

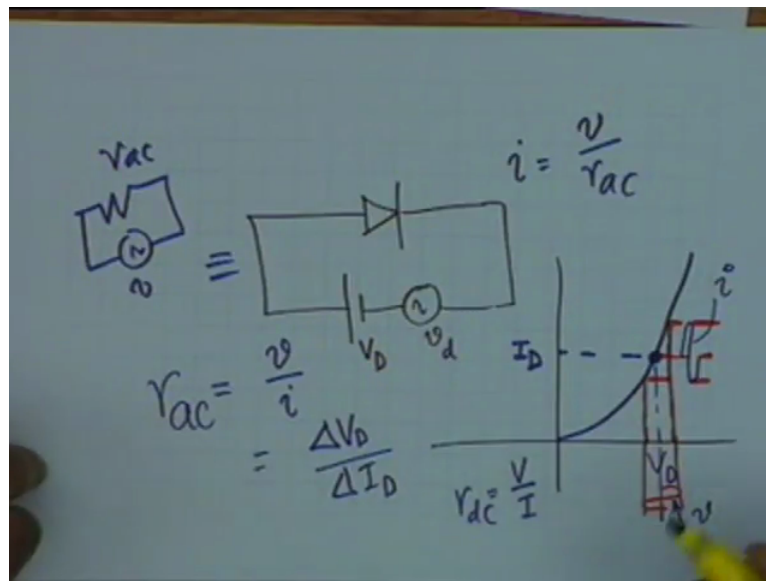
Introduction to Electronic Circuit
Prof. S.C Dutta Roy
Department of Electrical Engineering
Indian Institute of Technology Delhi
Lecture 34
Small Signal Models
& Small Signal Amplifiers

Yes, this is the 34th lecture and we are going to talk about small signal models and small signal amplifiers. The amplifiers that we have discussed in the last few lectures namely power amplifiers they basically use very large driving signals they are large signal amplifiers and that is why we have to bother about the placement of the Q point and maximum voltage and current swings because the objective there was to obtain as much power as you can from the given amplifier.

It is non-signal amplifier that is not the consideration, the consideration is a faithfulness of the fidelity of the amplifier that is whatever wave form you put at the input the same waveform should arrive at the output also; the object is either voltage amplification or current amplification but not both. We do not want power from small signal amplifiers, what you want is large voltages and large currents.

So it is not important, the Q point placement is not as important as in power amplifier. In a power amplifier you can tolerate certain amount of distortion; in fact certain amount of distortion is a fact of life, in a small signal amplifier where the fidelity or faithfulness is more important you cannot do that. We have already introduced this small signal model in the case of a diode.

(Refer Slide Time: 3:11)



If you recall, if we have a diode which is driven by a battery in series with let say an AC source of value small v . Let us say this is V_D , this is small v sub small d that is if the diode is being driven by a DC in series with a very small amount of AC then the Q point is obtained, first Q point is obtained by drawing characteristics and then ignoring this signal that is you find out the point at which v is equal to V_D than this current capital I_D , this determines the Q point the operating point and on this operating point you super impose a small signal.

Let us say this is AC then maybe the diode voltage can vary between these 2 limits, the limits drawn by the red lines, alright. Maybe the diode voltage varies like this, super imposed on a large DC where is a small voltage small v and then the current. So the diode shall also be sinusoidal and it will flow like this, alright. If you wish to find out this current i in relation to this voltage v then you know that you can work in terms of the slope of this line at the Q point.

In other words you can define that AC resistance small r_{ac} as equal to small v divided by small i which obviously is ΔV_D over ΔI_D incremental resistances and if it is imply that the diode is sitting at this Q point then given a signal you can always find the current i , the signal current i as v by r_{ac} . In other words this whole diode, this whole circuit can then be replaced by a simple resistance r_{ac} and a voltage v , we forget about the DC part, alright. This is called a small signal model of the diode, alright.

If we imply there is a diode sitting at the Q point such that it always conducts or there is a small v it conducts. What I am doing basically is to invoke linearity; we are making a linear equivalent circuit where DC and AC can be superimposed to get the total current. The DC resistance here for example r_{dc} is not equal to r_{ac} , it is simply equal to V by capital I which is quite different. V by capital I is quite different from r_{ac} , alright. DC resistance and AC resistance are quite different from each other.

(Refer Slide Time: 6:19)

$$I = I_s (e^{qV/(kT)} - 1)$$

$$\frac{dI}{dv} = \frac{q}{kT} (I + I_s)$$

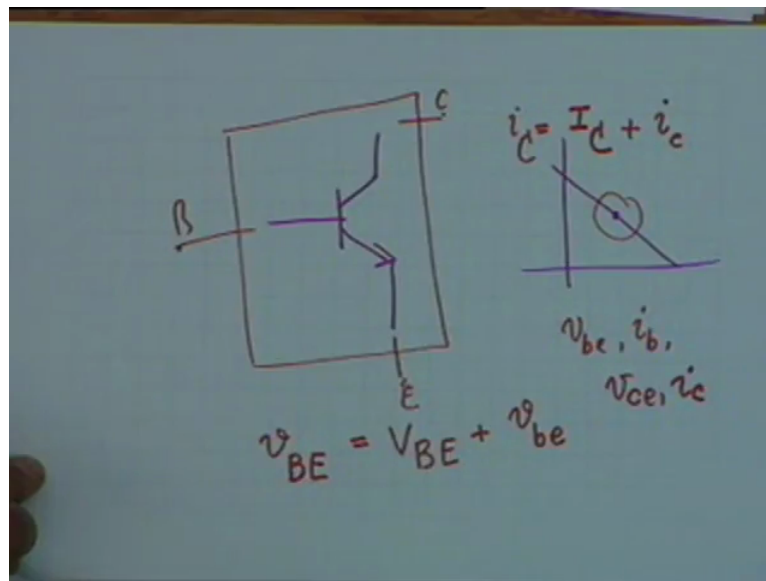
$$\approx \frac{qI}{kT}$$

$$r_{ac} = \frac{kT/q}{I} = \frac{0.025}{I}$$

For a diode for example you know that the current is given by $I_s e^{qV/(kT)} - 1$ and from this you can find out dI/dv by differentiation and if you do a bit of algebra then it simply comes out as $qI/(kT)$ plus I_s if you actually differentiate you can put it in this form which is approximately equal to $qI/(kT)$, alright. So that r_{ac} for the diode, would be given by kT/q divided by capital I , capital I is the DC current, DC Q point current of the diode and kT/q at room temperature you know this is 25 millivolts, so this is this will be 0.025 divided by capital I .

And this is an important relationship which you should be utilizing in transistor is also that is for a junction diode, for a junction PN junction, the dynamic resistance of the AC resistance is simply giving back 0.025 divided by the DC current in the diode, alright. It is related to these because we have found out that the slope of the current voltage characteristic depends on the current depends on the DC current, alright. This relation we shall be utilizing in the case of a transistor also.

(Refer Slide Time: 7:45)



Now let us look at a transistor and for the specific lessons it a common emitter transistor while you know we have to use DC, you have to use power supply VCC, we have to use resistances to bias the transistor properly and you know we have to determine a Q point at the middle of the load line to make maximum possible swing and all that.

Now for maximum linearity also the characteristics are maximal linear near the middle of the characteristics at the saturation point or at the end they become curved. So let say we had a Q point, now we want to operate around this Q point. We want to operate around this Q point that is at this Q point there is a certain value of IB base current we want to superimpose an alternating current on this and find out what is the corresponding change in the collector current? And we have seen that there is current amplification, alright?

So let us say we enclose this within a box, alright. And we have 3 terminals the collector, the emitter and the base and you see this is a 3 terminal method or 2 port networks which can be characterized in various different ways, this characterization is a small signal categorisation. In other words if you are talking of let us say and this pointy the voltage between this point.

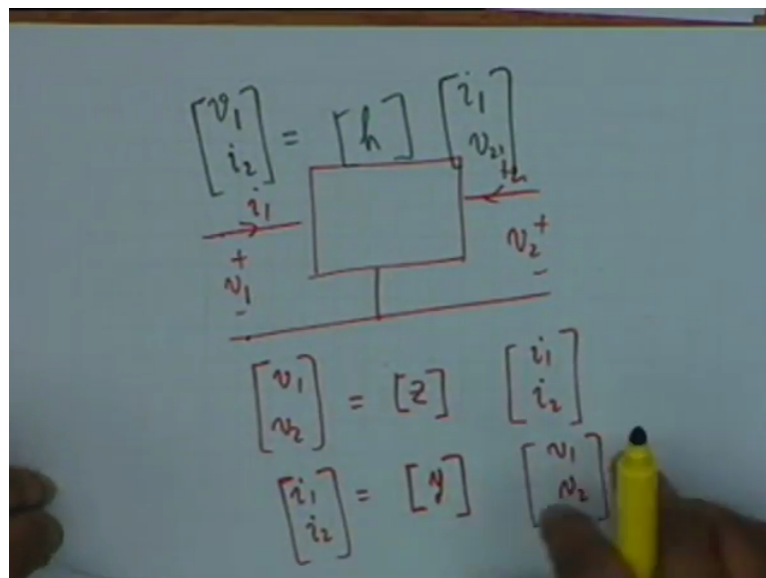
That the total voltage is small v subscript capital B capital E this notation I have explained earlier, let me repeat. The total voltage between base and emitter a small v subscript capital B capital E and this is a sum of a DC and AC, DC and an incremental value, the DC value we shall see V_{BE} capital V sub capital B capital E plus small v subscript small b small e, alright. This is the way we are going to represent every quantity.

The collector current for example, the total collector current would be i_C this is equal to I_C this is the DC value plus the incremental value which you shall represent by i_c for all such currents and voltages. The problem now, we know how to bias that, we know how to put the transistor at a particular we know how to choose the resistor, we know how to stabilise the bias point.

The next question is if you are concerned with small signals which do not drive the transistor to its limits, alright. That is maximum dissipation is not (()) (10:37). How do we characterize the transistor? Is there a simple way of doing it? Yes, we treat the transistor as a linear device, alright. For small signal purposes it is absolutely linear and therefore DC and AC quantity can be divorced from each other.

And therefore we recall, what we do is, we relate the voltages v_{be} that is the current going into the base, this is the signal current then v_{ce} that is the voltage from collector to emitter this small signal voltage and i_c as the 2 port variables there are 2 voltages and 2 currents and you know that the any 2 port can be characterized in 6 different ways. I repeat this characterization which we are talking of for the transistor is for incremental quantities only, small signals only we are divorcing DC from the picture altogether, is that clear? Okay.

(Refer Slide Time: 11:51)



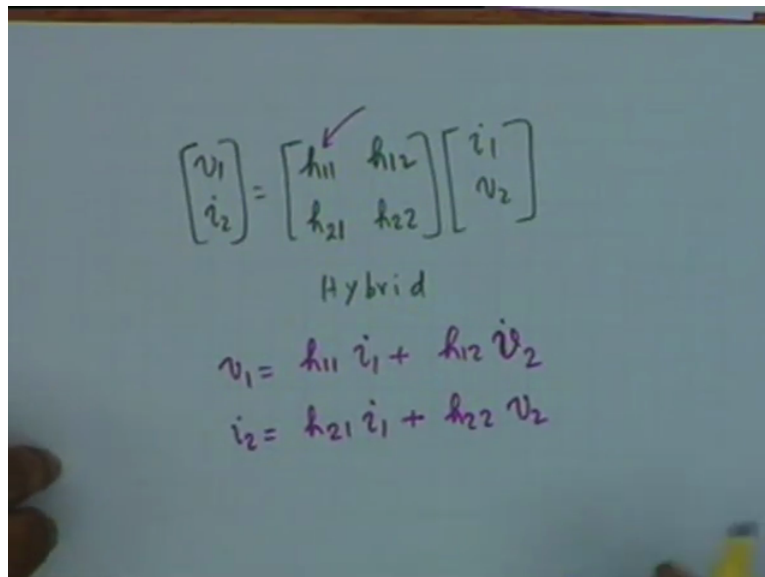
If we do that then you see any 2 port device which has 3 terminals. Well, we see this is v_1 i_1 in general, v_2 i_2 you know that we always use currents wave in v_2 i_2 and you know that this can be characterized in 6 different ways, if we take v_1 and v_2 as dependent variables and i_1

and i_2 as independent variables then the parameters are the so-called z parameters as (12:23) circuit impedance parameters.

On the other hand if I take i_1 i_2 as the dependent variables and v_1 v_2 as independent variables then the parameters that come into effect short circuit admittance parameters or small y parameters. There is third way which is been found very effective for transistors and these are the hybrid parameters that is your dependent parameters are v_1 and i_2 .

Dependent parameters is a combination of one voltage and one current, the input voltage v_1 and output current i_2 these are expressed in terms of i_1 and v_2 , i_1 and v_2 are made the independent variables and naturally the parameters shall no longer be impedance or admittance there will be a combination, is that clear? And this is where they are called hybrid. They are one of them is in impedance, one in an admittance and the other 2 as you will see a dimensional less and therefore they are represented by the h matrix, h stands for hybrid, alright. It is always the input voltage output current v_1 i_2 expressed in terms of i_1 and v_2 , it is the other the (13:56), alright.

(Refer Slide Time: 14:20)



The image shows a whiteboard with handwritten mathematical equations. At the top, a matrix equation is written:
$$\begin{bmatrix} v_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ v_2 \end{bmatrix}$$
 Below this, the word "Hybrid" is written. Underneath, two equations are written:
$$v_1 = h_{11} i_1 + h_{12} v_2$$

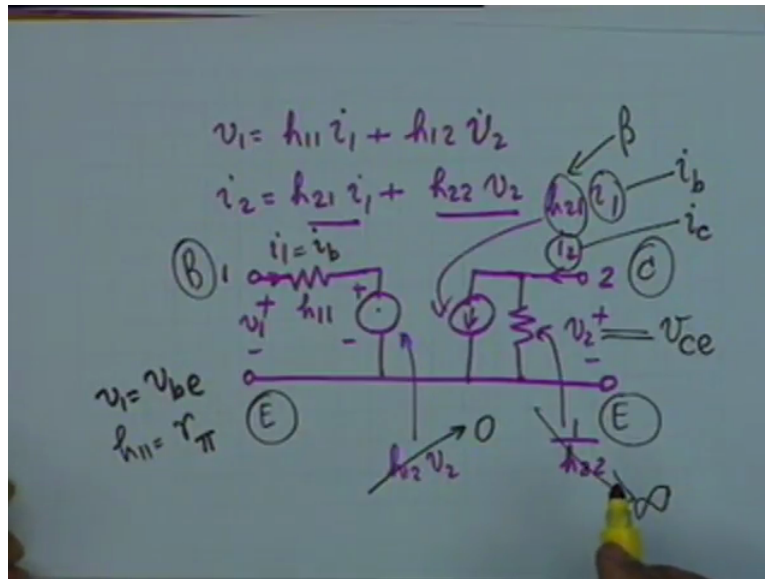
$$i_2 = h_{21} i_1 + h_{22} v_2$$

If we expand this relation, let me rewrite v_1 i_2 is the h parameter i_1 v_2 this parameters are named in the same manner that means recall h_{11} , h_{12} first row first column is h_{11} , first row second column h_{12} , second row first column h_{21} and h_{22} and these are called hybrid parameters, hybrid, H y b r i d. You can see very clearly that h_{11} for example, how would you define h_{11} ? h_{11} is v_1 divided by i_1 with v_2 equal to 0, alright.

If I write this specifically $v_1 = h_{11} i_1 + h_{12} v_2$, alright. $i_2 = h_{21} i_1 + h_{22} v_2$ then you notice that h_{11} is simply v_1 by i_1 with v_2 equal to 0 which means that this is an h_{11} has the dimension of impedance. Similarly you can see that h_{22} is an admittance whereas h_{12} , h_{12} is v_1 by v_2 with i_1 equal to 0 and therefore h_{12} is dimension less it is a voltage ratio and h_{21} is a current ratio and it is dimension less and therefore these are called hybrid parameters. In terms of an equivalent circuit you see that we can represent these relations.

What are these relations? $v_1 = h_{11} i_1 + h_{12} v_2$ and $i_2 = h_{21} i_1 + h_{22} v_2$, we can represent this in a very simple manner as a 2port, this voltage is v_1 and this current is i_1 , this voltage is v_2 and this current is i_2 and if you notice v_1 is $h_{11} i_1$ and therefore I shall have a resistance here for impedance which has a value of h_{11} , let us talk of resistive elements to start with.

(Refer Slide Time: 16:54)



v_1 is equal to $h_{11} i_1$ plus we want a coupled term, coupled, v_1 is now coupled to v_2 the other curb voltage through a term $h_{12} v_2$ and the simplest way is having voltage generator here whose value is $h_{12} v_2$ what would you call this voltage generator? It is a dependent generator. This voltage depends on v_2 and therefore this is a controlled source of dependent voltage source.

In a similar manner i_2 has 2 components 1 is $h_{22} v_2$ which means that this is v_2 which means that i_2 has 2 components, one flows through a resistance value 1 over h_{22} , not h_{22} , 1 over h_{22} , so that h_{22} is its admittance. So $v_2 h_{22}$ is the current and the other current is $h_{21} i_1$, once again can be represented by current generator, a dependent current generator. A current controlled current source this is $h_{21} i_1$, alright.

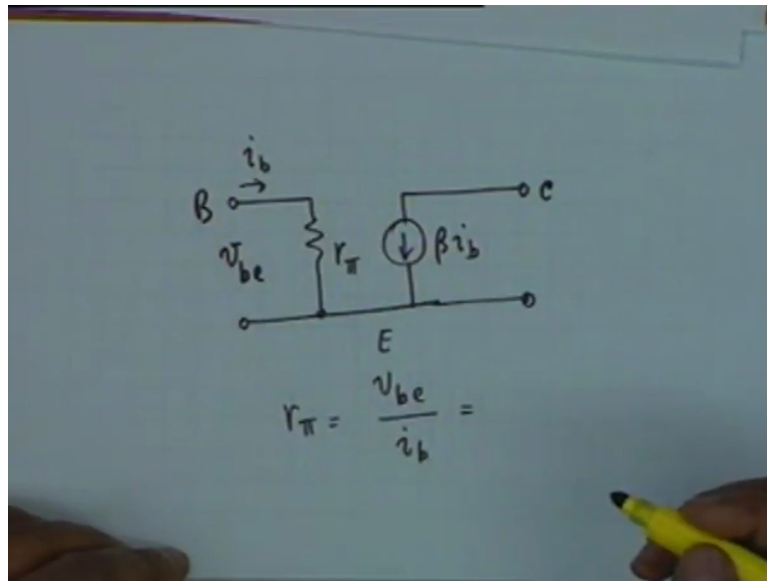
Now in a transistor if the terminal one is a base, terminal 2 is a collector and the common terminal is the emitter, this is emitter then you see v_1 is nothing but v_{be} , alright. v_1 is nothing but v_{be} , h_{11} , what is h_{11} then? It is dynamic resistance of the forward biased emitter base junction between base and emitter there is a junction, so h_{11} is resistance of the forward biased emitter base junction.

So h_{11} is represented as r_{pi} the subscript pi shall be clear a little later. h_{12} is usually a very small quantity 10 to the minus 3 is a typical value and therefore we usually ignore this, alright. h_{12} is usually ignored similarly h_{22} is a very small quantity, so that this resistance is very large and therefore this resistance also, yes, should be put equal to infinity.

That is this resistance one can do without, alright. And h_{21} can recognize what h_{21} is? What is i_1 ? i_1 is simply i_b the base current and therefore this i_1 is i_b then what is h_{21} ? It must be beta, h_{21} is beta, i_1 is i_b and i_2 is i_{c} the collector current and v_2 shall then be equal to v_{ce} , alright. With these simplifications therefore we get a simplified equivalent circuit of the common emitter transistor.

Note that the simplifications have been done under 2 conditions, one is that this control source can be ignored because h_{12} is a small quantity, this resistance can be ignored because h_{22} is a small quantity, alright. h_{12} and h_{22} both tend to 0, it is only under that condition that we have an equivalent circuit just one resistance and one controlled current source, alright.

(Refer Slide Time: 20:54)

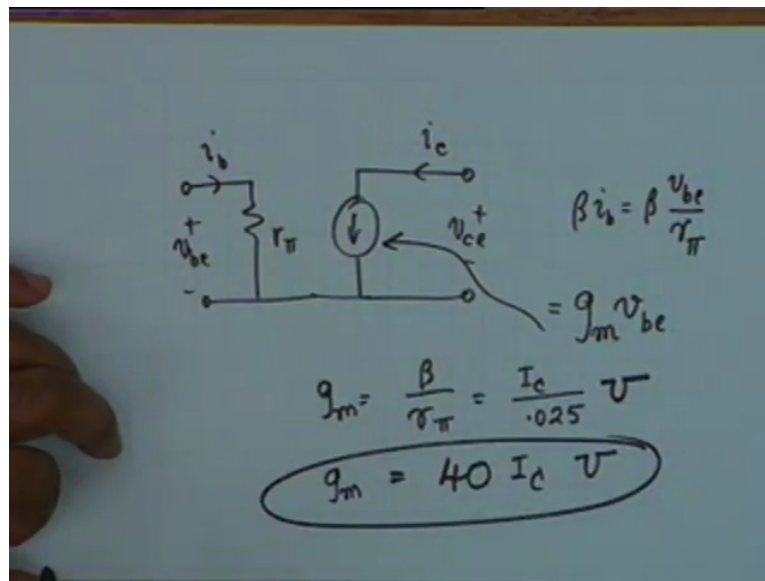


Beta i_b and therefore my equivalent circuit simply becomes r_{π} , this is v_{be} , this current is i_b and we have βi_b that is it. This is the collector, this is the base band this is the emitter, this is the equivalent circuit of the common emitter transistor. Well, you can find out what r_{π} is? r_{π} as I said is the dynamic resistance of the forward biased diode and therefore r_{π} shall be **it is** it is clear it is v_{be} divided by i_b , alright. And you know what this is?

This is as we had already found out 0.025 divided by capital i subscript capital b where is the DC value of the base current. Usually this is written in terms of the collector current, this relationship is written in terms of collector current, so if I put i_c here, naturally I should multiply this by β , β times 0.025 divided by i_c , this is the value of r_{π} and you see r_{π} depends on the Q point, r_{π} depends on the collector current at the Q point, alright.

Beta of course is the, beta is h_{21} , now this beta is slightly different from DC beta, this beta is AC beta, this beta is i_c divided by i_b that is it is the ratio of incremental collector current incremental base current, alright. And this beta is slightly different from the DC beta which is i_C divide by i_B for very obvious reasons. It depends on a slope the other one depends on the total quantities. Nevertheless the values are very close to each other, alright.

(Refer Slide Time: 23:16)

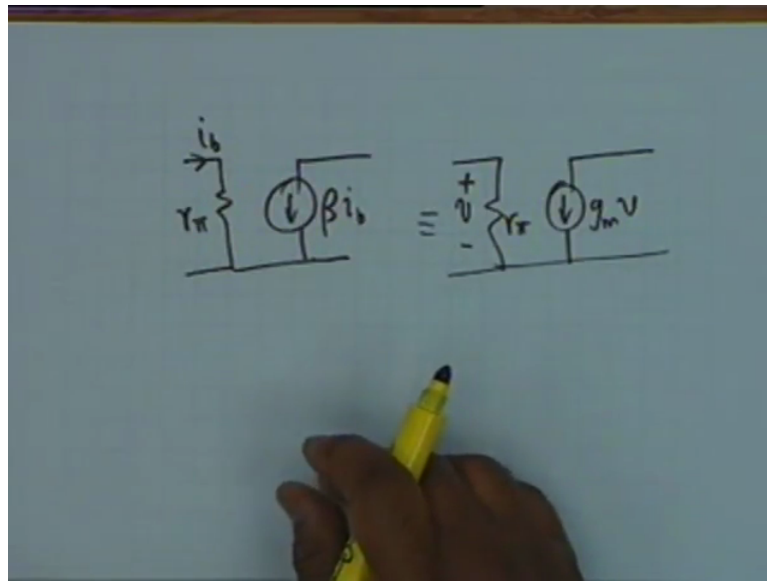


Now I want to represent this equivalent circuit it is so important that one has to draw it again and again. I want to represent this equivalent circuit in a slightly different form $i_{sub b}$, $v_{sub be}$ and $v_{sub ce}$ this current generator is $\beta i_{sub b}$ and I can write this as $\beta i_{sub b}$ can be written as v_{be} divided by r_{π} , alright. And therefore I can write this as, what would be the dimension of β by r_{π} conductance and therefore I represent it by g_m . g_m stands for transconductance or transfer conductance.

It is transferred because; well I represent this as $g_m v_{be}$, okay. This is a current generator which can be represented by $g_m v_{be}$ the current here depends on the voltage here and therefore it is a transfer conductance or transconductance. The value of g_m as you can see is β by r_{π} and if you recall what r_{π} was? You simply see that this is $I_{sub C}$ divided by 0.025, alright and the unit is (A/V) (24:45). 1 by 0.025 is approx is exactly 40 therefore this is extremely nice relation for 40times $I_{sub C}$ (A/V) (24:55) and this is what is used in practice rather than r_{π} rather than β .

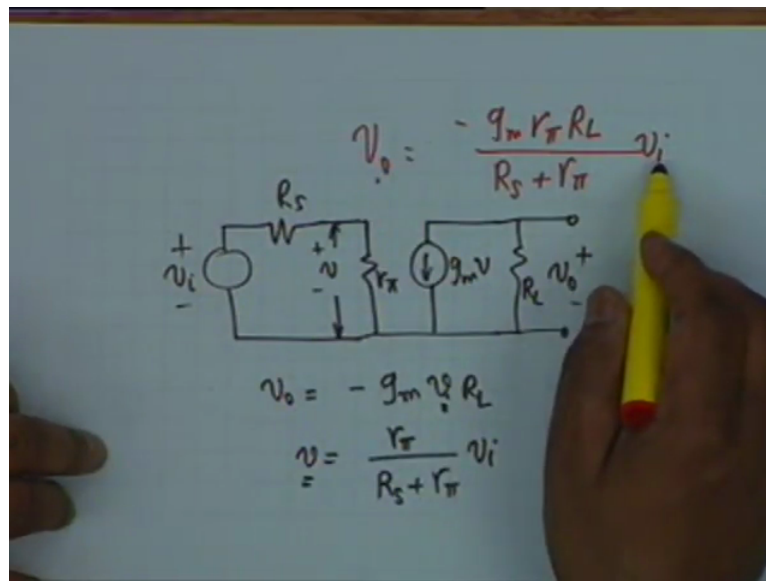
It is convenient to use g_m because it is very easy to calculate g_m , it is very easy to remember that g_m is simply 40 times $I_{sub C}$. For example if $I_{sub C}$ is 2 milliamperes then g_m would be 0.8 mA/V. Is it okay? 0.8 mA/V, no it is 0.08, 0.08 mA/V, alright.

(Refer Slide Time: 25:32)



So we shall use either of these 2 circuits one is called the r_π beta circuit βi_b , this is i_b equivalent second of the transistor or the same circuit represented like this, we shall use this as small v , it is v_{be} actually and we shall represent this as $g_m v$ this is your circuit, alright. They are absolutely equivalent to each other. Suppose now we make an amplifier, we make amplifier.

(Refer Slide Time: 26:12)



The most elementary amplifier that is we have a that is v_i , perhaps we can include a source resistance R_s then of course we have the DC bias let say V_{BB} , is the polarity correct? The base should be positive with respect to emitter, this is a PNP transistor and suppose in the collector circuit we have a load R_L and the collector biasing supplier minus plus and this is V_{CC} , this is our elementary amplifier and we want to know, what is the signal voltage across R_L ?

It is elementary amplifier; we wish to know what is the gain of the circuit? What is the amplification of this circuit? Alright? What we will do is, we will place this transistor and its associated DC biases by the incremental equivalent circuit and then calculate the ratio of this signal at the output to be signalled at the input and as you will see this would be extremely easy we do not have to refer to the characteristic curves at all, alright.

We shall do simply in terms of the equivalent circuit. What I do is, I divorce all the DC quantities $v_i R_s$ then between emitter between the base and the emitter I have simply r_{π} and this voltage I call v alright. Then I have g_m and v at the collector, what else do I have? Simply R_L , alright. The load R_L and this would be my output voltage v_o .

Easily see that the output voltage v_o is simply minus $g_m v$ times R_L , why is the negative sign? Because the current flows like this, the voltage clarity is positive and negative down, alright. So if I can find what v is? If I can relate v to v_i then I shall know what is the ratio of the output voltage to the input voltage and you can see that small v is nothing but r_{π} divided by R_s plus r_{π} times v_i .

So if I substitute this value of v in this relation then I get v_0 , let me use a different colour, v_0 I get equal to minus $g_m r_{\pi} R_L$ divided by R_s plus r_{π} times v_i therefore the gain of the circuit or the amplification of the circuit which is given by v_0 by v_1 will be simply equal to.

(Refer Slide Time: 29:27)

The image shows a handwritten derivation of the voltage gain $A = \frac{v_o}{v_i}$ for a common-emitter amplifier. The derivation is as follows:

$$\frac{v_o}{v_i} = - \frac{g_m r_{\pi} R_L}{R_s + r_{\pi}}$$

$$= - \frac{\beta R_L}{R_s + r_{\pi}}$$

Below the equations, the following values are substituted:

- $\beta = 100$
- $R_L = 1K$
- $R_s = .5K$
- $r_{\pi} = 1.5K$

The final calculation for the gain A is shown as:

$$A = \frac{-100}{2} = -50$$

v_0 by v_1 the gain of the circuit will be equal to minus $g_m r_{\pi} R_L$ divided by R_s plus r_{π} , what is $g_m r_{\pi}$? Beta and therefore this is minus beta R_L divided by R_s plus r_{π} . What is the significance of the negative sign here? Phase shift, the output voltage is out of phase with the input voltage and this I have explained again and again that an increase in input voltage causes an increase in the collector current and an increase in the collector current leads to reduce the value of collector voltage V_{CE} and therefore there is a phase change and this is reflected with the minus sign.

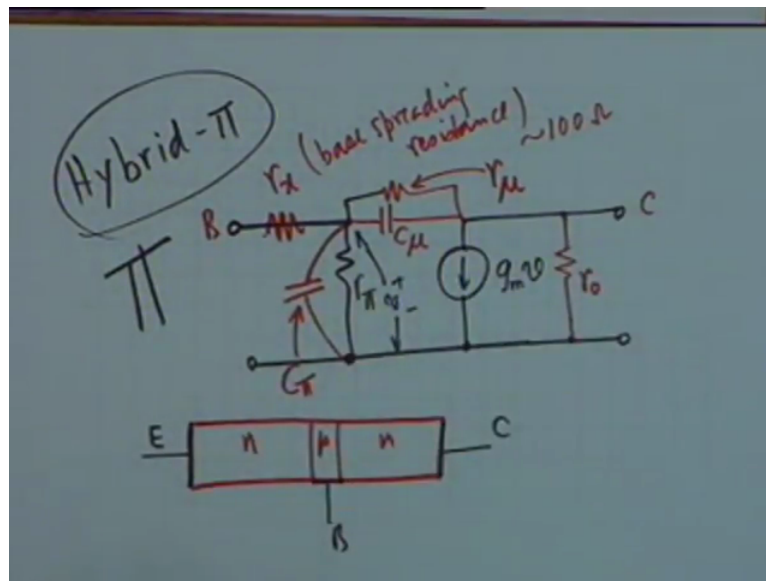
And this ratio has to be dimension less because it is the ratio of 2 voltages. Typically for example you may have a beta equal to 100, R_L can be let say 1k, R_s we would like to be as small as possible, let say this is 0.5k and r_{π} maybe of the order of let say 1.5k, alright. Then you say that the gain which is usually represented by the letter A standing for amplification, for this typical circuit it is minus 50 divided by 2 that is equal to minus 25, beta is hundred, okay. So this should be minus 50.

In other words if you put 1 millivolt at the input, 1 millivolt peak then you get at the output voltage which is 50 millivolt peak, alright. And if you say higher beta transistor or you can reduce R_s you can get a higher gain. A gain can be increased to there is an upper limit but it

can be increased to a useful value. For example you have a signal from maybe a process instrumentation of the order of let say microvolt which not be read by a meter, alright.

A microvolt meter is a very costly equipment, so what you do is, you put an inexpensive amplifier in between and erase it to 100 micro-holes, alright. Then you read 100 micro-holes is how many millivolts, 0.1, there are millivolt meter fractional millivolt meters and so on or maybe you want to lose this to drive a power amplifier. For example in the in the (()) (32:03) system, a microphone amplifier the microphone signal does not go directly to the power amplifier there is something called the preamplifier. Now what preamplifier does is simply to raise the voltage level, so that it can drive the power amplifier stage to its complete capability, alright. So that is the basic idea of amplification.

(Refer Slide Time: 32:38)

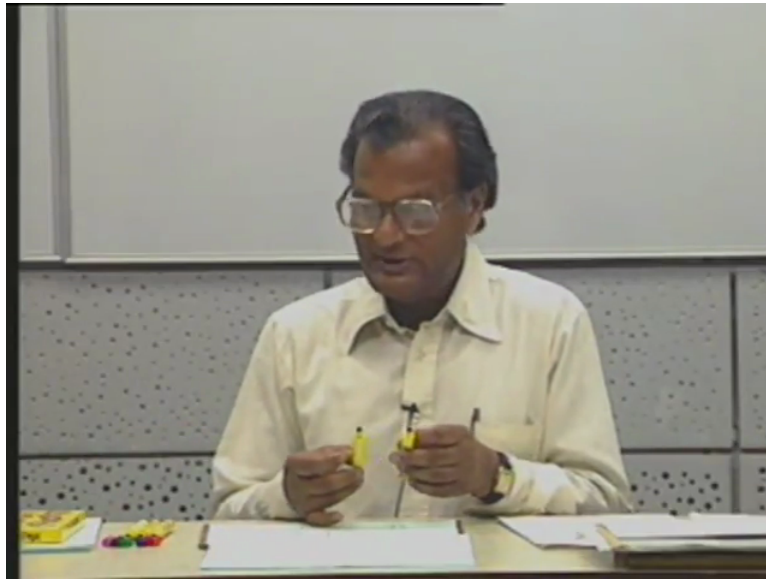


Now let us go back to this r_{π} beta model, r_{π} m plus $g_m v_{\pi}$ model and see as I said this is a very simple model, there are some modifications needed to take care of elements, to take care of performance at high frequencies in particular and this is a very gross model to sharpen the model we require several modifications. One is if you recall this structure, if you said npn transistor, np there is a connection here, which is the emitter, there is a connection here which is the collector, there is a connection here which is the base.

The base as you see is a thin long region and between the actual conduct of base and the base emitter junction or base collector junction there is a certain amount of resistance sometimes plays havoc and this resistance is called the base spreading resistance and it is denoted by r_x which is called the base spreading resistance. This happens because of the thin and round nature of the base.

The base spreading resistance a typical value is of the order of 100 ohms. A typical value for r_{π} that is the dynamic resistance of a base emitter junction of the orders of typical values about k. So r_{π} is usually 1 order of magnitude higher than r_x and in most of our analysis we shall neglect r_x , alright. The between the base and collector but there is a junction, what kind of biasing is there in this junction? Reverse biasing.

(Refer Slide Time: 34:59)



And therefore in a reverse biased junction, as you know there is a separation of charge, alright. This operation with reverse biased increases and therefore this acts as a capacitor which means that between these 2 points we should have a capacitor and this capacitor is given the impulse C_{m1} , the capacitor between the base and the collector C_{m1} . Unfortunately it is not a pure capacitor, there is also a conduction current and this conduction current is usually represented by a resistance in parallel (r_{m1}) (35:29) C_{m1} and it is called r_{m1} , alright. r_{m1} , r_{m1} is usually very large of the order of several (r_{m1}) (35:40) and in an usual circuit considerations r_{m1} can be ignored compared to $1/\omega C_{m1}$.

At high frequencies when C_{m1} comes into consideration it dominates that is one way ωC_{m1} is much smaller compared to r_{m1} , so r_{m1} can usually be ignored, alright. In addition you know the base emitter junction also contributes to a capacitor, alright. The base emitter junction also there is any separation charges, so there is a capacitance here also and this capacitance is called C_{p1} . The capacitance in parallel with r_{p1} is called C_{p1} , alright. Between the collector and emitter if you connect the battery a small current does flow and this current is taken care of by a resistance r_0 .

All that I show in red here are not desirable, they are all undesirable elements they are called parasitic elements. Unfortunately however parasites are facts of life and I has to take care of them, alright. Whether in public or in politics or in electronic circuits parasites are facts of life, okay. Now so in our infernal amplifier analysis at, yes.

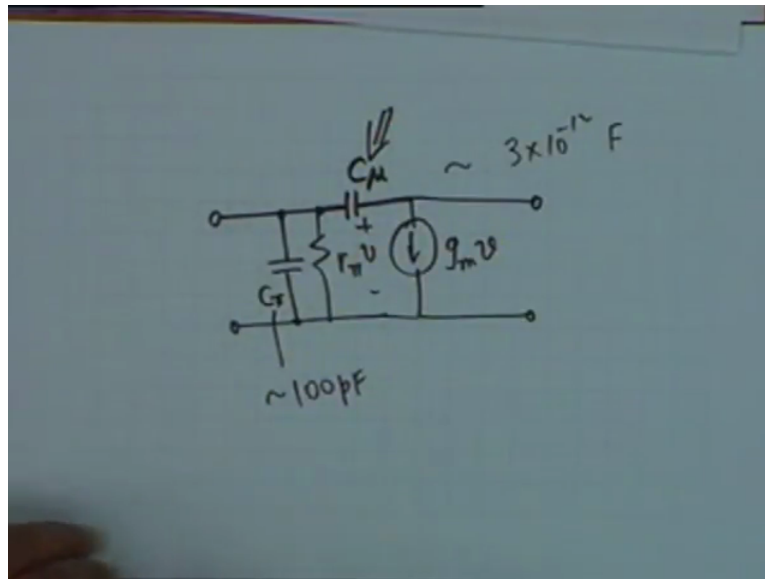
“Professor -Student conversation starts”

Student: Sir, what is v ?

Professor: Oh! What is v ? We is this voltage, I forgot to mention this v is the voltage across r_{pi} . This is why you prefer this model not only because g_m is very easily calculate it 40 times i_c but also because it does not take account of the current division, you see the i_b comes here it divides into one part, two-part, 3 and 4 parts we did not take care of the current we take care of the voltage and $g_m v$ this is the most accepted and the most general model of common emitter transistor.

And you see the model looks like π , you see it looks like a π and therefore it is called a hybrid π model of the transistor. It originates from the hybrid parameters h_{11} or h_{12} , h_{21} , h_{22} . We first went through a simplification and then brought back all the parasites and it looks like a π and therefore it is called a hybrid π model.

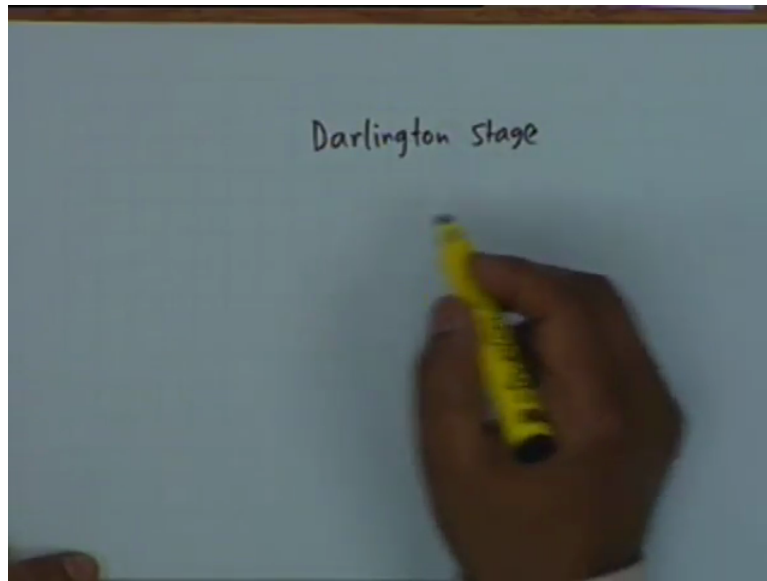
(Refer Slide Time: 38:37)



For the purpose of this course and for the rest of the lectures we shall be satisfied with a simplified model, we shall ignore r_x and therefore what we will have is in an r_{pi} , in parallel it is C_{pi} and this voltage is v then I shall have current generator of $g_m v$ and very unfortunate this capacitor C_{mu} is inferior very small capacitor of the order of 3 pugs that is 3 times 10 to the minus 12 farad.

C_{pi} is of the order of 100 pugs about 30 to 40 times larger, even than because of this voltage control current source C_{pi} can cause havoc am sorry C_{mu} , C_{mu} can reflect an input and can even swamp C_{pi} that means affective value of C_{mu} reflected across the input much larger than C_{pi} and therefore c_{mu} has to be considered in practice. We take an example to illustrate the usefulness of the model and this example is the so-called Darlington amplifier, Darlington it's a name.

(Refer Slide Time: 40:15)



Darlington stage as it is called. What is Darling? Is the following, you have common emitter stage, not common emitter common collector, the collector is connected directly to VCC and you apply an R_s and v_s here, this is the source I am not showing the V_c biasing I am only showing the incremental quantities or the signal quantities, alright. This emitter instead of going to ground goes to the base of another transistor, alright.

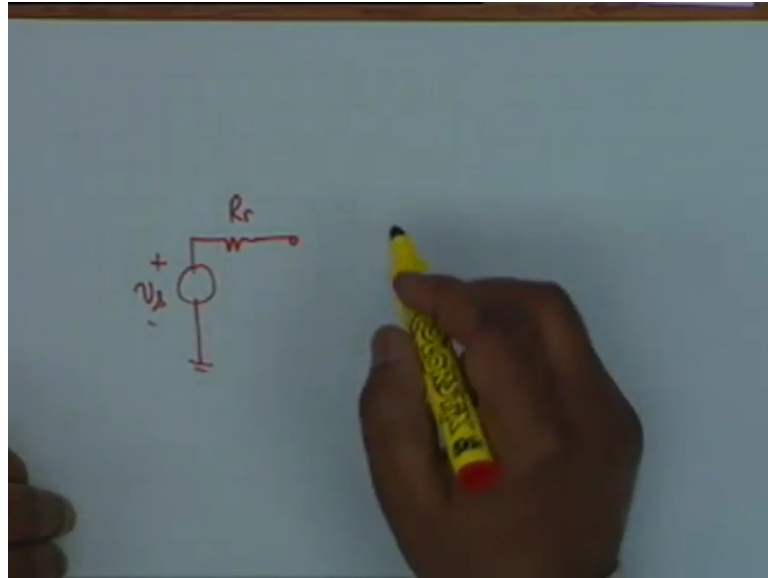
And the collector of which is connected to the same VCC, okay. Then this goes to ground through a resistance $R_{sub E}$ and it is across $R_{sub E}$ that you take the output voltage v_0 I am not showing the DC quantities I am showing only AC quantities, alright. Across this you take v_0 , we will see what in effect as it has that instead of a single transistor emitter follower as I have introduced last time in 23rd lecture.

A single transistor is not replaced by 2 transistors, the emitter current of 1 becomes the base current of the other and you can expect that there would be a very large current amplification. The current amplification would be very grossly you can see that the emitter current would be better plus one times the base current and this emitter current will be $\beta + 1$ times this base current and therefore the current amplification should be $\beta + 1$ times $\beta + 1$ times $\beta + 1$.

If this transistor you call Q1 and this you call as Q2 this is what will happen and this is what indeed happens you see if you have β_1 is 100 that approximately this is 10 to the power 4. A single transistor you get β of 10 to the power 4 cannot be fabricated and therefore this is

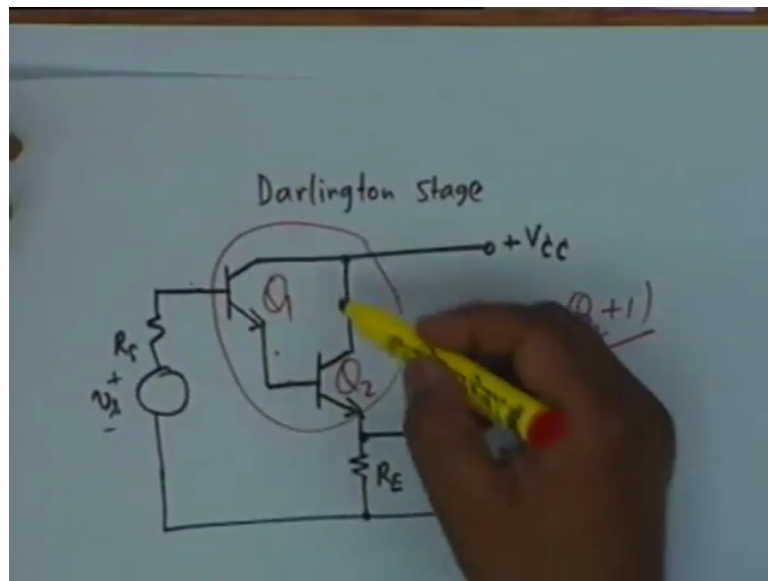
a way to have a high beta equivalent of a high beta transistor. If I draw the equivalent circuit then I will leave the rest of the analysis to you.

(Refer Slide Time: 42:57)



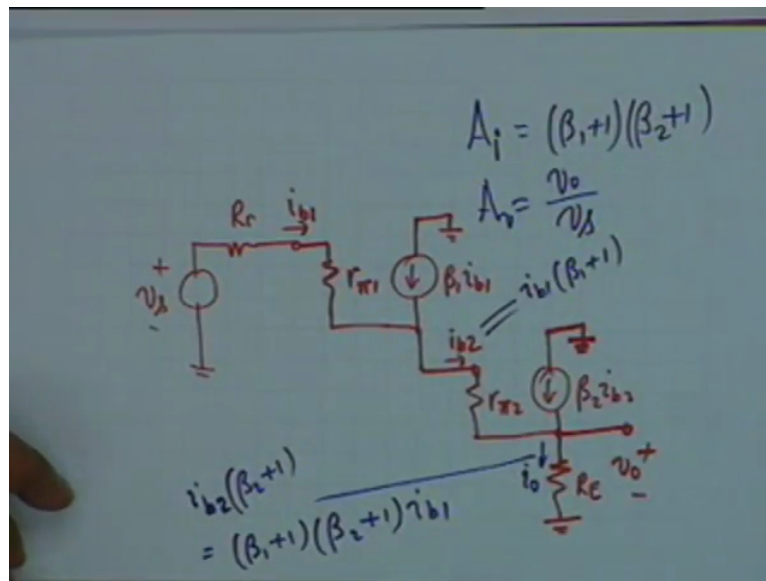
If I draw the equivalent circuit I have v_s in () (42:53) with R_s then for Q1 I have r_{pi} , alright. And I have β , if this current is I_{B1} I have βI_{B1} , where does this go? This point is the collector.

(Refer Slide Time: 43:20)



This point this is the collector, the collector is connected to VCC therefore it is equivalent to going to ground.

(Refer Slide Time: 43:30)



And therefore this goes to ground. Now this current whatever the current is goes to the second transistor B2 and we have r_{pi2} . So this current is i_{b2} and then we have $\beta_2 i_{b2}$ the 2 come together, where does this go? Ground once again and then this current now flows to $R_{sub e}$ and this is the circuit is v_o , this is the equivalent circuit and you can very easily analyze this just by looking just by commonsense.

You see that i_{b2} is simply i_{b1} times $\beta_1 + 1$ and therefore this current is i_{b2} times $\beta_2 + 1$ and therefore this is $\beta_1 + 1$ $\beta_2 + 1$ i_{b1} this current, this current is this current generator plus the current here, alright. So indeed you see that if I call this current is i_o the current through the load then i_o and current should be source is i_{b1} and therefore the current application A_i simply equal to $\beta_1 + 1$ $\beta_2 + 1$ is I have indicated from commonsense, alright.

“Professor -Student conversation starts”

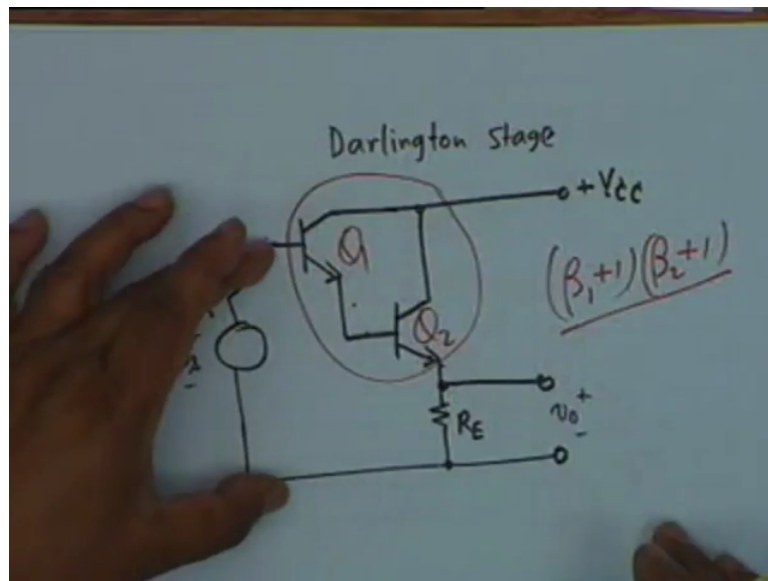
Professor: If you are going to calculate v_o by v_s that is the voltage gain A_v will be equal to v_o by v_s , what is your guess? What should be the voltage gain? Can the voltage gain be greater than 1?

Students: No.

Professor: No, it would be slightly less than 1 in fact, alright.

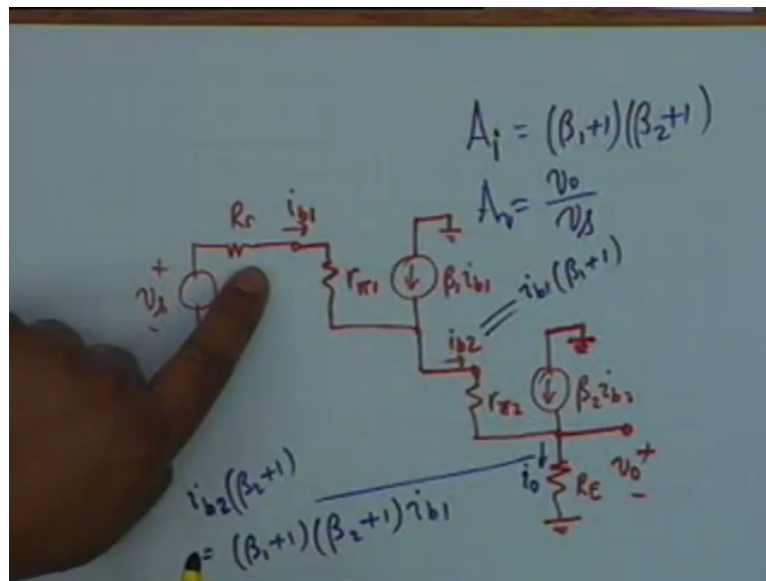
“Professor-Student conversation ends”

(Refer Slide Time: 45:39)



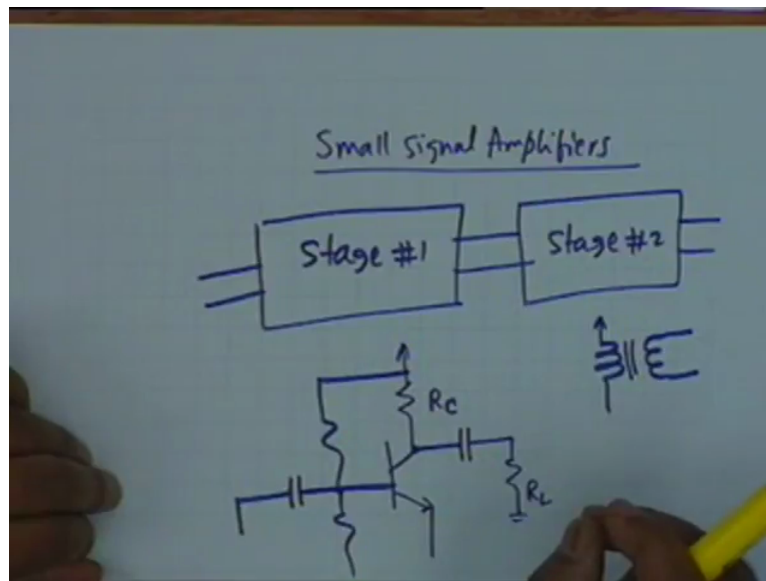
If you look at this circuit, you see this voltage minus v_{be1} minus v_{be2} is this voltage and for AC this voltage should be exactly equal to the AC of this voltage which means that the voltage gain should be equal to 1.

(Refer Slide Time: 46:01)



But because of R_s the voltage gain is slightly less than one because what we apply here is not v_s it is slightly less than one. The advantage however, if you recall another advantage besides the current gain is that it gives a very high input impedance, the input impedance is very high. You can derive what the input impedance is, that is find out this voltage from here to ground and divide by i_{b1} that will give you the input impedance, input impedance is very high and this is called Darlington stage, a very popular stage in integrated circuits. In integrated circuits all input stages are Darlington stages, so that you get the benefit of a very high input impedance, alright.

(Refer Slide Time: 47:11)

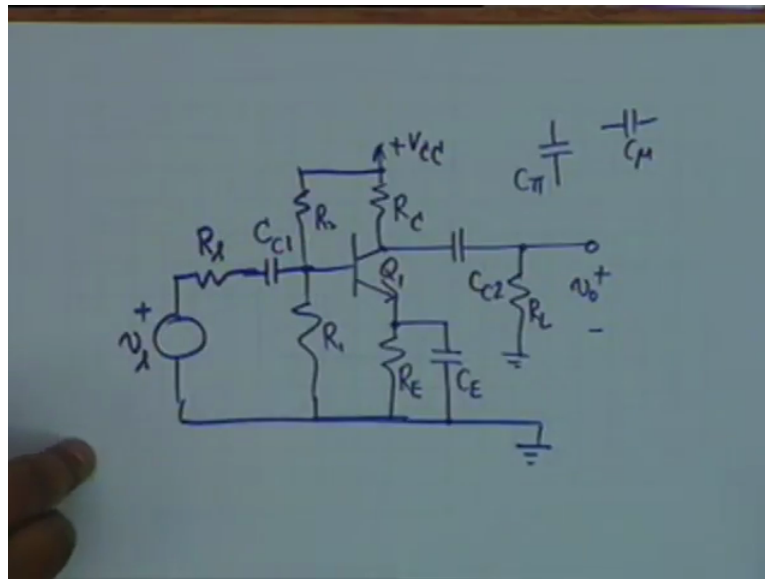


This is the model that we are now going to utilize to analyze small signal amplifiers and we shall introduce a couple of terms in this connection and then leave it for tomorrow's class. A small signal amplifier usually is classified according to the coupling that one makes from one stage to another. Stage 1 to stage 2, when 1 transistor is not enough for gaining you may have to use multiple transistors and the way stage one is connected to stage 2 is technically called coupling which is obvious.

It could be stage 1 to stage 2 or stage 1 to the load for example, okay. Usually the load is to be coupled, load is to be decoupled from DC and therefore use a capacitor and then the load, okay. Maybe this is R_L and this is R_c , this coupling stage 2 can be simply be load or can be another stage in amplifier, okay. For example the input stage also, input connection you know that even a biasing circuit like this and how do you connect the input through a capacitor?

Alright, so coupling to the transistor either at the load side or at the input side depending on what kind of coupling you imply? We call it by different names, for example this is called R_c coupling resistance capacitance coupling. On the other end you have (()) (48:44) in power amplifiers can coupled to the load through a transformer, this is called a transformer coupled amplifier, alright.

(Refer Slide Time: 49:01)



And a simple small signal amplifier that we shall analyze in great details next time is the most familiar circuit in which there is one transistor Q_1 , it is coupled to the load through a capacitor C_{RL} , the base is biased to R_1 and R_2 this is called the self biasing circuit and the input is coupled through let us say R_s and v_s our purpose will be to determine the voltage v_o in terms v_s and that will determine the gain.

The capacitors I made a mistake in this, this resistance R_E by means of a capacitor (()) (50:02) called C_E . There are 3 capacitor is, the first capacitor, if these 2 capacitors are coupling capacitors, this capacitor couples the source to the transistor, this capacitor couples the load to the transistor which is called C_{C1} coupling capacitors 1 and this is called C_{C2} . This capacitor is called C_E because it decouples the AC from R_E .

No AC is (()) (50:35) R_E , AC passes through C_E . Next time we shall see the effect of this 3 capacitors and also the capacitor is C_{pi} in the transistor model and C_{mu} by taking a specific circuit and analyzing it, thank you..