

NPTEL

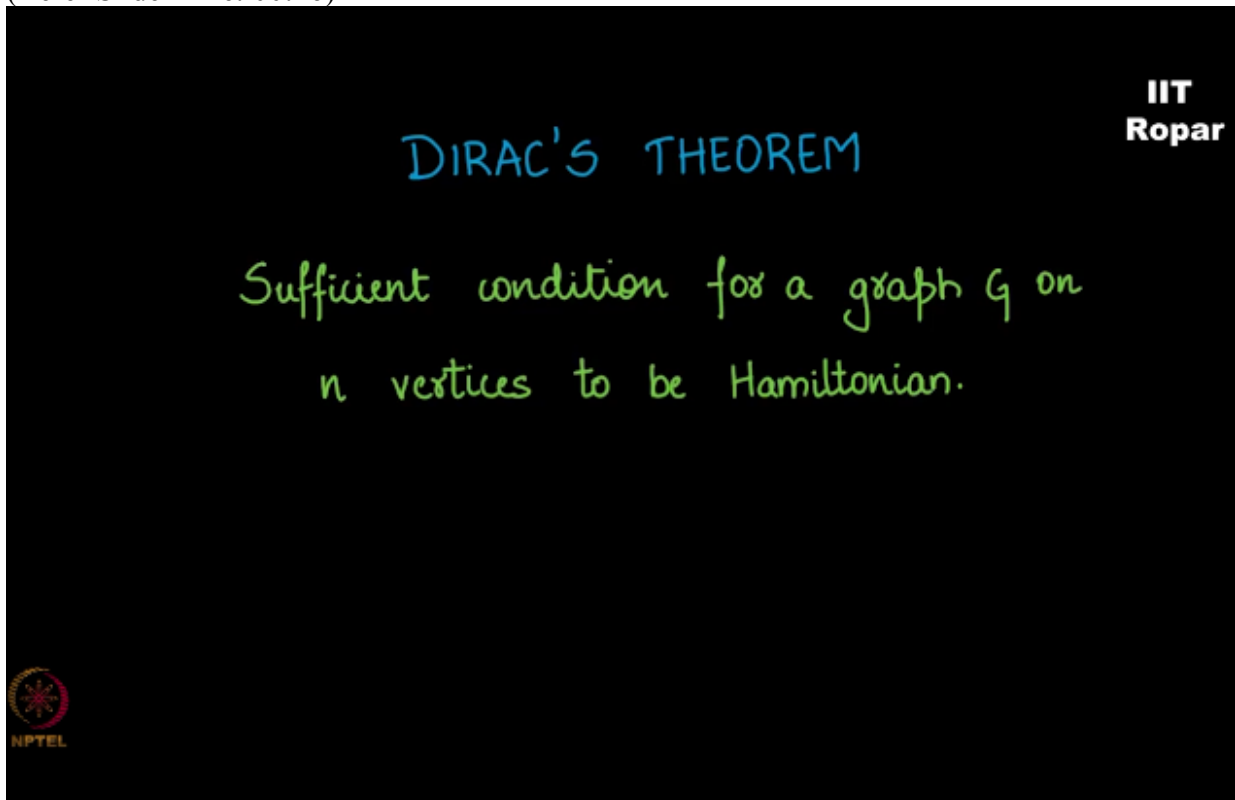
NPTEL ONLINE CERTIFICATION COURSE

Discrete Mathematics
Graph Theory - 2

Dirac's theorem - A note

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The theorem which the professor proved now is called the Dirac's theorem, it provides a sufficient condition for a graph G on N vertices to be Hamiltonian,
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it's just sufficient, but it is not necessary for Hamiltonian graph to satisfy the condition that degree of every vertex greater than or equal to $n/2$ for every vertex,
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DIRAC'S THEOREM

Sufficient condition for a graph G on
 n vertices to be Hamiltonian.

It is not necessary

$$\deg(v) \geq n/2$$

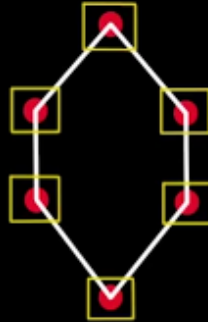


it's not necessary for this condition to be true, even without this condition sometimes the graph may be Hamiltonian.

Now an example for this situation will be any cycle C_n , you see let me take an example C_6 , degree of every vertex is 2 here, and $n/2$ is 3, and 2 is less than 3,
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Example : C_n

C_6 :



$$\text{deg } v = 2$$

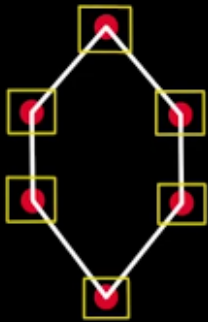
$$n/2 = 3 \quad 2 < 3$$



but still the graph is Hamiltonian, so as a counter example we can take all C_n ,
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Example : C_n

C_6 :



Hamiltonian

$$\text{deg } v = 2$$

$$n/2 = 3 \quad 2 < 3$$



so it just gives a sufficient condition but it is not necessary.

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