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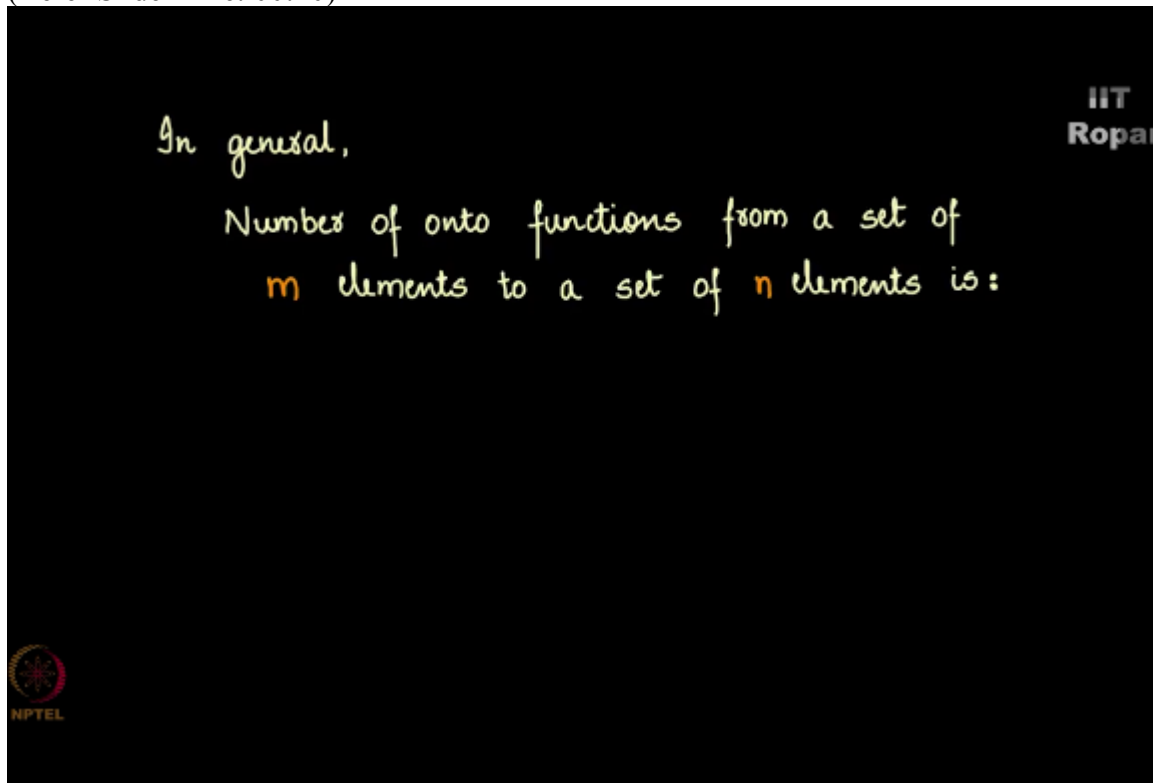
NPTEL ONLINE CERTIFICATION COURSE

Discrete Mathematics  
Principle of Inclusion and Exclusion

Formula for Number of Onto Functions

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In general the number of onto functions from a set of  $m$  elements to a set of  $N$  elements is given by, let us see the formula now,  
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$N$  choose 0 into  $N$  to the  $M - N$  choose 1 into  $N-1$  to the  $M + N$  choose 2 into  $N-2$  to the  $M - N$  choose 3 into  $N-3$  to the  $M + N$  choose 4 into  $N-4$  to the  $M$  so on + -1 to the  $N$  into  $N$  choose  $N$  into  $N-N$  to the  $M$ , do you see  $N-N$  would become 0.

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In general,  
 Number of onto functions from a set of  $m$  elements to a set of  $n$  elements is:

$$\binom{n}{0}n^m - \binom{n}{1}(n-1)^m + \binom{n}{2}(n-2)^m - \binom{n}{3}(n-3)^m + \binom{n}{4}(n-4)^m - \dots + (-1)^n \binom{n}{n}(n-n)^m$$

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Now how can I write it this formula as? I can write it as summation I from 0 to N, -1 to the I N choose I into N-I whole to the M,  
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In general,  
 Number of onto functions from a set of  $m$  elements to a set of  $n$  elements is:

$$\binom{n}{0}n^m - \binom{n}{1}(n-1)^m + \binom{n}{2}(n-2)^m - \binom{n}{3}(n-3)^m + \binom{n}{4}(n-4)^m - \dots + (-1)^n \binom{n}{n}(n-n)^m$$

$$= \sum_{i=0}^n (-1)^i \binom{n}{i} (n-i)^m$$

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so this is the formula for the number of onto functions from a set of M elements to a set of N elements, the professor in the previous video had taken a particular case and had solved the

problem, now this is the general formula, we'll be seeing a couple of problems in the next video.

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