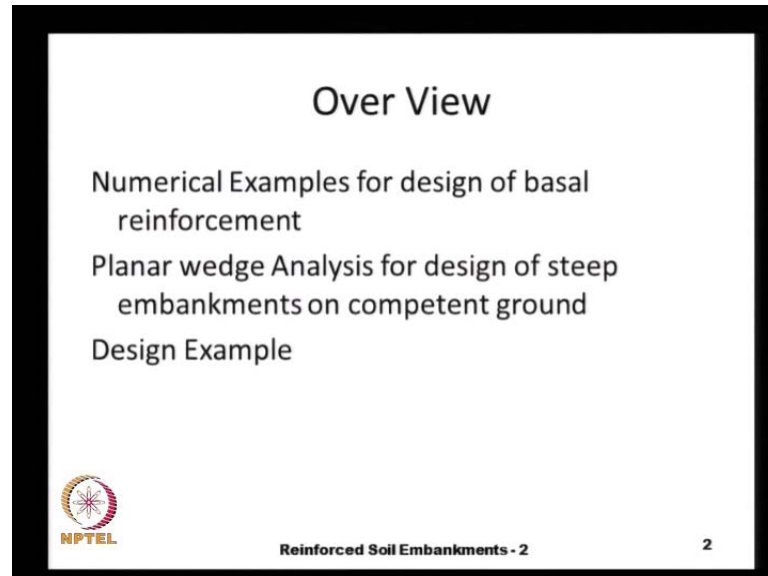


Geosynthetics and Reinforced Soil Structures
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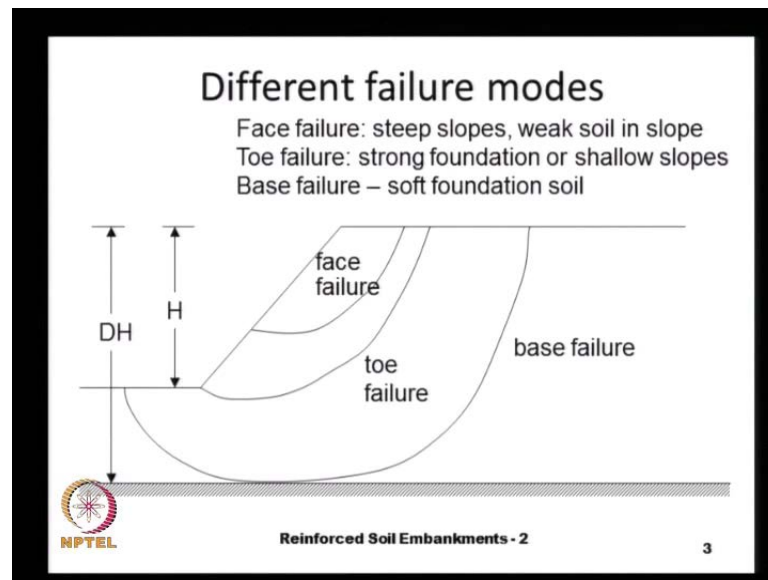
Lecture - 22
Geosynthetic Reinforced Soil Embankments - II

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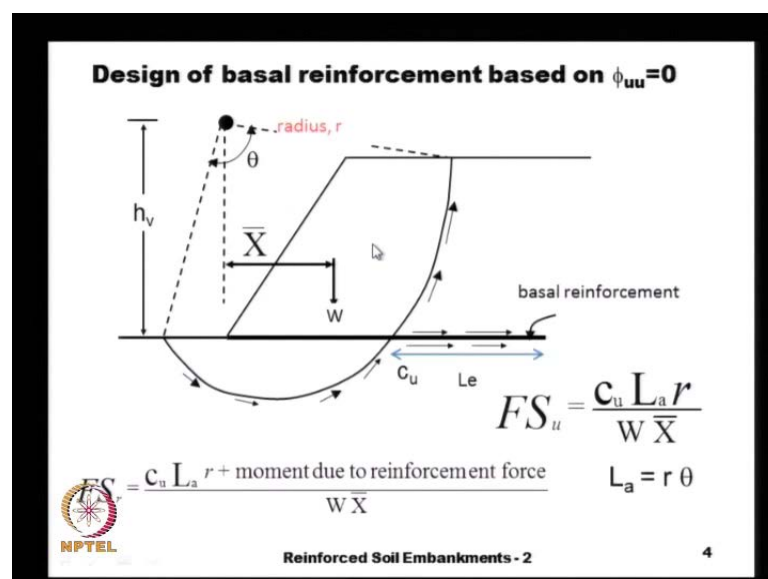
Very good morning students. In this lecture, we will go through some numerical examples for the design of basal reinforcement that we had studied in the previous lecture. And then the planar wedge analysis for design of very steep embankments on competent soils and some design examples.

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As you may recall from your other geotechnical engineering courses these are the different types of failures that we can have with these slopes. Let us say that you have a slope of height H and there are three possible modes of failure; one is the face failure the face failure happens in the case of steep slopes or if the embankment is formed with a relatively weak soil. And then the toe failure is is the failure that happens when we have a strong foundation soil or very, very shallow slope then base failure or deep seated failure happens when we have a an extremely soft foundation soil, and our embankment soil itself is relatively strong.

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And just to recall in the previous lecture we have seen the the design of soil slopes with basal reinforcement layer, and the basal reinforcement it is provided for several reasons especially in the case of extremely soft case we require a working platform. So, that we can even bring in our construction machinery and start mobilizing our equipment and then of course, on top of that we may require some extra reinforcement to improve the factor of safety and for a very simple case where our phi equal to 0.


We can get the factor of safety for a given circle a by just taking moments about this centre of rotation, and w is the weight of the soil within this wedge and X bar is the is the lever arm W times X bar is the destabilizing moment. And then the stabilizing moment is because of the the cohesive force that is acting along this slip circle length that is a C u times L a where L a is the length of the slip circle multiplied by this r radius r and that is the factor of safety of the unreinforced slope. And if you have a basal reinforcement we need to add extra stabilizing moment because of the basal reinforcement and. So, we have seen two cases of basal reinforcement one is a very stiff reinforcement that remains horizontal and another is flexible type reinforcement that bends that has a kink at this slip surface in which case the axial force in the reinforcement as tangential to the to the slip surface.

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Numerical example

Consider a clay soil embankment:
Height of embankment = 8 m
Slope angle = 45°
Both slope and foundation have same soil properties:
 $C=25 \text{ kPa}$, $\phi=0^\circ$; $\gamma=20 \text{ kN/m}^3$

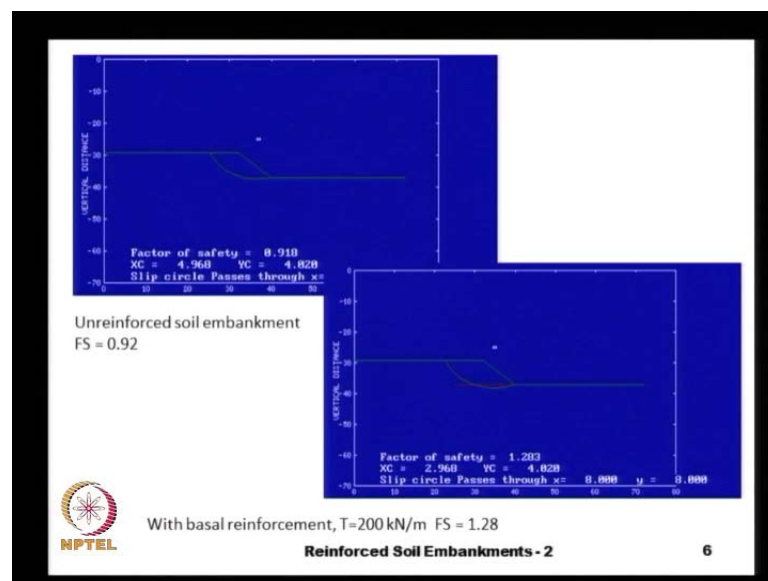
Toe circle is the most possible failure mode

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And now a let us look at a numerical example let us consider a a clay soil embankment height of a 8 meters, and the slope angle is 45 degrees. And let us say that both the slope

and the foundation soil have the same soil properties of C_u of 25 kPa, and friction angle is 0, and unit weight is 20 kilo newtons per cubic meter and this situation a toe circle is the most possible failure mode. And as we discussed in the previous lecture we need to consider several of these slip circles to get the circle with the least factor of safety, and whatever equation that you have seen is only for one single slip circle and we need to try out several of these to get our minimum factor of safety.

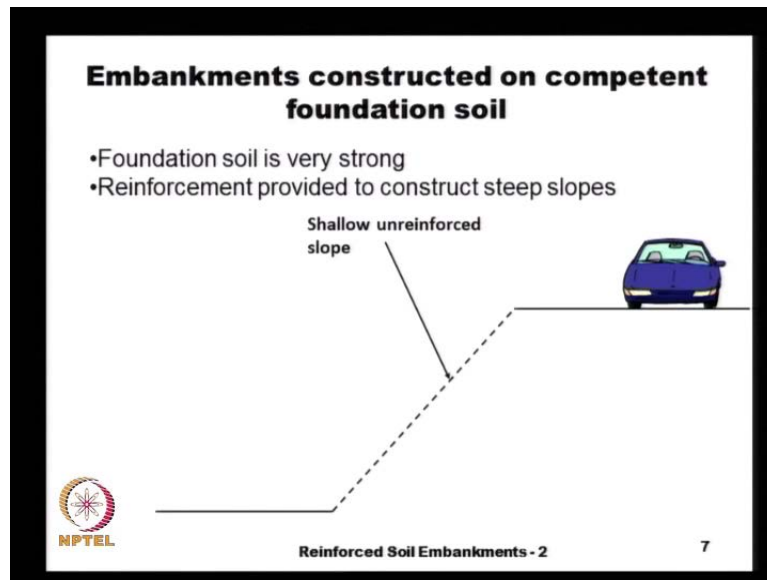
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And it is best done using some computer program, and in this case this is the result from one computer program that you are going to get as part of this course the height of the slope is 8 meters, and this slope angle is 45 degrees. And the the factor of safety of this unreinforced slope is 0.92 and we need to increase this factor of safety to a higher value and that is a trial and error process, and here we have the result from another slip circle analysis with basal reinforcement having a tensile strength of 200 kilo newtons per meter. And for this case the factor of safety is is come up to 1.3 and we may need to choose basal reinforcement provides higher force in case, if you want factor of safety higher value and the length of this reinforcement that we need to provide should be adequate. So, that the the it has sufficient pullout resistance and the pullout resistance is calculated based on the embedded length of reinforcement beyond the the most critical slip circle, and these are all based on using some programs. Because doing the hand calculations is quite tedious, because typically we look at least 2 to 300 slip circles for coming out with these minimum factor of safety, and in this case as I mentioned earlier

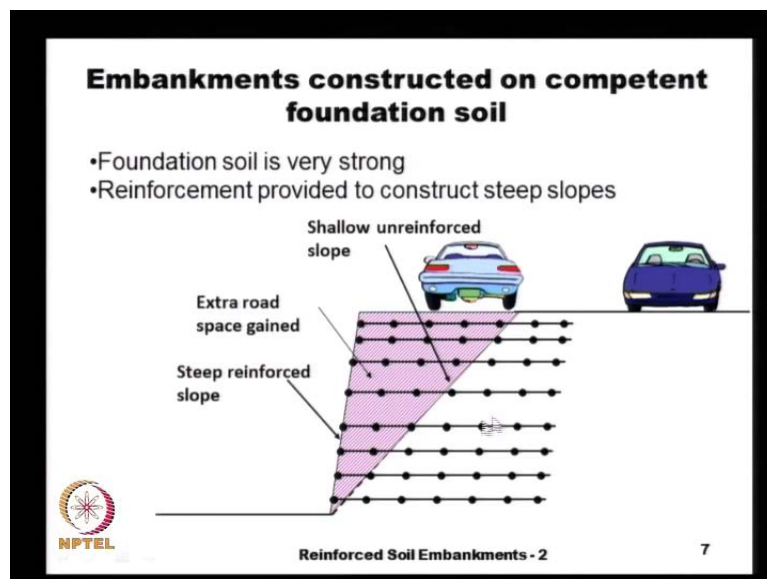
the, if you are not happy with this factor of safety we need to increase the increase the a tensile strength of the reinforcement. And typically we do not provide one single layer as illustrated here we may provide some two or three layers, so that we can achieve our target factor of safety.

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And continuing our discussion many many times, when we have road embankments and other things in the city areas we may be faced with a requirement that we need to construct a very steep slopes, and one example as we had seen earlier is is like this.

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Let say that we want to widen this road and the only way to widen this is either to make this slope as a steep slope, and so that we get extra space or or procure more land and and widen the construction area and in the city urban areas getting extra land for our construction is very difficult. So, in that case we going for going for steepest slope by providing horizontal layers of reinforcement.

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Slip circle analysis for cohesive-frictional soils

l_i = inclined length at base of slice
 W_i = weight of i^{th} slice
 R = radius of slip circle
 u_i = pore pressure at base

$$FS_r = \frac{c' L_a R + \tan \phi' R \sum_{i=1}^n (w_i \cos \alpha_i - u_i l_i) + \sum T_i y_i}{R \sum_{i=1}^n w_i \sin \alpha_i}$$


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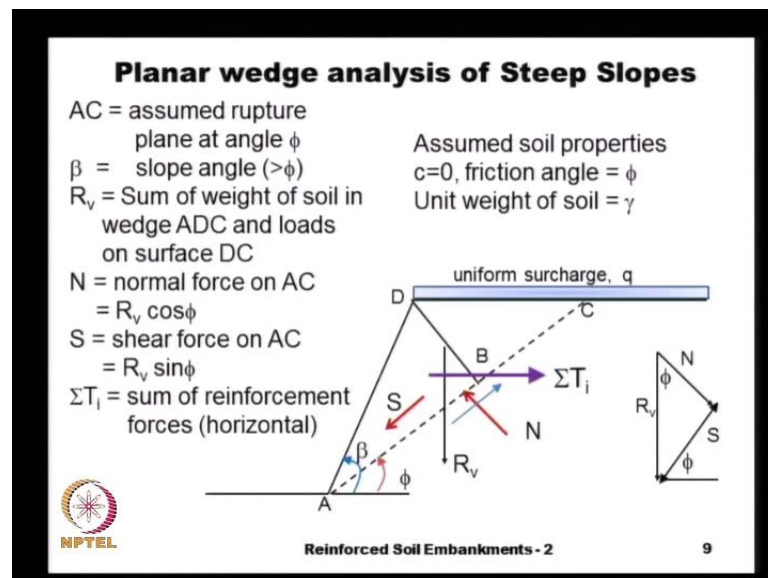
And how do we design this type slopes there are different design approaches one is the slip circle analysis, we can just do a the felonious or bishop's slip circle analysis and find out the factor of safety. And here this equation is from the felonious analysis or the ordinary method of slices once again we take moments about about the centre of rotation and for the convenience, we divide a this entire length of this slip circle into into certain number of slices. And typically at least minimum 6 to about 10, and we consider the equilibrium of each slice W_i is the weight of the soil that is acting down, and that causes some shear force T_i , that is trying to destabilize this wedge. And that force is T_i time W_i times $\sin \alpha_i$ that is just by resolving this force into into parallel to the to this to this base and perpendicular to this base.

And the perpendicular component N_i the normal component is W_i times cosine α_i , and let us say that l_i length of this base is L_i that is the incline length. And we can calculate the factor of safety of the reinforced slope as the resisting moment divided by the upsetting moment. And the resisting moment is because of two components, one is

because of the cohesion. And the other is because of the friction angle and the third one is because of the the reinforcement that we have, and say if you are working with effective stresses $C' L a$, that is the length of this slip circle r multiplied by r that is the the the lever arm for this cohesive force. And $\tan \phi$ times N_i' and N_i' is a nothing but $W_i \cos \alpha - u$ that is the pore pressure multiplied by base angle L_i . And this pore pressure is we can estimate it, if we have the a freeatic surface or in terms of the bishop's pore pressure parameter, we can as estimate u as some R_u times W . And this entire quantity that we have $w \cos \alpha - u_i L_i$ is similar to our effective stress and this whole thing multiplied by r that is the lever arm. And see we have certain number of reinforcement layers, we can take the summation of t times y and that the the resisting moment divided by the upsetting moment.

Because of this component of the force T_i is the $W_i \sin \alpha_i$ will give us the factor of safety of the reinforced slope, and this method is recommended in the in the federal highway administration code, and even in the b s code they recommend, but its only for preliminary analysis.

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And we have more number of other analysis that we can consider one simple method is the planar wedge analysis of the steep slopes, we will understand the principle of the slope stability analysis with this. And we will go on for looking at more complicated surfaces. Let us say that we have a slope within angle of beta, and then we want to

analysis and we have provided certain number of reinforcement layers, and the simplest one is, if we assume that the failure angle is at an angle of ϕ that is the angle of repose; that is the simplest one to consider. And let us say that there is a uniform surcharge of q and the failure is happening along the surface AC, and let us assume that our cohesive strength is C is 0. And the friction angle is ϕ and the unit weight of the soil is γ and let us say that this is the AC is the assumed rupture plane at the angle of ϕ and β is the slope of an angle. And β is much greater than ϕ and R_v is the sum of the weight of soil within this wedge ADC and the loads acting on the surface DC. And n is the normal force on the AC that is just simply R_v times cosine ϕ that is if you can see this force triangle R_v is the vertical force n is the normal component. And let us say that the sum of all the reinforcement forces is $\sum T_i$ that is the sum of all the reinforcement force that we have.

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Normal force on surface AC, $N = R_v \cos \phi$

Shear resistance = $N \tan \phi$

Reinforcement force component
up the slope = $\sum T \cos \phi$

Net shear resistance = $N \tan \phi + \sum T \cos \phi$

Shear force acting down the slope = $R_v \sin \phi$



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And we can do the equilibrium analysis of all the forces that are acting on the on the failure surface AC, as we have seen earlier the normal force is R_v times cosine ϕ . And the shear resistance is n times $\tan \phi$, because the friction here is because between two soil surfaces, because here this this slope AC is the rupture surface on both sides we have this the soil. And we can assume that the friction angle mobilized along that surface is only the ϕ and the reinforcement force component upwards of the slope is just simply $\sum t$ times cosine ϕ that is the the component of the reinforcement force, and then the net shear resistance is n times $\tan \phi$ plus $\sum t$ cosine ϕ . And the shear force

acting down the slope is R_v times $\sin \phi$, that is that is the shear force that is acting down here.


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Considering the force equilibrium along the sliding surface, AC

$$FS = \frac{\text{shear resistance}}{\text{shear force}} = \frac{R_v \cos \phi \tan \phi + \sum T_i \cos \phi}{R_v \sin \phi}$$

$$= \frac{R_v \sin \phi + \sum T_i \cos \phi}{R_v \sin \phi} = 1 + \frac{\sum T_i}{R_v \tan \phi}$$

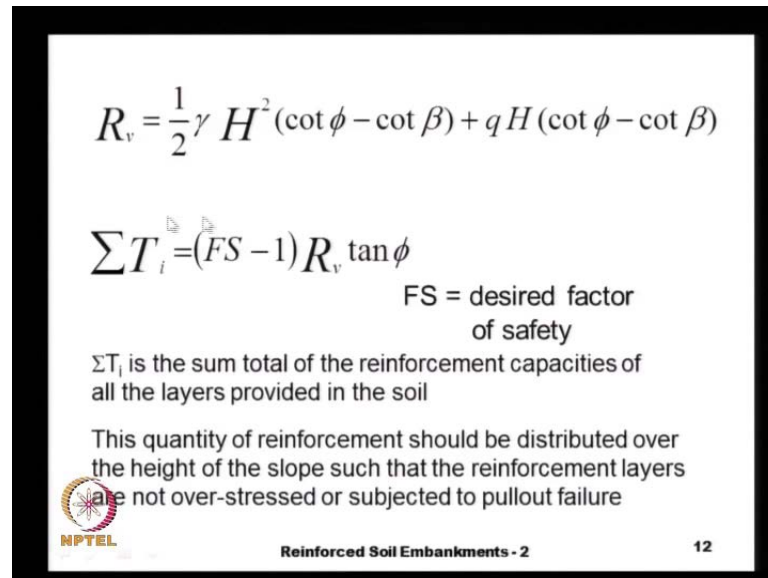
$R_v = \text{wt. of soil in ADC} + \text{surcharge on surface DC}$

$$DC = H (\cot \phi - \cot \beta)$$


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And if we consider the force equilibrium of all the forces acting along the sliding surface AC our factor of safety is the shear resistance divided by shear force, that is R_v times $\cos \phi$ times $\tan \phi$ plus $\sum T_i \cos \phi$ this whole thing divided by $R_v \sin \phi$ and. So, $\cos \phi$ times $\tan \phi$ is just simply $\sin \phi$. So, it is equal to $R_v \sin \phi$ plus $\sum T_i \cos \phi$ by $R_v \sin \phi$ that is $1 + \frac{\sum T_i}{R_v \tan \phi}$ by bringing this $\cos \phi$ to the denominator. And R_v is as we discussed earlier the weight of the soil within the triangle ADC plus the surcharge, that is acting on the surface DC , and this length DC is H times $\cot \phi$ minus $\cot \beta$.

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$$R_v = \frac{1}{2} \gamma H^2 (\cot \phi - \cot \beta) + q H (\cot \phi - \cot \beta)$$

$$\sum T_i = (FS - 1) R_v \tan \phi$$

FS = desired factor of safety

ΣT_i is the sum total of the reinforcement capacities of all the layers provided in the soil

This quantity of reinforcement should be distributed over the height of the slope such that the reinforcement layers are not over-stressed or subjected to pullout failure

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And our R_v now is just simply one half gamma square times cotangent phi minus cotangent beta plus the surcharge force acting on the surface D C; that is q times H cotangent phi minus cotangent beta. And so our factor of safety equation FS is one plus $\sum T_i$ by $R_v \tan \phi$ and by rearranging that equation. We can get our $\sum T_i$ in terms of the factor of safety and the other fact is as $FS - 1$ R_v times $\tan \phi$ where in our FS is the desired factor of safety.

And this one is the factor of safety for soil to soil slope failure, and because we have assumed that the slope failure is along this this angle of repose that factor of safety is one, and this FS is the the the desired factor of safety. Because of the provision of reinforcement layers our factor of safety is going to greater than 1, and so this $\sum T_i$ is the sum total of the reinforcement capacities of all the layers provided in the soil to increase the factor of safety of the slope from one to FS . And so this quantity of reinforcement should be distributed uniformly over the height of the soil of the the soil such that the reinforcement layers are not over-stressed or subjected to pullout failure over-stressed means the force; that is transferred into each reinforcement layer should be lower than the tensile strength with some adequate margin of safety.

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Force transferred into each reinforcement layer
 $= K_a S_v(z) (\gamma z + q)$

K_a = lateral earth pressure coefficient in soil

$S_v(z)$ = vertical spacing at depth z

q = surcharge pressure on slope surface

γ = unit weight of soil

$$K_a = \left[\frac{\sin(\beta - \phi)}{(\sin\beta)^{1.5} + \sin\phi \sqrt{\sin\beta}} \right]^2$$


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And as we have seen earlier in the case of reinforced soil retaining walls the force transferred into each reinforcement layer at a depth of Z is K_a times S_v of Z multiplied by the vertical pressure $\gamma Z + q$ in the case of retaining walls. We have considered a mayer half pressure distribution, but in the case of slopes we just considered only the vertical stress without any effect of overturning here our K_a is the lateral earth pressure coefficient in the slope.

But this is not equal to the rankine's at the coulombs earth pressure coefficient is much lower, because this K_a is operating in a in a shallow slope, and S_v of Z is the vertical spacing at depth of Z . And the q is the surcharge pressure acting on the slope surface and γ is the unit weight, and this k_a is is the $\sin \beta$ minus ϕ divided by $\sin \beta$ to the power 1.5 plus $\sin \phi$ square root of $\sin \beta$ to the whole of square. And this quantity if we substitute β of 90 degrees will be equal to our K_a for rankine theory that is $1 - \tan \phi$ by $1 + \sin \phi$. And for the slopes this is much lower as we will see later on.

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Pullout Resistance of reinforcement layers

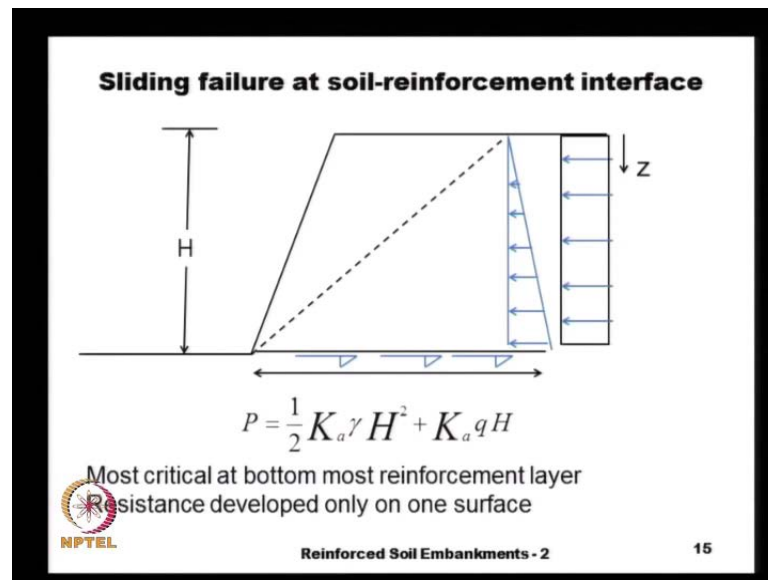
Pullout resistance
 $= 2 L_e (\gamma z + q) \tan \delta = 2 L_e (\gamma z + q) \mu \tan \phi$

$L_e = \text{anchorage length}$
 $= L - (H - z) (\cot \phi - \cot \beta)$

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And the pullout resistance is estimated based on the length of the reinforcement beyond the rupture plane like this. So, in our case our rupture surface is at an angle of phi like this and let us say our reinforcement length total length is l out of that l_e is the anchorage length. And this anchorage length l_e is l minus minus, this length that length is H minus Z times where Z is the the height from the top cotangent phi minus cotangent beta. So, this L_e if we have it, because our pullout resistance is mobilized on two surface we have a two here multiplied by L_e ; that is the anchorage length times. The vertical stress γZ plus q times $\tan \delta$ that is the delta is the the interface friction angle or we can also write it as $\sum \mu \tan \phi$, because where μ is called as the interaction factor and the pullout modular failure.

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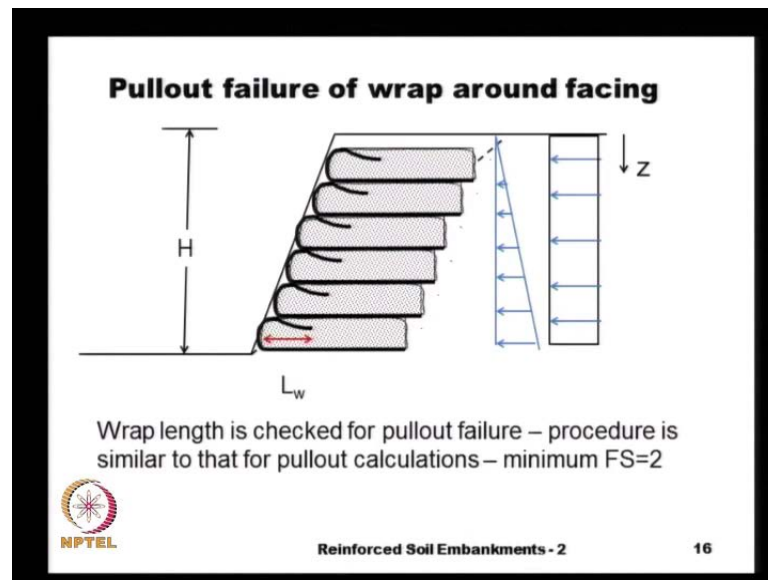


And phi is the friction angle, apart from second for the for the reinforcement rapture and the pullout we also need to look at some other modes of failure; that is let us say that this entire length of soil slope behaves like rigid body. And it is subjected to lateral earth pressure from behind, that is one is because of the self weight of the soil that has triangular pressure distribution, and the other because of uniform surcharge that has a rectangular pressure distribution and this rigid block of reinforced soil may slide away by sliding above the the bottom most reinforcement layer.

And the in this case our shear resistance or the base resistance is developed only on one surface like this and our total lateral force is one half K a gamma H square plus K a times q times H where our K a is the reduced earth pressure coefficient. As we have seen earlier and the most is actually this failure may happen at any depth, because wherever we have a reinforcement ah that may be the weakest plane, because the the friction angle that is mobilized between the soil and the reinforcement is usually slightly less than phi.

And we need to theoretically do the check at each and every reinforcement layer, but then the most critical one is at the bottom because the lateral force is the maximum at the at the base. And if our reinforcement wedge at different at different depths then we may have to check ah at all the depths, but in usually we provide equal length of reinforcement in the slopes because the from the construction point of view that is more easy.

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And apart from this the other earlier failures that we have considered whenever face is made up of wrap around facing especially with geogrid or geotextiles this length of wrap around we should check to make sure that there is good anchorage. If that wrap around length is not sufficient it will just get a pushed out and then we may have a face failure. And the minimum factor of safety that is required for this for this mode of failure is two and for this, what we do is? We assume that this particular wrap around is resisting the force that is coming from this height of the soil, and then equate the at the pullout resistance of this reinforcement length to this lateral force to make sure, that we have adequate embedment length and if it is not, it is not adequate. Then we will have to increase the embedment length, and typically this embedment length is at least 1 1 meter.

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Design Example

Design a reinforced steep slope at 70° angle and height of 9m. Soil has shear strength properties of $c=0$, $\phi=30^\circ$ and unit weight of 20 kN/m^3 . The long term allowable design strength of reinforcement is 25 kN/m . The pullout interaction factor is 0.80 and sliding interaction factor is 0.70. Uniform surcharge (q)= 20 kPa . Thickness of compaction layer is 250mm

Find the safe vertical spacing of reinforcement layers and the length of reinforcement layers. Required factor of safety is 1.50.



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So, now let us consider a simple example let us design a reinforced slope which has 70 degrees angle, and the height of the slope is 9 meters. And the shear strength properties of the soil or C equal to 0, and friction angle ϕ is 30 degrees and the unit weight of the soil is 20 kilo newtons per cubic meter. Then the long term allowable design strength of the reinforcement is a 25 kilo newtons per meter and the pullout interaction factor is 0.8 and the sliding interaction factor is 0.7, and the uniform surcharge is 20 k P a and then the thickness of the compaction layer is 250 millimeters. And as we have seen with the design of reinforced soil retaining walls the vertical spacing between the reinforcement layers should be multiples of the thickness of this compaction layer, and we are required to find the safe vertical spacing of the reinforcement layers, and the length of reinforcement layers and our required factor of safety is 1.5.

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$$K_a = \left[\frac{\sin(70 - 30)}{(\sin 70)^{1.5} + \sin 30 \sqrt{\sin 70}} \right]^2 = 0.212$$
$$R_v = (0.5 \cdot 20 \cdot 9 \cdot 9 + 20 \cdot 9)(\cot(30) - \cot(70)) = 1354.4 \text{ kN/m}$$
$$\Sigma T = (1.5 - 1) \cdot 1354.4 \cdot \tan(30) = 390 \text{ kN/m}$$

No. of reinforcement layers = $390/25 \cong 16$

Permissible vertical spacings at different depths



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So, now let us go back to our equations and our K_a for this case is if we substitute beta of 70 degrees and friction angle of 30 degrees into that equation, we get 0.212. And for a vertical soil retaining wall having a friction angle of phi our K_a is one third that is 0.33 whereas, here this value much lower 0.212, and our R_v that is the the vertical force acting in that triangular portion that is the sum of the soil weight. And then the surcharge load is one half gamma H square plus q times height H and cotangent 30 that is phi minus cotangent beta that is cotangent 70, that is 1354.4 kilo newtons per meter and as you may recall all our designs are done per unit length in the perpendicular direction to the plane of analysis.

And if you substitute this our sigma of t that is a sum total of our reinforcement forces comes out as 390 kilo newtons per meter, and our number of reinforcement layers is 390 by 25 that is approximately 16. And our 25 is the long term allowable design strength and this long term allowable design strength should include the construction induced damage biological damage then chemical degradation. And then the cre-prediction factor as we have discussed in earlier lectures, and so this the total reinforcement force required is 390, and the number of reinforcement layers is 25 sorry 16, and now we need to find the permissible vertical spacings at different depths.

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Maximum permissible spacings

Depth from surface (m)	Vertical pressure (kPa)	Permissible Spacing = $T_{LTDs}/K_n \cdot \sigma_v$	Provided spacing
1	1*20 + 20 = 40	25/(0.212*40)= 2.9 m	0.75m
2	2*20 + 20 = 60	25/(0.212*60)= 1.9m	0.75m
3	3*20 + 20 = 80	1.47m	0.75m
4	4*20 + 20 = 100	1.17	0.75m
5	5*20 + 20 = 120	0.98	0.75m
6	6*20 + 20 = 140	0.84	0.75m
7	7*20 + 20 = 160	0.73	0.50m
8	8*20 + 20 = 180	0.65m	0.50m
	9*20 + 20 = 200	0.58m	0.50m


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And for this our permissible spacing is the T, that is the the long term allowable design strength divided by the the force transferred over height of S v, that is the the spacing and that spacing. If we equate T 2 that permissible spacing in terms of s v our spacing comes out as T by T a times sigma v, and this we need to do at at all the depths at some convenient depths. So, at a depth of 1 meter the vertical pressure is 40. So, it is 25 by this quantity 0.212 times 40 and this comes out as a 2.9 meters, but then our if we provide reinforcement at a very large spacing, we may have failure between two reinforcement layers and because of that all the design codes they recommend the maximum spacing.

That you can provide usually it is not more than one meter because we have very large spacings each the soil height between the reinforcement layers may have failure because as you recall the action the reinforcement is only in its own plane, and the affect gets transferred to some height. So, here the last column is the provided spacing that is 0.75 meters and this 0.75 meters is in the multiples of the in the thickness of the compaction layer is 250 millimeters. So, if we do this calculations at a depth of two meters it is 1.9 at a depth of three meters 1.47 and it go it is reducing at the bottom most 0.9 meters it is 0.58 meters.

So, theoretically we cannot provide the 0.58 because our compaction layers or in a thickness of 250 mm. So, we need to provide at minimum 50 milli 50 centimeter spacing and as we go up even at a depth of 7 meters the spacing required is 500 m m and at a

depth of 6 meters our permissible spacing increases to 840 m m. So, we can provide at 750 m m. And now we need to a distribute these 16 layers or the height of soil by taking this as the guideline the maximum spacing that we provide at any depth should not exceed these values.


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The reinforcement layers are provided at depths from surface of 9, 8.75, 8.5, 8, 7.5, 7, 6.25, 5.5, 4.75, 4.0, 3.25, 2.5, 1.75, 1.0, 0.50, 0.25 = 16 layers

Top two layers are provided at 0.25 m spacing near to the surface to take care of surface loads

Length of Reinforcement layers:
As per FHWA guidelines, minimum embedment length beyond rupture surface is 1m.

Minimum Length of top most layer
 $= (9 - 0.25) * (\cot 30 - \cot 70) + 1 = 12.9 \approx 13\text{m}$

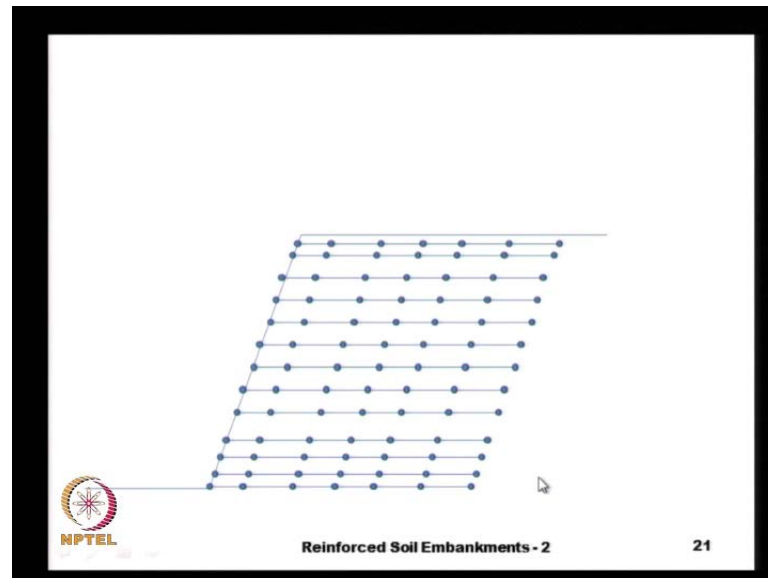
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So, by trial and error we can provide the 16 layers this particular case we can provide one reinforcement layer at the at the base that is at 9 meters depth, and another at two 50 m m 8.75, 8.5 8, and so on. And towards the top we need one extra layer of reinforcement, because that is to take care of any surface compaction pressure and then the surface traffic that is moving on and so this the we have provided as per the codal provisions the top most layer should be at a depth of one compaction layer.

So, that is a 250 m m in this case and is actually these provided spacings or slightly less than 500 m m, that is 250 m m to accommodate 16 layers. And now we need to once we choose the vertical layout, now we need to choose the the length of reinforcement layers. And the length of reinforcement layers is very simple to calculate if you understand that we need a certain minimum anchorage length, and the federal highway administration guidelines say that minimum embedment length is 1 meter. And that means, that the in terms of the criticality the top most reinforcement layer is the most critical. Because that will have the least embedment length assuming that all the reinforcement layers are of the same length. So, this calculating the length of the top most layer that is 1 meter is the

is the the length of reinforcement beyond the rapture surface. And the distance from the slope up to the to the rapture surface is 9 minus 0.25; that is H minus Z time cotangent phi minus cotangent beta plus 1 that is 12.9, that is you can round it off 13 meters.

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So, now we need to check whether this 13 meters length is adequate from from the other considerations, and this is the schematic of the different reinforcement layers. So, of totally 16 layers provided that different depths as as we have indicated here.

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Minimum length at 5m depth

$$= (9 - 5) * (\cot 30^\circ - \cot 70^\circ) + 1 = 6.5 \text{ m}$$

Provide reinforcement layers of length 6.5 m up to height of 5 m and 13 m beyond that height.

CHECK FOR BASE SLIDING

$$P = 0.5 * 0.212 * 20 * 9 * 9 + 0.212 * 9 * 20 = 210 \text{ kN/m}$$



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And let us calculate the what is the minimum length required at some other depths. Let us say that at 5 meters depth somewhere in between in in mid way through it is only 6.5 meters. So, now, let us aim for lower length of 6.5 meters in the bottom portion because in the in the bottom portion our a length of embedment is going to be very very high if you provide full 13 meters, and we can try it economize by providing a shorter length of reinforcement in the bottom portion.

So, now the provided reinforcement layer length is 6.5 meters up to a height of 5 meters and 13 meters beyond that height. Let us let us just have a very simple design only two lengths 6.5 meters in the bottom portion and 13 meters at the at the top of the the slope. Let us now check for the base sliding and the total lateral force is one half $K a \gamma H^2$ plus $K a \times H \times q$, that is 210 kilo newtons per meter.

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Check for pullout resistance of top most reinforcement layer:


$$S_v = 0.25 + 0.25/2 = 0.25 + 0.125 = 0.375$$

Vertical pressure at 0.25 m depth = $0.25 \times 20 + 20 = 25$ kPa

Force transferred into this layer = $0.212 \times 25 \times 0.375 = 1.99$ kN/m

Pullout resistance = $2 \times 0.25 \times 20 \times 0.8 \times \tan(30) \times 1 = 3.69$ kN/m

FS against pullout failure = $3.69/1.99 = 1.8 > 1.5$ (OK)

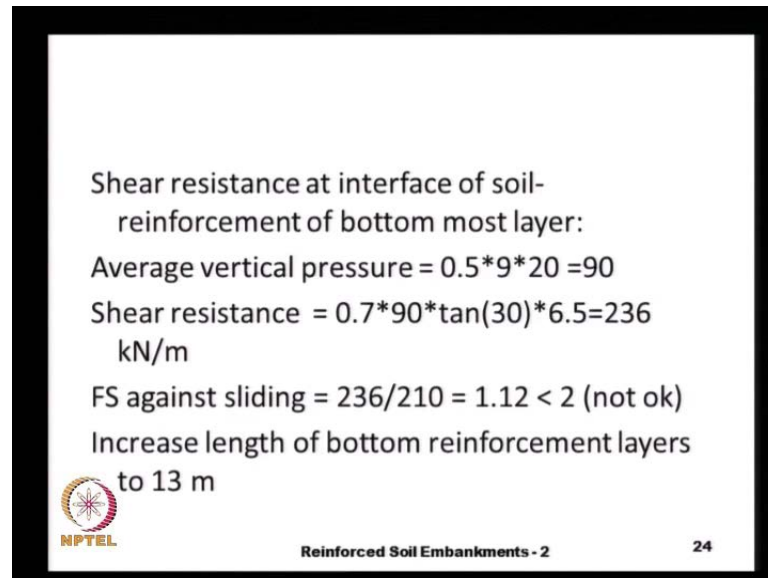


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And the oops.

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Shear resistance at interface of soil-reinforcement of bottom most layer:
Average vertical pressure = $0.5 \times 9 \times 20 = 90$
Shear resistance = $0.7 \times 90 \times \tan(30) \times 6.5 = 236$
kN/m
FS against sliding = $236/210 = 1.12 < 2$ (not ok)
Increase length of bottom reinforcement layers to 13 m

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The shear resistance at the interface of the soil to reinforcement layer is average vertical pressure is 0.5 times nine times 20 that is 90 k P a. And the shear resistance the our a shear interaction parameter is is 0.7 0.7 times vertical pressure is 90 times tan phi that is tan 30 times 6.5 that is 236 kilo newtons per meter, and the factor of safety against sliding is 236 divided by 210. And this factor of safety oops this factor of safety is coming as 1.12 which is less than 2. So, it is not sufficient. So, we need to increase the length of the reinforcement.

So, we need to increase the the length of the bottom reinforcement layers to 13 meters. So, we can provide uniform length of 13 meters of the full height of the the slope and now we need to also check for for the the pullout. And then the rapture let us check the and the top most reinforcement layer and the the the top most reinforcement layer takes the force that is coming from the soil above this reinforcement layer, and on the force over the half spacing that to the next bottom layer.

So, it is the S_v is 0.25, that is the the height of soil above the above that particular layer plus 0.25 by 2 that is 0.375. And the vertical pressure 0.25 meter depth is 0.25 times gamma plus q that is 25 k P a. And the force transferred into this layer is K_a times q times S_v 0.375 that is 1.99, and the pullout resistance, because at the this height we have only 1 meter embedment length. So, it is two times 0.25 times 0.25 is the height of soil times 20 as here, I am ignoring the effect of surcharge.

Because as per the codal requirements we should ignore the effect of live loads surcharge on the pullout resistance, because that is the worst case scenario is actually that is also as per the case b of the b s 8006. And the pullout interaction parameter is 0.8 and this two is because we have the shear force developed on both the surfaces times tan 30 times one is the embedment length; that is 3.69 kilo newtons per meter. So, the factor of safety against pullout failure is is greater than is greater than 1.5 it is its coming as 1.8. So, it is safe.

So, our the length of the reinforcement layer is 13 meters that is sufficient as far as the pullout and the base sliding is concerned, and the vertical spacings are as as designed earlier and because our vertical spacing that is provided is much lower than the permissible spacings. We will not have any rapture rapture failure and the. So, far we have discussed the stability of slopes under static loading, but in many cases will have to design the slopes even for earthquake forces.


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Stability Under Seismic Forces

F_h = seismic force acting in horizontal direction
(worst case is acting outwards)

F_v = seismic force acting in vertical direction
(downwards – acts along with weight
Upwards – reduces the weight)

$F_h = k_h W$, W = weight of soil in failure wedge
 $F_v = k_v W$
 k_h, k_v = seismic factors

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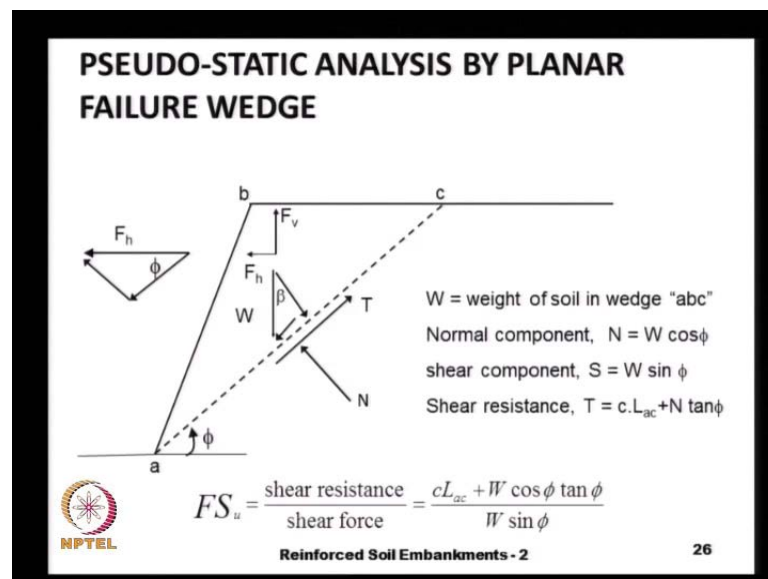
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And now let us include the additional force that we have, because of the seismic seismic forces and let us say that we have two extra forces F_h ; that is the seismic force acting in the horizontal direction and this horizontal force, because of the seismic action could act into the soil are away from this soil. And in the worst case is the F_s acting away from the soil, and because if it is acting into the soil, it tends to stabilize the soil, and F_v is the seismic force acting in the vertical direction. And it could act either downward or

upward, because it can act both ways. And if it act downwards it acts along with the weight of the soil. So, it increase the normal resistance, but then also increases the the shear force and if it acts upwards it reduces the weight. So, it reduce not only the normal force. But also the shear shear force and f h it can be written as sum factor K h times w where W is the weight of the soil within the failure wedge and F v is the K v times W where K h and K v are the seismic factors. And there are so many empirical factors given to estimate the K h and K v values and as we have discussed earlier.

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We need to use the earliest 1893 for estimating these factors . So, now let us look at the pseudo-static analysis of this slope the subjected to seismic action. Let us consider the same slope at an angle of beta, and the rapture surface is is is at an angle of phi that is the the the most critical rapture surface and we have are layer considered the normal force n t and then the shear force acting down. And now we need to consider two additional forces F h and F v and F h is the horizontal seismic force that is the most critical one if it is acting out outwards, and F v can act either upper down and the factor of safety of the unreinforced slope is is like this. As we have seen earlier and by considering the by considering the action of this additional forces. We need to consider the or we need to determine.

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PSEUDO-STATIC ANALYSIS BY PLANAR FAILURE WEDGE

Consideration of seismic loads

- Pseudostatic forces F_h and F_v act on the slope because of an earthquake.
- Worst possible direction for horizontal seismic force is the outward direction.
- The effect of vertical force is to reduce the weight of the wedge of soil to $(W-F_v)$.
- The horizontal force produces a normal component acting opposite to the weight and a tangential component that acts down the slope.



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The factor of safety of the slope the most critical case and our the pseudo-static forces are the F_h and F_v . And the worst possible direction for the horizontal seismic force is the outward direction, where as the the vertical load vertical force, because of the because of the seismic excitation is either to increase or decrease the effect of the weight.

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FS considering the pseudo-static forces

$$FS_{seismic} = \frac{\text{resisting force}}{\text{driving force}} = \frac{c L_{arc} + [(W - F_v) \cos \phi - F_h \sin \phi] \tan \phi}{(W - F_v) \sin \phi + F_h \cos \phi}$$

- Horizontal seismic force clearly reduces the factor of safety because it reduces the resisting force and increases the driving force.
- Effect of vertical seismic force is minimal because it decreases both the resisting and driving forces and hence it has lesser influence on the stability of slopes.



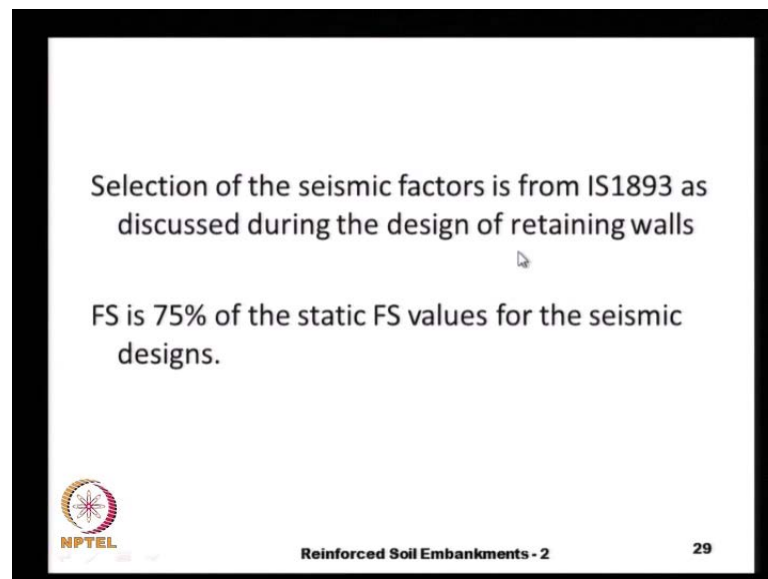
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And if you resolve all the forces our resisting force is C times L_a and W minus F_v times cosine phi assumed that the vertical force is acting up and minus $F_h \sin \phi$. This whole thing times tan phi. So, you see that the effect of the horizontal seismic force is to reduce

the resisting force, it is reducing the normal force; that is acting and this whole thing divided by the driving force that is the W minus F_v . That is the vertical force plus $F_h \cos \phi$ and $F_h \sin \phi$ is the shear force acting on the slope because this horizontal component. So, this the horizontal seismic force reduces the factor of safety because it is reducing the resisting force while increasing the driving force because it is reducing the a numerator.

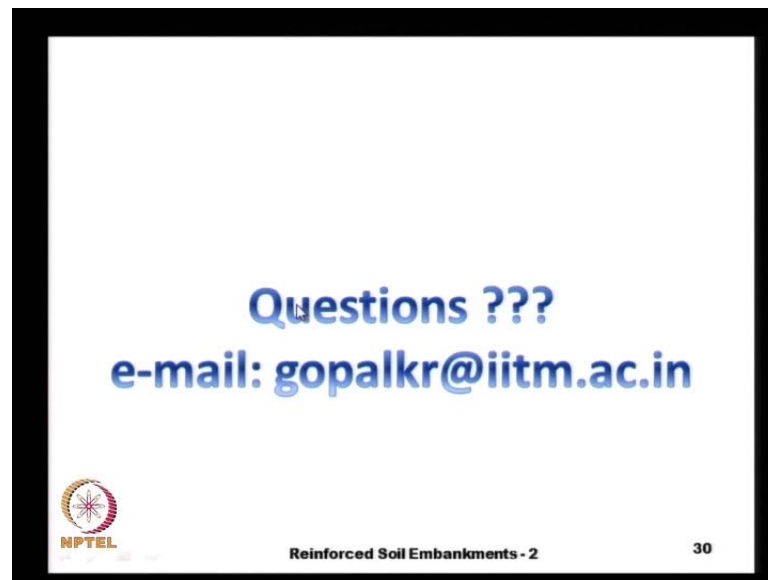
And increase in the denominator where as the effect of the vertical seismic force is the same like it is decreasing the the a numerator, and is also increase decreasing the denominator. And if we assume that the vertical force is acting down it becomes w plus F_v and the numerator and W plus F_v in the denominator. So, it is the effect of F_v is a very minimal whereas, effect of F_h is quite significant.

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And how do we select the K_h and K_v once again we can go back to our IS 1893 the the code of practice for design of the seismic resistance of the buildings. And this we have already seen how to apply for the design of retaining walls the same principles apply even for this case. And when we consider the seismic forces our factors of safety can be reduce by reduced to 75 percent and the static values as we discussed earlier say for example, if we need factor of safety of 1.5 and the static is under seismic case it should be it can be 1.125.

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So, that is the end of this lecture, and if you have any questions you can contact me at this email address.

Thank you.