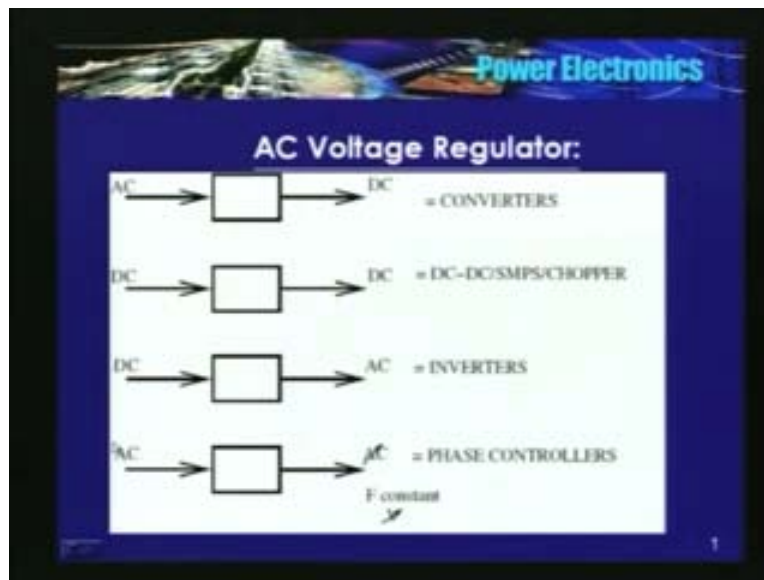


**Power Electronics**  
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**Indian Institute of Technology, Bombay**  
**Lecture - 43**

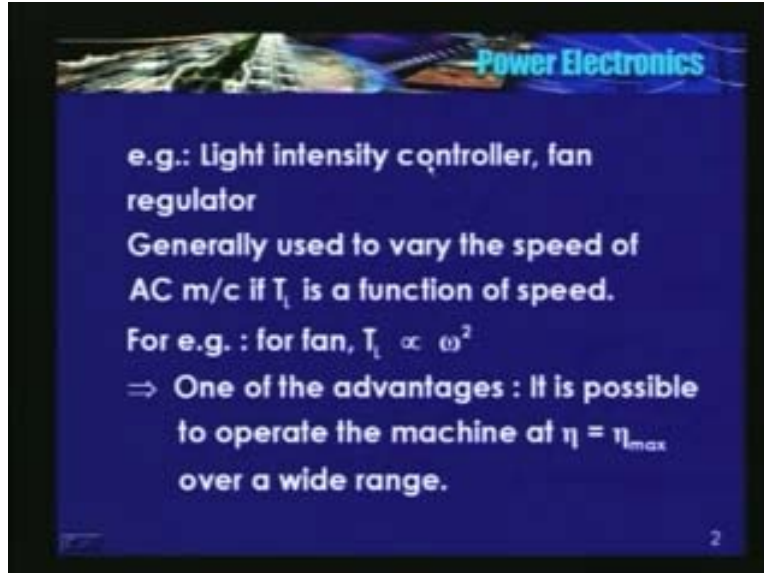
Hello, today probably I will be concluding lecture of my course on power electronics. I will try to cover AC voltage regulators. Input is AC, output is also AC. Frequency of input and output is the same, only the magnitude of output voltage is varied.

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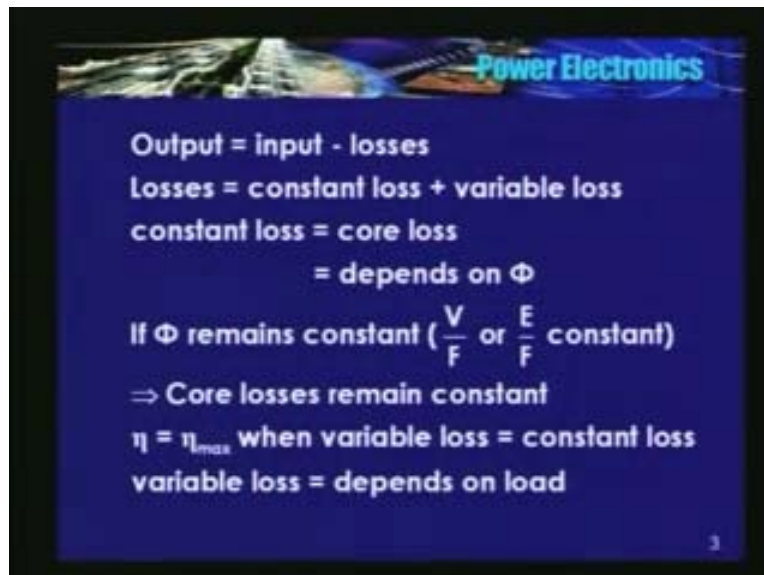
See here, we are here; input is AC, output is also AC. Frequency constant, variable voltage. They are known as AC voltage regulators **AC voltage regulators**.

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Where are they used? They are very popular in fan regulators, light intensity controllers. I have told you that if the induction machine is driving a fan type of load, the speed can be varied over a wide range by varying the magnitude of the input voltage frequency being the same. The type of load is fan type of load wherein  $T_L$  is proportional to omega square. What is another advantage? It is possible to operate the machine at maximum efficiency over a wide range.

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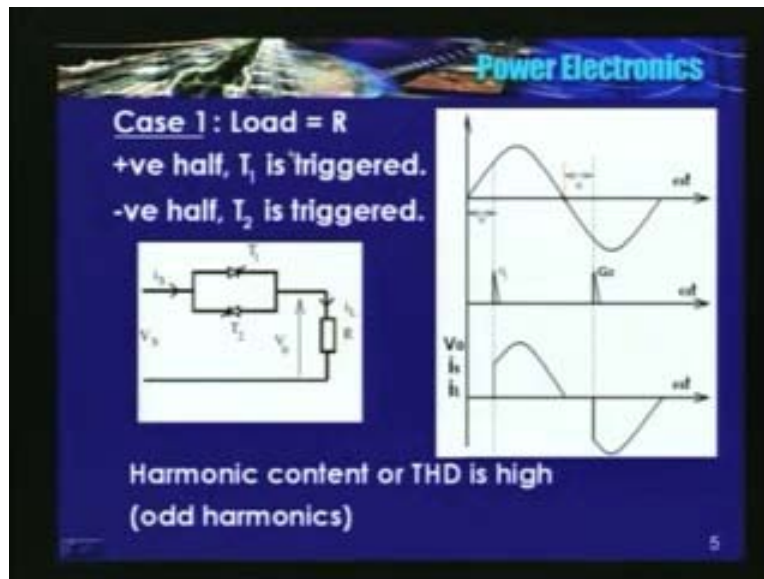
How is that possible? Let us see here. We all know that output is equal to input minus losses. Now, what are the losses? There are 2 types; one is constant loss plus the variable loss. Constant

loss is I will name them as core loss. They depend on flux. Frequency remains constant here, so it depends on flux. Flux in the machine remains constant if  $V$  by  $F$  or  $E$  by  $F$  is held constant. That we had seen while doing inverters. So, if flux remains constant; core loss in the machine, they remain constant. So, when does the efficiency of the motor is equal to the maximum efficiency? It is when the constant losses equal to the variable loss. The variable loss depends on load. Basically, they are  $I^2 R$  losses. Now, if the load and the machine comes down,  $I^2 R$  losses also comes down.

So, how do I operate the machine at  $\eta$  is equal to  $\eta_{max}$ ? What do I need to do is as the load comes down you reduce the flux such that motor operates at maximum efficiency. You have to reduce the flux such a way that constant losses is equal to the variable losses. So, in principle using the phase regulators or AC voltage regulator, it is possible to maximize the efficiency at light loads.

If I keep the frequency constant and try to reduce the voltage, we had seen that flux in the machine comes down, it reduces. Therefore, core losses reduces. Variable losses are the function of load. Since the load is reducing;  $I^2 R$  losses, they come down. Efficiency is maximum when core loss is equal to the variable loss. So, in principle it is possible to maximize the efficiency at loads. Why I am saying in principle? The reason I will tell you some time later.

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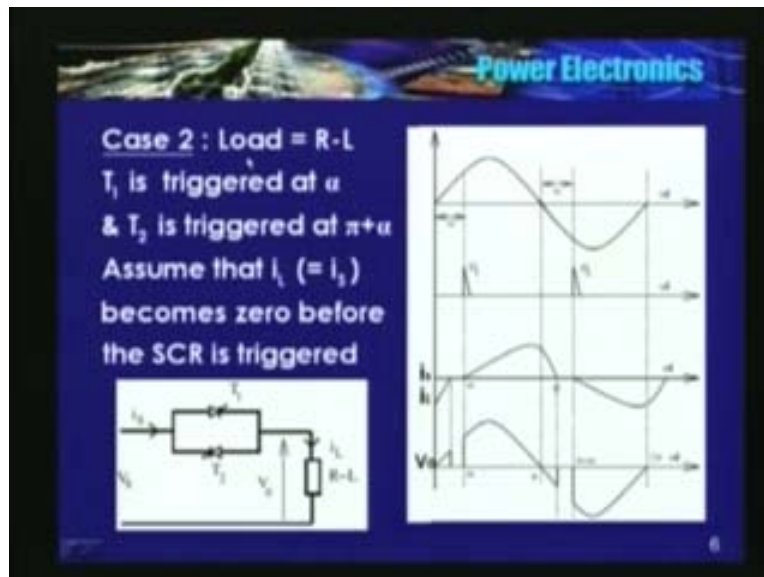
So, case one; load is purely resistive, input is single phase AC. I have used 2 SCRs,  $T_1$  and  $T_2$ . They are connected anti parallel. Now, you can replace this combination by a triac; the device which is used in fan regulators. I had shown the fan regulator also the device during my introductory lectures.

So, load is purely resistive. So, this is the input voltage, this sinusoidal. In the positive, half  $T_1$  is triggered at  $\alpha$ . Gate pulse to thyristor 1 and in the negative half cycle,  $T_2$  is triggered at an

angle  $\alpha$ . When  $T_1$  is triggered, input voltage  $V_s$  is equal to output voltage. Load is purely resistive, current and voltage are in phase. So, the waveform of source current which is equal to the load current is same as  $V_0$  itself. So, input voltage become 0 at  $\omega T$  is equal to  $\pi$ . At that instant, even  $V_0$  becomes 0,  $I_s$  also become 0, the load current also will become 0. I am assuming the device is ideal.

So, from  $\omega t$  is equal to  $\pi$  to  $\pi + \alpha$ , there is no current flowing in the circuit. Load is purely resistive that is the reason and at again at  $\pi + \alpha$ ,  $T_2$  is triggered and negative voltage is applied to the load. So, what is the limitation of this sort of a control? Harmonic content is high, is an odd function. Source current as well as the load current, they have all odd harmonics and they give rise to heating in the load and in the source side, they affect the voltage at the point of common coupling, I have told you that. Effect of harmonics I have discussed during my converters lecture. If there are harmonics in the line due to the finite impedance of the line voltage at the common point of coupling, it gets affected.

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Now, we will take a second case. Load is RL. Things are not as straight forward as when the load is purely resistive.  $T_1$  is triggered at  $\alpha$  and again  $T_2$  is triggered at  $\pi + \alpha$  and I am making another assumption; assume that  $i_L$  that is equal to the source current become 0 before the SCR is triggered.

I will repeat; the assumption is  $i_L$  become 0 before the SCR is triggered. So, load is passive at  $\alpha$   $T_1$  is triggered. So, when  $T_1$  starts conducting, input voltage is same as the load voltage. So, voltage is applied to RL load. Now, **it is** the circuit equation is  $R$  into  $i$  plus  $L$  di by dt is equal to  $V_m \sin \omega t$ .

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When thyristor is conducting

KVL gives  $L \frac{di}{dt} + Ri = V_m \sin \omega t$

$$i = \frac{V_m}{Z} \sin(\omega t - \phi) + Ae^{-\frac{t}{\tau}}$$
$$Z = \sqrt{R^2 + (\omega L)^2}, \quad \phi = \tan^{-1}\left(\frac{\omega L}{R}\right) \quad \& \quad \tau = \frac{L}{R}$$

$i = 0$  at  $\omega t = \alpha$

$$i = \frac{V_m}{Z} \left[ \sin(\omega t - \phi) - \sin(\alpha - \phi) e^{-\frac{R}{L}(\omega t - \alpha)} \right] \text{-----(1)}$$

See, I will show the equations. **These are** this is the equation. The solution looks like this or solution can be given by this equation  $V_m$  by  $Z \sin \omega t$  minus  $\phi$  plus  $A$  into  $e$  to the power minus  $t$  by  $\tau$ . We have derived this equation in the very first lecture in converters where  $Z$  is equal to square root of  $R$  squared plus  $\omega L$  square.  $\phi$  is  $\tan$  inverse  $\omega L$  by  $R$  and  $\tau$  is  $L$  by  $R$ .

So, how do I determine the value of  $A$ ? The boundary condition is  $i$  is equal to 0 at  $\omega t$  is equal to  $\alpha$ . I had told you that current becomes 0 much before the thyristor is triggered. Substituting or using this condition, I can solve the equation. I will get the expression for current. It is given by this equation;  $V_m$  by  $Z$  into  $\sin \omega t$  minus  $\phi$  minus  $\sin \alpha$  minus  $\phi$  into  $e$  to the power  $R$  by  $L$  into  $\alpha$  by  $\omega$  minus  $t$ . So, this is the equation for current. So, there is a sinusoidal component and a decaying component.

So, the current wave form looks something like this. It starts from 0, it attains a peak somewhere in between  $\pi/2$  to  $\pi$ . It attains a peak when instantaneous value of the input voltage is equal to  $R$  into  $i$ . When  $i$  is equal to  $i_{\max}$   $L \frac{di}{dt}$  is 0. So, at that time  $V_i$  should be equal to  $i_{\max}$  into  $R$ . Somewhere here, it attains a max. It reduces and it becomes 0 somewhere after  $\pi$  and till the current is flowing in the circuit, input voltage is equal to the output voltage. So, at  $\beta$ , current becomes 0 and till another thyristor is triggered that is  $T_2$  is triggered at  $\pi$  plus  $\alpha$ , there is no current flowing in the circuit **there is no current flowing in the circuit**.

See, from  $\beta$  to  $\alpha$  or  $\pi$  plus  $\alpha$ , there is no current and therefore there is no voltage and at  $\pi$  plus  $\alpha$ , you trigger  $T_2$  and whatever that happened in the positive half will happen in the negative half. Actually, this should continue beyond  $\beta$  here. See, current becomes 0; **that I have shown you** I have shown this waveform here. Actually, this part should come here. So, whatever that happened from  $\pi$  to  $\beta$  will happen from  $2\pi$  to  $\beta$ .

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Assume that at  $\omega t = \beta$ ,  $i = 0$

$$\therefore \sin(\beta - \varphi) = \sin(\alpha - \varphi) e^{i\left(\frac{\alpha - \beta}{\omega}\right)} \text{----- (2)}$$

If  $\alpha = \varphi$  equation (1) gives

$$i = \frac{V_m}{Z} \sin(\omega t - \varphi)$$

$\Rightarrow$  Sinusoidal 'i' lags V by  $\varphi$

Equation (2) gives

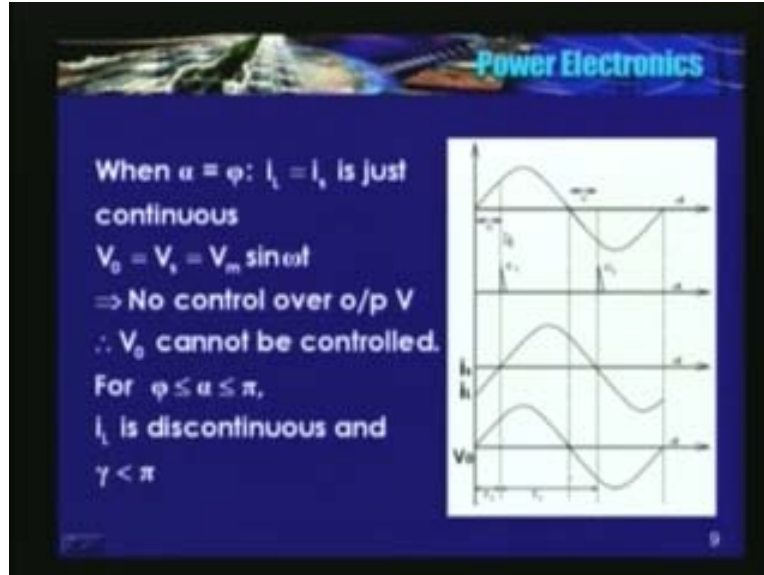
$$\sin(\beta - \alpha) = 0 \quad \therefore (\beta - \alpha) = \pi$$

$\Rightarrow$  Conduction angle  $\gamma = \pi$  rad

Now, see this is the equation. Assume that at  $\omega t$  is equal to  $\beta$ ,  $i$  will again become 0. So, you substitute this condition in the previous equation. So, what do I get? You will get  $\sin \beta$  minus  $\varphi$  is equal to  $\sin \alpha$  minus  $\varphi$  in this term. Now, if  $\alpha$  is equal to  $\varphi$ , in other words, if the trigger angle is same as the power factor angle, what does the equation 1 say? It says that this term will become 0.

So, you have the current which is given by  $V_m$  by  $Z$  into  $\sin \omega t$  minus  $\varphi$ . Current is sinusoidal **current is sinusoidal**, lacks the input voltage by an angle  $\varphi$  **which is given** which is equal to the impedance angle. So, if trigger angle  $\alpha$  is equal to **the if** the power factor angle; current is sinusoidal, lacks the input voltage by an angle  $\varphi$  which is equal to the power factor angle. How does the voltage and current look like?

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See here, trigger angle alpha is equal to phi, current is sinusoidal. Now, current is sinusoidal. That means either it has to flow through either  $T_1$  or  $T_2$ . So, you will have the input voltage is same as the output voltage. The **output load** applied voltage to the load is sinusoidal and it is equal to the input voltage  $V_i$  itself.

Therefore,  $V_o$  is equal to  $V_s$  is equal to  $V_m \sin \omega t$ . There is no control over the output voltage, whatever is there at the input appears at the output. Current is sinusoidal, lacks the voltage by an angle phi because SCR is triggered at an angle alpha which is equal to phi. The previous case, we saw current most discontinuous current was discontinuous. This can happen only when alpha is greater than the power factor angle.

I will repeat; current is discontinuous when alpha is greater than the power factor angle. So, this is the condition. When alpha is equal to phi,  $i_L$  is equal to  $i_s$ , it is just continuous and  $V_o$  is equal to  $V_i$ . At this instant,  $T_1$  is triggered. It continues to conduct till pi plus alpha. At that instant current becomes 0. So,  $T_1$  turns off. Immediately  $T_2$  is triggered. So, it goes on. So, output voltage cannot be control or in other words, **input volt** output voltage is equal to the input voltage. Whereas, if alpha greater than phi,  $i_L$  is discontinuous. See, current become 0 here and thyristor may be triggered somewhere here, current starts increasing. So, **this for** during this period you will not have any current. So, during this direction  $T_1$  is conducting and the conduction period for each device is pi radians **pi radians**.

So, we have seen in a **in a** AC voltage regulator you can control the output voltage if the trigger angle alpha is greater than the power factor angle. Current is discontinuous, current is just continuous and it is sinusoidal if the trigger angle alpha is equal to the power factor angle. Output voltage is equal to input voltage. There is no control over the output voltage. Conduction period for each thyristor is pi radians. Now, what happens if alpha is less than phi?

If  $\alpha$  is less than  $\phi$ ,  $V_0$  and  $i_L$  do not vary with  $\alpha$ . In the positive half, you might have triggered  $T_1$  at  $\alpha$  and  $\alpha$  is less than the power factor angle. Current is negative and cuts the 0 axis at  $\phi$ . So, even if you have triggered  $T_1$ , it will not carry the current or current will not flow through it because current is negative. See here, current is negative only when it cuts the X axis. This current starts flowing through  $T_1$  and this instant is fixed by the power factor angle  $\phi$ . So, till  $\phi$ , current is negative. So, even if you try to trigger  $T_1$ , it will not carry the current **it will not carry the current**. This current is being carried by  $T_2$ .

So, if there is just a sharp pulse as I shown here and if your trigger angle  $\alpha$  is less than the power factor angle, there may not be any current because there is only 1 sharp pulse. Current is negative, it is flowing through  $T_2$ . It has to become 0 and that instant is fixed by the power factor angle. We know that in SCR gate **gate** signal should be present till the current through it is higher than the latching current. There is only one pulse and that has come much before current becoming 0 and then it has to become positive.

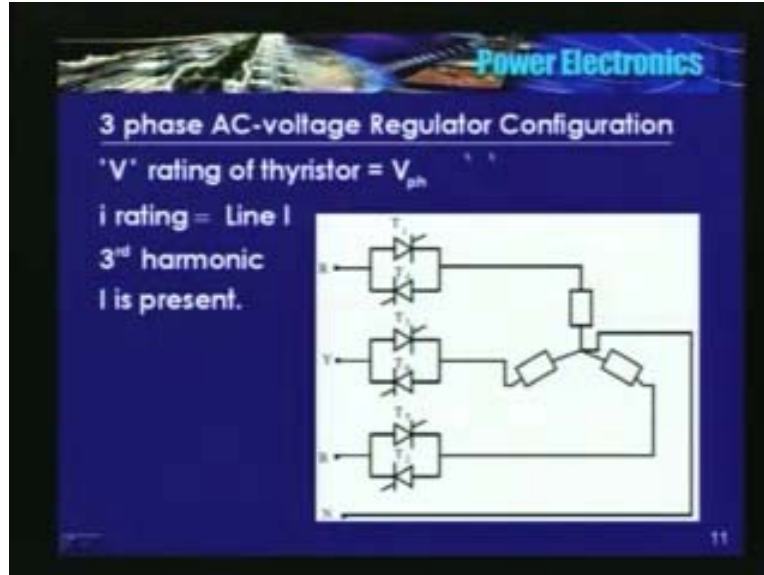
So, there may not be any current or  $T_1$  may not go into conduction. So, you need to have a series of large number of pulses. Till  $\omega t$  is equal to  $\phi$ , in other words till  $\omega t$  is equal to  $\phi$ , you should have or there should be triggered pulses. Only then you will have a sinusoidal current and a sinusoidal voltage applied to the load. So, even if you trigger at  $\alpha$  which is less than the power factor angle, change over from one device to another device will take place only at  $\omega t$  is equal to  $\phi$ .

To achieve that you need to have a series of pulses. There should be a gate pulse present at  $\omega t$  is equal to  $\phi$ , a theoretical element. Of course, it is always preferred to have pulses beyond  $\omega t$  is equal to  $\phi$ . So, there is a control over the output voltage for  $\alpha$  greater than  $\phi$ . For  $\alpha$  equal to  $\phi$  and  $\alpha$  less than  $\phi$ , there is no control over the output voltage. Both voltage and current, they are sinusoidal. Current lags the voltage by an angle  $\phi$ .

So, that is about the single phase AC voltage regulators: the principle that is used to control the speed of a ceiling fan or light intensity controller. Now, how about controlling the speed of a 3 phase induction machine or a 3 phase load? What are the possible circuit configurations? I will show you.



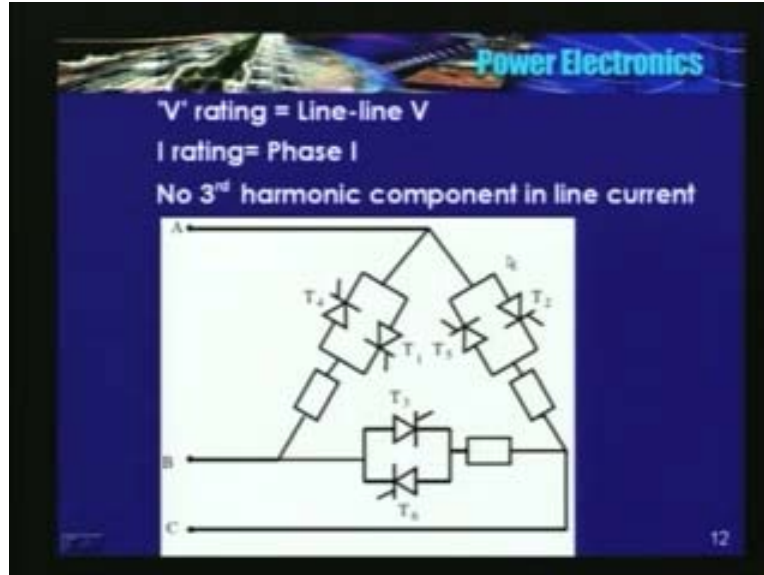
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There are various configurations, numerous. I will just show you very few. There are 3 bands here, see, numbering is the same as what we did in 3 phase AC to DC converters. 3 phase bridge  $T_1 T_4, T_3 T_6, T_5 T_2$  or say  $T_1 3, 5, 4, 6, 2$  and load is star connected and the neutral wire, the star point is connected to the neutral. I have told you that in single phase load current which is equal to the source current is an odd function. There are all odd harmonics.

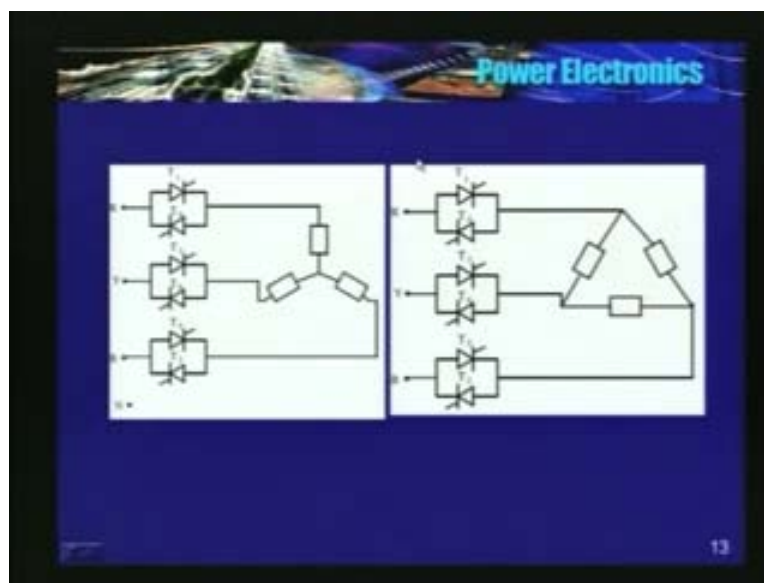
How about in 3 phase? We know that in 3 phase 4 wire system, a current that is flowing in the neutral wire is minus of  $i_A$  plus  $i_B$  plus  $i_C$ . So, all the triplen harmonics or third harmonic currents will flow through this wire because the fundamental component that is  $i_A \sin \omega t, \sin \omega t \text{ minus } 120, \sin \omega t \text{ minus } 240$ ; the some of these component, the fundamental component will be 0. Whereas, third harmonic component, they add up and they will flow through this line because  $\sin 3 \omega t$ , here  $\sin 3 \text{ into } \omega t \text{ minus } 120$  that is  $360$  that is equal to  $\sin 3 \omega t$  itself and same here. So, all triplen harmonics will flow through this. So, you will have triplen harmonics in the line current. So, voltage rating of each thyristor is a phase voltage and current rating is the line current that is flowing. Because it is a 3 phase 4 wire system, you will have a third harmonic current here.

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Now, when the load is connected in delta? This could be one of the configurations. Again, back to back 3 bands; these are 3 loads, they are connected in each phase. What happens here? The current through the SCR is the phase current but then the voltage is the line to line voltage. But then you will not have third harmonic current in the line. In the previous case, because there is a neutral you will have third harmonic currents in the line. But in a 3 phase 3 wire system no triplen harmonics.

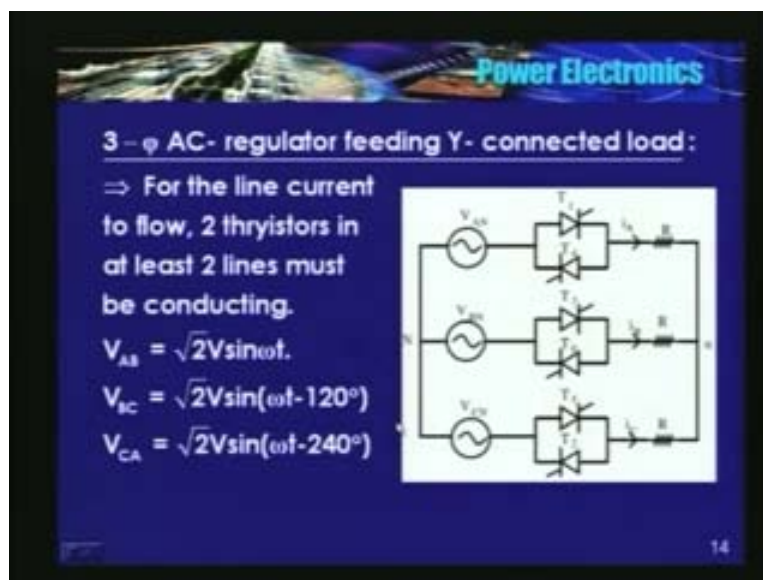
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So, this is another configuration. Another 3 bands **connecting**, feeding a star connected load, isolated neutral **isolated neutral**. Now, there are no triplen harmonics here, no triplen harmonics because if I apply KCL at this point;  $i_A$  plus  $i_B$  plus  $i_C$  **should be equal to** it should be 0. Now, we found that third harmonic components;  $\sin 3 \omega t$ , this also will be  $\sin 3 \omega t$  itself because 3 multiplied by 120 is 360 that is again 0. This is also  $\sin 3 \omega t$ . So, **they will** they are in phase. They add up here. So, KCL fails. So therefore, you will not have triplen harmonics in this case. So, **if you** there will be triplen harmonics if there is a fourth wire.

Now, same as before we have connected this band outside, not in series with the load. There are various possible configurations. We will analyze one of them: a 3 phase AC regulator feeding a star connected load.

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Let me tell you one thing; analysis of 3 phase AC voltage regulator is bit difficult compared to a 3 phase AC to DC converter. So, that is a reason I will use a resistive load. I will not analyze the circuit for a RL load. So, this is the possible configuration; AN BN CN are the phase voltages, a 3 phase resistive load, star connected and you have 3 pairs of back to back connected SCRs.

In this circuit, for the current to flow in the load, 2 thyristors at least 2 thyristors in two different phases should be on. So, if  $T_1$  is on, current can flow through  $T_6$  or  $T_2$ . So, this is the condition: for the line current to flow, 2 thyristors in at least two lines must be conducting. Now, for the analysis I will take the line voltages as the reference. So, I will take  $V_{AB}$  as root 2 V sin omega t. BC lagging AB by 120 degrees and CA by 240 degrees.

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**Reference point for  $\alpha$  :**

$$V_m = \sqrt{\frac{2}{3}} V \sin(\omega t - \frac{\pi}{6})$$

$\alpha$  is delay by phase control in relation to natural operation that would occur without switches in circuit and source supplies a purely 'R' load.

The slide contains three diagrams: a circuit diagram of a three-phase bridge rectifier with a purely resistive load, a vector diagram showing the phase relationship between  $V_{AB}$ ,  $V_{AN}$ , and  $I_A$ , and a small diagram showing the reference point for  $\alpha$  at the zero crossing of the line-to-line voltage  $V_{AB}$ .

Now, what is the reference point for alpha or where do I start measuring alpha from? What did you do in 3 phase AC to DC rectification? We took the point of natural commutation as the reference point. Now here, the reference point is taken as I will show you, see, here it is mentioned alpha is a delay by a phase control in relation to the natural operation that would occur without switches in circuit and source supply a purely a resistive load.

It is like this. What this sentence means is I have a 3 phase voltages, load is purely resistive, alpha is the instant where  $I_A$  cuts the X axis or a 0 axis and becomes positive. That is the reference point. I will repeat; so reference point alpha is **when** in this circuit  $i_A$  become 0 and becomes positive goes positive. So, when does it occur? I have defined  $V_{AB}$  line to line voltage as root to  $V \sin \omega t$ .

So, we know that phase voltage lacks the line voltage by 30 degrees. So, it is like this. So,  $V_{AN}$  is given by this equation - minus pi by 6. So, in the vector diagram if I draw  $V_{AB}$  is here,  $V_{AN}$  is lacks by 30 degrees and this current is in phase with the phase voltage. So,  $i_A$ . So, reference point for alpha is 30 degrees from the 0 crossing of the line to line voltage  $V_{AB}$ . I will repeat; reference point for alpha is 30 degrees from the 0 crossing of the line to line voltage.

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$\Rightarrow \alpha = 0$ , when +ve zero crossing of  $i_A$  takes place.

$\Rightarrow \omega t = \frac{\pi}{6}$ .

$\therefore$  For any value of  $\alpha$ ,  $\alpha = \omega t - \frac{\pi}{6}$

$\Rightarrow$  Gating signals of the thyristors in 3 branches must have same sequence & phase displacement as the source voltage.

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Now, I will show you, see here, alpha is 0 when positive 0 crossing of  $i_A$  takes place. That is omega t is equal to pi by 6. So therefore, for any value of alpha; that is this, omega t minus pi by 6. Now, what is another condition? We all know that a 3 phase supply is being applied to a 3 phase load, voltages have to be balanced. So, the gating signals for the thyristors in 3 branches must have the same sequence and the phase displacement as the source voltages. See here, gating signals of the thyristors in 3 braches must have the same sequence and phase displacement as the source voltage.

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$\Rightarrow$  If  $\alpha$  for  $T_1, T_2 = \alpha + \frac{2\pi}{3}$ ,  $T_3 = \alpha + \frac{4\pi}{3}$

$T_4 = \pi + \alpha$ ,  $T_5 = \alpha + \frac{2\pi}{3} + \pi$ ,  $T_6 = \alpha + \frac{4\pi}{3} + \pi$

$= \alpha - \frac{\pi}{3}$   $= \alpha + \frac{\pi}{3}$

No. of devices conducting at a time?

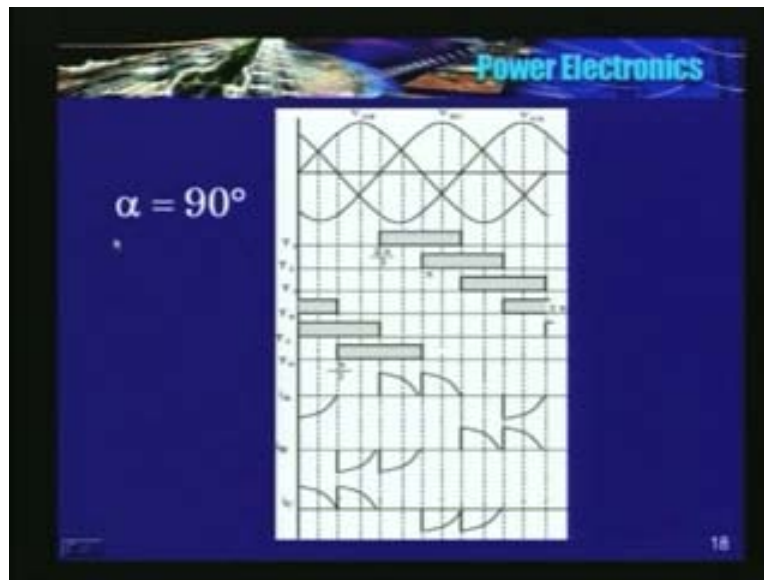
$\alpha = 90^\circ$

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What does it mean? It is this. If alpha for  $T_1$ , so  $T_3$  is connected to B phase. So, alpha plus 2 pi by 3 and  $T_5$  and alpha plus 4 pi by 3 and  $T_4$  is anti parallel with the  $T_1$ , it is pi plus alpha. For  $T_6$ , this angle plus pi and  $T_2$  this angle plus pi. These are the angles. So,  $T_1$  is triggered at alpha,  $T_2$  is triggered at alpha plus pi by 3 - 60 degrees,  $T_3$  is triggered at alpha plus 2 pi by 3 - 120 degrees,  $T_4$  alpha plus 5,  $T_5$  alpha plus 4 pi by 3 because pi plus alpha plus 60 degrees it is this and so on.

Now, coming to the number of devices conducting at a time; things were straight forward in AC to DC conversion with 0 source inductance. That means there is no overlap, commutation overlap here. At any given time 2 devices were conducting. Things are not very straight forward in AC voltage regulators. I will just show you 2 different cases: alpha is 90 and in another case is alpha is 30.

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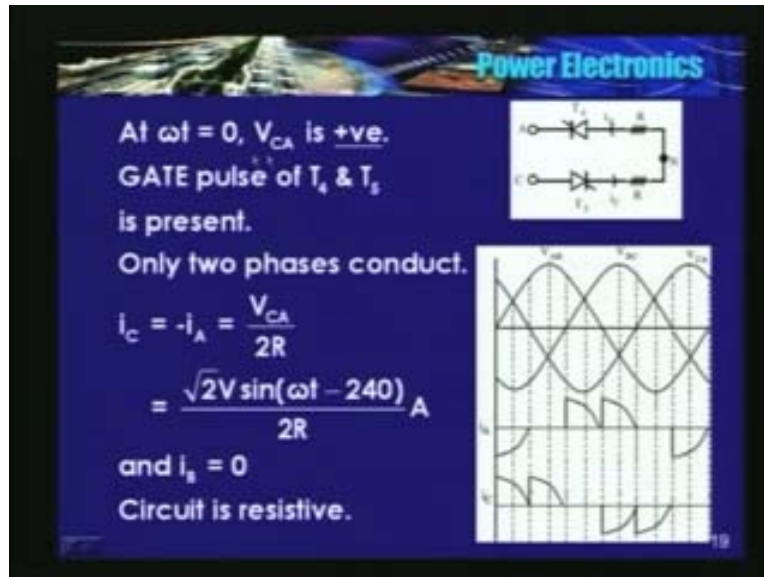


For alpha is equal to 90 degree; see, I have drawn the line to line voltages  $V_{AB}$ ,  $V_{BC}$  and  $V_{CA}$ . Alpha is 90 degrees, reference point for alpha is this point. Wherein, this point is 30 degrees from  $V_{AB}$ , pi by 6. So, this is the reference point. From here 90 degrees: wherein, you will trigger  $T_1$ . So, if this is this is 30; 60, 90. At this point,  $T_1$  is triggered. I will not tell you the width of the pulse at the gate right now. Maybe sometime later I will tell.

After 60 degrees  $T_2$  is triggered and again after 60 degrees  $T_3$  is triggered and again at 60 degrees  $T_4$  is triggered and again at 60 degree is  $T_5$  is triggered and this  $T_5$  this is 2 pi, just see here. This is this wave form has completed one cycle. In case of  $V_{AB}$  has completed one cycle. At that instant  $T_5$  is getting triggered. So, this point is same as this and after 60 degrees from here,  $T_6$  will get triggered. Now, since the width of the gate pulse would be anything. So, I have drawn even  $T_4$  here. See, it has started from here. It is 2 pi; I can continue in this direction, instead of continuing in this direction I have drawn it here.

Now, if you see at the 0 crossing  $\omega t$ ,  $T_4$  and  $T_5$  are gated or there triggered pulse exists for  $T_4$  and  $T_5$  and  $V_{CA}$  is positive  $V_{CA}$  is positive; 4 and 5 there are trigger pulses, can they conduct? Let us see the equivalent circuit.

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At  $\omega t$  equal to 0,  $V_{CA}$  is positive. Gate pulses for  $T_4$  and  $T_5$  is present. Now,  $V_{CA}$  is positive; 5 connected in this manner, 4 is connected in this manner. Resistive load current can flow, current can flow in this direction because  $V_{CA}$  is positive. Nothing happens in B phase because sixth that is connected. See here, nothing happens in B phase here. Sixth that is connected gets trigger pulse after some time. So, only 2 phases are conducting, only 2 phases and what is the equation for current?

$i_C$  is equal to minus  $i_A$   $i_C$  is equal to minus  $i_A$ . It is given by  $V_{CA}$   $V_{CA}$  divided by  $2R$ . Two circuits are in series, I am neglecting the drop. So,  $V_{CA}$  is this waveform. Magnitude of current is divided by  $2R$ . So, almost the same waveform; magnitude could be different, that is all. Same waveform as  $V_{CA}$ , current  $i_C$  and  $i_R$   $I_A$ .  $I_A$  is negative but  $i_C$  is positive. Now, what happens at  $\omega t$  is equal to  $\pi$  by 3?

At  $\omega t$  equal to  $\pi$  by 3,  $V_{CA}$  is 0 and becomes negative. That means potential of A is higher than potential of C. Resistor circuit, current cannot flow in this direction. So, at this point,  $T_4$  turns off and if you see the previous waveform, see at this point, I had stopped the gate pulses for  $T_4$  because no point having gate pulses beyond this point. But if you see at that point itself,  $T_6$  is getting triggered  $T_6$ . At this point,  $T_6$  is getting triggered.

Now,  $T_5$  is connected to C phase, 6 is connected to B phase. See the circuit configuration, it is something like this; C, B - 6 and 5. Now, current can flow in this direction, provided,  $V_{CB}$  is positive.  $V_{CB}$  should be positive, only then you can have current in this way. Now, let us see what happens. See here,  $V_{BC}$  is negative. So,  $\omega t$  equal to  $\pi$  by 3,  $V_{BC}$  is negative.

Therefore,  $V_{CB}$  is positive. So,  $V_{CB}$  is positive, therefore **and** current can flow and what is that current?  $i_C$  is equal to minus  $i_B$  equal to  $V_{CB}$  divided by  $2R$ .

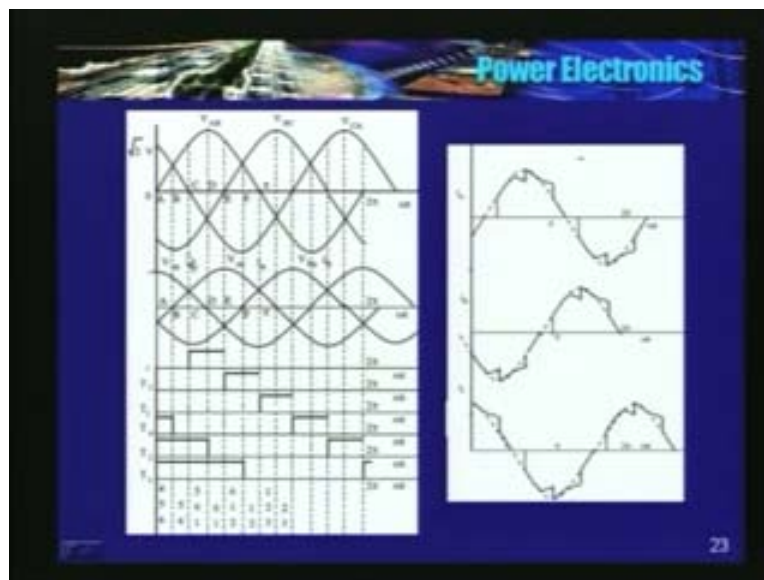
Now,  $V_{BC}$  is  $V_m \sin \omega t$  minus 120 degrees. For CB, I am adding 180 degrees because we have defined AB, BC and CA. So, divided by  $2R$  and  $I_A$  is equal to 0 and what is this value of current? This value of current, you need to substitute  $\omega t$  is equal to 60 degrees. So, you will get the value of this current by substituting it here. That is the value of  $i_C$ .

So, where does  $T_5$  stop conducting? Now, at  $\omega t$  is equal to  $2\pi$  by 3,  $V_{BC}$  becomes 0 or  $V_{CB}$  become 0 and  $V_{BC}$  becomes positive. In other words,  $V_{CB}$  becomes negative.  $T_5$  has to turn off at this point because see in this direction, current to flow in this way, C should be at a higher potential than B. So, that means  $V_{CB}$  should be positive. So, when it is 0,  $T_5$  turns off. Where does it become 0? At this point, it becomes 0. So, at that point,  $i_C$  or  $T_5$  turns off.

So till here, I have shown the gate pulses for  $T_5$ , see this figure. See here, at this point I have shown the trigger pulses for 5 and that point,  $T_1$  gets triggered  **$T_1$** , 1 and 6 will conduct, **1 and 6**, voltage is  $V_{AB}$ . See, I will show you; 1 and 6 **1 and 6**; same thing that we did for 4 and 5, 5 and 6 and 1 and 6. So, at any given time, only 2 thyristors are conducting where  $\alpha$  is equal to 90 degrees.

Now, we will see for  $\alpha$  is equal to 30 degrees, what does it? So, here are for  $\alpha$  is equal to 90 degrees, I have shown you the line voltages, gate pulses and currents. Only 2 phases carry current at a time, one phase is open **one phase is open**. See, there is no current here. Now, for  $\alpha$  is equal to 30 degrees. Now, I have shown here; in addition, I have shown you the phase voltages also.

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Phase voltages as well as the line to line voltages. Alpha is equal to 30 is somewhere at this point. This alpha is equal to 30 degrees. There is  $T_1, T_2, T_3, T_4, T_5, T_6$ . Now, if you see in this figure, at  $\omega t$  is equal to 0;  $T_4$  is getting a trigger pulse,  $T_5$  is getting a trigger pulse,  $T_6$  is getting a trigger pulse. Now, can they conduct? See, if you see the equivalent circuit;  $T_4$  is connected like this,  $T_5$  is connecting in this fashion,  $T_6$  is connected in this fashion.

Now, you can have a current flowing from  $T_5$  to  $T_4$ , provided,  $V_{CA}$  is positive  **$V_{CA}$  is positive**. Yes, in this region  $V_{CA}$  is positive,  **$C_A$  is positive**. You can have current flowing from  $T_5$  to  $T_6$ , provided,  $V_{CB}$  is positive. Yes,  $V_{BC}$  is negative. So therefore,  $V_{CB}$  is positive. So therefore,  $T_4, T_5, T_6$  can conduct because all the conditions are satisfied. They are getting trigger pulses, they are forward biased. Since all 3 phases are conducting, I need to use the rule **that is** which is used in 3 phase circuits that  $i_A + i_B + i_C$  should be equal to 0.

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**Power Electronics**

$\alpha = 30^\circ$   
 at  $\omega t = 0$  (point A)  
 $T_4, T_5,$  and  $T_6$  have been triggered.  
 $V_{CA}$  is +ve.  $\rightarrow T_4, T_5$  can conduct.  
 $T_6$  can conduct if  $V_{CB}$  is +ve.  
 ( $V_{BC}$  is -ve &  $V_{CB}$  is +ve)  
 $\rightarrow$  all the phases are conducting.  
 $\therefore i_A + i_B + i_C = 0$   
 $i_C = -(i_A + i_B)$

So,  $i_C$  is equal to minus of  $i_A$  plus  $i_B$  and where does  $i_A$  becomes 0? See here,  $i_A$  becomes 0 at this point where  $V_{AN}$  becomes 0 **where  $V_{AN}$  becomes 0**. At this point,  $i_A$  becomes 0. So, when  $i_A$  become 0,  $T_4$  turns off. So, at  $\omega t$  is equal to  $\pi/6$ ,  $V_{AN}$  becomes 0. Therefore,  $i_A$  becomes 0,  $T_4$  turns off. Now,  $T_1$  is getting triggered at this point. See, alpha is measured with respect to this point at 30 degrees. See,  $T_1$  is getting triggered at this point.

So, for **the first** sometime of 30 degrees, only 5 and 6 are conducting. What is the condition for 5 and 6 to conduct? 5 is connected to C phase, 6 is **conducted** connected to B phase.  $V_{CB}$  should be positive  **$V_{CB}$  should be positive**. See here, this is  $V_{BC}$ . So,  $V_{BC}$  is negative. Therefore,  $V_{CB}$  is positive. So, they can conduct; 5 and 6 can conduct at this point. Now, the circuit equation is  $i_C$  is equal to minus  $i_B$  and current is  $V_{CB}$  divided by  $2R$ . So, the current waveform is see in this region, 0 to  $\pi/6$   $i_A + i_B + i_C$  is equal to 0. See,  $i_A$  is negative,  $i_B$  is also negative and  $i_C$  is positive.

Now, from  $\pi/6$  to  $\pi/3$ ,  $I_A$  is 0 and at that time,  $i_C$  is equal to minus of  $i_B$ . This is correct. At  $\omega t$  is equal to  $\pi/3$ ,  $T_1$  is triggered. Now, what happens? Now, the circuit diagram is something like this;  $T_1$  is triggered, now current can flow from  $T_1$  to  $T_6$  if  $V_{AB}$  is positive. Yes, it is;  $V_{AB}$  is positive  **$V_{AB}$  is positive.**

See, **at this** this is a line to line voltage. Reference point is alpha is equal to 0. This is the point alpha 30 is this. So **this** beyond,  $V_{AB}$  is positive. Now, current flow in this way,  $V_{CB}$  also should be positive. Yes, see here, this is  $V_{BC}$ , we are somewhere in this zone. Now,  $V_{BC}$  is negative, therefore  $V_{CB}$  is positive.  $V_{BC}$  is negative, therefore  $V_{CB}$  is positive. So therefore, it is possible. So, current will start flowing in this direction. So, in this mode 3 thyristors are conducting. What are they?  $T_1$ ,  $T_5$  and  $T_6$ . This continues for another 30 degrees. At that time, after 30 degrees,  $T_5$  turns off. Why? When 3 thyristors are conducting, I need to use this same rule;  $i_A$  plus  $i_B$  plus  $i_C$  should be equal to 0. So, if any one of the phase voltage has become 0, at that time the thyristor which is connected to that phase should turn off.

See, I will show you the phase voltages. After 30 degree, somewhere at this point, see  $V_{CN}$  is becoming 0  **$V_{CN}$  is becoming 0.** So,  $T_5$  turns off  **$T_5$  turns off.** So, I have stopped or this is the boundary for  $T_5$  gate pulses. So remember, if 3 thyristor are conducting, I need to use  $i_A$  plus  $i_B$  plus  $i_C$  is equal to 0, load is resistive. So, till the phase voltage becomes 0, the equivalent circuit which consists of 3 thyristors is valid. The moment the one of the phase voltage is becomes 0, the thyristor which is connected to that phase turns off and till the new thyristor is triggered, only two of them will be carrying current and this principle you need to use to analyze 3 phase AC voltage regulators.

It is not very straight forward as compared to a 3 phase AC to DC bridge rectifiers. That is the reason I told you this is not very straight forward but then it is not very difficult either. With that I conclude my lecture on power electronics. For the last 43 lectures or so, I have tried to give you just the overview of the power electronics. Subject is really vast. I encourage you people to take up a good text book. Fortunately, a large number of very good text books are available which was not the case during my under graduate days. Not many books on power electronics were available which is not the case now. Large number of very good books are available. Pickup a book, a good book on power electronics and start reading it. Only then, the efforts which have taken will bear fruit.

Thank you and good luck to all of you.