

Geotechnical Engineering II / Foundation Engineering
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Lecture – 50
Anchor Bulkhead (Contd.)

In my previous lecture I just showed how to analyze Anchor Bulkhead and particularly anchor bulkhead can be of 2 time 2 types, that I have mentioned. That is one is free earth support another is fix earth support and again as I have mentioned that fix earth support I will not consider only I will consider free earth support.

And then free earth support design also can be done 2 ways, that is one is actually just by considering equilibrium find out depth required and then increased by 30-40 percent to have a factor of safety of 1.5 to 2. And, that is the method I have discussed and another method was actually we can apply that what are getting the earth pressure diagram in the passive pressure actually is the supporting actually resisting and active pressure is at disturbing.

So, the resisting pressure actually we can reduce by providing a factor of safety and then consider equilibrium and from there if you get the depth that become the final depth. So, that is another approach that is also I am not discussed, only I have discussed that free earth support with straight equilibrium pressure diagram consider equilibrium and find out the depth and then increased by some 30 to 40 percent. So, that is the way I have done and that same problem at one problem I will just try to show how to actually numerical problem how to solve. So, that problem let me start one problem.

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Deep Excavation

Determine the depth of embedment and the force in the tie rod of the anchored bulkhead shown in the Figure. The backfill and the soil below the dredge line is sand having the following properties: $G = 2.6$, $e = 1.0$, $\phi = 10$ degrees, $h_1 = 2$ m, $h_2 = 3$ m, and $h_3 = 4$ m.

Depth of embedment of an anchored bulkhead by the free-earth support method

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This is a problem suppose you can say the problem is given here determine the depth embedment and the force the tie rod of the anchored bulkhead shown in the figure. This may be the anchored bulkshead it is with pressure diagram of course, this will never be like that. In the problem always will be like this it will be like this it will be like this and it will be like this anchored bulkhead. And, then all dimensions will be the backfield and the soil below the dredge line is sand actually sand here, sand also here. I have shown actually this with pressure diagram because, same figure I have used otherwise most of the if in your in your exam problem all always will be like this.

And it will be shown this dimension it will shown this dimension it will show this dimension; if water table is here this dimension it will show and this is the unknown things ok. So, otherwise these are the things will be given to here also it is given you can see the both the sand and instead of unit weight it is given actually G value is given 2.6, e value might be void ration is given 1. And, ϕ that mean angle of internal friction is given as 10 degrees and it is 10 degrees or 30 degrees; it will be 30 degrees actually; do not you so, less cannot be it will be 30 degrees ok.

And h_1 h_2 h_3 is this one is 2 metre and h_2 is this one is 3 meter and h_3 actually from your h_3 is from tie rod to the dredge line that is actually 4 meter you can see this is 4 meter. So, this is 4 this is 2 and this is 3 show 2 3 5 and this is this is 4; that means, this distance will be 1 meter; so, that is not given, but one can find out. So, under this

condition actually the; what is the thing you have to do; you have to find out the depth of embedment that is D and you have to find out what is unknown force T a acting in the tie rod. So, this is the problem; so this problem I will try to same diagram will be similar, but I will draw once again maybe in the next slide ok.

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Deep Excavation

$$K_a = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ} = \frac{1}{3}$$

$$K_p = \frac{1}{K_a} = 3$$

$$K = K_p - K_a = 2.67$$

$$P_a = 10 + 8 = 18$$

$$P_b = (18 - 10) = 8 \text{ kN/m}$$

$$\gamma_s = \frac{2.6 + 1.0}{1 + 1.0} \cdot 10 = 18 \text{ kN/m}$$

$$\gamma_{bulk} = 15 \text{ kN/m}$$

$$P_1 = 15 \times 2 \times \frac{2}{3} = 10 \text{ kN/m}$$

$$T_a = P_a - P_1 + \gamma_b \times 2 \times \frac{2}{3}$$

$$\gamma = \frac{G - \gamma_w}{1 + e}$$

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So, this is the one and you can see the your rod is here and this is T a this distance is 2 metre and of course, this distance is 3 meter and this is y naught and your we can find out there are many things to be obtained. So, with this actually we can find out actually your P p will be acting somewhere and P a will be acting somewhere and T a will be acting there.

So, we have to find out in the previous diagram whatever notation I have shown same notation will be used; I have corresponding to this present problem I have shown this. Now what would be the pressure here at this point what is the pressure? At this point pressure will be gamma dry times 2 2 times K a. So, K a is how much here? K a equal to 1 minus sin 30 divided by 1 plus sin 30 and if I do that it will come at 1.3 1 by 3 and your K p will be coming just 1 by K a. So, it will be 3 so, K will be equal to K p minus K a equal to 2.67 these are the things will come.

And you can see that gamma is not given instead of G and vertices given. So, gamma saturated will be equal to G plus e by 1 plus e multiplied by gamma w. So, if I put the all values that is 2.6 plus 1 divide by 1 plus 1 and multiplied by gamma w, suppose if I take

10 then this will come actually 18 kilo Newton per meter cube; 18 kilo Newton per metre cube this is coming ok. So, gamma gamma saturated is coming 18 18 point kilo Newton per where so gamma submerge gamma b will be 18 minus again 10 if I take; so, it will come 8 kilo Newton per meter cube gamma b will come 8 kilo.

And now above dredge level above dredge level what is the value I could have done, but I have not done actually that will be actually your gamma dry will be equal to G by 1 plus e multiplied by gamma w this is the way it could have done. So, I have not done so, let me see I have used 15 let me see what is the value here; let me see by calculation. This may come something different I could have done that it is 2.6 divided by 2 multiplied by 10. So, it is 13 actually so, it is 13 actually dry unit weight actually 13.

So, as the close to water table the soil hardly will be dry ok. So, it will be generally some dry unit weight we have to take the bulk unit weight and bulk unit weight slightly more than the dry unit weight because, the other moisture present. So, in this calculation I have taken gamma bulk that mean or gamma bulk above water table as taken as 15. So, this is the way I have taken. So, 15 here gamma here actually gamma submerge 8 every everywhere gamma submerge 8.

So, now without going further I can find out straight this intensity here I can find out p_1 bar that will be how much, that will p_1 bar actually it will be 15 multiplied by 2 multiplied by 1 by 3. How much it is? It is coming 10 kilo Newton per meter square. Similarly, I can find out at this point what is the value. So, this is actually P_a bar; P_a bar will be equal to p_1 bar plus gamma b multiplied by this is 3 and multiplied by 1 by 3. So, it will be 10 plus 8.

So, it will be 18 at this point it will be 18 and similarly I can find out it here I will not going to find out it will be in terms d naught we do not know y naught and we do not know d . So, these are the things are known. Now, I will go to the next one I could have done this one in the differently, but anyway. So, next part will be if I do I will continue to the next part; so up to P_a bar I have done.

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Deep Excavation

$$y_0 = \frac{p_a}{\gamma_b K} = \frac{18}{8 \times 2.67} = 0.84$$

$$P_a = \frac{1}{2} \bar{p}_1 h_1 + \bar{p}_1 h_2 + \frac{1}{2} \gamma_b h_2^2 + \frac{1}{2} \bar{p}_a \times y_0$$

$$= 59.56 \text{ kN/m}$$

$$59.56 \bar{y} = \frac{1}{2} \times 10 \times 2 \times (3 + 2 + 0.84) + 10 \times 2 \times (\frac{3}{2} + 0.84) + \frac{1}{2} \times 8 \times (3 + \frac{3}{2} + 0.84) + \frac{1}{2} \times 18 \times 0.84 (\frac{2}{3} \times 0.84)$$

$$P_1 y_1 + P_2 y_2 + P_3 y_3 + P_4 y_4$$

$$\bar{y} = 2.37 \text{ m} \quad y_c = 4 + 0.84 - 2.37 = 2.47 \text{ m}$$

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And your what is y naught? y naught will be equal to P a bar divided by gamma b multiplied by K. So, it will be how much then P a bar is how much? We have got 18 divided by gamma b is 18 8 and K is 2.67. So, how much it comes? It will come 0.84 ok. And what will what about P a? P a is P a will be now actually we have got this diagram we have got this then we have got this and we have got this. So that means, how many component will be there? This is 1, this is 2, 3 and this 4 there will 4 parts.

So, this one first part will be half p 1 bar multiplied by h 1 ok; that means, P a total plus I will take this triangle this rectangle that will be equal to p 1 multiplied by h 2 plus this portion that will be equal to that will be half gamma b multiplied by h 2 square. Or, this way we can do yeah; this is the way we can do plus half P a bar; that means, this one this one P a bar multiplied by y naught nothing, but actually I am find out area of this area of this area of this and area of this. So, that become P a; so, if I put all values p 1 value is 10 p 1 bar is 10.

So, and h 1 is 2 meter then p 1 and here actually we can 10 and 2 and here actually gamma b 8 and h 2 square. P a bar actually 18 y naught is 0.84 all values if I put then this will come actually P a is coming actually 59.56 59.56 kilo Newton per metre square ok. And to find out the y bar, y bar actually what is shown actually the point of application from the tie rod. So, so 59.56 59.56 multiplied by y bar and then I will take half into 10

half; that means, first diagram 10 multiplied by 2 multiplied by from here actually it is 3
3 plus 2 into 1 by 3 and plus 0.84.

So, from here from here two point of application actually I will try to find out; this one
the I have consider only this first part K. So, actually see this is 2 meter the point of
application will be one-third of 2. So, that is what one-third of 2 then 3 then 0.4 so; that
means, distance of this force from here actually we have got. And, then actually y bar
actually we are calculating y bar is nothing, but your point of application from here ok.
And, we are considering the all forces distance from here this is the reference I am
considering this distance first that is done plus I will consider second one: 10 multiplied
by 3 10 multiplied by 3 multiplied by that what distance. It will be 3 by 2; that means, it
will be midpoint plus this 0.84. Then I will find out this third triangle that will be equal
to half multiplied by 8 multiplied by 3.

And this is the diagram and y bar will be how much, that will be this distance is 3 and it
will be one-third from this side. So, 3 multiplied by one-third plus and this distance so,
0.84 Then I have to find out from here to centre of this triangle. So, that first of all I will
take the area of the triangle; the area of the triangle will be half multiplied by 18
multiplied by this distance is 0.84 this is the area of the triangle. And, multiplied by two-
third of 0.84 so; that means, from this side it will be two-third. So; that means, what I
have done from here actually I have considered force 1 force 2, this is force 1, this is
force 2, this is force 3 and this is force 4; 4 different forces they are lever arm distance
from here I have done.

So; that means, what I have done $p_1 y_1$ plus $p_2 y_2$ plus $p_3 y_3$ plus $p_4 y_4$ I have
done ok. So, I have calculated this diagram distance from here this diagram distance
from here this diagram distance from here this diagram distance from here. So, this is the
equation I have written and this is of course resultant. So, total force multiplied by y bar
that must be equal and from here I will get y bar, y bar equal to I am getting 2.37 meter.
That means, 2.37 meter; that means, from this 0 pressure point the point of application of
P a total active force is at a distance of 2.37 meter ok

Then y c y c is actually what y c actually distance from the anchor rod. So, this force this
force to anchor rod we have to find out. So, I have got from here to this force I have got
2.37 and from anchor rod to 0 force is how much distance; anchor the this is the anchor

position anchor position somewhere here. Anchor position to your anchor position to your anchor position to your 0 position, that is actually it was 4 meter from anchor to the dredge level plus if I go y naught 0.84; that means, from 0 pressure to the anchor this much distance and, I know from here to point of application of force is 2.37.

So; that means, you are getting the distance between the point of application of force to the this is actually y c ultimately; that means, at force I have to take moment of force P a force to the anchor rod. So, I have to I have to know the distance so, that become y c. So, this become 4 plus 8 4; that means, from here to this 4 meter and plus I add 0.84 and then subtracted y bar that is 2.37 So, that become your y c so, that become actually your 2.47 meter ok. So; that means, now I have got the lever arm from P a to anchor rod I have got and I now P p 2 anchor rod I will get; then I will take the moment. Then I will be able to formulate the equation and then solve for D naught ok.

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Deep Excavation

$$P_p = \frac{1}{2} \times \gamma_b \times K \times D_0^2 = \frac{1}{2} \times 8 \times 2.67 \times D_0^2 = 10.66 D_0^2$$

$$h_4 = h_2 + y_0 + \frac{2}{3} D_0 = 4.84 + 0.67 D_0$$

$$P_k \times y_c = P_p \times h_4$$

$$59.56 \times 2.47 = 10.66 \times (4.84 + 0.67 D_0)$$

$$f = D_0 + 7.22 D_0 - 2.06 = 0$$

$$D_0 = 1.54 \text{ m}$$

$$D = D_0 + y_0 = 1.54 + 2.84 = 2.38 \text{ m}$$

The diagram shows a retaining wall with height h_4 . The dredge level is at y_0 . The point of application of force is at $h_4/3$ from the dredge line. The diagram also shows a force P_p acting at a distance D_0 from the dredge line. The diagram is annotated with values: $D_0 = 1.54$, $D_0 = 1.6 \rightarrow 1979$, $D_0 = 1.5 \rightarrow 1078$, $1.55 \rightarrow 1667$, and 1.55 circled in red.

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So, next I will go to and your P p actually your P p equal to your P p equal to half gamma b times K D naught square. So, that will be equal to then if I put the values half multiplied by 8 multiplied by 2.67 multiplied by D naught square. So, that if I equate then it will become 10.66 D square and h 4 h 4 actually is nothing, but the point of application of P p to the anchor rod. So; that means, if I draw the diagram once again let me draw the diagram once again this is dredge line sorry; let me suppose this line

somewhere here h_4 actually your anchor rod is here and the point of application here. So, this is h_4 this is the anchor and the point of application of P_p this is P_p .

So, h_4 then it will be h_3 plus y_{naught} h_3 actually from here plus y_{naught} plus from here I am getting actually and then I have to go two-third of D_{naught} . So, that plus two-third of D_{naught} so; that means, it will be 4 plus; that means, this is 4 and this is y_{naught} 84. So, it will be 4.84 plus 0.67 D_{naught} square sorry D_{naught} . So now, P_a multiplied by y_c equal to P_p multiplied by h_4 that must be equal. And if I do this then it will be 59.56 multiplied by 2.47 we have got before equal to 10.66 is the P_p multiplied by this 4.84 plus 0.67 D_{naught} .

So, this is the equation I am getting and if I simplify this equation I will get equation- further D_{naught} cube plus 7.22 D_{naught} square plus minus it will be not plus minus 20.6 equal to 0. So; that means, this is the equation you can see oh; so, here I have wrongly written 10.66 D_{naught} square. So, this D_{naught} square and D_{naught} become cube so, this I have got So; that means, if I simplify this equation I will get a equation like this 10 D_{naught} cube plus 7.22 D_{naught} square minus 20.6 equal to 0. So, this is a cubic equation and this equation we can solve only by trial and error. And that means, I can assume some depth and then if I assume D_{naught} equal to D_{naught} equal to 1.6 if I assume, then the value of this function become this function become 1.979 1.979.

And, if I take D_{naught} equal to 1.55 or 1.5 if I take D_{naught} equal to 1.5 then you are getting this value as minus 0.98 minus 0.98. If I take 1.55 1.5 I get this one as 0.6 0.469 and if I take 1.54 then I get 0.175. So, this is coming to very close to 0 so, I can consider as; that means, D_{naught} value can be taken as 1.54 meter ok. So that means, so, this depth this depth is known now D_{naught} we got equal to 1.54. Now, once you know the D_{naught} then D will be equal to D_{naught} plus y_{naught} so; that means, 1.54 plus 0.84 that become your 2.38 meter. And then based on that 2.38 meter so, D_{naught} already known now this D_{naught} is known now P_p is known P_a already known 59 point something.

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Deep Excavation

$$P_p = 10.66 D^2 = 25.3$$
$$T_a = P_a - P_p = 59.56 - 25.3 = 34.27$$
$$D = 2.38$$
$$D_{req} = D_{design} = 1.4 \times 2.38 = 3.32m$$
$$T_a = 34.27 kN$$

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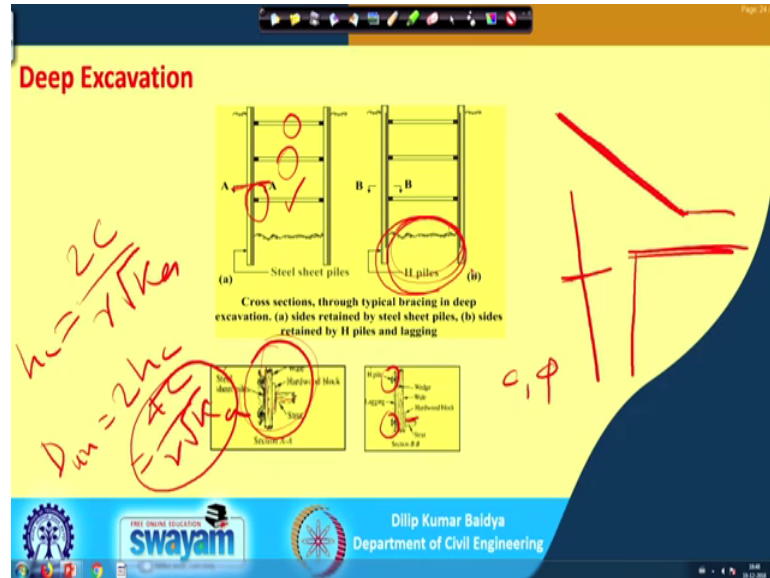
So, I can find out I can find out P_p now; P_p will be equal to your P_p actually $10.66 D$ naught square. So, that become your something value $10.66 D$ naught square; D naught is actually we have got 1.54 1.54 multiplied by 1.54 multiplied by 10.66 . So, it become sorry 1 sorry 1.54 multiplied by 1.54 equal to this multiplied by 10.66 . So, that become 25 point 25.3 suppose and then T_a will be equal to P_a minus P_p so; that means, how much it is 59.6 59.56 minus 25.3 . So, the difference will become 34.27 so; that means, your in that anchor rod force T_a is 34.27 . So that means, you have got the solution now we have got D equal to 2.38 and we can multiply by 1.4 .

So, D required or D design will be 1.4 multiplied by 2.38 so, that will be equal to 1.4 into 2.38 1.4 multiplied by 2.38 . So, that become 3.3 so, 3.3 2 meter and your T_a become 34.27 kilo Newton. And, this is the two things we have we have getting we are getting from here. And, if you want to find out the bending moment also first you find out what the pressure become 0 and then after knowing that you can find out the bending moment. So, that I am not done, but if you wish you can do it. So, otherwise this problem whatever asked actually we have achieved.

So, this is nothing actually simply you have to understand the pressure diagram and then this pressure diagram when the complicated pressure diagram we have to divide it into number of parts 1 2 3 4 . The only triangle and rectangle if you divide so, that you know the $c g$ and you know the area easily. And, based on that you can find out the lever arm to

take the moment and by doing that we can find out the D and T; so this is actually 1 part that is over.

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Now, let me after this actually this is the some sheet pile wall to retain the soil or to develop some facility water from facility. But, in some other purpose actually you need to excavate the soil sometime for different purpose. For example, for construction of metro railway suppose you have to excavate up to 30 meters, but that you know that we cannot excavate unlimited length without support vertical particularly. If you make a slope if you make a slope curve if you make a slope, then we can go quiet significant depth.

But, if you want to cut vertical then there is a limitation and that limitation actually while discussing earth pressure theories we have discussed actually that because, of that c ϕ soil the depth of tension crack actually $2c$ by $\gamma \sqrt{K_a}$ and that is actually depth of tension cap h_c . And, your depth of unsupported excavation depth of unsupported excavation will be twice of h_c so; that means, it will be $4c$ by $\gamma \sqrt{K_a}$. So, that is the thing I have we have discussed while discussing earth pressure theory; that means, if there is a ground surface having value of c and ϕ then up to what depth we can excavate without support by this equation we can find out. But, my if your excavation is much larger than that much deeper than that then what you have to do you have to give the support.

And, then you have to design the support system; that means, this is the different types of support system; you can see this is the one type of support system there will be sheet pile wall. And, then well and then there will be a hardwood block and then there will be start these are the start.

And this particular section if you see the enlarge you will see this actually cross section, if I see the cross section you will see the different component. Again another type of wall actually you can see H pile is used and then laggings are used and then whales and then again starts are given here actually. So, this is the way also can be done. So, if this is the type of support system is done for the excavation purpose particular deep excavation how to how much force will be required taken by the each start; that means, how much force is coming to the start that to be estimated.

So, for that actually some analysis has to be done; again while excavation there can be instability in the bottom also that to be investigated. So, these are the things actually I will be taking in the next class maybe next lecture; today I will stop here ok.

Thank you.