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Lecture – 59 Attribute Selection Measures in CART – II

In this lecture, we are going to see how to select attributes in CART model. In our previous lectures, we have seen how to choose attributes by using gain value. In this lecture, there are another two methods for choosing the attributes. One is gain ratio; another one is Gini index. This lecture we are going to see other two criteria for choosing the attributes.

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Gain Ratio

- · The information gain measure is biased toward tests with many outcomes
- · That is, it prefers to select attributes having a large number of values
- For example, consider an attribute that acts as a unique identifier, such as product ID.
- A split on product ID would result in a large number of partitions (as many as there are values), each one containing just one tuple

First, we will look at the Gain ratio. The information gain measure is biased towards tests with many outcomes. That is, it prefers to select attributes having a large number of values. For example, consider an attribute that act as a unique identifier, such as product ID. (Refer Slide Time: 01:41)

Gain Ratio

- Because each partition is pure, the information required to classify dataset D based on this partitioning would be Info product ID(D) = 0
- Information Gain = Info D- Info product ID(D) = maximum
- Therefore, the information gained by partitioning on this attribute is maximal
- Clearly, such a partitioning is useless for classification
- Gain ratio is an extension to information gain which attempts to overcome this bias

A split on product ID would result in a large number of partitions as many as there values each one containing just one tuple because each partition is pure, the information required to classify dataset D based on this partitioning would be Info product ID will be 0, because there might be only one value in each partition. So Information gain is we know the formula, the formula for information gain is Info D – Info product ID D because this value is going to be 0, so the information gain will be maximum.

Therefore, the information gained by partitioning on this attribute is maximal. Clearly, such partitioning is useless for classification, because there are going to be one element for each partition. So, the gain ratio is an extension to information gain, which attempts to overcome this bias.

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Split information

• It applies a kind of normalization to information gain using a "split information" value defined analogously with Info(D) as:

$$SplitInfo_{\underline{\Lambda}}(D) = -\sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times \log_2\left(\frac{|D_j|}{|D|}\right)$$

- D_i= single partion
- D = Data set
- This value represents the potential information generated by splitting the training data set, D, into v partitions, corresponding to the v outcomes of a test on attribute A

Let us see what is split information. It applies a kind of normalization to information gain using a split information value defined analogously with Info D. So, how to find out the split info for level for D is – summation j = 1 to v, v is different levels. Dj divided by D, multiplied by log Dj divided by D to the base 2. Here the Dj is the single partition. In the next example, I will explain the Dj. D is dataset. So, this value that is the split info represents the potential information generated by splitting the training data set D into v partitions, corresponding to the v outcomes of test on attribute A.

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Gain ratio Gain ratio differs from information gain, which measures the information with respect to classification that is acquired based on the same partitioning The gain ratio is defined as GainRatio(A) = Gain(A) / SplitInfo(A) The attribute with the maximum gain ratio is selected as the splitting attribute

So, let us see the formula for the gain ratio. The gain ratio differs from the information gain, which measures the information with respect to classification that is acquired based on the same partitioning. So, the gain ratio is Gain of A divided by Split Info of A. The attribute with the maximum gain ratio is selected as the splitting attribute. I have an example; with that I can explain how to use this gain ratio for choosing the attribute.

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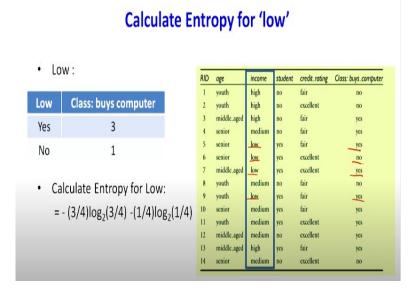
Gain Ratio example

Consider the previous example	RID	age	income	student	credit_rating	Class: buys_computer
for computation of gain ratio	1	vouth	high	no	fair	no
for the attribute income	2	youth	high	no	excellent	no
for the attribute income	3	middle_aged	high	no	fair	yes
 A test on income splits the 	4	senior	medium	no	fair	yes
	5	senior	low	yes	fair	yes
data of the following Table into	6	senior	low	yes	excellent	no
three partitions, namely low,-	7	middle_aged	low	yes	excellent	yes
	8	youth	medium	no	fair	no
medium, and high, containing	9	youth	low	yes	fair	yes
four, six, and four	10	senior	medium	yes	fair	yes
	11	youth	medium	yes	excellent	yes
tuples, respectively	12	middle_aged	medium	no	excellent	yes
	13	middle_aged	hiġh	yes	fair	yes
an, J., Pei, J. and Kamber, M., 2011. Data mining: concepts and chniques. Elsevier.	14	senior	medium	no	excellent	no

Look at this example. In my previous lecture, I was showing this dataset. Consider in our previous example for computation of gain ratio for the attribute income. So, we are going to take this variable first. We are going to find out gain ratio. I am going to say the procedure for only one attribute, like that you have to try for age attribute, for student attribute, for credit rating attribute.

Whichever is high that variable should be chosen for classification. A test on income splits the data into following table into three partitions. See, when you look at this income column, there are three levels, one is low, medium, and high containing in low, there are 6 element is there, in medium 6 is there, in high there is 4. This example is taken from the book data mining concepts and techniques and compare.

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Now, let us calculate the Entropy for level low. In level low, how many have answered yes to by computer when it is low. So how many people have answered low. When the level is low, so the entropy is -3/4, log 3/4 to the base $2 - 1/4 \log 1/4$ to the base 2.

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Calculate Entropy for buying class D

- Calculate information:
- = $-p_v \log_2 (p_v) p_n \log_2 (p_n)$
- Where p_v is probability of yes and p_n is probability of no

$$Info(D) = -\frac{9}{14}\log_2\left(\frac{9}{14}\right) - \frac{5}{14}\log_2\left(\frac{5}{14}\right) = 0.940$$
 bits.

For finding the information gain for the attribute income, first we need to know the entropy for the class D. We know that how to find the entropy for the class D. It is – py log py to the base 2 – pn log pn to the base 2. So, the py is in our class, how many people have answered yes. When you look at the table, there was 9 yes and there is 5 no. So, for s it is 9 / 14, log 9 / 14 to the base 2 minus no. There is 5 no, so it is 5 no, so 5 / 14, log 5 / 14 to the base 2 equal to 0.940 bits.

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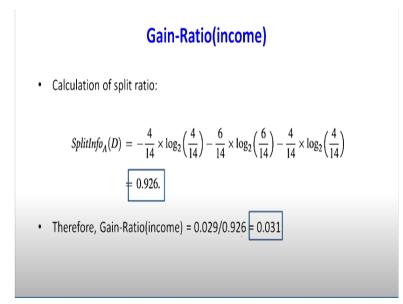
Gain of income

- The expected information needed to classify a tuple in D if the tuples are partitioned according to income is:
- $Info_{income}(D) = (4/14) (-(2/4)log_2(2/4) (2/4)log_2(2/4)) + (6/14) (-(4/6)log_2(4/6) (2/6)log_2(2/6)) + (4/14) (-(1/4)log_2(1/4) (3/4)log_2(3/4)) = 0.911 bits$ Gain of income : $Info(D) - Info_{income}(D) = 0.94 - 0.911 = 0.029$

Now, let us find out the information gain for the attribute income. What is the meaning is, if you use income as an attribute for the classification, how much information you can gain. So the expected information needed to classify a tuple in D if the tuples are partitioned according to income is, so Info for attribute income is 4 / 14, we got this 4 for the attribute income, there was three levels low, medium, and high.

In low, there was a 4, in medium there was 6, and in high there was 4 values. So, it is a kind of weighted attributed, because it is nothing but expected information needed. So, it is nothing but our weighted entropy. So, the weighted entropy is 0.911 bits. So, the gain of income is Info D – Info for the attribute income. So, we got this 0.94, which we got from this value, 0.94 - 0.911 = 0.029.

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Now, we will go for split ratio. So, the split ratio is equal to -4/14 multiplied log 4/14 base 2-6/14, log 6/14 to the base $2-4/14 \log 4/14$ to the base 2. So, split info is 0.926. Therefore, the Gain-Ratio for the attribute income is 0.029/0.926 is equal to 0.031. (Refer Slide Time: 09:05)

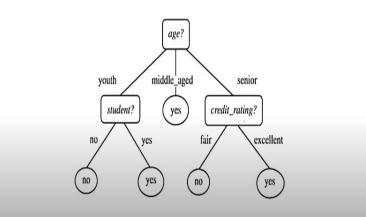
Interpretation

- Further we calculate the same for the rest 3 criteria (age, student, credit rating)
- The one with <u>maximum Gain ratio value will</u> results in the maximum reduction in impurity of the tuples in D and is returned as the splitting criterion

Further, we calculate the same for the rest of 3 criteria, what are the other three attributes, age is there, student is there, credit rating is there. The one with the maximum Gain ratio value will result in maximum reduction in impurity of the tuples in D and is returned as the splitting criterion. So, what we have to do, we have seen for one attribute that is income. There are another 3 attributes, such as age, student and credit rating. For these attributes also, we have to find out the information gained ratio.

That corresponding attribute should be taken as the splitting criterion. We have found the Gain ratio for the attribute income. The same way, there are other attributes like age, student and credit rating. For these attributes also, we have to find out the Gain ratio. One with the maximum gain ratio value will result in maximum reduction and impurities of the tuples in D and is written as the splitting criterion.

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For example, assume that the attribute age is having maximum gain ratio, so that variable should be chosen as the splitting variable. Then from there, if there is a student, assume that the attribute age is having highest gain ratio, so that age is taken as the splitting variable. Then, there is a student. There are remaining other variables, for example, student, credit rating and so on. So, out of these, again you have to find the Gain ratio. So, out of this, which one is giving the maximum Gain ratio, that should be taken as the splitting criterion.

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Decision tree using Gini index

	Let's take the Introduction of	RID	age	income	student	credit_rating	Class: buys_computer
		1	youth	high	no	fair	no
	a decision tree using Gini	2	youth	high	no	excellent	no
	index	3	middle.aged	high	no	fair	yes
		4	senior	medium	no	fair	yes
•	Let D be the training data of	5	senior	low	yes	fair	yes
	the following table	6	senior	low	yes	excellent	no
	the following table	7	middle.aged	low	yes	excellent	yes
		8	youth	medium	no	fair	no
		9	youth	low	yes	fair	yes
		10	senior	medium	yes	fair	yes
	Pei, J. and Kamber, M., 2011. Data mining: concepts and ues. Elsevier.	11	youth	medium	yes	excellent	yes
ermide	res. usever.	12	middle.aged	medium	no	excellent	yes
		13	middle.aged	high	yes	fair	yes
		14	senior	medium	no	excellent	no

Next, we will go to another criterion for choosing the attribute, that is Gini index. Let us take the introduction of decision tree using Gini index. Let D be the training data of the following table. So, this data also taken from the book data mining, concepts and techniques, the source is given here. Now, we are going to see how to find out the Gini index.

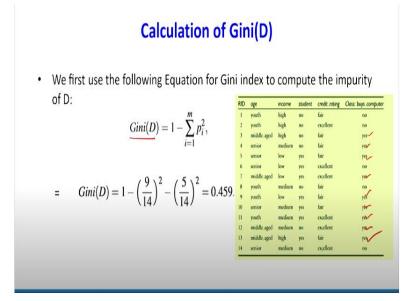
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Example

- · In this example, each attribute is discrete-valued
- Continuous-valued attributes have been generalized
- The class label attribute, buys computer, has two distinct values (namely, {yes, no}); therefore, there are two distinct classes (that is, m = <u>2</u>)
- Let class C₁ correspond to 'yes' and class C₂ correspond to 'no'.
- There are nine tuples of class 'yes' and five tuples of class 'no'.
- A (root) node N is created for the tuples in D

In this example, each attribute is discrete-valued because all are in different category, so continuous-valued attributes have been generalized. We did not take continuous value. The class label attribute, buy computer, has two distinct values, yes or no, therefore, there are two distinct classes, m = 2. Let class C1 correspond to yes and class C2 correspond to no. There are nine tuples of class yes and five tuples of class no. A root n is created for the tuples D.

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Now, we go for calculation of Gini index. We first use the following equation for Gini index to compute the impurity of D. So, first we will find out the Gini of class D is 1 - summation of i =1 to m, m is number of levels, pi square. So, what is the p, how many s is there. So, 1 - 9/14 whole square, how many no is there, next level, so the Gini of class D equal to 1 - 9/14 whole square -5/14 whole square, that is 0.459.

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Gini index for income attribute

- Lets calculate Gini index for income attribute
- To find the splitting criterion for the tuples in D, we need to compute the Gini index for each attribute
- Let's start with the attribute income and consider each of the possible splitting subsets
- Income has three possible values, namely {low, medium, high}, then the possible subsets are {low, medium, high}, {low, medium}, {low, high}, {medium, high}, {low, high}, {medium, high}, {low}, {medium}, {high}, and {}
- · Power set and empty set will not be used for splitting

Let us calculate, Gini index, previously found the Gini, the Gini index for income attribute. To find the splitting criterion for the tuples in D, we need to compute the Gini index for each attribute. In this, you take an example, income. Let us start with the attributes income and consider each of the possible splitting subsets. Incomes has three possible values, namely low, medium, high.

The possible subsets are low, medium, high, then all possible combinations low and medium, low and high, medium and high, then values which is having one value in the set, low, medium, high and null set. Power set and empty set will not be used for splitting. What is the power set where all the element is there, for example, low, medium, high is the power set, the null set is nothing but the empty set.

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Consider the subset{low,	RID	age	income	student	credit_rating	Class: buys_computer
	1	youth	high	no	fair	no
medium}	2	youth	high	no	excellent	no
This would result in 10 tuples	3	middle.aged	high	no	fair	yes
	4	senior	medium	no	fair	yes
in partition D1 satisfying the	5	senior	low	yes	fair	yes
condition "income ∈{low,	6	senior	low	yes	excellent	no
	7	middle.aged	low	yes	excellent	yes
medium}"	8	youth	medium	по	fair	no
The remaining four tuples of D	9	youth	low	yes	fair	yes
	10	senior	medium	yes	fair	yes
(high) would be assigned to	11	youth	medium	yes	excellent	yes
partition D2	12	middle.aged	medium	no	excellent	yes
	13	middle_aged	high	yes	fair	yes
(H) ?: (H) ?:	14	senior	medium	no	excellent	no

So this will not be used for splitting. Now, we are going to split into two category. One is subset low and medium, because it is a binary classification, when you go for low and medium, another group. Suppose, there are two group is there, group 1 and group 2, in group 1, we have taken low and medium, obviously another set will be high. So, this would result in 10 tuples in partition D1.

We have to count how many low medium is there. We have got 10 tuples in partition D1, so this group is D1, that is why the condition income in the set low and medium. The remaining four tuples of D, the remaining is high, that is the remaining 4 that is D2, the remaining four tuples of D would be assigned to partition D2. What has happened, we have made a two subset, one is low medium and the remaining one is high.

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Tuples in partition D1

• Low + Medium:

19161 192		RID	oge	income	student	credit_rating	Class: buys_compute
Medium	Class: buys computer	1	youth	high	no	fair	no
+ Low		2	youth	high	no	excellent	no
		3	middle_age	high	no	fair	yes
Yes	3+4 =7	4	senior	medium	no	fair	yes
	-	5	senior	low	yes	fair	yes
No	1+2=3	6	senior	low	yes	excellent	no
		7	middle_age	low	yes	excellent	yes
		8	youth	medium	no	fair	no
		9	youth	low	yes	fair	yes
		10	senior	medium	yes	fair	yes
		11	youth	medium	yes	excellent	yes
		12	middle.age	medium	no	excellent	yes
		13	middle.age	high	yes	fair	yes
	,	14	senior	medium	no	excellent	BÖ

For the low and medium, for the class variable buys computer, we are going to see how many yes is there. By looking at together, the level medium and low, there are 7 yes is there, and there are 3 no is there.

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		Tuples in p	art	ition	D2			
• н	igh : (Dy)	Classe huma annual tar	RID	age	income	student	credit_rating	Class: buys_computer
	High	Class: buys computer	1	youth	high	no	fair	no
	Yes	2	2	youth middle.age	high high	no no	excellent fair	D0
			4	senior	medium	no	fair	yes yes
	No	2	5	senior	low	yes	fair	yes
			6	senior	low	yes	excellent	no
			7	middle.age	low	yes	excellent	yes
			8	youth	medium	no	fair	no
			9	youth	low	ycs	fair	yes
			10	senior	medium	ycs	fair	yes
			11	youth	medium	yes	excellent	yes
			12	middle.age	10000	no	excellent	yes
			13 14	middle_ager senior	, high medium	yes no	fair excellent	NO

For high, because that was group D1, this is for group D2, how many yes is there, 2, how many no is there, 2 no is there. So, two yes is there and 2 no is there.

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Gini index for income attribute

The Gini index value computed based on this partitioning is

$$Gini_{income \in \{low, medium\}}(D)$$

$$= \frac{10}{14}Gini(D_1) + \frac{4}{14}Gini(D_2)$$

$$= (10/14) (1 - (7/10)^2 - (3/10)^2) + (4/14) (1 - (2/4)^2 - (2/4)^2)$$

$$= 0.443 = Gini_{income \in \{high\}}$$

The Gini index for income attribute. The Gini index value computed based on this partitioning is Gini income to the set low and medium, so 10 / 14 Gini D1 + 4 / 14 Gini D2, so how we got this four, by looking at the low and medium, there are 10 values is there, out of 14, so 10 / 14. The another set, the remaining is 4. In D2, there is only 4, so 4 / 14. So Gini D we have seen in the previous lecture, 1 - 7 / 10 whole square - 3 / 10 the whole square.

How we got this 7, you see that there are 7 yes and there are 3 no. That is why it is 7 / 10 whole square minus 3 / 10 whole square. For D2, there are two yes, there are two no. So, 4 / 14, 1 - 2 / 4 whole square minus 2 / 4 whole square, so this value is 0.443, so this is Gini

value for the income high. For example, if you found the Gini value for low and medium, that is equivalent to finding the Gini value for the next group, that is the high.

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 Consider the subset{high, 	RID	age	income	student	credit_rating	Class: buys_computer
consider the subset(ingh)	1	youth	high	no	fair	no
medium}	2	youth	high	no	excellent	no
• This would result in <u>10</u> tuples	3	middle.aged	high	no	fair	yes
	4	senior	medium	no	fair	yes
in partition D1 satisfying the	5	senior	low	ycs	fair	yes
condition "income ∈{high,	6	senior	low	yes	excellent	no
	7	middle.aged	low	yes	excellent	yes
medium}"	8	youth	medium	no	fair	no
• The remaining four tuples of	9	youth	low	yes	fair	yes
	10	senior	medium	ycs	fair	yes
D (low) would be assigned to	11	youth	medium	yes	excellent	yes
partition D ₂	12	middle_aged	medium	no	excellent	yes
	13	middle.aged	high	yes	fair	yes
(1×1M)	14	senior	medium	no	excellent	no

Gini index for income attribute

Consider the next subset, that is high and medium. When you look at high and medium, there will be 10 tuples in partitioning D1, so here also we are going for two group, one group is D1, and another group is D2. Here high and medium is in one set, that is D1, so when you go for high and medium, obviously the next will be low. Low will be in the set D2. High and medium, there will be 10 tuples satisfying the condition, remaining 4 tuples of D would be assigned to partitioning D2.

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		Tuples in pa	art	ition	D1			
High	+ Medium	1:	8	_		_		
	Medium + high	Class: buys computer	RID 1 2 3	age youth youth middle.age	income high high high	student no no	credit_rating fair excellent fair	Class: buys.computer no no yes
	Yes	2+4	4	senior	medium	no	fair	yes
	No	2 + 2	5 6 7	senior senior middle_agee	low low low	yes yes yes	fair excellent excellent	yes no yes
			8 9	youth youth	medium low	no yes	fair fair	no yes
			10 11	senior youth	medium medium	yes ves	fair excellent	yes yes
			12	, middle.age	medium	по	excellent	yes
			13 14	middle_age senior	high medium	yes no	fair excellent	yes no

When you look at high and medium together, 6 yes for buying computer, 4 no for buying computer.

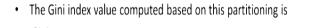
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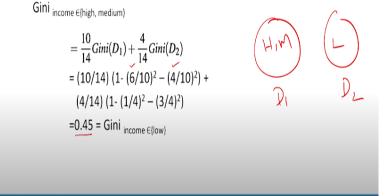
•	011/1							
	Low :		RID	age	income	student	credit_rating	Class: buys_compute
	Low	Class: buys computer	1	youth	high	no	fair	no
			2	youth	high	no	excellent	no
	No	1	3	middle.aget	high	no	fair	yes
			4	senior	medium	no	fair	yes
	Yes	3	5	senior	low	ycs	fair	yes
			6	senior	low	yes	excellent	no
		-	7	middle.age	low	yes	excellent	yes
			8	youth	medium	no	fair	no
			9	youth	low	yes	fair	yes
			10	senior	medium	yes	fair	yes
			11	youth	medium	yes	excellent	yes
			12	middle.agee	medium	no	excellent	yes
			13	middle.age	high	yes	fair	yes
			14	senior	medium	no	excellent	по

Then the next group, that is the tuples in partition D2, for low, there is one person has answered no, and 3 people has answered yes for buys a computer.

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Gini index for income attribute





Now, we will find out Gini index value computed based on this partitioning. Gini index for income attribute, Gini index value based on the computed partitioning for Gini is for income, we had two category, one is D1 and D2. D1, we had high and medium, and D2 we had low. Now for high and medium, let us find out the Gini index because there was 10 out of 14 that comes high and medium, so the Gini for D1 plus 4, in this low, there was 4 out of 14, so Gini for D2.

So, what is the value of D1, because in D1, for high and medium together, there was 6 yes was there and 4 no was there. For D1, that is the Gini index value. For D2, the Gini index value is 4 / 14, 1 yes was there and 3 no was there. So 1 / 4 whole square minus 3/4 whole square, so the Gini index for high and medium group is 0.45, that is nothing but the Gini index for the group also.

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 Consider the subset{high, 	RID	age	income	student	credit_rating	Class: buys_computer
	1	youth	high	no	fair	no
low}	2	youth	high	no	excellent	no
• This would result in 8 tuples	3	middle.aged	high	no	fair	yes
	4	senior	medium	no	fair	yes
in partition D1 satisfying the	5	senior	low	yes	fair	yes
condition "income ∈{high,	6	senior	low	yes	excellent	no
	7	middle_aged	low	yes	excellent	yes
low}"	8	youth	medium	no	fair	no
• The remaining six tuples of D	9	youth	low	yes	fair	yes
	10	senior	medium	ycs	fair	yes
(medium) would be assigned	11	youth	medium	yes	excellent	yes
to partition D_2	12	middle_aged	medium	no	excellent	yes
	13	middle.aged	high	yes	fair	yes
V(HL)(M)	14	senior	medium	no	excellent	no

Gini index for income attribute

Now, we go for another subset, high and low. Now, here what we are going to do. We are going to have two groups because it is a binary classification, so high, low is one group, so this is D1, and D2 obviously it is D2. So here for this, this would result that is 8 tuples in partition D1 satisfying the income is high and low, the remaining 6 tuples of D would be assigned to partitioning D2.

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-			RID	age	income	student	credit_rating	Class: buys_computer
	Low	Class: buys computer	1	youth	high	no	fair	no
			2	youth	high	no	excellent	no
١	NO	2	3	middle_age	high	no	fair	yes
			4	senior	medium	no	fair	yes
١	/es	4	5	senior	low	ycs	fair	yes
			6	senior	low	yes	excellent	no
			7	middle.age	low	yes	excellent	yes
			8	youth	medium	no	fair	во
			9	youth	low	yes	fair	yes
			10	senior	medium	yes	fair	yes
			11	youth	medium	yes	excellent	yes
			12	middle_age	medium	no	excellent	yes
			13	middle_age	high	yes	fair	yes
			14	senior	medium	no	excellent	no

Tuples in partition D2

For high and low, there was 5 yes is there, for high and low, there was 3 no is there. Another group is D2. In that, there was a medium. In that medium, there was a 2 no, and 4 yes. (**Refer Slide Time: 20:41**)

Gini index for income attr	ribute
 The Gini index value computed based on this parti Gini income E{high, low} 	itioning is
= $(8/14) (1 - (5/8)^2 - (3/8)^2) + (6/14) (1 - (2/6)^2 - (4/6)^2)$	M
=0.458 =Gini _{income ∈{medium}}	

We will find out the Gini index value computed based on the partitioning that is for this group, high and low. In high and low, totally there was 8 value, 8 / 14, in that 1 - 5 yes out of 8, so 5/8 whole square, there are 3 no, 3 / 8 whole square plus for group D2, that is medium that was in another group, in that 6 elements was there out of 14, 6 / 14, 1 - how many yes was there, two no was there, 2 / 6 whole square, four yes was there, 4 / 6 whole square. So, the Gini index for the group high and low that is equivalent to. For the medium group, Gini index value, that also 0.458.

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Gini Index values

	Gini Index values
Gini income ∈{high, low}	0.458
Gini income ∈{high, medium}	0.45
Gini income ∈{medium, low}	0.443
income equeorani, iowy	

We have completed all possible binary classifications, so Gini income high and low, Gini index value 0.458, the Gini group for high and medium is 0.45, for medium low, the Gini index value is 0.443. How to interpret this table, so this value 0.443, this is having the minimum Gini index value.

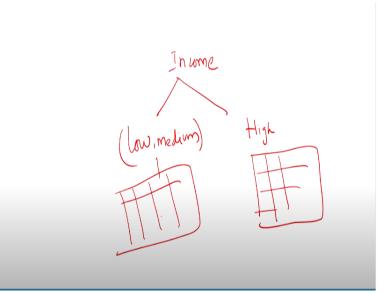
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	Interpretation
•	The best binary split for attribute income is on {medium, low} (or {high}) because it minimizes the Gini index
•	The splitting subset {medium,low} therefore give the minimum Gini index for attribute income
•	Reduction in impurity = 0.459 - 0.443 = 0.016
•	Further we calculate the same for the rest 3 criteria (age, student, credit rating)
•	The one with minimum Gini index value will results in the maximum reduction in impurity of the tuples in D and is returned as the splitting criterion

The best binary split for the attribute income is on medium and low, otherwise high, because it minimizes the Gini index. When you look at the previous table, it is having the minimum Gini index value. The splitting subset, medium and low therefore gives the minimum Gini index for attribute income. So, the reduction in impurity is 0.459, this value which we got from slide number 18, this for the class D, - 0.443.

We got from this value, Gini index value for each subset. So the difference is 0.016. Further, we calculate the same for the rest of 3 criteria, so we got for reduction impurity for, this is income, there are another 3 attributes that is age, student and credit rating. For each attribute, we have to find out the reduction in impurity. The one with minimum Gini index value will result in the maximum reduction in impurity of the tuples in D and is returned as the splitting criterion.

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Now, how to have the classifications. For example, we have income is the splitting variable. There was a 2 binary split. The first one was low and medium is one group, and high is another group. Now, in the high also, you might have some other table like this. For each value, we have to find out the Gini index, for low and medium group also, we will have another table. For this value also, we have to find out the Gini index.

After finding out the Gini index, whichever is having highest level of reduction impurity, otherwise lowest value of Gini index should be chosen as the splitting criteria for further classification. In this lecture, I have explained how to choose an attribute for the CART model, by using two criteria. One is gain ratio and Gini index. For both the method, I have taken a numerical example. With the help of numerical example, I have explained how to choose an attribute. In the next lecture, we are going to use Python for making a CART model. Thank you.