



NPTEL

NPTEL ONLINE COURSE

Discrete Mathematics

Functions

Advanced Topics

Distinct partitions and odd partitions

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Here is something very interesting. Look at these partitions of 6. 6 can be written as 6. 4 plus 2. 4 plus 1 plus 1. 5 plus 1. 3 plus 3. 3 plus 2 plus 1. 3 plus 1 plus 1 plus 1. 2 plus 2 plus 2. 2 plus 2 plus 1 plus 1. 2 plus 1 plus 1 plus 1 plus 1. 1. plus 1 plus 1 plus 1 plus 1 plus 1. All 1s. Now these are the partitions of 6. Observe something now.

I am going to box some partitions like this. Keenly observe this partitions. 6 equals 6. 4 plus 2. 5 plus 1. 3, 2, 1. Take a minute's pause observe these and observe the unboxed ones and you will be able to find out something very interesting. Now I hope you have taken a pause. Here is the observation.

These partitions have all distinct summands. What do I mean by summands? If this is one part 6, 4 plus 2 these are called summands. 5 and 1 are called as summands and so on. So I hope you have understood what is a summand. 5 is a summand. 1 is a summand. So what constitutes the partition the integers which constitutes the partitions are called as summands. 3 is a summand. Here 2 is a summand. So on.

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$6 = \boxed{6}$	$6 = 3 + 1 + 1 + 1$
$6 = \boxed{4 + 2}$	$6 = 2 + 2 + 2$
$6 = 4 + 1 + 1$	$6 = \boxed{2} + 2 + 1 + 1$
$6 = \boxed{5 + 1}$	$6 = 2 + 1 + 1 + 1 + 1$
$6 = \boxed{3} + 3$	$6 = 1 + 1 + 1 + 1 + 1 + 1$
$6 = \boxed{3 + 2 + 1}$	



So now observe these boxed partitions. What did we see? We saw that all of them have distinct summands. The partitions with distinct summands. I am going to write the mass Pd of n in and for in general we have seen what was Pd of n , d stands for distinct which is in the subscript. So Pd of n or Pd of 6 for n equal 6 is 4. Now again observe the partitions of 6. 4 plus 1, 1. 3, 3. 3, 2, 1. 3, 1, 1, 1. 2, 2, 2. 2, 2, 1, 1. 2, 1, 1, 1, 1. And all 1s. I have again written down all the partitions.

Now observe these partitions. 5, 1. 3, 3. 3, 1, 1, 1 and all 1s. Observe these boxed partitions. Earlier we saw that the summands were distinct. What can you comment upon the summands of these partitions.

$$6 = 6$$

$$6 = 4 + 2$$

$$6 = 4 + 1 + 1$$

$$6 = 5 + 1$$

$$6 = 3 + 3$$

$$6 = 3 + 2 + 1$$

$$6 = 3 + 1 + 1 + 1$$

$$6 = 2 + 2 + 2$$

$$6 = 2 + 2 + 1 + 1$$

$$6 = 2 + 1 + 1 + 1 + 1$$

$$6 = 1 + 1 + 1 + 1 + 1 + 1$$



Do you observe that here we have all odd summands. 5, 1, 3, 3, 1s here. All are 1s and here it is 3,1, 1 so on. Do you observe that all are odd in the partitions which are boxed. Now we have seen the partitions with odd summands. All of them were odd. I have not boxed those which had even one even summand. I am going to represent it as P_o of n O stands for odd here. We have seen what was P_o of 6 it is 4. Well remember whatever we have learned in this video we will be seeing something more in the next one.

Partitions with odd summands.

$$P_o(6) = 4$$

odd ←