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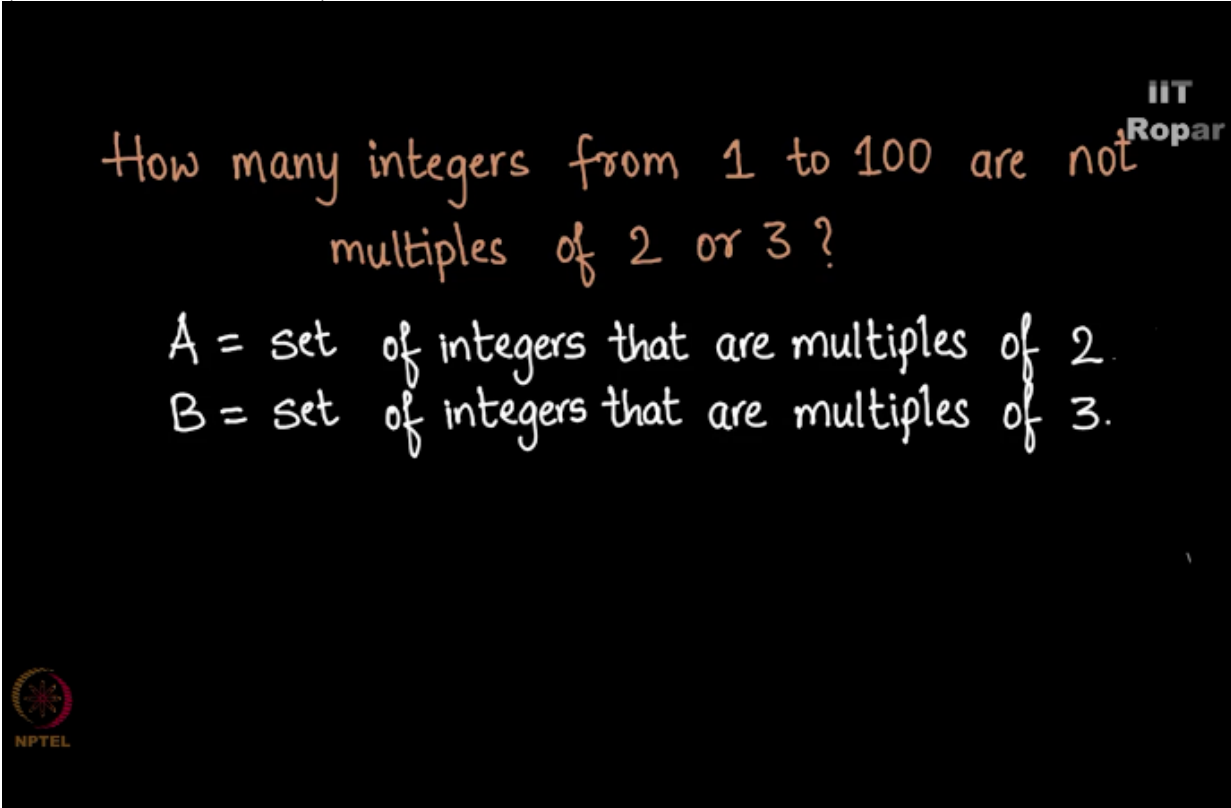
NPTEL ONLINE CERTIFICATION COURSE

Discrete Mathematics
Principle of Inclusion and Exclusion

Example 5 - Non multiples of 2 or 3

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How many integers from 1 to 100 are not multiples of 2 or 3? So let A be the set of integers which are multiples of 2, and let B be the set of integers which are multiples of 3,
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How many integers from 1 to 100 are not multiples of 2 or 3?

A = set of integers that are multiples of 2.
B = set of integers that are multiples of 3.

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so now I have these 2 sets A and B, so what do we have to find out? We have to find out $A \cap B$, or if I say C1 is the condition where an integers satisfies C1 if it is a multiple of 2, and C2 is the condition where an integers satisfies C2 if it is a multiple of 3,
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How many integers from 1 to 100 are not multiples of 2 or 3?

C_1 = set of integers that are multiples of 2.

C_2 = set of integers that are multiples of 3.

$$|\bar{A} \cap \bar{B}| = ?$$



so you have to find out $N(\bar{C}_1, \bar{C}_2)$, what is it going to be?
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How many integers from 1 to 100 are not multiples of 2 or 3?

C_1 = set of integers that are multiples of 2.

C_2 = set of integers that are multiples of 3.

$$N(\bar{C}_1, \bar{C}_2) = ?$$



We know that N here is 100, that is integers from 1 to 100 so you have 100 of them here.

Now what is $N(C_1)$? How many integers are multiples of 2? 2, 4, 6, 8, 10 so on, so you have 50 of them, $N(C_1) = 50$, and how many are multiples of 3? 3, 6, 9, 12, 15 so on, so 33 of them are multiples of 3 here, how did we do that?

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$N = 100$
 $N(C_1) = 50$
 $N(C_2) = 33$

1, 2, 3, ..., 100
Multiples of 2:
2, 4, 6, ..., 100
Multiples of 3:
3, 6, 9, 12, ..., 99

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We did it like this $100/3$ apply the lowest integer function or called as the floor function where you take the greatest integer which is less than or equal to that number, so here it happens to be 33.

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$$N = 100$$
$$N(C_1) = 50$$
$$N(C_2) = 33$$

$$1, 2, 3, \dots, 100$$
$$\left\lfloor \frac{100}{3} \right\rfloor = 33$$

Multiples of 3:

$$3, 6, 9, 12, \dots, 99$$



Now $N(\bar{C}_1, \bar{C}_2)$ will be given by $N - N(C_1) + N(C_2) - N(C_1, C_2)$, what is $N(C_1, C_2)$ here?

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$$N = 100$$

$$N(C_1) = 50$$

$$N(C_2) = 33$$

$$1, 2, 3, \dots, 100$$
$$\left\lfloor \frac{100}{3} \right\rfloor = 33$$

Multiples of 3:

$$3, 6, 9, 12, \dots, 99$$

$$N(\bar{C}_1 \bar{C}_2) = N - [N(C_1) + N(C_2)] + N(C_1 C_2)$$



We have not found it out yet, $N(C_1, C_2)$ happens to be those integers which are multiples of 2 and 3, so how do we do that? We take the LCM of 2 and 3 which happens to be 6, so those integers which are multiples of 6 will satisfy C_1, C_2 , which means we have 16 integers which satisfy C_1, C_2 , which means $N(C_1, C_2)$ is 16.

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$$\begin{aligned}N &= 100 \\N(C_1) &= 50 \\N(C_2) &= 33 \\N(C_1 C_2) &= 16\end{aligned}$$

$$\begin{aligned}&1, 2, 3, \dots, 100 \\&\text{Multiples of 2 and 3:} \\&6, 12, 18, 24, \dots, 96 \\&\left\lfloor \frac{100}{6} \right\rfloor = 16\end{aligned}$$

$$N(\bar{C}_1 \bar{C}_2) = N - [N(C_1) + N(C_2)] + N(C_1 C_2)$$



Now what is the answer then? So we have $N(\bar{C}_1 \bar{C}_2)$ happens to be $100 - (50+33) + 16$, which is $100 - 83 + 16$, $100 - 83$ is $17 + 16$ and the answer is 33, so 33 integers are not multiples of 2 or 3 in the range 1 to 100.
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How many integers from 1 to 100 are not multiples of 2 or 3?

Answer: 33



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