

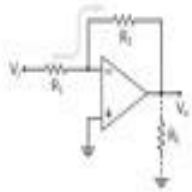
Basic Electronics
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Lecture – 50
Schmitt triggers

Welcome back to Basic Electronics. We will now start with a new topic namely op amp circuits based on positive feedback. First, we will take a qualitative look at positive and negative feedback and revisit our old (Refer Time: 00:34) inverting and non-inverting amplifiers in this context. We will then look at the Schmitt trigger circuit, which is based on positive feedback. Let us start.

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Feedback: inverting amplifier



$$V_o = A_o(V_i - V_-) \quad (1)$$

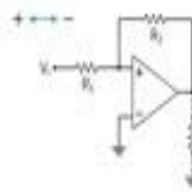
Since the Op Amp has a high input resistance, $i_+ = i_- = 0$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \frac{V_i \uparrow}{R_1} \rightarrow V_o \downarrow \rightarrow \frac{V_o \downarrow}{R_2}$$

Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.



$$V_o = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_2}{R_1 + R_2} \quad (3)$$

$$V_i \uparrow \rightarrow \frac{V_i \uparrow}{R_1} \rightarrow V_o \uparrow \rightarrow \frac{V_o \uparrow}{R_2}$$

Eq. 3 Eq. 1 Eq. 3

We now have a positive feedback situation. As a result, V_o rises (or falls) indefinitely, limited finally by saturation.

Let us now discuss feedback and our discussion will be qualitative in nature. And let us start with this inverting amplifier circuit, which we have seen before. And if you recall, we had mentioned earlier that these connections are very, very important. So, if you interchange the inverting and non-inverting terminals, the circuit would not work as an amplifier. And now let us see at least qualitatively, why it would not work as an amplifier.

Let us start with V_o equal to $A V_i$ times V_i plus minus V_o minus and this equation holds if the op amp is working in the linear region. Now, since the op amp has a high input resistance, this current is 0 and therefore, i_{R1} is equal to i_{R2} , this current and this

current are equal. And in this situation, we can obtain V_{minus} using super position and this is what we get. And from this equation, we note that if V_i increases or V_o increases, then V_{minus} will go up.

Now, let us perform a thought experiment, so to say in which V_i is increasing, so this voltage is increasing. As a result what happens to V_{minus} V_i appears here and that is increasing, so therefore, the equation two V_{minus} will also increase. Now, as V_{minus} increases by equation 1 V_o will decrease because this V_{minus} appears with a negative sign here and therefore, V_o decreases. If V_o decreases this term decreases and therefore, V_{minus} decreases, so that is what we have here. In other words, we have these opposing trends over here an increase in V_{minus} causes a decrease in V_{minus} . And this a negative feedback situation, which makes the circuit stable and therefore, we can proceed with the analysis that we carried out earlier.

Let us now consider this same circuit with the plus and minus terminals interchanged and see what happens. In this case, V_{plus} is given by this equation here similar to this equation. And now let us imagine that V_i have increased. What would happen as a result V_{plus} would increase by equation 3; if V_{plus} increases, V_o will increase by equation 1; and if V_o increases by equation 3 V_{plus} will increase. And now we see that this trend is the same V_{plus} increasing causes V_{plus} too increase further and this situation is called a positive feedback situation and what happens is as a result V_o rises or falls indefinitely limited finally, by saturation. So, V_o will reach either plus V_{sat} or minus V_{sat} . And of course, the circuit cannot be used any more as an amplifier.

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Feedback: non-inverting amplifier

$$V_o = A_o(V_i - V_-) \quad (1)$$

Since the Op Amp has a high input resistance, $i_+ = i_- = 0$ and we get

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i = \frac{V_o R_1}{R_1 + R_2} \rightarrow V_i = \frac{V_o R_1}{R_1 + R_2} \quad \text{Eq. 1}$$

The circuit reaches a stable equilibrium

$$V_o = V_i \frac{R_2}{R_1 + R_2} \quad (3)$$

$$V_i = \frac{V_o R_1}{R_1 + R_2} \rightarrow V_i = \frac{V_o R_1}{R_1 + R_2} \quad \text{Eq. 1}$$

We now have a positive feedback situation. As a result, V_o rises (or falls) indefinitely, limited finally by saturation.

Let us now look at the feedback in a non-inverting amplifier. Here is the circuit. Once again, we have V_o is equal to a V_i times V_o plus minus V_o minus and this V_o plus is the same as the V_i here. Since the op amp has a high input resistance this current is zero and i_{R1} is equal to i_{R2} . And in this case, V_o minus can be obtained simply by voltage division, so that is V_o times R_1 by R_1 plus R_2 that is our equation 2.

Now, let us imagine that V_i has increased V_i is as same as V_o plus. If V_o plus increases V_o will increase by equation 1; if V_o increases V_o minus increases by equation 2; if V_o minus increases because of this negative sign, V_o will decrease. And we see that this is a negative feedback situation because these trends are opposite. So, the circuit is stable and we can proceed with our analysis.

Let us now see what happens if we interchange the non-inverting and inverting terminals given by this circuit here. In this case, V_o plus is given by voltage division that gives us this equation 3. And let us now imagine that V_i have increased. What is V_i in this case V_i is same as the V_o minus. And if V_o minus increases because of this negative sign V_o will decrease like that; if V_o decreases V_o plus will decrease by equation 3; and if V_o plus decreases V_o will decrease by equation 1. So, clearly we have a positive feedback situation, because these trends are the same; a decrease in V_o will cause a further decrease in V_o , and as a result V_o will rise or fall indefinitely limited finally, by saturation. And this circuit of course cannot be used as an amplifier.

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Feedback

Inverting amplifier with $+ \leftrightarrow -$

Non-inverting amplifier with $+ \leftrightarrow -$

- Because of positive feedback, both of these circuits are unstable.
- The output at any time is only limited by saturation of the op-amp, i.e., $V_o = \pm V_{sat}$.
- Of what use is a circuit that is stuck at $V_o = \pm V_{sat}$? It turns out that these circuits are actually useful! Let us see how.

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Let us summarize. Here is the inverting amplifier with the plus and minus input terminals interchanged. And here is the non-inverting amplifier also with the plus and minus input terminals interchanged. And as we have seen both of these circuits are unstable because of positive feedback. And the output at any time then is only limited by saturation of the op amp. So, V_o here or V_o here will be plus minus V_{sat} . Now, the question is of what use is a circuit that is stuck at V_o equal to plus V_{sat} or V_o equal to minus V_{sat} . It turns out that these circuits are actually useful and let us see how.

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Inverting Schmitt trigger

$V_{sat} = 10V$

Because of positive feedback, V_o can only be $+V_{sat}$ (if $V_i > V_{i+}$) or $-V_{sat}$ (if $V_i < V_{i-}$).

Consider $V_i = 5V$

Case (I): $V_o = +V_{sat} = +10V \rightarrow V_i = \frac{R_1}{R_1 + R_2} V_o = \frac{1k}{1k + 9k} \cdot 10V = 1V$.
 $(V_i - V_{i+}) = (5 - 1) = +4V \rightarrow V_o = -V_{sat}$
 This is inconsistent with our assumption ($V_o = +V_{sat}$)

Case (II): $V_o = -V_{sat} = -10V \rightarrow V_i = \frac{R_1}{R_1 + R_2} V_o = \frac{1k}{1k + 9k} \cdot (-10V) = -1V$.
 $(V_i - V_{i-}) = (5 - (-1)) = +6V \rightarrow V_o = -V_{sat}$ [consistent]

If we move to the right (increasing V_i), the same situation applies, i.e., $V_o = -V_{sat}$.

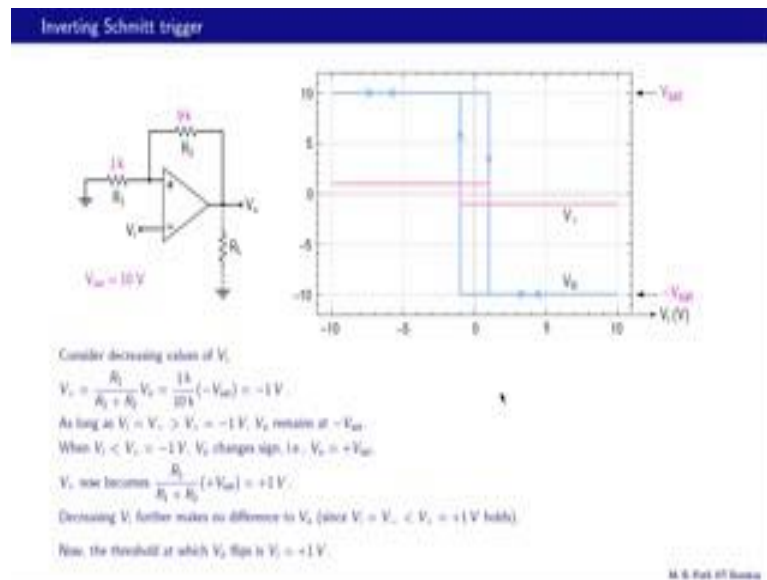
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Let us look at the circuit, which is our non-inverting amplifier with the plus minus inputs interchanged. R_2 is 9 k, R_1 is 1 k and we were assumed V_{sat} to be 10 volts. Now, as we have seen because of positive feedback V_o can only be either plus V_{sat} or minus V_{sat} ; it will be plus V_{sat} if V_{plus} is greater than V_{minus} ; otherwise it will be minus V_{sat} .

Now, let us take an example. So, V_i is equal to 5 volts. So, we have 5 volts here, and figure out whether the output would be plus V_{sat} or minus V_{sat} . Let us take case one first in which V_o is plus V_{sat} . So, we have 5 volts here, we have 10 volts here; if this is 10 volts then by voltage division this V_{plus} would be 1 k divided by 10 k times 10 volts or 1 volt. And the situation now is V_{plus} is 1 volt V_{minus} is 5 volts. So, V_{plus} is smaller than V_i or V_{minus} , and therefore V_o should actually be minus V_{sat} . So, clearly there is an inconsistent situation here, and therefore this cannot happen. So, what happens in this case is V_o is equal to minus V_{sat} , and let us check quickly whether that is consistent or not.

So, we have 5 volts here, minus 10 volts here. And by voltage division V_{plus} would be minus 10 times 1 by 10 or minus 1 volt. So, V_{plus} is minus 1 V_{minus} is 5, and therefore, V_o would be minus V_{sat} and everything is consistent. Let us show that data point on this plot here. What are we plotting, we are plotting V_{plus} as well as V_o as a function of V_i . And right now we have only one data point that is V_i equal to 5; for V_i equal to 5, we have V_{plus} equal to minus 1 volt; and V_o equal to minus 10 volts that is the same as minus V_{sat} . And if we move to the right that is increasing V_i , the same situation applies and V_o remains equal to minus V_{sat} as shown here. So, in this entire range, V_o remains equal to minus V_{sat} and V_{plus} remains equal to minus 1 volt.

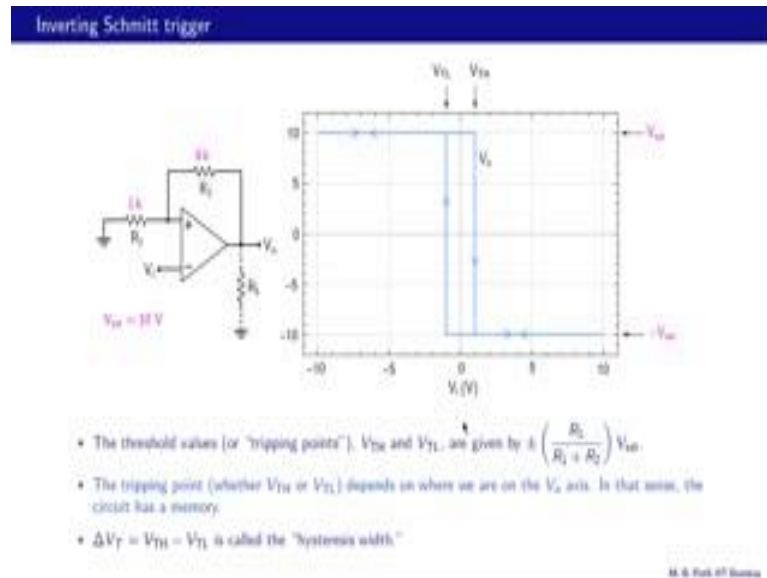
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So, we have got this part of the V_o versus V_i relationship. And now let us consider decreasing V_i so that means we are going in that direction. And V_+ as we have seen is $V_o \times \frac{R_1}{R_1 + R_2}$; and since V_o is minus V_{sat} V_+ is minus 1 volt and that is what we have shown here as well. Now, as long as V_i which is same as V_+ remains greater than V_i V_o will remain at minus V_{sat} , and what is V_+ V_+ is minus 1 volt. So, up to this point, things will not change. If V_i is decreased further that means it goes below V_+ which is minus 1 then V_o will change sign, V_o will become plus V_{sat} and that is shown over here. And if V_o changes V_+ also changes, it will now become $\frac{R_1}{R_1 + R_2} \times \text{plus } V_{sat}$ or plus 1 volt. So, V_+ has also changed from minus 1 volt to plus 1 volt here.

And if we go on decreasing V_i further, what happens this V_+ is equal to 1 volt and we are decreasing this V_i further. So, nothing is going to really change, because V_+ will remain larger than V_i and that is what we get if we go on decreasing V_i . Now, the threshold that which V_o flips is plus 1 volt. So, now imagine that we are increasing V_i in that direction and V_+ is sitting at 1 volt when V_i crosses that 1 volt the output is going to change again like that. So, that is our V_o versus V_i relationship and we see this strange plot here which is called hysteresis.

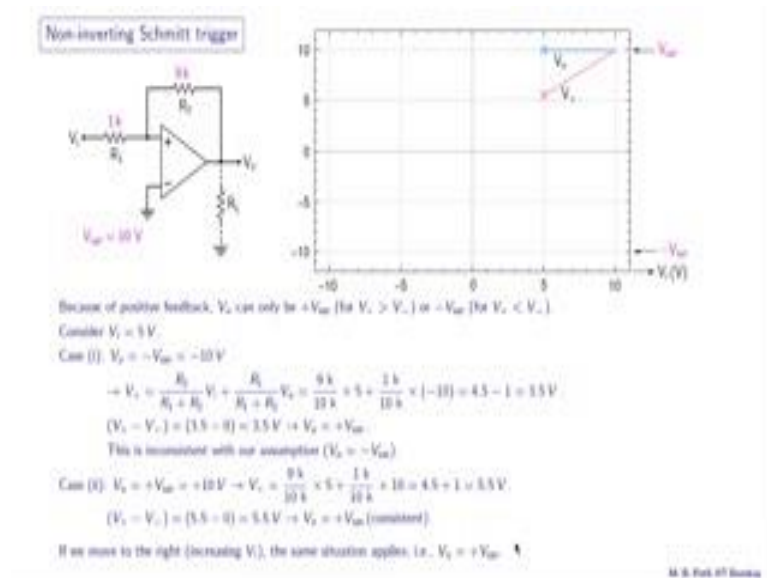
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Here is the V_o versus V_i relationship again and this circuit is called the inverting Schmitt trigger. And let us summarize the salient features now. First, there are these threshold values - lower threshold and higher threshold. The lower threshold is called V_{TL} and the higher threshold is called V_{TH} . And these threshold values are also called tripping points denoted by V_{TH} and V_{TL} . And as we have seen in the last slide, they are given by plus minus R_1 by R_1 plus R_2 times V_{sat} . Now, which tripping point applies really depends on where we are on the V_o axis and that is a big difference between this circuit and other circuits, we have seen earlier.

For example, if we are here then the tripping point that is relevant is this one - V_{TH} , and that is also the reason we have used these arrows here. If you are here and we keep reducing V_i now then the tripping point that is relevant is this one - V_{TL} . So, in that sense, the circuit has a memory, because its behavior depends on the past. What is the past that is whether V_o has high earlier or whether V_o was lower? And this quantity ΔV_t which is the difference between the V_{TH} and V_{TL} is called the hysteresis width, this width here.

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Let us now look at the non-inverting Schmitt trigger which is obtained from an inverting amplifier by interchanging the inverting and non-inverting op amp inputs like that. And as we said earlier because of positive feedback V_o can only be either plus V_{sat} or minus V_{sat} , plus V_{sat} if V_+ is larger than V_- and minus V_{sat} otherwise. So, let us take an example say V_i equal to 5 volts, and see whether V_o is expected to be plus V_{sat} or minus V_{sat} in this case. Suppose V_o is minus V_{sat} , so this V_o is minus 10 volts, what is V_+ then this current is 0, and V_+ can be obtained by super position.

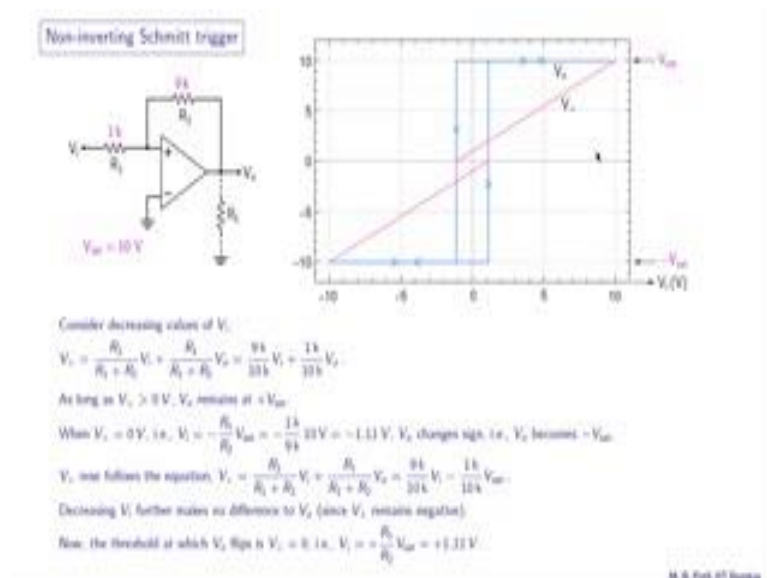
So, we have V_i here and V_o here, consider these two as independent voltage sources, and then we get this expression here. So, R_2 by R_1 plus R_2 times V_i plus R_1 by R_1 plus R_2 times V_o , R_2 is 9 k R_1 plus R_2 is 10 k. So, 9 k by 10 k times V_i which is 5 volts plus R_1 1 k R_1 plus R_2 10 k times V_o , V_o we have assumed to be minus 10 volts, minus 10, so that turns out to 3.5 volts. So, V_+ minus V_- is 3.5 minus 0, so obviously, V_+ is greater than V_- , and therefore V_o must be plus V_{sat} . And clearly there is some inconsistency here because we started assuming V_o equal to minus V_{sat} and we ended up with V_o equal to plus V_{sat} . So, clearly this is not going to happen.

So, what does happen is V_o becomes equal to plus V_{sat} that is plus 10 volts and let us now check whether that is consistent. So, let us first find V_+ from this same

expression here 9 k by 10 k again times V_i which is 5 volts plus 1 k by 10 k times V_o which is 10 volts , so that turns out to be 5.5 volts . So, V_{plus} is 5.5 , V_{minus} is 0 . So, therefore, V_o is plus V_{sat} and that is consistent with our original assumption. So, that is the data point not over here V_o is 10 for V_i equal to 5 volts , and at that input voltage V_{plus} is 5.5 .

Now, if move to the right that is in the direction of increasing V_i . What do we expect to happen, it turns that V_o remains equal to plus V_{sat} of course, V_{plus} is not constant anymore because V_{plus} varies as V_i varies. So, the relationship between V_{plus} and V_i is a straight line and the slope is positive and that is what we get. And now what we want to do is as we decrease V_i , we want to see what happens.

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Now, let us see what we expect as V_i is decreased, V_{plus} is going to decrease, because as we saw in the last slide V_{plus} is proportional to V_i . And at some point, V_{plus} would become negative and at that point V_o will flip from plus V_{sat} to minus V_{sat} , and let us see when that happens. So, consider decreasing values of V_i , V_{plus} the same expression as we saw earlier R_2 by R_1 plus R_2 times V_i plus R_1 by R_1 plus R_2 times V_o . So, that is 9 by 10 times V_i plus 1 by 10 times V_o .

Now, as long as V_{plus} is positive V_o will remain equal to plus V_{sat} like that and that happens up to this point. So, V_{plus} is positive just positive at this point. And if we decrease V_i further in that direction, then V_{plus} is going to cross 0 , and then V_o is

going to flip from plus V_{sat} to minus V_{sat} . And when does that happen, when does V_{plus} become 0; for V_{plus} to become 0; this expression has to become 0 and that gives us V_i equal to minus R_1 by R_2 times V_{sat} which is minus 1 by 9 times 10 or minus 1.11 volts.

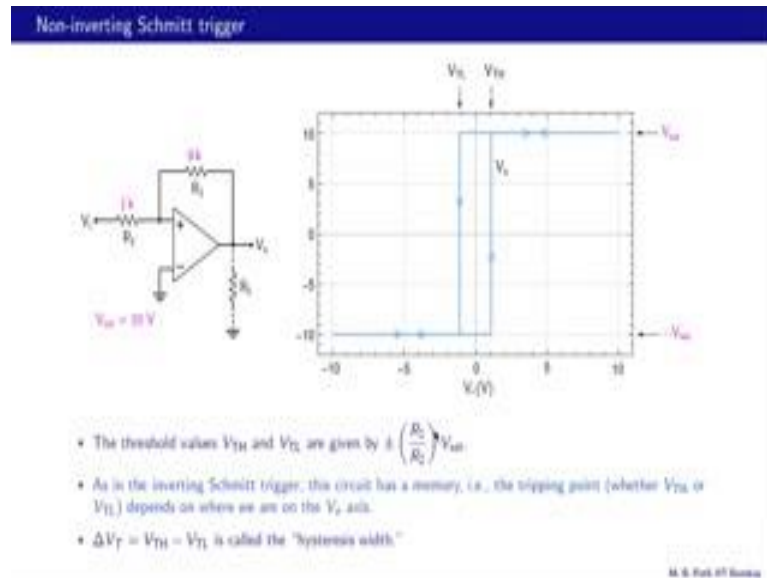
So, when V_i is minus 1.11 volt then V_o changes sign that is it goes from plus V_{sat} to minus V_{sat} . So, this is how V_o has changed from plus V_{sat} to minus V_{sat} . What about V_{plus} , V_{plus} is given by this equation, the same equation as this one except, now V_o has become minus V_{sat} . At this point, V_i is minus 1.11 volt as we saw earlier. So, this term is already negative and this term is also negative now, because V_o is minus V_{sat} . So, the net result is at this point V_{plus} is a negative number, we can calculate that.

So, now what happens as we continue to decrease V_i further in that direction V_{plus} is proportional to V_i . So, as V_i is decreased V_{plus} will also decrease and at this point V_{plus} is already negative. So, what will happen V_{plus} will keep going down, it will become more and more negative as V_i is decreased. If V_{plus} continues to be negative that is less than V_{minus} , V_o will then continue to be minus V_{sat} and we would expect V_o to stay at minus V_{sat} .

And let us now look at the equation that V_{plus} will follow in this region. V_{plus} is given by this expression same as this one except now V_o has become minus V_{sat} . So, we have V_{plus} equal to 9 by 10 times V_i minus 1 by 10 times V_{sat} . So, V_{plus} versus V_i is still a straight line with a positive slope, but now the x intercept has changed. So, we will now have this line here and its x intercept will be somewhere here like that.

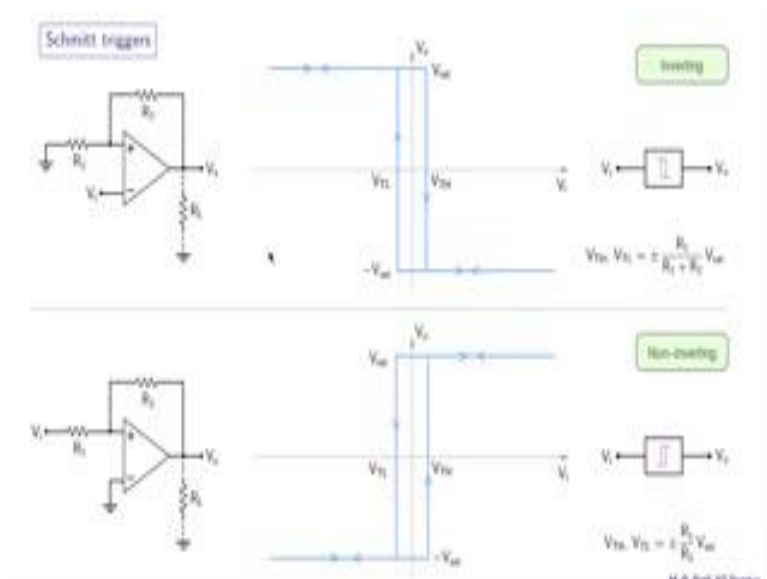
Now, let us consider V_i increasing. So, we go in that direction now. And V_{plus} will also increase and at some point V_{plus} will cross 0 and that is where V_o will flip from minus V_{sat} to plus V_{sat} . And what is V_i at that time. So, what is the threshold that is given by V_{plus} equal to 0. So, we have 0 equal to 9 by 10 times V_i minus 1 by 10 times 10. So, V_i turns out to be R_1 by R_2 times V_{sat} or plus 1.11 volts like that. And now if we keep increasing V_i , V_o will not change and we have completed the V_o versus V_i picture.

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Let us summarize the situation for the non-inverting Schmitt trigger. Here are the threshold values V_{TH} and V_{TL} ; V_{TH} is given by plus R_1 by R_2 times V_{sat} , and V_{TL} is given by minus R_1 by R_2 times V_{sat} . And as in the inverting Schmitt trigger this circuit also has memory. Why do we say that? Because the tripping point or the threshold point depends on where we are in this V_o versus V_i plane. If we are here and if we are increasing V_i then the tripping point is V_{TH} . If we are here and if we are decreasing V_i then the tripping point is V_{TL} and that is indicated by the arrows here. Once again ΔV_T equal to V_{TH} minus V_{TL} is called a hysteresis width.

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Here is a summary of both types of Schmitt triggers which we have seen inverting and non-inverting. The inverting Schmitt trigger is denoted by this symbol here; and the non-inverting Schmitt trigger by this symbol; essentially this symbol comes from the V_o versus V_i relationship. The V_{TH} , V_{TL} expressions are also included here. And it is a good idea to turn off your monitor at this point. Draw the circuits, go through the derivation in your mind and come up with the V_o versus V_i relationship for each of these Schmitt triggers. And also remember to derive the expressions for V_{TH} and V_{TL} rather than remembering these.

To summarize we have started looking at a different class of circuits in this lecture. In contrast to the circuits we have seen earlier the circuits we have seen today, the Schmitt trigger circuits are based on positive feedback. In the next class we will look at some applications on the Schmitt trigger, until then goodbye.