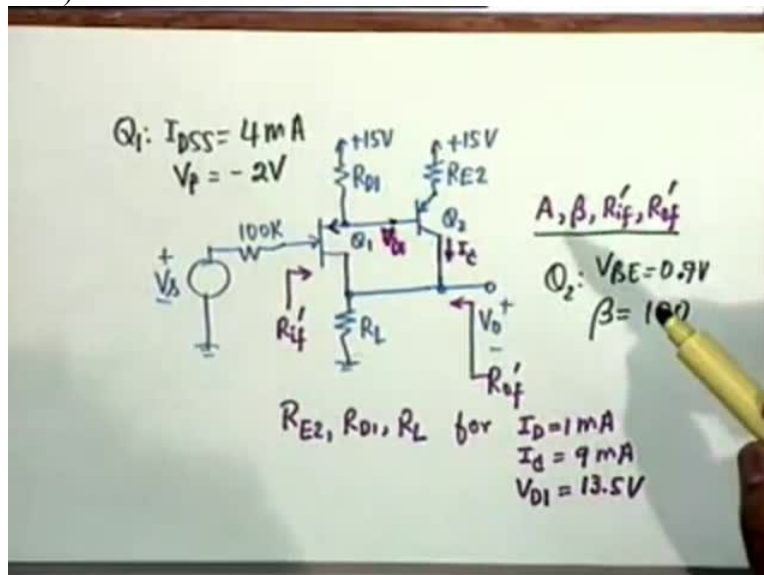


**Analog Electronic Circuits**  
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**Module No 01**

**Lecture 33: Problem Session-8 on Feedback Amplifiers**

The 1<sup>st</sup> problem that we tackle, these problems are on feedback amplifiers. The 1<sup>st</sup> problem is the following.

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We have a source,  $V_S$ . I have chosen 4 problems to illustrate the 4 different kinds of feedback architecture. The source resistance is 100 K and to bring variety into experience, we have a fet, FET goes to + 15 volts and the resistance is  $R_{D1}$  okay. It is not specified. And then the output of this is directly coupled to a BJT all right? It is an FET-BJT combination and the BJT is also not npn, it is pnp and the source is the supply is the same, 15 volt. There is a resistance  $R_{E2}$ .

Do you understand why it is + 15? Because it is connected to the emitter and this is the emitter resistance, not the collector resistance okay. It is very easy to make a mistake and therefore we should be careful. This is  $Q_2$ , we call this as  $Q_1$ . The source and the collector are connected together and there is a resistance to ground here which is  $R_L$ . What you have to find out is, the output is taken from here,  $V_O$ . This is the circuit. It is a somewhat unconventional circuit.

What you have to find out is the input impedance here. Call this  $R_{if}$  prime. You have to find out  $A$ ,  $\beta$ ,  $R_{if}$  and  $R_{of}$ .  $R_{of}$  prime is this. Okay. In addition, you have to find the resistor values, that is you have to find  $R_{E2}$ ,  $R_{D1}$  and  $R_L$  such that  $I_{D1}$  for  $I_{D1}$ , that means this current, the DC drain current of the transistor Q1. It is not the same as the current through  $R_{D1}$ . You must not make that mistake because that is a base current here okay.

For  $I_{D1}$  equal to 1 milliamperere and  $I_{C1}$  which is this current, in this direction,  $I_{C1}$  is equal to 9 milliamperere all right? And  $V_{D1}$ , that means this voltage, this voltage to ground,  $V_{D1}$ , DC voltage, I will not show this. I could as well show this okay.  $V_{D1}$  to ground is equal to 13.5volts. The transistors have the following parameters. For Q1 what you need is  $I_{DSS}$ . This is given as 4 milliamperere and  $V_P$ , this also you need, it is given as - 2 volts. All right?

And for Q2 the given data is  $V_{BE}$ , that is 0.7 volt. If it was not given, we would have assumed it but what we need most is the  $\beta$ .  $\beta$  is 100. Okay. The problem specification clear? Now obviously what you have to do is no order to find out these parameters, these are for AC analysis, you require the values of  $G_M$  for the 2 transistors. And for this transfer, you also require the value of  $R_{\pi}$   $R_{\pi 2}$  all right. This is why the DC questions have to be solved 1<sup>st</sup> to find the DC operating condition, the Q point, then find the  $G_M$ s and  $R_{\pi}$  and go ahead with the AC analysis.

The saving grace is that this voltage is given,  $V_{D1}$ , 13.5. If you go, see  $V_{D1}$ , let me write this equation. I have no more space here. So I must change.

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$$V_{D1} = 13.5V = V_{BE}$$

$$V_{E2} = 13.5 + 0.7 = 14.2V$$

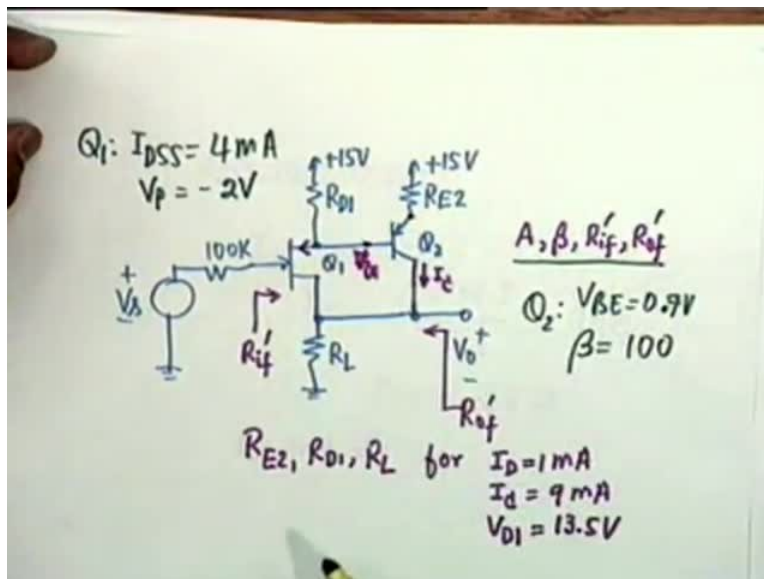
$$I_{E2} = \frac{15 - 14.2}{R_{E2}} = 9mA$$

$$R_{E2} \cong 88\Omega$$

$$I_D = 1mA \Rightarrow I_{B2} = 0.09mA$$

$$R_{D1} = 1.65K$$

$\frac{15 - 13.5}{0.09} K$



You must keep on looking at the circuit.  $V_{D1}$  which is 13.5 volt is the same as  $V_{B2}$  which is equal to  $V_{B2}$ .

Student: (0)(6:41)

Professor: No, we do not want to do that. We want to find out.

Student: RE2.

Professor: yes, we want to find out ...

Student: We have to find out RE2 because IC is 0.7 volts so.

Professor: That is right. I wanted to find out IE2 1<sup>st</sup> which is the same as RE2, that is correct.

You see, IE2. Hold it, what is VE2? This voltage. This is  $13.5 + 0.7$ , this is the point that I wanted to make. Do not make a mistake. It is not - because it is a pnp transistor. So  $13.5 + 0.7$ . Now we are in business. This is 14.2 volts. And therefore, IE2 which is equal to  $15 - 14.2$ , the supply divided by RE2 and this can be taken approximately as 9 milliamperes. If you are very fuzzy, then you divide 9 milliamperes divided by.

Student: Beta.

Professor: Alpha, not beta. Alpha which is beta divided by beta + 1 and but since beta is 100, we can ignore that.

Therefore, this is equal to 9 milliamperes. And from which, RE2 comes out as approximately 88 ohms. I have made some rounding, just to make a quick calculation, just not to spend more time on the calculator. So there may be a small difference in the 2<sup>nd</sup> place of decimal. Next, I sub D is given as 1 milliamperes which means, I sub D is given as 1 milliamperes and IB2, you look at this. This is I sub D and IB2 would be 9 milliamperes divided by.

Student: beta

Professor: beta. And therefore IB2 is 0.09 milliamperes and my equation would be, to find RD1, that  $15 - 13.5$  divided by the total current through RD1 which is  $I_D + I_{B2}$ . And therefore RD1 can be found out. Let me not write the equation. I have explained what it is. RD1 is 1.65 K. This is what I find. What I did was  $15 - 13.5$  divided by 9 milliamperes and 0.09.

Student: 1 milliamperes

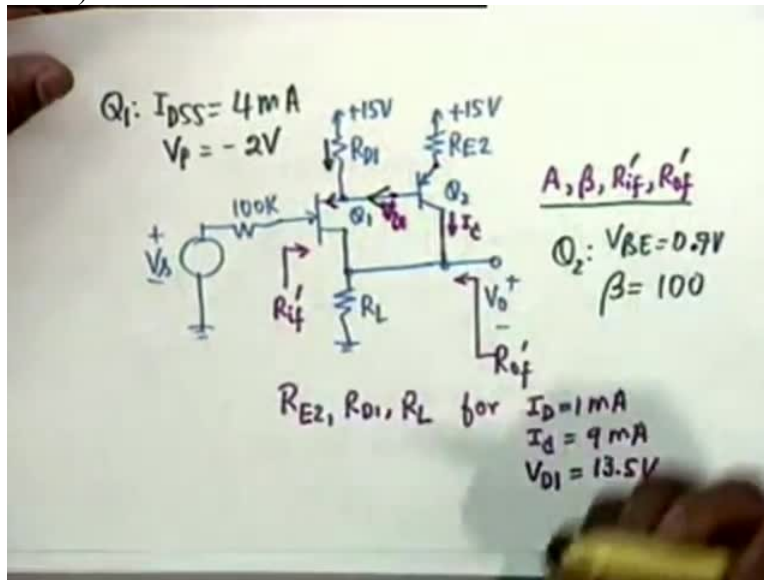
Student: Sir, 1 milliamperes

Student: Sir, 1 milliampere

Professor: 1.09 milliampere. So many k which is equal to RD1. Pardon me.

Student: Sir, (())(9:55)

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~~$V_{D1} = 13.5 \text{ V} = V_{B2}$~~

~~$V_{E2} = 13.5 + 0.7 = 14.2 \text{ V}$~~

$V_{E2} = 13.5 + 0.7 = 14.2 \text{ V}$

$I_{E2} = \frac{15 - 14.2}{R_{E2}} = 9 \text{ mA}$

$R_{E2} \cong 88 \Omega$

$I_D = 1 \text{ mA} \Rightarrow I_{B2} = 0.09 \text{ mA}$

$R_{D1} = 1.65 \text{ K}$

$\frac{15 - 13.5}{0.09} \text{ K}$

Professor: IB is in the?

Student: Opposite direction.

Professor: Oh, how wonderful? That is right. Therefore, I have made a mistake. Okay. So it should be  $I_B$ , I beg your pardon. I this current would be

Student: ID -...

Professor: ID?

Student: ID -  $I_{B2}$ .

Professor:-  $I_{B2}$ . Okay. So it would be  $1 - 0.09$ .

Student: Excuse me Sir.

Professor: yes.

Student: Is there any specific reason for neglecting the base current?

Professor: Is there any specific reason for neglecting the base current? Well, we do not know because the base current may be comparable to the drain current of the previous amplifier. You see I can neglect the base current if I compare it with  $I_{sub C}$ . Right? But the base current is being compared with the drain current here. Okay. It may not be negligible. For example, it is  $1 - 0.09$  which is 10 percent. No, not 10 percent. How much is it? Approximately 1 percent.

Student: 9 percent.

Professor: 0.0, a 9 percent. 9 percent obviously cannot be ignored. We will not ignore this okay. Anyway. So you understand where one can make mistakes. In the sign of  $V_{BE}$ , in the direction of the base current. All right.

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11:48

If we cross these hurdles, the last thing to do out is to find out, this is not a simple problem although it looks very simple. You have to find out  $I_{RL}$  and obviously, for  $I_{RL}$ , you require  $V_{GS}$ . Because the equation for  $I_{sub D}$  is  $I_{DSS} (1 -$

VGS by VP whole square. And VGS can be written in terms of ID. So it would be an implicit, no it will not be. Let us see.

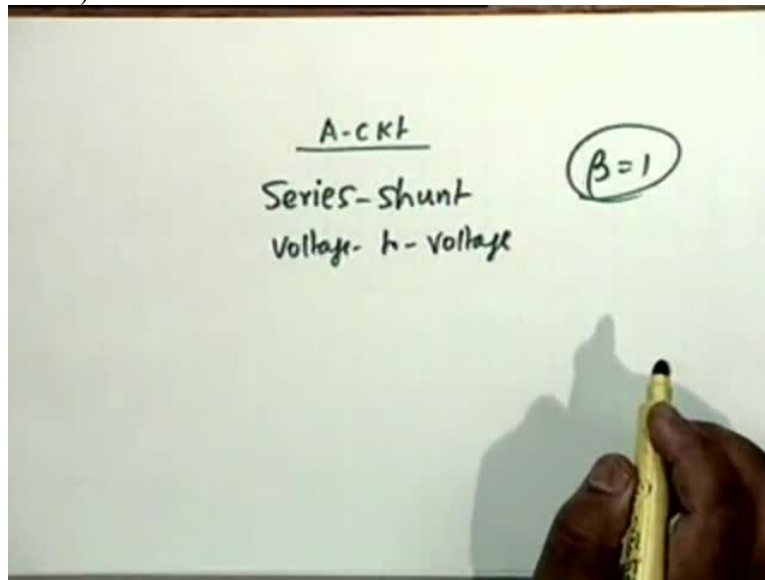
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$$\begin{aligned}
 I_D &= I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2 \\
 &= 4 \left(1 + \frac{V_{GS}}{2}\right)^2 = 1 \text{ mA} \\
 V_{GS} &= -1 \text{ V} \\
 V_G - V_S &= -1 \text{ V} \\
 V_S &= 1 \text{ V} = (1 \text{ mA} + 9 \text{ mA}) R_L \\
 R_L &= 100 \Omega
 \end{aligned}$$

Our I sub D is IDSS 1 - VGS by VP whole square. You are used to getting implicit equations in ID, quadratic equation. This will not be the case here because our IDSS is given as 4 milliampere, 1, VP is equal to - 2. So 1 + VGS by 2 whole square and this is given as 1 milliampere which makes VGS equal to - 1 volts. Is not that right? Now VGS is VG - VS which is - 1 volt. And if you look at the circuit, what is VG? What is the volt, DC voltage here? There is no source, there is no DC source. Therefore it is 0. Is that clear?

So VG is equal to 0 which means that VS is equal to 1 volt. Now what is VS? VS is this current + this current, IC + ID into RD okay. So this is 1 milliampere + 9 milliampere multiplied by, this is the current flowing through RL. Therefore RL is equal to 100 ohms, correct. So you have found out all the parameters. Agreed? Now after you have found out the 3 resistances, the currents are given. 1 milliampere, 9 milliampere, okay. Now after we have found out these, we can now go to the AC equivalent circuit and we will not draw the AC equivalent circuit, we will draw the A circuit and the beta circuit right by looking at the given circuit okay.

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For the A circuit for example, this is where you will have to pay attention. Now 1<sup>st</sup> thing is, you have to identify the kind of architecture because the A circuit shall have to be drawn in the proper model. Proper model whether it is a voltage to current, voltage to voltage, current to voltage or current to current. Now what is this connection? Obviously the input connection is series, the output connection is?

Student: Shunt.

Student: Series.

Student: Series.

Professor: No.

Student: Shunt.

Professor: It is shunt because the output voltage is taken here. The voltage is being directly fed and therefore this is a shunt connection.

Student: Sir, please explain.



Professor: Please explain. The output, if the output voltage was being taken here then it would have been a series connection here.

Student:  $R_{\pi}$  (15:11)

Professor: Not, it is not the question of  $R_{\pi}$ . Where it is connected, the feedback voltage,  $V_F$ , is it proportional to the current through the load or the voltage across the load? It is obviously is exactly equal to  $V_0$  and therefore there can be no question. It is a shunt connection. It is also obvious that beta in this case, we do not have to do anything. What is beta?

Student: 1.

Student: 1.

Professor: Beta is 1 because  $V_0'$  will be equal to  $V_F'$ . There is only a shunt resistance across it.

So one thing we identify immediately is beta equal to 1 and the connection is series-shunt. Now in series-shunt, what should be the model of the amplifier that determines the drawing of the A circuit. What should be the model of the amplifier? Voltage to?

Student: Current.

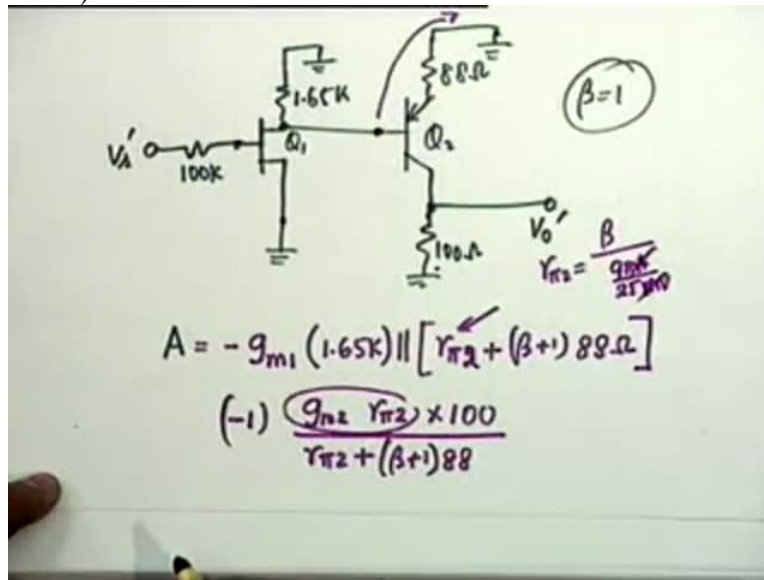
Student: Current.

Professor: No.

Student: Voltage to voltage.

Professor: Voltage to voltage. Do not make such mistakes. This is a voltage to voltage and therefore capital A shall be found as voltage ratio and therefore I do not have to convert the source into a Norton one okay. So my circuit is the following. Let me draw it on a separate sheet.

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Please check with your original circuit. I have always used these primes to find the A circuit okay. There is a 100 K resistance, then we have this, now what will come here? Q1, at the source terminal of Q1, there was this RL which is part of the feedback network. Since the output is a shunt connection, we short this to ground. Okay. The A circuit. Then of course, we have the 1.65 K which we found out, this goes to ground and then this voltage goes to Q2, the pnp. Now what will be here? Since this connection is series, we have to open that. Therefore, all I will get here is 100 ohms.

And the output voltage is taken here. This is V0 prime. Q2 is connected to, we found out an 88 ohm resistance which goes to ground. And beta we have already found out to be equal to 1. Therefore, now I want you to calculate the gain A.

Student: Sir please explain why RL was grounded.

Professor: Why RL was grounded? Because the output is a shunt connection. Shunt means short. Shunt has to be shorted and therefore RL was shorted for this, RL was open for this.

Input connection is series, so it was open. It is a series-shunt okay. Now I want you to calculate the gain by inspection. If go from here to here okay, as far as this point is concerned, there is no drop. So this is also VS prime. Agree? Because the input is open. It is a JFET, therefore the input resistance is infinity. Therefore, from here to here, voltage it would be - GM of this transistor,

GM 1 multiplied by 1.6 5K parallel, the impedance coming from here to ground, you have to go via this, not via this. Is the point clear?

Student: No Sir.

Professor: No. I have to go from here to ground. I do not know the resistance between the base and the collector. I have to go via base and emitter and therefore I have to follow this route.

That is what we do for npn. Why not for pnp? Okay, what would this be? This would be obviously  $R_{\pi 2} + \beta + 1$  if you are fussy. Okay.  $\beta + 1$  times 88 ohms. This is the gain of the 1<sup>st</sup> stage. Now the gain of the 2<sup>nd</sup> stage you see you have a resistance here as well as here approximately, it would be 100 by 88 but let us calculate exactly what it is. It would be - okay. How do I take care of this? - 1, let me multiply by this for the 2<sup>nd</sup> stage, Q2.

It would be -  $G_{M2}$  times  $V_{\pi 2}$  okay.  $G_{M2}$  times  $V_{\pi 2}$  which would be  $R_{\pi 2}$  divided by, okay divided by  $R_{\pi 2} + \beta + 188$  ohms okay. This is the current, this current flows through 100 ohms to make  $V_0$  prime, therefore I have to multiply by 100. Is that clear? I have written this by inspection. I did not draw an equivalent circuit. If it proves to be difficult to see, to observe, then you draw the equivalent circuit. You draw the equi so that you do not make a mistake. But with experience, you should be able to do this by inspection.

Now in this in this, all that is, you see I do not have this quantity is  $\beta^2$  which is known. But I require an  $R_{\pi 2}$  because  $R_{\pi 2}$  occurs here as well as here. And therefore, I will calculate  $R_{\pi 2}$ , that is not a problem.  $\beta$  divided by  $G_{M2}$  which is  $I_{sub C}$ , how much?

Student: 48 ohms.

Professor: 9 milliamperes. Okay? 9 milliamperes divided by 25 volts. So it is 2500 by 9. So many ohms.

Student: 25 millivolts.

Student: millivolts.

Student: millivolts.

Student: millivolts.

Professor: 25 millivolts, yes. Millivolts and milliampere shall cancel and that is why it becomes 2500 by 9 ohms. Substitute this and make the numerical calculation. My calculation. Oh no, I still have something else to do. I have not found out GM1 okay?

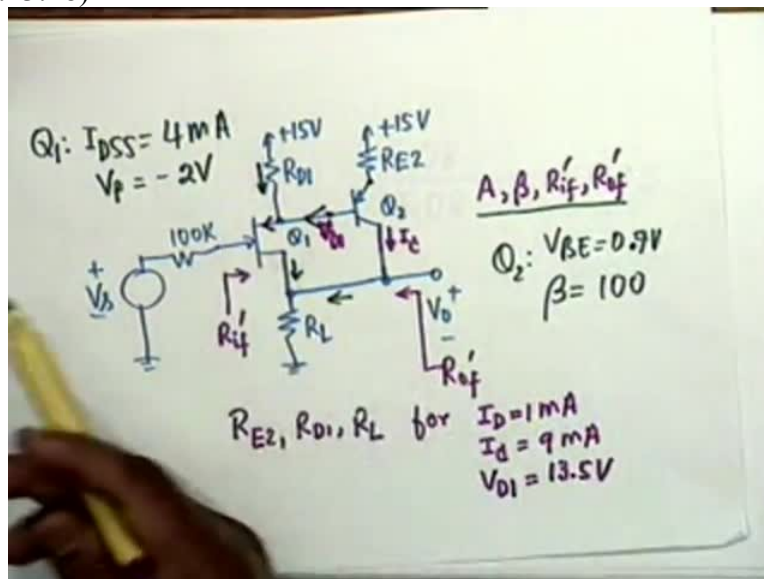
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$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$
$$g_{m1} = \frac{-2 I_{DSS}}{V_P} \left(1 - \frac{V_{GS}}{V_P}\right)$$
$$= 2 \text{ mV}^{-1}$$
$$A = 3.08 \quad \beta = 1$$

I have to go back my equation  $I_D$  equal to  $I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$  and I find GM as  $-2 I_{DSS} / V_P$ , you do not have to remember this formula. All that you have to remember is this one that there is a square. The differentiation is obvious, multiplied by  $1 - \frac{V_{GS}}{V_P}$ . And if you substitute this, if you substitute the values, my value comes as 2 millimho. And therefore, capital A after substituting this, I am omitting some number crunching. Capital A my value comes

as 3.08 and beta is 1. Therefore everything else falls into place. Agreed?

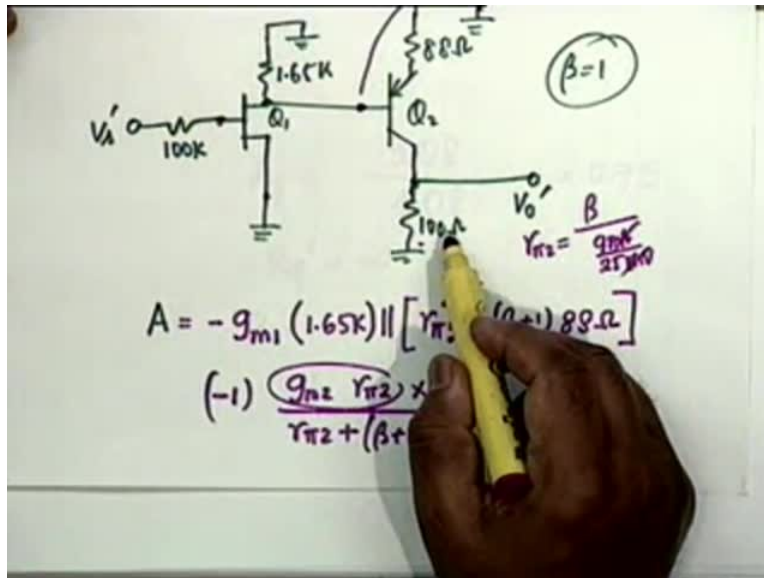
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$$A_f = \frac{3.08}{4.08} = 0.75$$

$$R_{if}' = \infty$$

$$R_o =$$



AF, the feedback gain, it is 3.08 divided by  $1 + A\beta$ , so 4.08. It is less than 1, it is 0.75. RIF prime, now if I go back to this circuit, if I did not, I do not require any calculations to say what RIF prime would be. It is

Student:- RI.

Professor: Oh no. What is RI? What does the source see at Q1?

Student: 1 upon  $G_{M1}$ .

Student: Infinity.

Professor: Infinity. This, the gate is opened and therefore nothing can change. Make any feedback that you like, nothing changes okay.

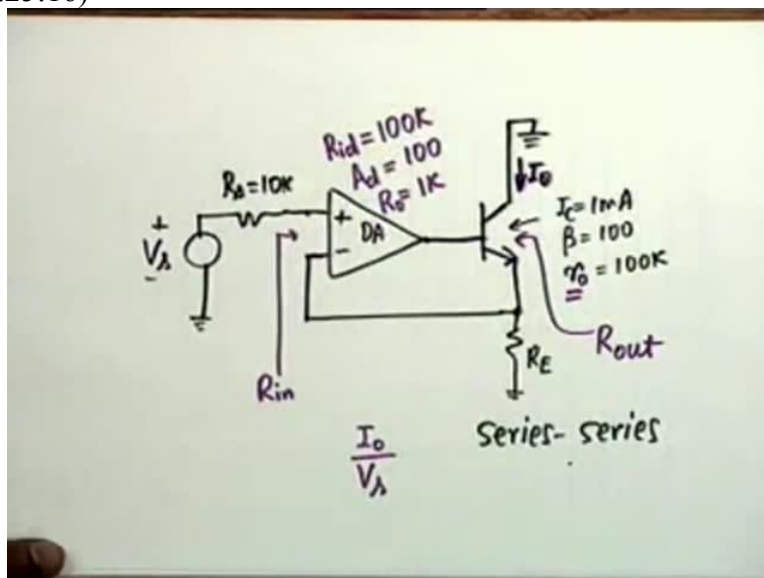
So RIF is RIF prime is infinity, that is no problem. My RO, that is without feedback, now look at the look at this circuit, A circuit look at the A circuit, what is RO? RO is 100 ohms and therefore this shall change.

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$$A_f = \frac{3.08}{4.08} = 0.75$$
$$R_{if}' = \infty$$
$$R_{of}' = \frac{100}{4.08} = 24.5 \Omega$$

Now ROF prime would be 100 ohm divided by how much? 4.08.  $1 + A \beta$  we have already found out and therefore this becomes 24.5 ohm and that completes the example okay? You have to proceed carefully. Now in the next few examples I will not go into the details of the numerical calculations. I will show where the trick is and how to break it. Any question on this? The next example is also a very interesting example.

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A simple circuit but you look at the complications that it creates. We have a  $V_s$  in series with an  $R_s$  which is given as 10 K, then this goes to a differential amplifier. This is a DA, not an op-

amp. Differential amplifier in which the negative, the inverting terminal is connected to a resistance  $R_{sub E}$  to ground and the output goes to a BJT. Output goes to a BJT, the emitter of which is connected here, that is why this resistance is  $R_E$ . Please follow carefully. I am not showing the biasing circuit. The collector is virtually grounded and this is the current that we are interested in.

This is my output.  $I_0$  okay? We have to find out. Okay what we have to find out will be shown later but it is given that this transistor is biased at  $I_{sub C}$  equal to 1 milliamperes and for this transistor,  $\beta$  is 100, small  $R_0$  okay for a change this is given to be 100 K. We will see how to take care of this. And the differential amplifier has the following specifications. Its  $R_{ID}$  is given as 100 K. The differential amplifier has a differential input resistance, that is between these 2 terminals as 100 K.  $R_{ICM}$  is not given. So we safely assume it to be unit infinity.

The differential gain is given as 100,  $\alpha_C$  is not given. So you assume that to be 0 okay. We assume  $CMRR$  to be infinity and the output resistance capital  $R_0$  is given as 1K. Do not confuse this with the output resistance. Since I have already used small  $r_0$ , I have no other option. I used a capital  $R_0$  is 1K. Is that clear? The model is floating in front of your eyes. There are 2 terminals. In between them, there is a resistance,  $R_{ID}$ . The voltage is  $V_1$  let us say. Then the output voltage is 100 times  $V_1$  in series with a 1K resistance.

That is the model. Nothing else is given, so we do not take care of anything else. So I must change my terminology now. What we have to find out is  $R$ , we can call this  $R_{out}$ . I would not use the symbol capital  $R_0$  output resistance. Then we have to find the input resistance, that is looking from here,  $R_{in}$ , obviously this will not be  $R_{ID}$  anymore because there is feedback okay. These are the things to be found out. Oh, I also have to find out  $I_0$  by  $V_S$ .

Student: Sir, where will you take the output from?

Professor: Output is this. The current  $I_0$  is my output. This is actually a circuit of a voltage to current converter. Can you identify what the feedback connection is?

Student: Series.

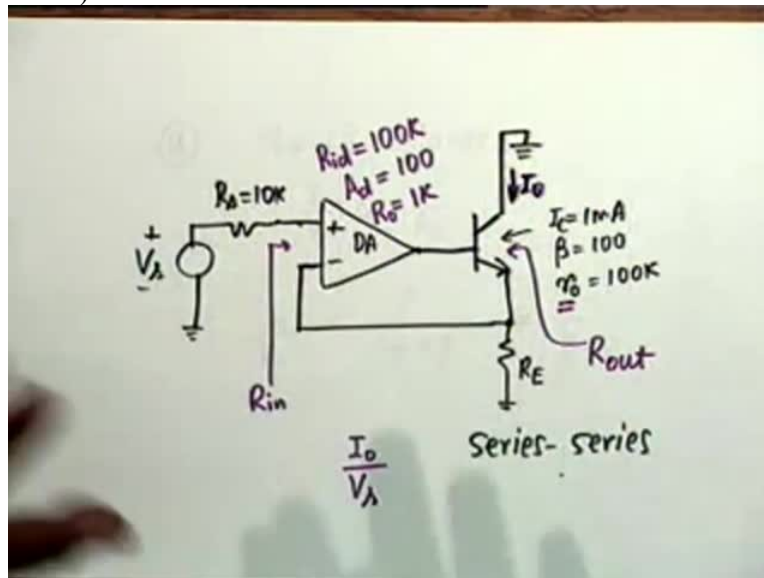
Professor: series and?



Student: series-series.

Professor: series-series. Wonderful. This is a series-series which means that it is a voltage to current converter and therefore I do not have to change this. My output shall be a current. The 1<sup>st</sup> question that it asks is the following.

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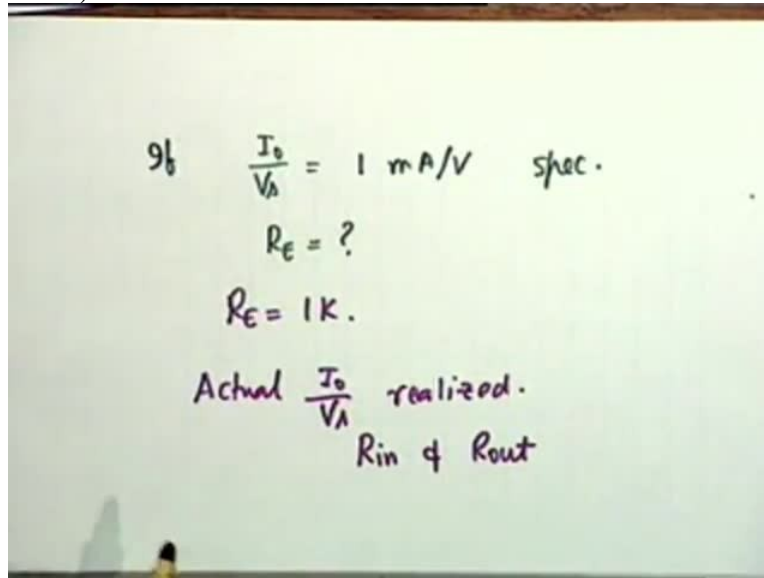
Without going into any numerical values, it says, show that if  $A\beta$  is large then  $I_0$  by  $V_s$  is approximately equal to  $1$  over  $R_E$ . This is the 1<sup>st</sup> part of the question, part A. Show that if  $A\beta$  is large then  $I_0$  by  $V_s$  is approximately equal to  $1$  over  $R_E$ . Now we know, this solution is extremely easy.  $I_0$  by  $V_s$  would be  $A$  divided by  $1 + A\beta$ . If  $A\beta$  is large compared to  $1$ , then obviously this is equal to or approximately equal to  $1$  by  $\beta$ . Now what is  $\beta$ ?  $\beta$  is simply  $R_E$ . Why  $R_E$ ? Not  $1$  by  $R_E$ . Because the voltage fed back,  $V_f$  prime is equal to  $I_0$  prime multiplied by  $R_E$  and therefore,  $V_f$  prime divided by  $I_0$  prime is equal to  $R_E$ . Is it obvious or I should draw the diagram?

Student: Obvious.

Professor: It is obvious. And therefore this is equal to  $1$  over  $R_E$ .

This is the 1<sup>st</sup> part of the question without looking at anything else.

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The 2<sup>nd</sup> part of the question says that if  $I_0$  by  $V_S$  is specified as 1 milliamperes per volt find  $R_E$ . Obviously,  $R_E$  would be equal to

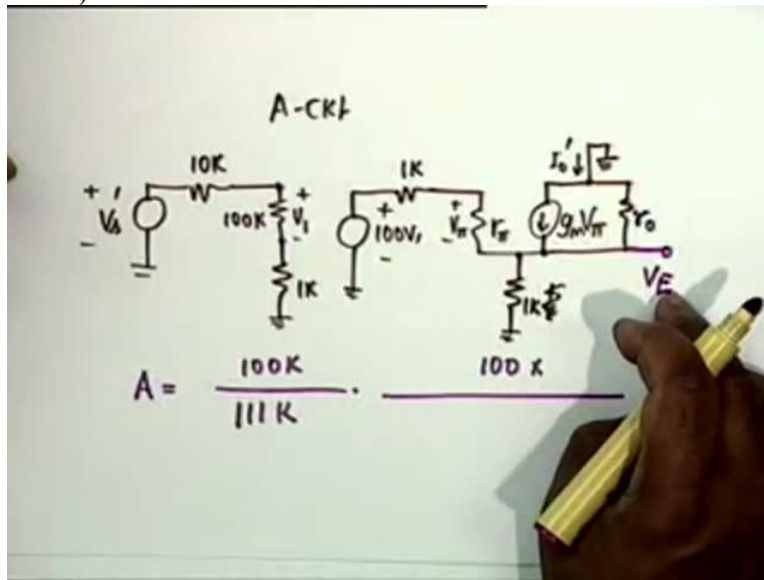
Student: 1.

Student: 1K.

Professor: 1K all right. This solution is also very easy.

Now comes the actual problem.  $R_E$  equal to 1K. Now it says, make a feedback analysis and find the actual transconductance realized because this is under the condition that  $\beta$  is large. So you now analyse the circuit to find out what is the actual  $I_0$  by  $V_S$  that is realized and also find out  $R_{in}$  and  $R_{out}$ . This is the total problem. Now let us look at the problem. This is also a very simple problem provided you view it as simple provided you look at it carefully.

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Now if you look at the circuit, I can draw the A circuit quite easily. The A circuit would be  $V_s$  prime. Now comes the question of the model.  $V_s$  prime, my source resistance is  $10K$ . Did I say this  $10K$  or  $100K$ ?

Student:  $10K$ .

Professor:  $10K$  all right.

Then comes the 2 terminals of the differential amplifier between which there is a resistance of  $100K$ , that is  $R_{ID}$  is given as  $100K$ . Then we have a  $1K$ . Now what do I do to this feedback circuit? This is a series-series. So I shall have to open the output which means that  $1K$  shall come here. Agreed? Series-series. And this voltage is  $V_1$ .

Student: Sir, which  $1K$ ?

Professor: Which  $1K$ ? It is  $R_{sub E}$ .

Student: Sir, that would be considered as an assumption?

Professor: What assumption?

Student: If it is  $(\ )$ (33:19)

Professor: okay. We have used an RE equal to 1 K now okay, on the basis of approximation. Then the question is with RE equal to 1K what is the actual  $I_0$  by VS realised? Okay. Now to get the A circuit, obviously what you have to do is open here, so I get RE and as far as this transistor is concerned what shall it see? It will also see RE. Why? Because it is a series-series. Okay fine. So we go to the model, the differential gain is given as 100. So 100 V1. Too many 100s and 10s. Do not confuse. 100V1, then it has an output resistance, the differential amplifier has an output resistance of 1K.

So 1K goes here. Then comes the model. Shall we draw the model or shall we do it by inspection? We want the model. Okay. Then comes an R pi and this voltage is V pi, this is GM V pi okay. This resistance is 1K, this is that RE and in addition, you have the resistance small r0, this is grounded, the collector is grounded and where is the output now? It is the current flowing through. Is that correct?

Student: No Sir.

Professor: No.

Student: Sir, it is coming from the ground.

Professor: From the ground. So it is this current,  $I_0$  prime. Very good. Very good identification. Once you have done that, now you can write down the gain by inspection. It is a long circuit but it does not matter. You see, 1<sup>st</sup> you have to find out V1 in terms of VS prime. So the gain I can write this by inspection, the gain would be 100 K divided by 10 K, 100 K and 1K, so 111 K. 111 K, this is for the 1<sup>st</sup> stage. For the 2<sup>nd</sup> stage you have to find out  $I_0$  prime by V1. So 1<sup>st</sup> thing is you write 100 because there is a 100 V1. All right? Then you have to find out GM. Well we will see how find that out. Will you require GM or you do not require because  $I_0$  prime is the current that is needed. Suppose suppose we find out VE, this voltage, suppose we find out VE, is not it the same current flowing through 1K? No, it is not.

Student: Sir, we need GM.

Professor: pardon me?

Student: Sir, we shall need GM.

Professor: We shall need GM, that is correct.

(Refer Slide Time:36:46)

$$V_E = \frac{100V_1 \cdot (1+\beta) \cdot (1K \parallel 100K)}{(1+\beta) \cdot (1K \parallel 100K) + r_{\pi} + 1K}$$

$$\frac{I_0'}{V_s'} \approx \frac{V_E}{1K} = \cancel{86mA}$$

$$\frac{I_0'}{V_s'} = 86mV$$

$\frac{V_{\pi}}{r_{\pi}} + g_m V_{\pi}$   
 $\frac{\beta+1}{r_{\pi}} V_{\pi}$

But you see that  $V_E$  if you look at this circuit if you look at this circuit,  $V_E$  is equal to  $100 V_1$ . Well, what is this resistance appears as effectively  $1K$  just a minute  $V_E$  is  $1K$  parallel  $R_0$  and the current that flows through is  $\beta + 1$  per whatever current flows here, agreed? So I can write down by inspection  $V_E$  as  $100 V_1$ , then  $1 + \beta$  times  $1K$  parallel  $100 K$ . This is the drop across  $1K$  parallel  $100 K$ . Divided by  $1 + \beta$   $1K$  parallel  $100 K + R_{\pi} + 1K$ . Right? This is  $V_E$ .

Student: Sir please explain the numerator.

Professor: The numerator. The numerator is,  $V_E$  is this voltage. How is this voltage created?  $1K$  parallel  $100 K$ .

Student:  $R_0$  is  $100$ .

Professor: That is right.  $R_0$  is  $100 K$ . Given. So I know  $V_E$ . Therefore  $I_0$  prime by  $V_s$  prime would be equal to, if this is  $I_0$  prime, how does this current differ from  $I_0$  prime?

Student: ( ) (38:27)

Professor: This current is also  $I_0$  prime but we have the base current here okay. So  $\beta$ , that is why that  $\beta + 1$  comes. And since  $1$  can be ignored compared to  $\beta$ , this is approximately the

same as  $V_E$  by  $1K$  which is 86 millimhos, my calculation. All right? And what was beta? What was beta? Have not we already found out what beta is?

Student: RE.

Student: RE.

Professor: Beta is RE. So beta is  $1K$ .

Student: How  $V_E$  by  $1K$ .

Professor: How  $V_E$  by  $1K$ .

Student: Sir, dimensionally  $(\text{ohm})^{-1}$  (39:13)

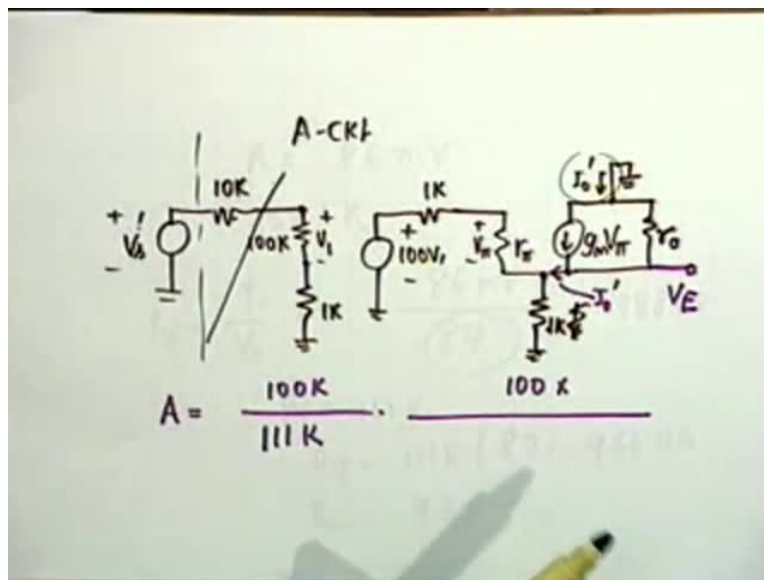
Professor: yes. Oh. I am sorry. This is  $I_0$  prime. I beg your pardon. So I have made a mistake. Okay,  $I_0$  prime is  $V_E$  by  $1K$  and  $V_E$  is given by this and  $V_1$  was found out in terms of  $V_S$  prime. And therefore we have to combine all these 3 questions and my final equation becomes  $I_0$  by  $V_S$  prime. This becomes equal to 86 millimhos. The previous equation was not correct. This is the equation for the current. Thank you for pointing this out.

Student:  $(\text{ohm})^{-1}$  (40:11)  $V$  prime by  $I$  prime? Sir, we are neglecting that?

Professor: we are neglecting that. You see, that contributes to  $\beta + 1$  and we are ignoring 1 with respect to  $\beta$ . Does this require an explanation? Has the rest of the class understood? No? You see, my current is  $V_{pi}$  by  $R_{pi} + GM V_{pi}$ . We are ignoring the shunting effect of  $R_0$  okay? And this is  $\beta + 1$  divided by  $R_{pi}$  into  $V_{pi}$  and we are ignoring 1 with respect to  $\beta$  and therefore it simply becomes  $GM V_{pi}$ . Is that clear? This we have done again and again. But still.

(Refer Slide Time:41:05)

$$A = 86 \text{ m}\Omega$$
$$\beta = 1 \text{ K}$$
$$A_f = \frac{I_o}{V_s} = \frac{86 \text{ m}\Omega}{87} = 0.988 \text{ m}\Omega$$
$$R_i = 111 \text{ K}$$
$$R_{if} = 111 \text{ K} (87) = 9.66 \text{ M}\Omega$$
$$R_{in} = 9.65 \text{ M}\Omega$$



Okayso finally what we have is capital A is equal to 86millimho, beta is equal to 1 and therefore  $I_o$  by  $V_s$  which is  $A_f$  is given by 86 divided by, beta equal to 1.

Student: in terms of  $R_E$ .

Student:  $R_E$

Professor:  $1 \text{ K}$ .

Student: Beta in terms of  $R_E$ .

Professor: Right, so it is 1K, not 1. You must not forget the dimension because A beta must be dimensionless. Millimho multiplied by K obviously is dimensionless. So this would be 86 by 87 which is 0.988, what is the unit?

Student: millimho.

Professor: millimho. This is 86 millimho divided by  $1 + 86$ . So it becomes 0.988 millimho and obviously RI if you look at the circuit again, what is RI? Differential amplifier, 100 K, 10 K and 1 K. So it is 111 K and RIF therefore would be 111 K multiplied by how much?

Student: 1 by (0)(42:18)

Professor: increase or decrease?

Student: increase.

Professor: Increase. It is a series-series. And therefore it will be multiplied by?

Student: 87.

Professor: 87. I have already found this factor out and this comes as 9.66 meg but this is not the impedance faced by the source. What is the impedance faced by the source,  $R_{in}$ ?

Student: - 10K.

Student: - 10K.

Professor: - 10 K which makes it 9.65 meg.

Student: Sir, should not  $R_{in}$  be 101 K? Sir because  $R_S$  was 10k.

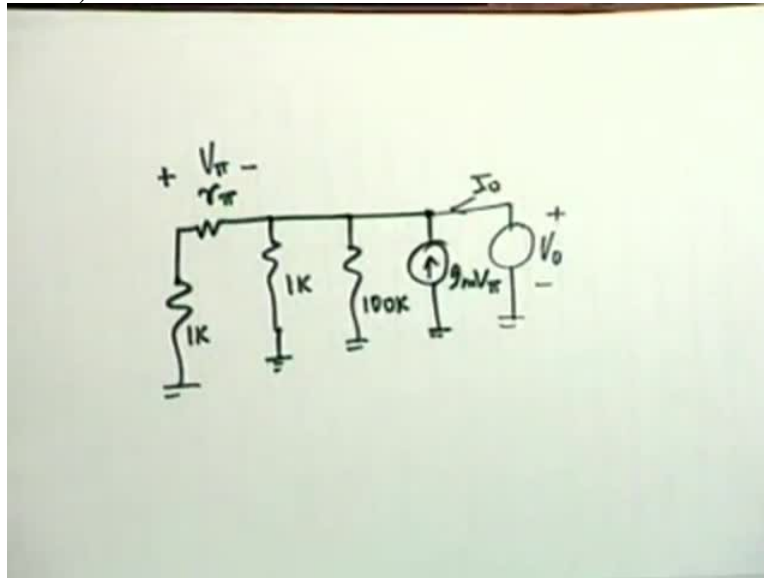
Professor: okay. I am glad you raised the question. Nobody raised the question earlier. This is the confusion that I want you to avoid. I have warned you before that your A circuit is now this, between  $V_S$  prime and  $I_0$  prime. So it is included .

You see, if this was a current source and you have to combine this, here of course it is obvious that 10k has to be subtracted. It may not have been obvious. If this was a current source and 10k



was absorbed in the circuit, you have to absorb it because one of the fundamental steps is the A circuit must absorb  $R_S$  and  $R_L$ . And therefore, it is not 101K, it is 111 K. okay. And the rest of the circuit, rest of the analysis, you can do yourself.  $R_0$ ,  $R_{out}$  is not trivial.  $R_{out}$  calculation is not trivial.  $R_{out}$  calculation, you have to apply a voltage source and find the current.

(Refer Slide Time:44:08)



And a circuit, let me draw the circuit. You have to connect a voltage source and find the current. The equivalent circuit is, there is a  $g_m V_{pi}$ . Then there is a 100 K. What is this 100 K due to?

Student:  $R_0$ .

Professor:  $r_0$ , small  $r_0$ . Then you have a 1K. What is this 1K?

Student:  $R_E$ .

Professor:  $R_E$ . And then you have  $R_{pi}$  and then 1 K going to ground.  $V_S$  has to be made equal to 0 and  $V_{pi}$ , do not confuse the polarity. Polarity is + to the right or + to the left?

Student: To the left.

Professor: left. + to the left and -.

Student: excuse me, sir.

Professor: yes.

Student: how is RE coming parallel with GM and R0?

Professor: Oh, you look at the circuit. You look at the circuit. This is coming in parallel to R0 because this is grounded.

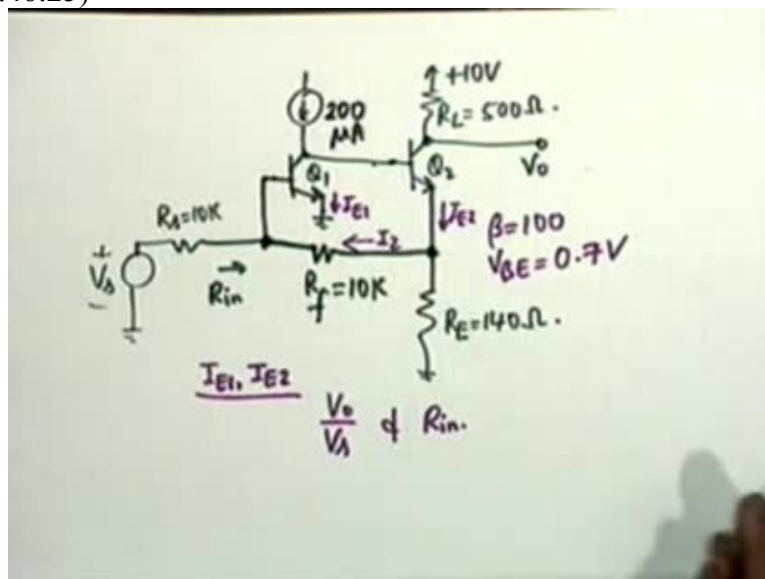
Student: Sir? Sir, if our output is the collector current, so the input V not should also be given to the collector.

Professor: Input V not. That is what we have done.

Student: Sir, we have given it to the emitter. The 1<sup>st</sup> one is to the emitter, it should be to the collector.

Professor: You see, between the collector and ground, just 2 minutes. My output impedance is between the collector and emitter. You see. This is what I wanted. Collector and emitter. Now that means between emitter and, collector is grounded. So emitter and ground. That's what I have found here. Is the point clear? Okay. Now the next problem oh you calculate this out. The next problem I will simply indicate and then ask you to work it out. I will take the most complicated one. I have 4 problems but let me take the most complicated one. Just draw the circuit with me.

(Refer Slide Time:46:25)



$V_S$ ,  $R_S$  given as 10k, you have to find out  $R_{in}$ . This goes to a transistor Q1 whose emitter is grounded and which is biased by a constant current source, 200 micro ampere. Very practical circuit. It forms part of a chip. There is a 2<sup>nd</sup> transistor Q2 which goes to resistance  $R_E$  equal to 140 ohms and between this point and  $R_E$ , there is a feedback resistance  $R_F$  which is equal to 10k. The transistor Q2 is biased by a 10 volt source through an  $R_L$  which is 500 ohms. The output is taken here,  $V_0$ .

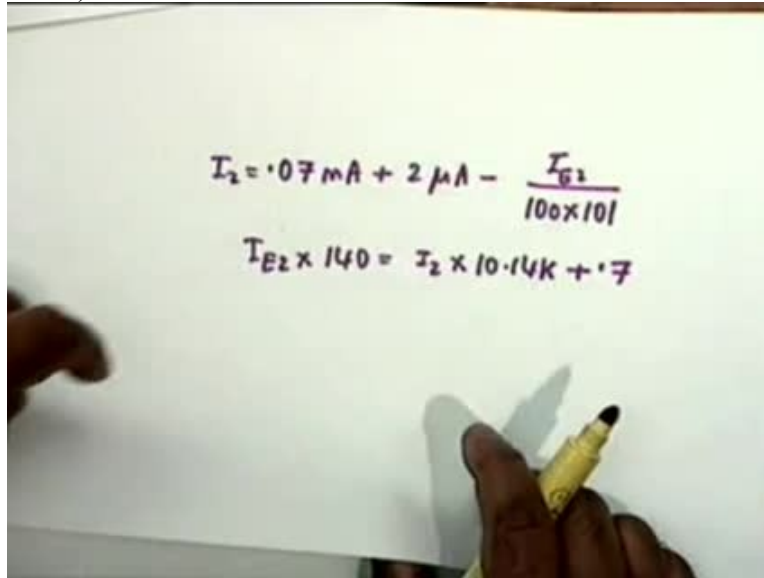
The problem is, alright, you require some data. Beta is equal to 100 for both the transistors. What else do you need? And  $V_{BE}$ , you can assume the  $V_{BE}$  to be 0.7 for both the transistors, 0.7 volt. What you have to find out is  $I_{E1}$  DC,  $I_{E2}$ , again DC value. Find out  $I_{E1}$ ,  $I_{E2}$  and the node voltages for all the nodes. That means you have to find out this voltage, this voltage, this voltage and this voltage. How much is this voltage?

Student: 0.

Professor: 0.7 volt. This is grounded. From base to emitter, it is 0.7. And that is the starting point of the solution. This is 0.7 and therefore you can find this current and therefore, you can sum up this current and this current and so on. But let me state the problem 1<sup>st</sup>. Find  $V_0$  by  $V_S$  and  $R_{in}$ . Okay? The major effort for this problem is in finding the 2 currents,  $I_{E1}$  and  $I_{E2}$ . Let me tell you how to do this. This current, you ignore the base current. No, you cannot ignore the base currents now because this current, this base current would be comparable to 200 microampere.

You cannot ignore. So what you do is, this current  $I_{E2}$  is obviously  $I_{C1} + I_{B1}$  by beta okay. You do not ignore it now because this will have to compare with 200, this is a constant current biasing okay? There is a temptation to ignore this. Then that current - the current that goes through here is dropped across here. So you know this voltage. Okay. This voltage can also be written as this voltage, the drop in this + 0.7. K? So ultimately what you will get is if this current is  $I_2$ ,  $I_2$ , please check my solution.

(Refer Slide Time:50:48)



The image shows a whiteboard with two handwritten equations. The first equation is  $I_2 = 0.07 \text{ mA} + 2 \mu\text{A} - \frac{I_{E2}}{100 \times 101}$ . The second equation is  $I_{E2} \times 140 = I_2 \times 10.14 \text{ K} + 0.7$ . A hand holding a yellow marker is visible at the bottom right of the whiteboard.

You get the following 2 equations,  $I_2$  equal to 0.07 milliampere+ 2 microampere -  $I_{E2}$  divided by 100 into 101. I did not ignore that beta + 1. I did not ignore here. Yes. This is one of the equations and the other equation is  $I_{E2}$  multiplied by 140 equal to  $I_2$  multiplied by 10.14 K. This is 200 microampere divided by 100.

Student: ( ) (51:23)

Professor: pardon me?

Student: ( ) (51:24).

Professor: No, this comes after the manipulation. You have to write the KVLs, 2 KVLs and then this is what comes, from which you can find out  $I_{E2}$  and therefore you can find all other currents.

Student: Sir ( ) (51:42).

Professor: This is my solution, it may be correct, it may not be correct okay. I may have intentionally made a mistake. Do not trust me. These are my equations. I did not go further. But tell me what is the architecture?

Student: Shunt-series.

Student: Shunt-series.

Student: Shunt-series.

Professor: Are you sure?

Student: yes sir.

Professor: okay. Shunt-series. Now what is beta? What is the beta network? What is the beta network?

Student: R2 parallel RL.

Professor: Not parallel.

Student: RE parallel RF.

Professor: Yes, that is right. RE parallel RF. And beta would be found out as the current rising through RF divided by the voltage across RE. Is that clear? Okay.

Therefore beta would be simply  $-1$  by RF. With a little practice, you need not draw the beta circuit at all. And the rest of the solution (52:46).

Student: Sir, in the solution sir, for I2 you said it is 0.07 microampere + 200 microampere.

Professor: yes.

Student: Sir, you assumed that 200 microampere is straightaway going through the...

Professor: Partly going through the base of the 2 and partly going through the collector and you can show that they are some approximately equal. That is my solution. Okay.