with the collector current $i_{sub\ capital\ C}$, well, it is the sum of $I_{sub\ capital\ C}$ this is the DC value plus small i subscript small c it is AC value and the RMS value of this shall be denoted by capital I subscript small c, okay. This is the notation

that you shall follow and therefore what should we call this voltage? This voltage root mean square value.

We will only write root mean square values now, it should be called $V_{small\ c}$ then, that is all. It is a voltage of this point with respect to, no, respect to ground because CE is short, CE makes our each short and therefore this is the voltage, wait, okay, VCE or VCG ground is a same thing, so you should call it V_c , simply V_c , alright. And we will note down a polarity, this polarity shall be related polarity, alright.

For example if $V_{sub\ capital\ B}$ is positive then you know that $V_{small\ c}$ shall be negative there is a phase change, well, this will be clear in the subsequent discussions then the base circuit is biased by means of R_2 and R_1 and the base circuit is coupled to the voltage source or current source.

Let us represent this by a general source, a general source has an internal resistance R_s and the voltage if it is AC then we shall say $v_{small\ i}$ input or $v_{small\ s}$ and if I want to only write the RMS values. We will write this as $v_{small\ s}$, we shall follow this discipline throughout. For example the AC base current shall now be denoted by $I_{small\ b}$ that means the root mean square value of the signal voltage.

And as I have repeatedly told you we can divorce signal quantities from DC quantities and therefore we can analyze by means of this small signal model of the transistor. There are 3 capacitor's CC_1 , CC_2 and C_E . 2 of them CC_1 and CC_2 are coupling capacitors, they couple the AC to the transistor, this couples the collector voltage to load, so these are coupling capacitors and $C_{sub\ E}$ is a bypass capacitor, it bypasses the AC to ground, so that nothing drops across $R_{sub\ E}$.

Now if I follow the hybrid pi models strictly than my AC incremental equivalent circuit we like this and try to draw with me. What we have is, we are representing every quantity by means of its RMS value. So V_s then in R_s then CC_1 the coupling capacitor and then as far as AC is concerned from this point to ground R_1 and R_2 come in parallel and we have chosen to call R_1 parallel R_2 as $R_{sub\ capital\ B}$, R_B is the parallel combination R_1 parallel R_2 , Parallel combination R_1 and R_2 , alright, R_B .

Then comes the base, from the base to the emitter it is r_{pi} , alright. Then R_E and C_E , well, there is a parallel combination we will see the effect of this R_E and C_E this terminal comes here, alright. R_E and C_E and then this voltage, if I call this voltage as capital V , this voltage is capital V voltage across r_{pi} then at the output you have g_m times capital V this is the collector terminal and from collector to ground goes a resistance R_C and then from the same point collector, a capacitance C_C goes to R_L and this voltage is V_c or V_0 the output voltage, okay.

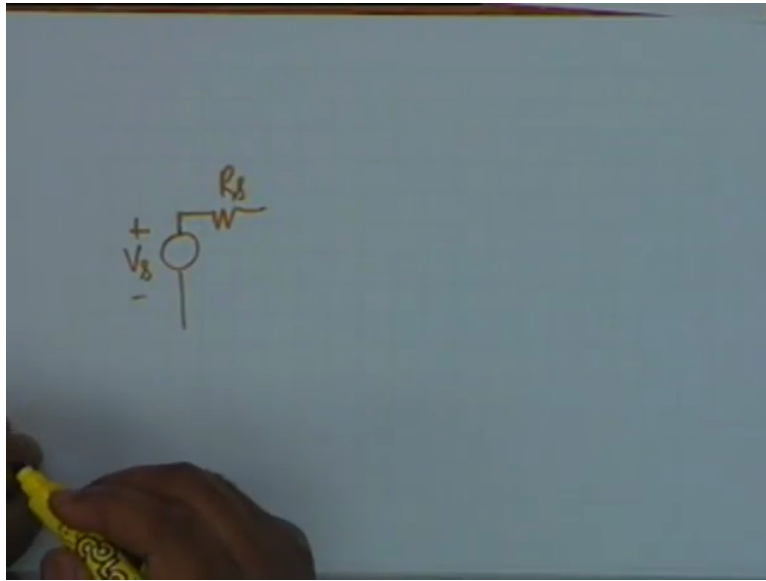
In order to determine the performance characteristic of this amplifier, that is the amplification property, what we have to find out? By circuit analysis we have to find out V_0 by V_s that would be the gain of the circuit, we have to find, in general you see because there are resistance as well as capacitances this gain would be a complex quantity. It would be a complex quantity either to replace the capacitors by 1 by $g \omega c$.

To be fair to make this circuit applicable at all frequencies we should introduce the terms the capacitances which are internal with transistor. If this circuit is to represent high frequencies for example we should introduce the C_{pi} , C_{pi} is across r_{pi} and another capacitor we should introduce between this point and the collector this is C_{mui} , alright. If we introduced these 2 then this circuit is complete.

It can represent low frequencies it can represent high frequencies it can also represent medium frequencies and the most convenient calculation for gain comes at medium frequencies. At medium frequencies, while the frequencies are defined, medium frequencies are defined as the frequencies neither too low nor too high these are frequencies at which the effect of capacitances can be ignored which means that at medium frequencies C_C , C_C and C_E should act as short-circuits.

Medium frequencies are those at which C_C the 2 coupling capacitors and the emitter bypass capacitor the 3 act as short-circuits and the internal capacitances which are very small at medium frequencies they act as open that is C_{mui} and C_{pi} they act as open and therefore at medium frequencies which is also called the mid band are equivalent circuit.

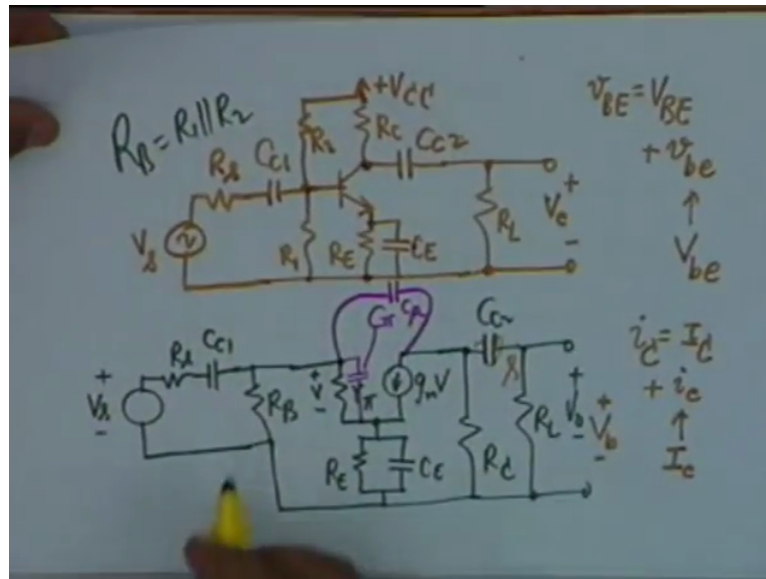
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If we follow this carefully our equivalent circuit would be V_s then R_s $CC1$ will act as a short then we shall have R_B in parallel with r_{pi} , now r_i comes across R_B because R_E is assured, C_E is assured and therefore r_{pi} comes across R_B and this voltage is v , okay. Then we have $g_m v$ no capacitances C_{pi} is ignored, C_{mi} is ignored and we have $g_m v$ in parallel $R_{sub C}$ than the capacitor $CC2$ also acts as a short-circuit and therefore this is $R_{sub L}$ and this voltage is V_0 , this is the situation and the mid frequency range sometimes called mid band equivalent circuit, mid band frequency range.

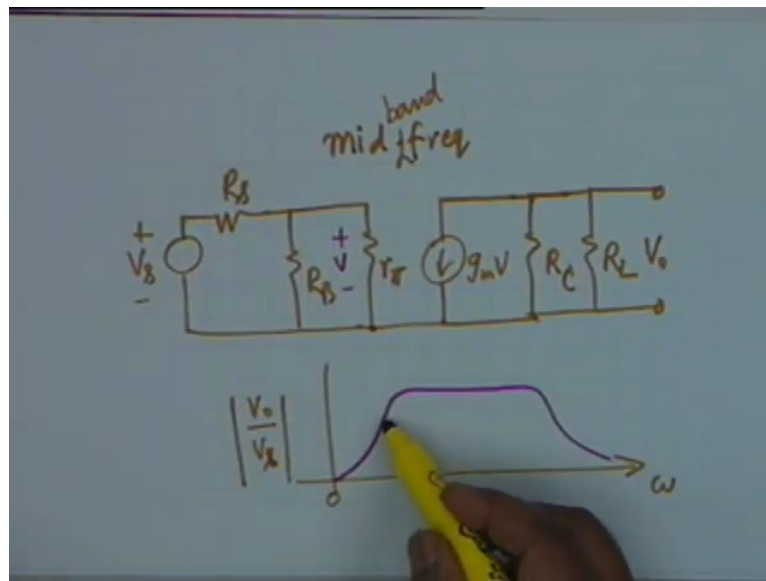
Well, I should mention here and if you plot the gain, that is if you plot V_0/z by V_s versus frequency Ω then in general for the RC coupled amplifier the curve looks like this. That is at DC again is 0, why is it 0 at DC?

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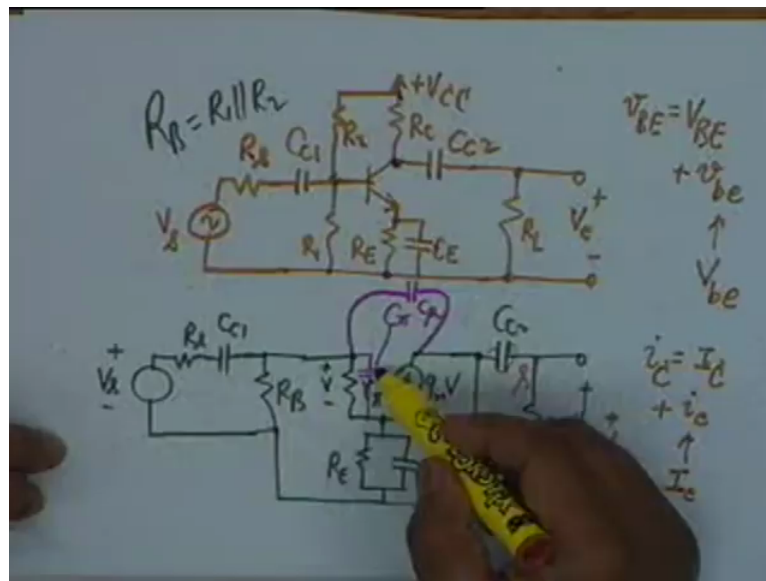
Because this coupling capacitors refuse to pass DC, alright. This coupling capacitor, this coupling capacitor, so at DC nothing reaches the transistor, transistor does not amplifier, alright. That is why the gain is 0. As the frequency increases these 2 capacitors, they become often less and less impedance and therefore signal passes to the transistor and the transistor does amplify, so the gain rises.

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Then around, let us say there is a set of frequencies at which the gain is a constant, the gain can be a constant only if there are no capacitances in the circuit which means that this is the mid band frequency range. This is the mid band, mid band range and then as the frequency is increase the coupling capacitances and the bypass capacitance they remain short because they react the impedance is 1 by $J\omega C$.

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So the higher the alloy frequency, the lower is the impedance they remain short but what we had assumed as open that is the 2 internal capacitances C_{pi} and $C_{m\mu i}$ they now show their treat and therefore their effect then dominates and it is because of these 2 capacitances that the gain once again falls, alright. So it is a well shaped curve, this region, the region from 0 to the beginning of the mid frequency is denoted as the low frequency region.

And the region the frequency range from the end of the mid band to in finite frequency theoretically is the high frequency band and you know that in such a characteristic not only the mid band gain is important, mid band gain we should denote by A_0 but also the 2 frequencies at which the gain falls below the mid band value by 1 by root 2 and therefore this value is A_0 by root 2 there are therefore 2 frequencies, and we call ω_L and the other we call ω_H .

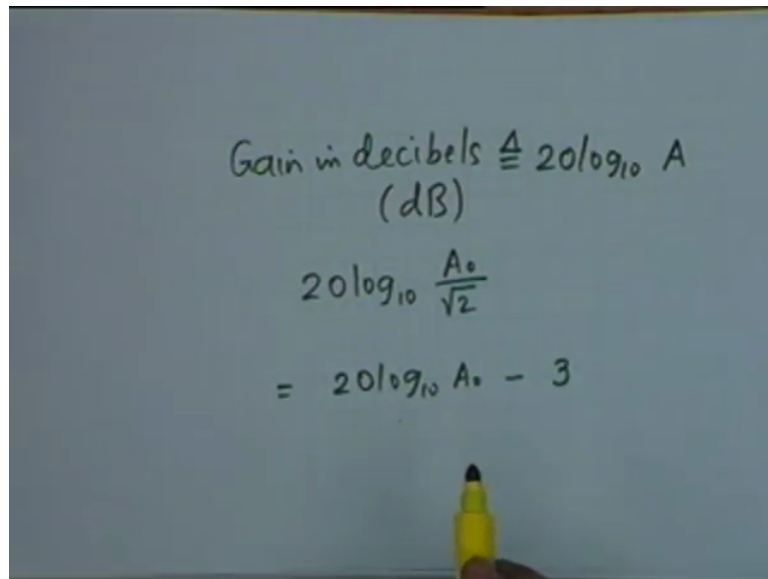
ω_L is called a low frequency cut-off this is a frequency and the ω_H is the high frequency cut-off that means between ω_L and ω_H the gain remains 70.7 percent of its mid band value. I was told you that the gain is usually expressed in terms of decibels and decibel gain is $20 \log_{10} A$ and $\log_{10} 20 \log_{10} 1$ by root 2 is approximately minus 3 therefore if the mid band value is taken as the reference then this level is 3 decibels below the mid band value.

If the mid band value is taken as 0 decibels then this is minus 3dB this point and this point. Is that point clear? Did I not discuss decibels earlier? Oh, I did not, okay. The gain, you see the gain could be a very large quantity it may vary from 0 right up to let say 10 to the 5 or 10 to

the 6 and it is very difficult to represent such a large dynamic range and therefore what you do is, you compress the range by a logarithmic transformation.

For example if A that is from 1 to let say 10 to the 5, then at 1 the value is 0 $20 \log_{10} A$ and at 10 to the 5 it is simply 100. So what you represent is 0 to 100, instead of 1 to 10 to the power 5.

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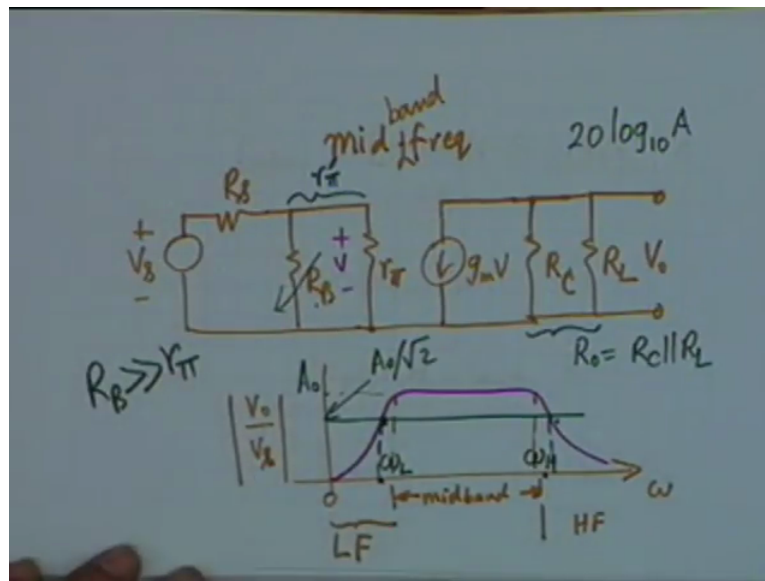


A photograph of a hand-drawn equation on a chalkboard. The text is written in black marker on a light blue background. A yellow highlighter is visible at the bottom center of the frame.

$$\begin{aligned} \text{Gain in decibels} &\triangleq 20 \log_{10} A \\ &(\text{dB}) \\ 20 \log_{10} \frac{A_0}{\sqrt{2}} \\ &= 20 \log_{10} A_0 - 3 \end{aligned}$$

So you compress the range and therefore gain is always in electrical engineering practice, gain is expressed in decibels D E C I B E L S and if is it (()) (16:15) small v capital V the definition is that this is 20 log 10 of gain as a number, alright, $20 \log_{10} A$. And you see if the if the gain is A_0 by root2 then it is simply as you know $20 \log_{10} A_0$ minus 3 half of \log_2 , \log_2 is 0.30103, alright. Is this clear? $20 \log_{10} A_0$ minus $20 \log_{10}$ of root 2, $20 \log_{10}$ of root 2 is approximately 3, actually this 3.0103 we ignore that.

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And therefore these are frequencies, ω_L and ω_H these are frequencies at which the gain is reduced by 3 decibels and this ω_L and ω_H therefore I have got another name, one of the names is low frequency cut-off, high frequency cut-off or they are also called 3 dB points that is the frequencies at which the gain is down by 3 decibels 3 dB points ω_L and ω_H , alright.

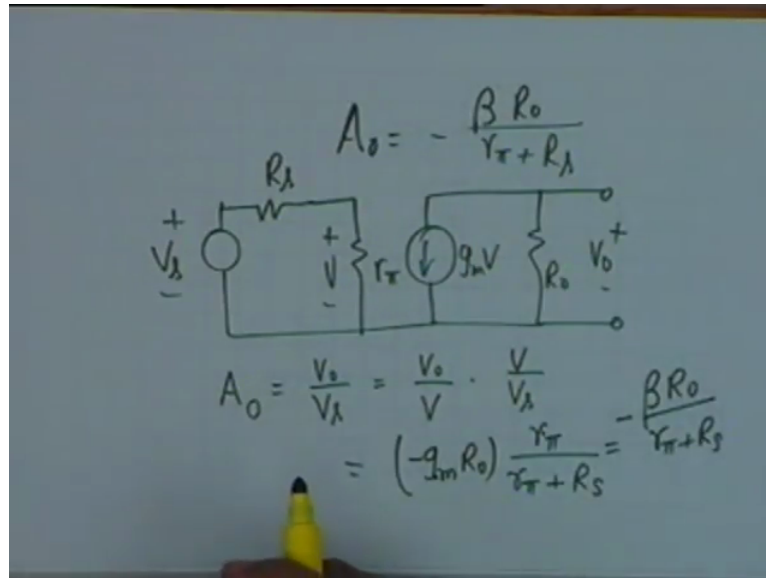
We shall calculate what ω_L and ω_H is for the RC coupled amplifier but at the present time we are concerned with the calculation of the mid band gain, mid band frequency range by definition is 1 in which the effect of all capacitances can be ignored which the coupling in bypass capacitances are shorts and the internal capacitances C_{pi} and $C_{m\mu i}$ are open, alright.

If that is the case then this becomes the equivalent circuit and it simplifies the equivalent circuit by noting that R_C and R_L are in parallel and we can call this by R_o , let us call this R_o is equal to R_C parallel R_L . You also notice that R_B and r_{π} are in parallel and if R_B and r_{π} are comparable then you can combine the 2 and you can call this resulting 1 as r_{π}' that the usual design consideration is that R_B is usually much greater than r_{π} , r_{π} is the order of the k and R_B would be of the order of the 10k and 1 is to 10 can be considered as much greater than.

And therefore in our subsequent calculations we shall ignore the effect of R_B . If needed if your design is such that R_B is comparable r_{π} then you simply combine the 2 that is you take

instead of r_{pi} you take r_{pi} prime is a parallel combination of R_B and r_{pi} and therefore our equivalent circuit then simplifies to the following.

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We have V_s R_s , R_s is the source resistance then we have r_{pi} this voltage is V then we have $g_m V$ and simply R_o this is equal to V_o and you notice that the gain A , we are calculating the mid band gain and therefore I would subscript 0, A_0 is v_o by V_s which I can write as v_o by V multiplied by V by V_s , is it okay? V_o by V_s I have written as V_o by V multiplied by V by V_s .

What is V_o by V ? You see this current flows through R_o and therefore V_o will be equal to minus $g_m V$ times R_o and therefore V_o by V is simply minus $g_m R_o$ and V by V_s is simply a potential division that is r_{pi} divided by r_{pi} plus R_s you see that g_m and r_{pi} come as a products now the product is β and therefore I can write this as minus βR_o divided by r_{pi} plus R_s you can see what happens if capacitor R_B it cannot be ignored then r_{pi} shall simply be replaced by r_{pi} prime which is the parallel combination of r_{pi} and R_B , so this is a simple formula for the mid band gain that is minus βR_o divided by r_{pi} plus R_s .

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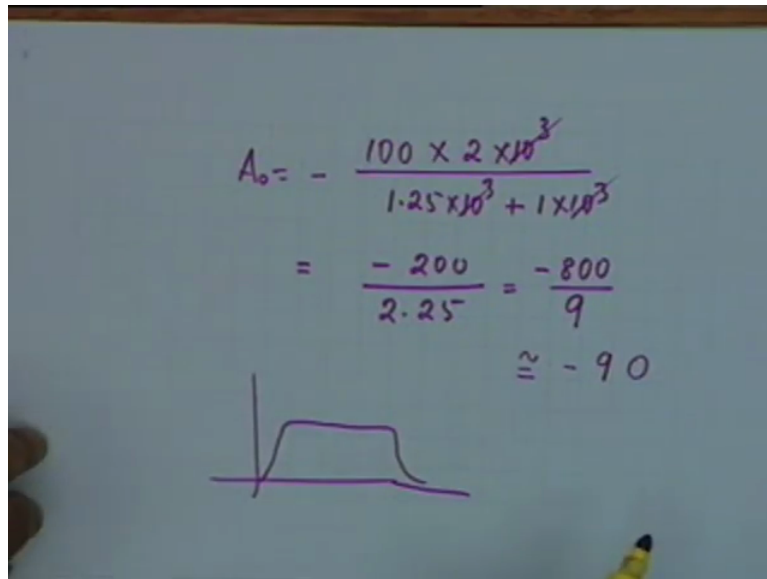
$\beta = 100$ $R_s = 1000 \Omega$
 $R_E = 500 \Omega$
 $R_1 = 20K$
 $R_2 = 50K$ } $R_B = 14.3K$
 $g_m = 40 \times 2 \times 10^{-3} = 0.08 A/V$
 $R_C = 4K$
 $R_L = 4K$ } $R_0 = 2K$
 $I_C = 2 mA$
 $A_0 = ?$
 $Y_{\pi} = \frac{100}{0.08} = 1.25K$

Let us take some typical values, for a certain transistor 2m series, beta is typically 100, the source resistance typically is 1k 1000 ohms. RE is of the order of 500 ohms, RE does not enter into the mid band calculation because RE is (()) (21:58) by capacitance which is sufficiently large R1 is 20k, R2 is 50k therefore RB is how much? 20 times 50 divided by 70 that is 14.3k, alright.

RC is let say 4k, RL is 4k, so that R0 is simply equal to 2k, R0 is a parallel combination of the 2 and I sub C the collector current is given as 2 milliampere, alright. You are required to calculate the mid band theory A0. Obviously for mid band gain calculation minus beta R0 divided by rpi you understand the meaning of the minus sign because the output voltage is out of phase with the input voltage, okay. rpi plus Rs therefore indeed the value of rpi, we have been given the value of beta.

And we know what is I sub C is, that is the quiescent collector current and therefore can calculate the value of gm, gm is 40 times I sub C therefore 40 times 2 times 10 to the minus 3 which is equal to 0.08, is it okay? And therefore what is rpi then beta divided by gm therefore 100 divided by 0.08, have I made a mistake? So how much is this? 1.25k, alright. That is correct 1.25k and you notice that indeed 1.25k rpi is small compared to RB which is 14.3, 1 order of magnitude difference is good enough for much greater than. So we can indeed ignore this.

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The image shows a whiteboard with handwritten mathematical work. At the top, the equation for the mid-band gain A_o is written as:

$$A_o = - \frac{100 \times 2 \times 10^3}{1.25 \times 10^3 + 1 \times 10^3}$$

This is simplified to:

$$= \frac{-200}{2.25} = \frac{-800}{9}$$

The final result is given as:

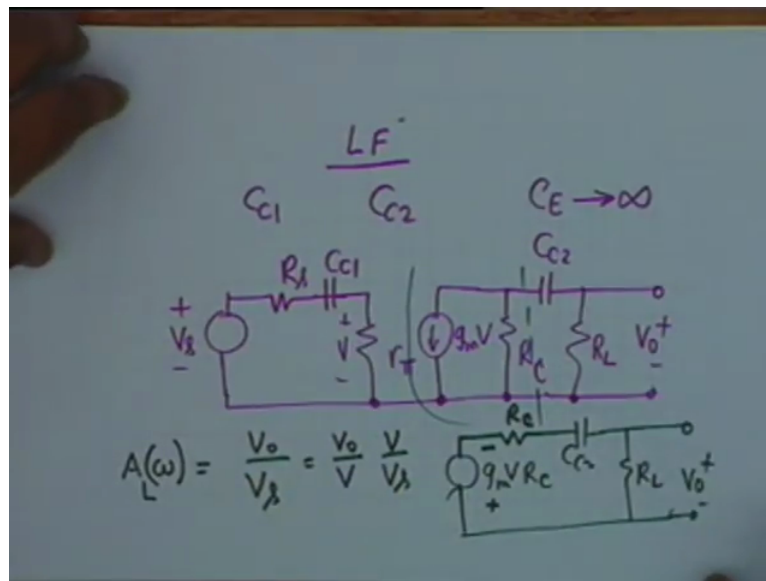
$$\approx -90$$

Below the equations, there is a hand-drawn graph. The vertical axis represents gain and the horizontal axis represents frequency. The graph shows a rectangular pulse, indicating a constant gain in the mid-band region, with roll-offs at the low and high frequency ends.

Now if we substitute this value, so we can indeed ignore this, now if we substitute these values in the mid band gain and I get A_o as equal to minus 100 beta, R_o is 2k 2 times 10 to 3 divided by r_{pi} which is 1.25 times 10 to the 3 plus R_s which is 1 times 10 to the 3, so 10 to the 3 can be ignored this is minus 200 divided by 2.25. In this minus 800 by 9, yes and as you can see this is approximately equal to minus 90, alright.

Approximately it is slightly less than 90, 89 point something but this is the typical mid band gain, you can get a gain of 90 to 100 and if you couple another stage you can get 8100 in 90 times 90, alright. Many large gains are indeed possible. Now let us look at, it is the mid band situation, mid band situation as I said is a situation in which the gain remains approximately a constant, why does it remain constant? Because effect of capacitances can be ignored, alright.

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Let's look at the new frequency situation, what happens at low frequencies? At low frequencies the internal capacitances of your transistor can be ignored but the coupling capacitances must be taken into account and also the bypass capacitor. Now since there are 3 capacitances to be taken into account, 3 capacitances C_{C1} , C_{C2} and C_E circuit analysis becomes a bit complicated.

Also I tends to get lost into mathematics of the algebra of the situation I tends to get loose site of the physical situations, so what we will do is, for an engineer it is very important, it is very convenient to consider one at a time, one effect at a time. We shall be shall be a little more prudent, we shall be a little more flexible and say 2 at a time, let us take the effect of C_{C1} and C_{C2} into effect.

Which in effect means that C_E we are assuming go to infinity, the largest possible C_E we put there and therefore we look at the effect of C_{C1} and C_{C2} (()) (27:18) and if you draw the equivalent circuit then the RMS value of the signal R_s then there is a C_{C1} the coupling capacitance, we have the r_{π} and this voltage is V . You see the advantage of having V instead of current I sub B.

Then we have $g_m V$ and we have $g_m V$ in parallel with R_C then we have the second coupling capacitor C_{C2} and the load resistance R_L this is V_0 . Now unlike the mid band situation we cannot combine R_C and R_L because C_{C2} is not a short it offers appreciate all impedance, impedance can be comparable to that of R_C and R_L therefore we cannot consider this but we

can do one thing very interestingly we can replace this part by $(\)$ (28:30) and therefore what we can do is that RC and RL will come in series, you see the point.

So what we can do is this part I can write as $g_m V$ times R_c , this is the open circuit voltage with what polarity? Minus plus then the $(\)$ (28:51) resistance is RC then we have CC2 and we have RL, the output circuit can be represented like this and this is V_0 , alright. Let the input circuit remain as it is. We have to calculate the gain, the gain A, now A is a function of frequency Ω .

So we say A function of frequency, alright. And since we are considering no frequencies we say $A_L \omega$, this L stands for low frequency gain. In the previous case when we calculate the mid band gain we should have written a subscript of m but I prefer to write A_0 this is conventional, at mid band gain where it is a constant you write A_0 . So $A_L \omega$ now is V_0 by V_s and this is the circuit that has to be analyzed now.

Input part is this, output part is this and the analyses can be done by inspection just by looking at the circuit because you see V_0 by V_s can be written as V_0 by V multiplied by V by V_s .

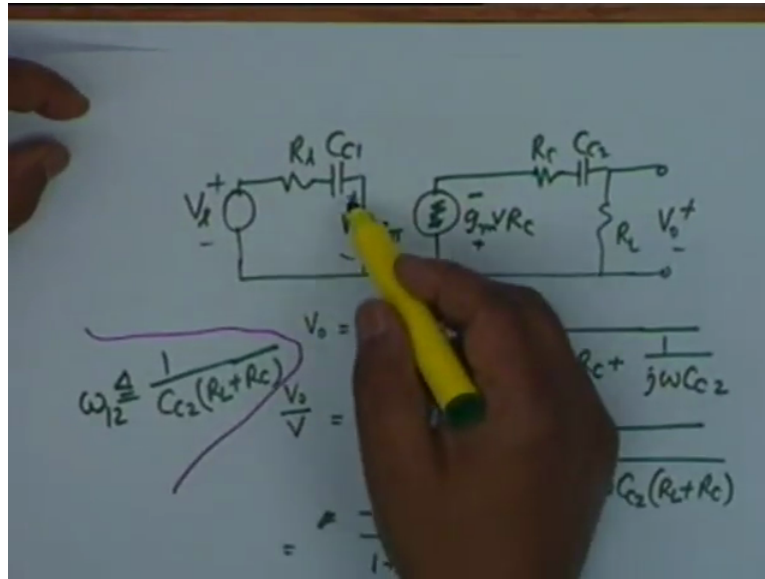
Now let us look at this circuit once again and calculate these 2 quantities separately now equivalent circuit let us draw it again V_s , R_s , CC1, r_{pi} and this voltage is V , then you have, no I am sorry, $g_m V R_c$ is a voltage generator now with this polarity minus plus and R_c , CC2, RL and this is V_0 . You can see that V_0 is equal to minus $g_m V R_c$, alright. Minus $g_m V R_c$ then a potential division RL and RC in series with CC2.

Therefore it would be RL divided by RL plus RC plus 1 over $g \omega$ CC2, is it okay? I write this is my inspection, okay. Now I can do a bit of simplification, you see minus, let us write V_0 by V this is what I want, I want V_0 by V , so let us write V_0 by V this is minus g_m , look at the same simplification I have RC RL then for the denominator let me take RL plus RC out, alright.

Then I get 1 by 1 plus 1 $j \omega$ CC2 RL plus RC, is it all right? Now do not you see that this is simply the parallel combination of RC and RL and therefore I can write this as minus $g_m R_0$ divided by 1 plus now I introduce a term $\omega \tau$ by $j \Omega$? I introduce a term $\omega \tau$ where I define $\omega \tau$ as 1 over CC2 RL plus RC. You see the definition is, that it is inverse of the time constant of the circuit.

What is the time constant? Product of capacitance and resistance, RC and RL are in series and therefore the time constant of the output circuit is given by $C_2 R_L$ plus RC and the reciprocal of that I express I give the symbol ω_{12} then my V_0 by V becomes minus $g_m R_0$ divided by $1 - \text{minus}$ now I have take j up $1 - \text{minus}$ $j \omega_{12}$ divided by Ω , alright. This is the low frequency gain as far as the output circuit is concerned.

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We have however a task of finding V by V_s and if you notice this circuit as I have done earlier V by V_s is simply a potential division between r_{pi} and R_s and C_1 .

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$$\frac{V_0}{V} = \frac{-g_m R_o}{1 - j \frac{\omega_{12}}{\omega}}$$

$$\frac{V}{V_s} = \frac{r_{\pi}}{r_{\pi} + R_s + \frac{1}{j\omega C_{c1}}}$$

$$\frac{1}{C_{c1}(R_s + r_{\pi})} = \frac{r_{\pi}}{r_{\pi} + R_s} \frac{1}{1 + \frac{1}{j\omega C_{c1}(r_{\pi} + R_s)}}$$

$$\frac{V}{V_s} = \frac{r_{\pi}}{r_{\pi} + R_s} \frac{1}{1 - j \frac{\omega_{11}}{\omega}}$$

And therefore I can also write that down by inspection that is r_{π} divided by r_{π} plus R_s plus 1 over $j\omega C_{c1}$, this I now write as r_{π} divided by r_{π} I take this out, alright. And then I can write 1 divided by 1 plus 1 over $j\omega C_{c1} r_{\pi} + R_s$, any objection? Is that true? Have I distorted anything? Not yet, alright. So I prefer to write this in the form r_{π} divided by $r_{\pi} + R_s$ $1 - j$, 1 by j is minus j and then I write ω_{11} divided by ω , alright.

ω_{11} divided by ω is ω_{11} is now defined as the time constant of the input circuit, reciprocal of the time constant of the input circuit which means C_{c1} , input circuit is C_{c1} in series with R_s plus r_{π} , alright. This is ω_{11} is defined as the reciprocal of the time constant of the input circuit, alright. Now if I substitute these 2 values that is V_0 by V this expression and V by V_s this expression and I multiply the 2 then I get V_0 by V_s that is the overall gain.

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$$\frac{V_o}{V_s} = \frac{-g_m R_o r_{\pi}}{r_{\pi} + R_s} \frac{1}{\left(1 - j \frac{\omega_{11}}{\omega}\right) \left(1 - j \frac{\omega_{12}}{\omega}\right)}$$

$$A_L(\omega) = \frac{-\beta R_o}{r_{\pi} + R_s} \frac{1}{\text{"}}$$

$$\frac{A_L(\omega)}{A_0} = \frac{1}{\left(1 - j \frac{\omega_{11}}{\omega}\right) \left(1 - j \frac{\omega_{12}}{\omega}\right)}$$

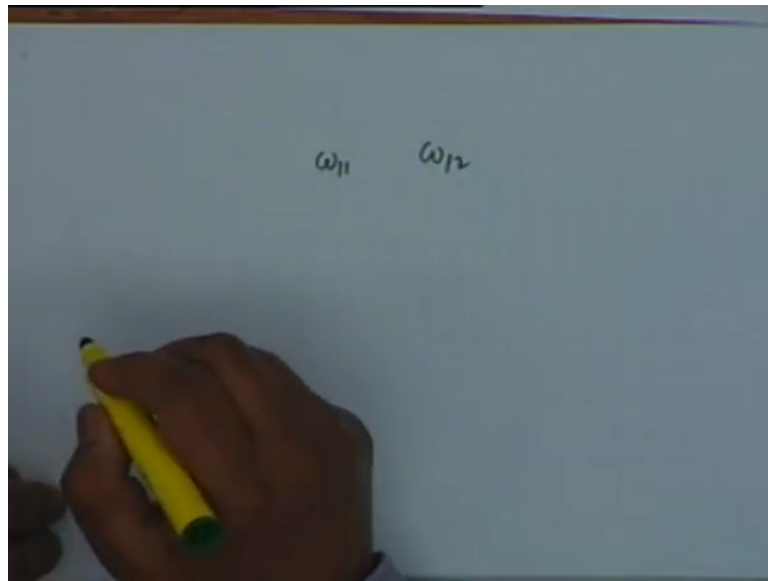
And this obviously V_0 by V_s becomes equal to, if you notice carefully minus $g_m R_0$ I think the constant term of the other expression r_{π} given by r_{π} plus R_s , alright. Then I have 2 terms $1 - j \omega_{11} / \omega$ by ω $1 - j \omega_{12} / \omega$ by ω , is that clear? And if you notice the constant term here you see that $g_m r_{\pi}$ is β and therefore this is minus βr_0 divided by r_{π} plus R_s times 1 over these 2 terms.

This is $A_L(\omega)$ the low frequency gain as a function of frequency. What do you recognize this as? This is the mid band gain that is A_0 and therefore the normalised gain that is $A_L(\omega) / A_0$, if we normalise again with respect to A_0 , it is simply given by one by one minus $j \omega_{11} / \omega$ $1 - j \omega_{12} / \omega$, it is a product of 2 terms like this and you notice that if ω , what is the value at ω equal to 0?

Obviously this is 1 and as ω increases, the gain increases, when ω becomes large compared ω_{11} as well as ω_{12} , gain becomes 1 it simply becomes 1, right? And therefore it does explain the rise of gain from 0 to the mid band value A_0 . The question now is where is ω_L ? What is the frequency at which the gain is 3dB down the mid band value.

3 dB would be less than the mid band value or $1 / \sqrt{2}$ times the mid band value. Well, strictly what we have to do is, we have to take the magnitude and equate that to $1 / \sqrt{2}$ you will get a quadratic equation ω to the power 4, engineers do not like to solve equations electrical engineers in particular try to find a shortcut, what we will do is the following.

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He says alright I have 2 frequencies ω_{11} and ω_{12} . Suppose they are several times apart from each other, let say ω_{11} is greater than ω_{12} and maybe greater than is let say of the order of 3 times, what is the square of 3? 9 and much greater than means in electrical engineering is 1 is to 10.

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$$\frac{V_o}{V_s} = \frac{-g_m R_o r_\pi}{r_\pi + R_s} \frac{1}{\left(1 - j \frac{\omega_{11}}{\omega}\right) \left(1 - j \frac{\omega_{12}}{\omega}\right)}$$
$$A_L(\omega) = \frac{-\beta R_o}{r_\pi + R_s} \frac{1}{\left(1 - j \frac{\omega_{11}}{\omega}\right) \left(1 - j \frac{\omega_{12}}{\omega}\right)}$$
$$\frac{A_L(\omega)}{A_o} = \frac{1}{\left(1 - j \frac{\omega_{11}}{\omega}\right) \left(1 - j \frac{\omega_{12}}{\omega}\right)}$$
$$\sqrt{1 + \left(\frac{\omega_{11}}{\omega}\right)^2} \sqrt{1 + \left(\frac{\omega_{12}}{\omega}\right)^2}$$

Now in this case you see when I take the magnitude, what is a magnitude of this term? Square root of one plus omega 11 by omega square, now the other term is 1 plus omega 12 by omega square. If one of these terms is approximately 10 times the other term then obviously one can ignore the other term and this qualitative argument it can be strictly put on quantitative terms.

This qualitative argument says that which one...

“Professor -Student conversation starts”

Student: because you are multiplying...

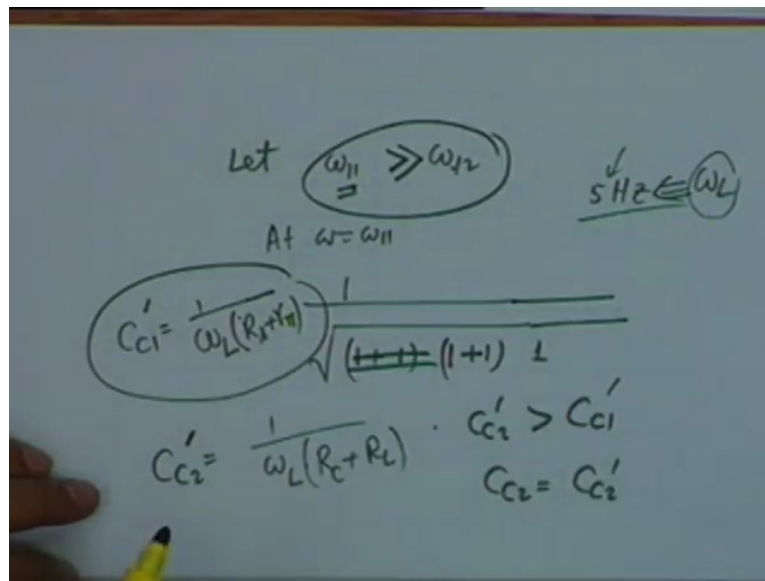
Professor: Yes.

Student: subtracting or adding sir.

Professor: Okay.

“Professor-Student conversation ends”

(Refer Slide Time: 40:10)



Let us say that omega 11 is much greater than omega 12, let this be the case, okay. Then at omega equal to omega 11, what is the value? What is the magnitude? Magnitude is square root of 1 plus 1, okay. And the other one is approximately 1? And therefore omega 11 determines the low frequency cut-off, is that clear? This is the point that I was making, if one of them is much greater than the other, I will come to what is much greater little later.

If one of them is much greater than the other than the greater one determines the low frequency cut-off. Now how much greater? In practice 3 times is good enough because the quantity is involved here not as omega 11 but omega 11 squared, alright. If one is 3 times the other, 3.3 times approximately than the square shall be one order of magnitude apart and therefore 3 times greater is good enough, alright.

So what one does is the following, given a circuit, if you see that omega 11 and omega 12 before by at least a factor of 3 and you take the higher one as the low frequency cut-off, as have shown in here, the higher one, alright. On the other hand if they are comparable, if this much greater than sign does not hold, suppose one of them is 10 hertz and the other one is 15 then we have to solve this equation exactly, the quadratic equation there is no other way but that is hardly even the case.

What an engineer does, engineers like new IIT graduates they design, so you are told by the boss we want a high fidelity stereo amplifier whose low frequency cut-off is let say 5 hertz, you are told that audio frequencies go from 16 hertz to 16 kilohertz but if your amplifier

satisfies only this the drums, the left-handed (()) (42:45) in particular which is very rich in low frequency that sound is lost, alright.

If you want a very high fidelity stereo amplifier then you must go down to about 5 hertz is the low frequency cut-off alright. You have to design an amplifier with 5 hertz cut-off then what you do is, you find CC_1 , okay. You find CC_1 prime let say from whatever the specified ωL is, what is ωL if low frequency cut-off is 5 hertz?

“Professor -Student conversation starts”

Professor: What is the value for ωL ?

Student: 5.

Professor: No, ωL .

Student: 10π .

Professor: 2π times 5, you must not big mistake.

“Professor-Student conversation ends”

So what you do is, from the specified ωL you find out CC_1 the coupling capacitor 1 which would be ωL times, what is the resistance? R_s plus r_{π} you calculate this capacitor, alright. Then you get calculate the other capacitance CC_2 prime, are you following the design process? Given if the ωL is specified you calculate the necessary values of CC_1 and CC_2 each satisfying this value of ωL .

How do you find CC_2 ? Not I am not putting CC_2 , I am putting CC_2 prime because the design values will be different, alright. So what I do is CC_2 prime, I also calculate from the same ωL , I say ωL , what is the resistance as I said? R_C plus R_L then from these 2 I find out which one is larger. Suppose CC_2 prime is larger, if this is larger CC_2 prime is better than CC_1 then what I do is, I put CC_2 equal to CC_2 prime whatever the calculative value is, alright.

And I increase the other capacitor that means 5 times 3 is a good figure but to be on the safe side I increase 5 times, what does that mean? It means that ω_{11} shall now be at least 5 times less than ω_{12} and that is what ω_{12} shall determine below frequency cut-off,

is the design process clear? We shall illustrate this by means of an example, mind you we have not talked about CE at all so far.

(Refer Slide Time: 45:50)

Handwritten calculations on a chalkboard:

$$\omega_L = 333.3 \text{ rad/s}$$

$$R_s = 1 \text{ k} \quad r_{\pi} = 2 \text{ k}$$

$$R_c = 4.5 \text{ k} \quad R_L = 9 \text{ k}$$

$$g_m = 60 \text{ mS} \quad C_{C1} = C_{C2} = 1 \mu\text{F}$$

$$A_o ? \quad \omega_L ?$$

$$A_o = \frac{-\beta R_o}{r_{\pi} + R_s} = \frac{-120 \times (4.5 \text{ k} \parallel 9 \text{ k})}{2 \text{ k} + 1 \text{ k}} = -120$$

$$\omega_{11} = \frac{1}{C_{C1}(r_{\pi} + R_s)} = 333.3 \text{ rad/s}$$

$$\omega_{12} = \frac{1}{C_{C2}(R_c + R_L)} = 74.1 \text{ rad/s}$$

What will be the value of CE? We will consider that also a moment but let us consider example first. Suppose you are given amplifier in which R_s is 1k, the source resistance is 1k the same design data but to give variety let us say r_{π} is 2k, R_c is 4.5k and R_L is 9k, g_m is let us say 60 millimoh, what does this correspond to? I_{CQ} , yes, so what is I_{CQ} ? 1.5 milliamper.

If g_m is specified then you know what is I_{CQ} , if I_{CQ} is specified then you know what is g_m , g_m is 60 milli moh and C_{C1} and C_{C2} both are specified as 1 microfarad. You are required to find out A_o that is the mid band gain and ω_L ? Alright this is not a design problem, this is a analysis problem. Now obviously what you can do is A_o is minus beta, if you remember R_o divided by r_{π} plus R_s and you simply substitute.

Is beta given, no beta is not given, r_{π} and g_m are given, so beta must be 120, is it right? 60 times 2 is 120, k and millimoh they cancel each other 120 R_o is 4.5k parallel 9 K divided by r_{π} is given 2 (k) (47:35) in k because it will cancel 2 plus R_s is 1, so I can forget about k. What is the parallel 4.5 and 9? Oh! Its 3, so 3 by 3 this is simply minus 120 than with the given C_{C1} and C_{C2} calculate ω_{11} and ω_{12} .

ω_{11} as you know is 1 over C_{C1} , r_{π} plus R_s and ω_{12} calculate as 1 over C_{C2} R_c plus R_L and during this calculation one finds that ω_{11} comes as 333.3 radian per

second and ω_{12} comes at 74.1 radian per second. Well, this is about 5 times, is not that right? This is about 5 times this and therefore your ω_L is equal to 333.3 radian per second, alright.

This was the example of analysis, now if you want to design we will consider the design problem along with that of emitter bypass capacitor and it is at this point that we should take a 5 minute break, we reassemble at 500.