

**NPTEL ONLINE CERTIFICATION COURSES**

**Course  
on  
Reinforced Concrete Road Bridges**

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**Lecture 5 : Design Codes**

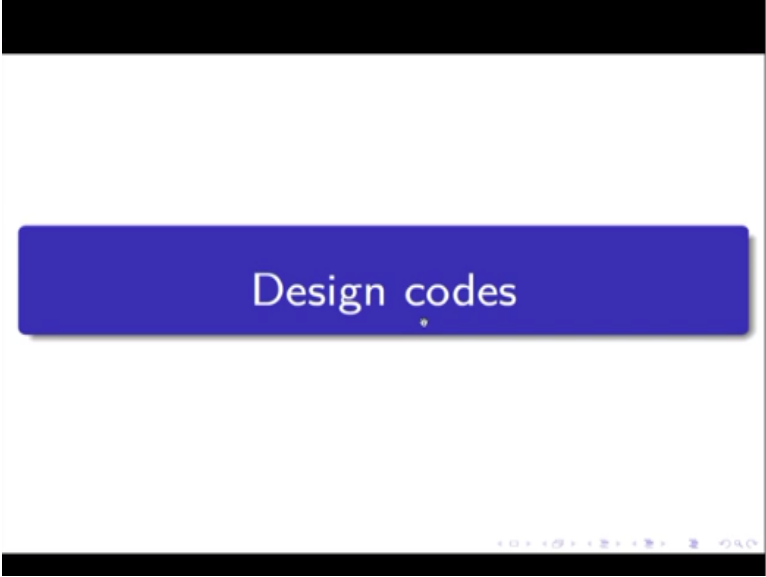
Hello every buddy. So let us start with the last part of last week that is the 5<sup>th</sup> lecture of Reinforced concrete road bridges that is lecture 5.

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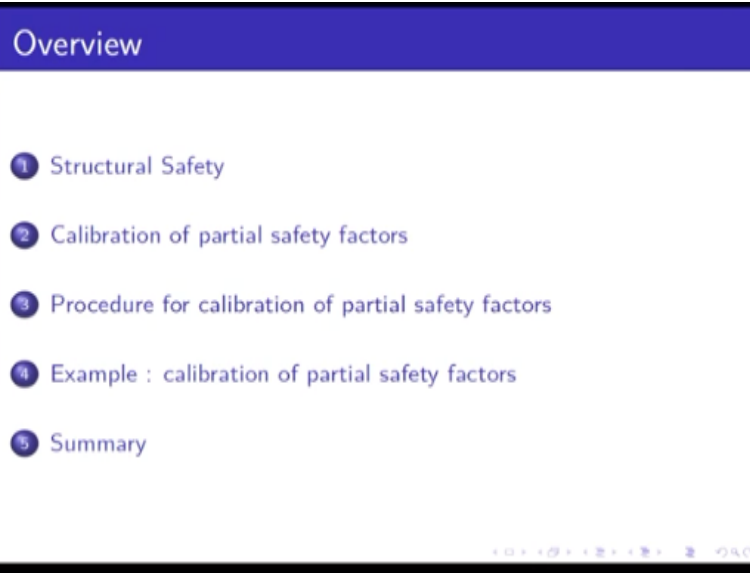


Here you shall consider the design codes.

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The basic principles of that and we shall consider the structural safety that is the first part, calibration of partial safety factors because we have observe that many times we consider that only multiplied with the different factors how do it come to that one. So I feel that with appropriate to tell something about that you can understand that how it comes that one those factors and certain calibration of partial safety factors we called and one example just simple one is I will tell you today though it is would have time is very tight but anyway since will go to the video so I hope that you can understand that the reinforced.

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## Structural Safety



To structure safety when we are considering that.

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## Structural Safety

- Structural safety appears in different forms when criteria for design are stated in codes and specifications.
- The most commonly encountered criteria for design are :
  - Allowable stress design(ASD)
  - Ultimate strength design(USD)
  - Load and resistance factor design(LRFD)



Structure safety appears in different forms when criteria for design are stated in codes and specifications so most common one allowable stress design, ultimate strength design and load and resistance factor design. So inaudible method that these are the one consider here. Let us see first what the basic idea of that is.

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## Structural Safety(contd...)

- Allowable stress design(ASD)
  - Structural members are designed such that the computed elastic stress is less than or equal to a fraction of a limiting value such as the yield stress of the material
  - The computed elastic stress is obtained from an analysis of the structure using specified design loads.



So structural members are designed such that the computed elastic stress is less than or equal to a fraction of a limiting value such as the yield stress of the material. The computed elastic stress is obtained from an analysis of the structure using specific design loads. So here in this case also we are having define design loads then you can retain load that impact factor other things you shall get that one that below which we have to overcome that is the strength of the material, strength of the axon should not be less than the applet force.

So that is the one which is called a resistant and other one you are having the applet load. So the meant so the one can consider the meant and another one consider the supply so divine means that this much load in a formal bendy moment or from a CL force. So that we have to overcome and for that these much exhibits the strength of the xn that we consider and that is the basic one if you know the ill states of particular material.

You will say it should not be more than this below. In stress with certain kind of factors of safety we can say. That means if I consider can 100 so I can say okay I shall not go more than 60. If you really consider that I can say in this particular case for limas trite we are getting point for 5 FCK that is the one as per higher scored IS456 so coming to this structural here whenever we consider the design loads that overcome here?

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## Structural Safety(contd...)

- Ultimate strength design(USD)
  - Design loads are increased by a factor
  - The computed strength of a structural member is reduced by a factor
  - The computed strength of a structural member is based on ultimate behaviour
  - An elastic analysis is used to obtain the member forces

$$V_u \leq \phi V_n \quad (1)$$

where  $\phi$  is a strength reduction factor,  $V_n$  is the nominal shear strength of the beam and  $V_u$  is the factored shear force at the section under consideration



Another one is ultimate strength design, design loads are increased by a factor the computed strength of a structural member is reduced by a factor is very interesting the thing that one way load applied your thinking okay whatever load applied should not be more let us take it. The strength whatever you got it so know I shall take less than that so that is the one you can got it. Computed strength of a strength member is based on ultimate behavior.

An elastic analysis is used to obtain the member forces so  $V_u \leq \Phi V_n$  the nominal strength here one particular reduction factor  $V_n$  is the nominal shear strength of the beam and  $V_u$  is the factored shear force at the section under consideration so this is the one basic idea of the ultimate strength design.

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## Structural Safety(contd...)

- Load and resistance factor design(LRFD)
  - This method has been introduced by the American Institute of Steel Construction(AISC).
  - It is characterized by an expression of the form

$$\sum \gamma_i Q_i \leq \phi R_n \quad (2)$$

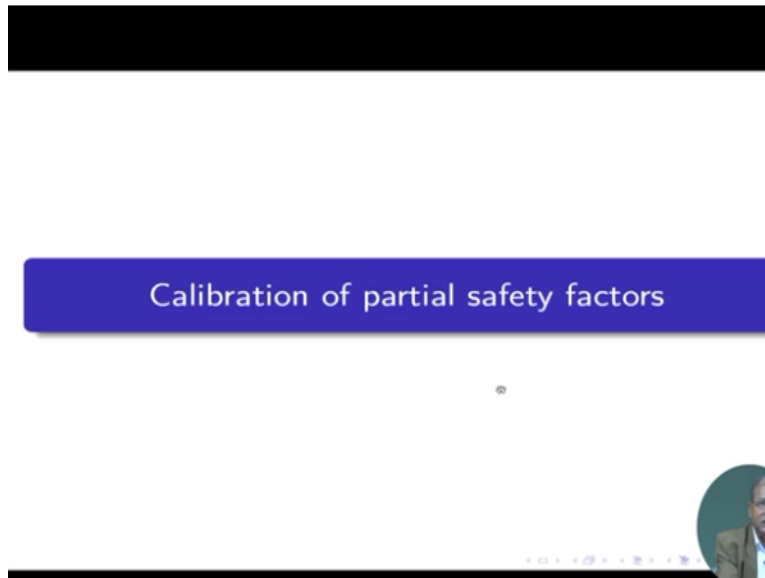
where  $\gamma_i$  is the load factor for the  $i$ th load effect,  $Q_i$  is the  $i$ th load effect,  $\phi$  is a resistance factor, and  $R_n$  is the nominal resistance(strength).

- A similar method is used in the AASHTO specification Standard Specifications for Highway Bridges

And LRFD method Load and resistance factor this method has been introduced by the American Institute of steel construction. It is characterized by an expression of the form  $\sum \gamma_i Q_i \leq \phi R_n$  where  $\gamma_i$  is the load factor for the  $i^{\text{th}}$  load effect,  $Q_i$  is the  $i$ th load effect,  $\phi$  is a resistance factor, and  $R_n$  is the nominal resistance strength.

Generally for the linear limit state function this is the one  $\beta = \mu R - \mu Q / \sqrt{\sigma^2 R + \sigma^2 Q}$  there is whenever we consider the  $\mu R$  the resistance value and  $\mu Q$  that is the one demand that were we can concentrate here this the one standard dividers but I am not telling that only one mean value here. I am telling certain kind of distribution and there is a that one is reasoning by the standard deviation so those to follows the basic of that linear one you consider that  $\beta = \mu R - \mu Q / \sqrt{\sigma^2 R + \sigma^2 Q}$  this is the one we consider here.

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Now I am not because these factor one you can consider as a part of reliability of structures that is separate subject and only I c an taken this futurology code and for reason where who are busy to do it that is a objective just to inform you that hoe it actually works so major part here calibration of partial safety factor.

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## Calibration of partial safety factors

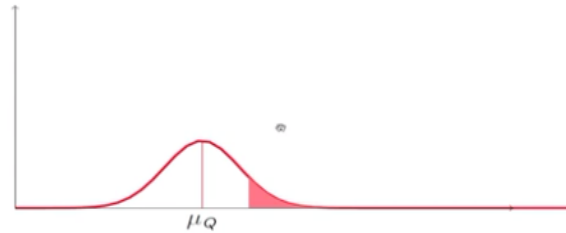


Figure 1: Relationships among nominal load, mean load and factored load

In this case as I told you whenever you having the standard deviation that means it is it not the  $\mu_Q$  means this the mean when w required here we getting this. And then you are having certain distribution that means the value whatever you are getting all those things it is having for minus minute to plus minute you can say. So I am restricted that one it should not be more than this value, this is a value this is a mean value and this is the one that I cannot go more than that, so mean value and factor load that means this is the mean value then I am telling that thing factor of that which is coming here upto this.

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## Calibration of partial safety factors

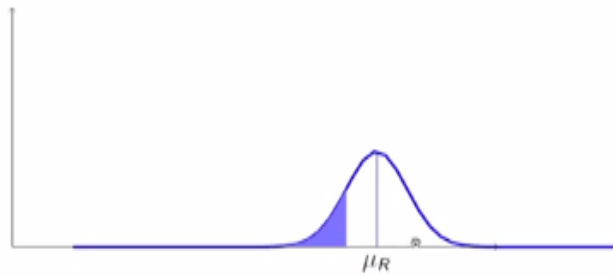


Figure 2: Relationships among nominal resistance, mean resistance and factored resistance

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Similarly for the resistance we are getting that resistance these are mean value of resistance and obviously at my strength is reduced I shall never go this side.

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## Calibration of partial safety factors

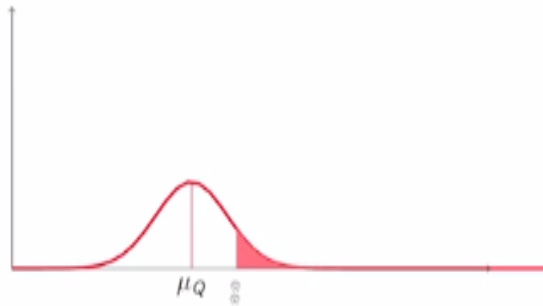


Figure 1: Relationships among nominal load, mean load and factored load

So you can see for load we are increasing that, this is the mean value I am going increasing.

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## Calibration of partial safety factors

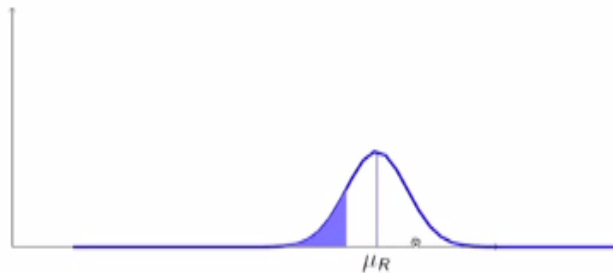


Figure 2: Relationships among nominal resistance, mean resistance and factored resistance

Whereas in the strength one I am reducing that value that mean you are certain factor that mean it should be less than one but whereas for load it should be greater than one, 1.2 1.5 if you remembered those particular value you are getting but in other side you are dividing by 1.5 you are dividing by 1.15 that means still your value is less than 1, so this is the one you are getting it here.

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## Calibration of partial safety factors

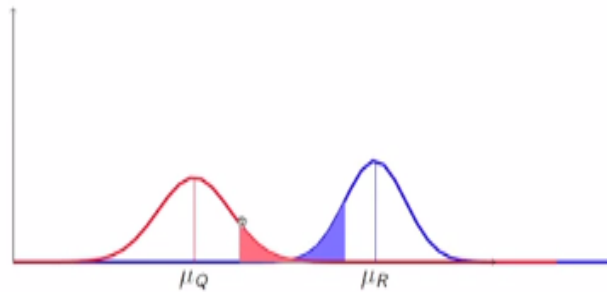


Figure 3: Relationships among nominal, mean and factored load and resistance

So coming to this one here I have increase this value here so obviously it is the very good decision that wherever value you are telling that how much load is coming you have told me something or I am telling you that one this much value is coming but your wise no okay let us take something more so you have taken something more, whenever I am telling the obvious strength of the material I might tell this one this is the mean value I am telling.

Then your flavor that intelligent that you know I shall tell little less so that means here this particular value is greater than this particular value this is the basic idea of our thing that means I have find out these value how much shall I increase how much shall I decrease that factors we have to calculate and that is called that partial safety factors.

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## Calibration of partial safety factors(contd..)

- In load and resistance factor design (LRFD) or limit state design (LSD), load components are multiplied by load factors and resistance is multiplied by a resistance factor.

- The basic form of the LRFD equation is

$$\phi R \geq \sum \gamma_i Q_i \quad (4)$$

- where  $\gamma_i$  is a load factor applied to load components (or load effect)  $Q_i$  and  $\phi$  is a resistance factor applied to the resistance (measure of load carrying capacity)  $R$ .

And the obviously there is a basis on that so this is your limits state this one so now the thing is that let me tell you another important aspect whenever we consider the limit state design that allowance state design all in popularly known as say working state design that is also another form of limit state so limit state means actually whatever in a conventional way whatever we are familiar that is not the only one the others also another way of talking that one say limit state here.

So basic form of the elaborated method five here  $\geq \sum \gamma$  if you guide for define loads your factors should be different that factor one will be there, so  $\gamma$  is a load factor applied to the load components  $U_i N \emptyset$  is resistor factor applied with the resistance so that way we can find out okay.

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## Calibration of partial safety factors(contd...)

- The basic form of the LRFD equation is

$$\phi R \geq \sum \gamma_i Q_i \quad (5)$$

- In words, the equation says that the capacity of the structural member (modified by the factor  $\phi$ ) must be larger than the total effect of all the loads acting on the member.

And similarly that particular one equation we are getting it here in word the equation says that the capacity of the structural member modified by the factor  $\phi$  must be larger than the total effect of all the loads acting on the member and obviously it is true then only otherwise it will fail.

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## Calibration of partial safety factors(contd...)

- Forward problem: To determine  $\beta$  given a limit state function (or performance function) and the mean and variance (or standard deviation or coefficient of variation) for each of the random variables used in the limit state function.
- Inverse problem: A target  $\beta$  is specified and it is then necessary to determine the required mean values of the resistance and loads to achieve the target.
- This means that we need to find the design point  $\{z^*\}$  corresponding to the target  $\beta$ .

And this is one we consider that one say forward problem inverse problem, forward problem it means that you are giving a you do not know that value whatever value you are getting that you know the mean values standard deviation all those things and on the basis of that you are finding out the reliability but inverse problem it means which is our actual code how it does it, inverse problem it means that you are giving a target  $\beta$ .

And on the basis of that you have to find out your, that factors different factors, different factors for load different factors for materials that you have to find out that and then.

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## Calibration of partial safety factors(contd...)

- Assume that the design points  $\{z^*\}$  (in reduced coordinates) corresponding to a target  $\beta$  is known. To get the corresponding design point  $\{x^*\}$  in original coordinates, the following relation is used for each variable.

$$x_i^* = \mu_{x_i} + z_i^* \sigma_{x_i} \quad (6)$$

- Since the design point must be on the failure boundary, the limit state function must satisfy

$$g(x_1^*, x_2^*, \dots, x_j^*) = 0 \quad (7)$$

- For design purposes, it is necessary to relate each design point value  $x_i^*$  to a value of the variable used in design (e.g. a nominal design value specified by the code).

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We consider all of them we consider here that  $x_i^* = \mu_{x_i} + z_i^* \sigma_{x_i}$  that means I shall assume it is a one process and then this is a limiting factor design point where it works so I have to settle that, that is the numerical solution that you have to do it that means you have to find you can do it in a by guessing also that means I shall take different values and finally I shall get that G the limiting function value that one boundary value once we can consider that one should be satisfied our objective is that, that it as to be to satisfied like that.

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## Calibration of partial safety factors(contd...)

- If the nominal design value of  $X_i$  is denoted by  $\tilde{x}_i$ , then the partial safety factor  $\gamma_i$  is defined as

$$\gamma_i = \frac{x_i^*}{\tilde{x}_i} \quad (8)$$

- The partial safety factor is nothing more than a scaling factor that allows the designer to convert a nominal design value of a variable to the value needed to satisfy the limit state function for a target  $\beta$ .

$$g(x_1^*, x_2^*, \dots, x_j^*) = 0 \quad (9)$$



And finally we shall get that  $\gamma_i$  that  $X_i^*$  by this particular one here that design value that denoted by here from where we can get that  $\gamma_i$  that we can find out.

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## Procedure for calibration of partial safety factors

So just because this is the one that we have given so now what we shall do it here.

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## Procedure for calibration of partial safety factors

- Formulate the limit state function and the design equation
- Determine the probability distributions and appropriate parameters for as many of the random variables  $X_i (i = 1, 2, \dots, n)$  as possible
- It is assumed that the coefficient of variation or standard deviation is known for all random variables

Just quickly let me tell you because it is wise to what to show you that formulate the limit state function and the design equation, determine the probability distribution and appropriate parameters for as many of the random variables, so how many are random variables you just find out let us say length or span so span obviously we shall not consider because it does not exchange much so that during construction it does not change, so width that also it does not change much, D also it will not change much the materials value may change so that one particular construct it is assume the coefficient of variation or standard deviation is known for all random variables.

So out of that which one actually you are deterministic one and which one random that variables we have to find out from that particular one, you need not all of them are not random.

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## Procedure for calibration of partial safety factors(contd...)

- There can be at most only two unknown mean values in the analysis
- Typically, one unknown mean value corresponds to the resistance variable, and the other unknown mean value corresponds to a load variable
- For the first iteration, the limit state function  $g=0$  is evaluated at the mean values to get a relationship between the two unknown means



There can be at most only two unknown mean values in the analysis one unknown mean value corresponds to the resistance value and the other unknown mean value corresponds to a load variable. For the first iteration the limit state function  $g=0$  is evaluated as the mean values to get a relationship between the two unknown means, so we can find out that particular one here.

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## Procedure for calibration of partial safety factors(contd...)

- Obtain an initial design point  $\{x_i^*\}$  by assuming values for n-1 of the random variables  $X_i$ .
- Note : mean values are often a reasonable initial choice
- Solve the limit state equation  $g = 0$  to obtain a value for the remaining variable. This ensures that the trial design point is on the failure boundary



Obtain an initial  $x^*$  by assuming values for n-1 of the random variables, mean values are often a reasonable initial choice that means I have taking a certain mean value that particular one we are considering and on the basis of that we shall move on. Solve the limit state equation  $g=0$  to obtain a value for the remaining variable this ensures that the trial design point is on the failure boundary that is the one. Again let me tell you though it looks like.

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## Calibration of partial safety factors(contd...)

- If the nominal design value of  $X_i$  is denoted by  $\bar{x}_i$ , then the partial safety factor  $\gamma_i$  is defined as

$$\gamma_i = \frac{x_i^*}{\bar{x}_i} \quad (8)$$

- The partial safety factor is nothing more than a scaling factor that allows the designer to convert a nominal design value of a variable to the value needed to satisfy the limit state function for a target  $\beta$ .

$$g(x_1^*, x_2^*, \dots, x_i^*) = 0 \quad (9)$$



So this is your that function which you have to satisfied.

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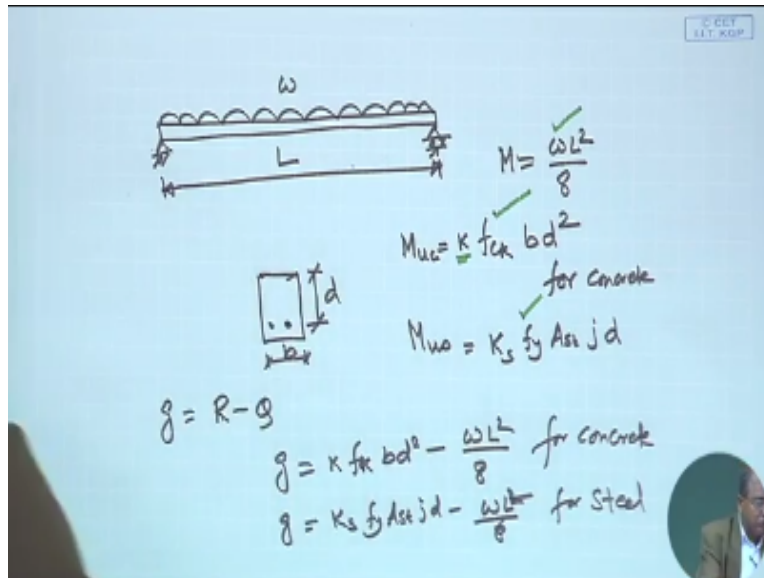
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## Procedure for calibration of partial safety factors



Because your P means there for example you are considering that bending movement and ICR force that particular one we are considering here. This particular case whatever we can consider here that we can say.

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Just let me tell you a very simple one so this is your  $w$ , this is your  $L$  so  $M =$  maximum in the moment and as you know  $0.138 f_{ck} b d^2$  that is the section we are using so this is your say  $b$ , this one your  $d$ , this is for concrete. Similarly we can write down say let us say  $M_u$  this is let us say  $M_{uc}$ , this is  $M_{us}$  so  $K_s$  this is the one we are getting, out of that length will never actually say length whatever we are considering that 5m or 10m you count that one that it will be not change much.

So that means here in this case we can consider that is  $W$  I have given generally we know that point  $0.138 f_{ck} b d^2$  but here you need that you have to find out that value this is your sat  $f_{ck}$  and may be that  $f_y$  so these are the three parameters that means I can consider this one  $M$  and  $M_{uc}$  so  $g =$  that particular one we can consider just to tell you, so we can consider that  $g$  here that value I can consider here so  $R - Q$  we can consider  $g$  and obviously these case are should be always greater than  $Q$  then only I can say that particular one at least.

It should be equal it should not be less than so these one we can say one way I can say  $G$  so I can say  $K f_{ck} b d^2 - \frac{wL^2}{8}$  this is one or I can say  $g = K_s f_y A_s t d - \frac{wL^2}{8}$ . So these are you are call limit state that mean these limit state and these limit state that one this is for concrete this is for steel and these one to be satisfied and on the basis of that you have to find out that factor how much factor we shall give. So that particular value of  $\beta$  so we shall consider for a particular value of  $\beta$ .

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## Procedure for calibration of partial safety factors(contd...)

- Determine the partial derivatives of the limit state function with respect to the reduced variables

$$\{G\} = \begin{Bmatrix} G_1 \\ G_2 \\ \cdot \\ \cdot \\ G_n \end{Bmatrix} \quad \text{where } G_i = -\frac{\partial g}{\partial Z_i} \quad (10)$$

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So that is a procedure here I am not going to detail of all those things just to give you an idea that how it works, so that you can understand that one I shall give reference which you can follow.

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## Procedure for calibration of partial safety factors(contd...)

- Consider the column vector  $\{\alpha\}$  using

$$\{\alpha\} = \frac{[\rho]\{G\}}{\sqrt{\{G\}^T [\rho] \{G\}}} \quad (11)$$

- where  $[\rho]$  is the matrix of correlation coefficients,



So we can find out certain value here so G is this one and which is actually nothing but the first derivative with respect to the mean value and then you can find out that coordination coefficient we can find out here this particular one this is coordinator.

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## Procedure for calibration of partial safety factors(contd...)

- Determine a design point in reduced variates for  $n-1$  of the variables using

$$z_i^* = \alpha_i \beta_{target} \quad (12)$$

- where  $\beta_{target}$  is the target reliability to be found.
- Design the corresponding design point values in original coordinates for the  $n-1$  values using

$$x_i^* = \mu_{x_i}^e + z_i^* \sigma_{x_i}^e \quad (13)$$

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And then you can find out the target value on the values of that I can give the  $\mu$  value and so then I can get that from the mean I shall get the  $\mu$   $X_i$ .

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## Procedure for calibration of partial safety factors(contd...)

- Determine the value of the remaining random variable (i.e. the one not found in previous steps) by solving the limit state function  $g=0$ .
- Update the relationship between the two unknown mean values(if applicable).

$$\gamma_i = \frac{x_i^*}{\mu_{x_i}} = \frac{\mu_{x_i} + z_i^* \sigma_{x_i}}{\mu_{x_i}} = 1 + z_i^* V_{x_i} = 1 + \alpha_i \beta V_{x_i} \quad (14)$$

$$\text{Therefore, } \mu_{x_i} = \frac{x_i^*}{1 + \alpha_i \beta V_{x_i}} \quad (15)$$

Like that I can keep on doing that particular procedure and then I can get that value  $1 + \alpha_i \beta V_{x_i}$ . This is the procedure we will follow, so we can find out that  $\gamma_i$  that  $X_i$  share by  $\mu_{x_i}$  so that means here mean objective is there this  $\beta$  value how much your target that means your deliberative will be that mean say  $\beta = 0$  that means just only it 0 if you increase that  $\beta$  then only you can find out that I want to say  $\beta_2$  I want  $\beta_3$  that on the basis of that we can find out.

On the basis of that  $\alpha_i$  which we have calculated like this so  $G$  we have to calculate  $G_i$  is nothing but this one that means  $G$  is nothing but this one. So and  $G$  is the limit state function form there you will get  $g_i$  so this particular one on the ways of the you are getting  $\alpha$  and  $\rho$  and then you are getting the  $\mu z_i$  considering  $Z_i$  I can get the  $\mu x_i^*$  and then I can find out that  $\gamma$  is for individual  $X_i$  is there by  $\mu x_i$  which will give me that  $\gamma_i$  that particular value it will give me.

And then we can solve and from there we can find out the value of  $\mu x$ ,  $\mu x_i$  we can say that we can find out.

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## Procedure for calibration of partial safety factors(contd...)

- Repeat steps until  $\{\alpha\}$  converges.
- Once convergence is achieved, calculate the design factors.

$$\gamma_i = \frac{X_i^*}{\bar{X}_i} \quad (16)$$



Then we have repeat that one and then when the convergence is achieved  $\gamma = X_i^* / X_i$  that we can find out here. That is the one we can do it here so this is the positively follow.

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Example : calibration of partial safety factors



So let us give you one example so it will be clear actually.

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## Example : calibration of partial safety factors

- Consider the fundamental case

$$g = R - Q \quad (17)$$

where R is the resistance and Q is the load.

- A possible design equation (in LRFD format) is

$$\gamma_R \mu_R \geq \gamma_Q \mu_Q \quad (18)$$

- The nominal values are assumed to be equal to the mean values
- Assume,  $V_R$  as 10 percent and  $V_Q$  as 12 percent
- To determine the partial safety factors that must be used in design to achieve the reliability index,  $\beta_{target}=3.0$
- Assume that both R and Q are normally distributed and uncorrelated



So consider the fundamental case  $G = R - Q$  this is very, very common R is the resistance Q is the load are equally demand and supply possible design equation is  $\gamma_R \mu_R \geq \gamma_Q \mu_Q$  that is obviously we are having two unknown variables so  $\gamma_R$  we have find out and  $\gamma_Q$  we have to find out from this particular one the nominal value assume to be equal to the mean values that the first one assume  $V_r$  as 10% and  $V_q$  is 12% that means there is a variants.

Variants that we can find out 10% and 12% to determine the partial safety factors that must be used in design to achieve the reliability index  $\beta_t$  target = 3.0 so generally most of the cases we should consider  $\beta$  actually 3 that will consider you know on the basis of that we calculate those values. So our objective is that this particular one  $\beta$  target we have to find out we have to achieve for a particular value of  $\gamma_R$  and  $\gamma_Q$ .

Assume that both R and Q are normally distributed and uncorrelated this is very, very important actually here because a statistically that each of them actually variable each actually follow certain distribution so that distribution whether normal distribution log distribution log normal distribution like that many more distribution available. Normal distribution is very common, so we can find out the R and Q are normally distributed and uncorrelated.  
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## Example : calibration of partial safety factors(contd...)

- The limit state function :

$$g = R - Q \quad (19)$$

where R is the resistance and Q is the load.

- Obtain an initial design point, say  $r^* = q^*$ .
- There are two variables, so we have two unknown mean values
- Use limit state function at the mean values to relate the two unknown mean values. This results,  $\mu_R = \mu_Q$

So limit state function as usual  $g = R - Q$ . Obtain the initial design point say  $r^* = q^*$  between the value, so we have two unknown mean values. Use limit state function at the mean value to relate the two unknown mean values that is  $\mu_r = \mu_q$ . That is the one you can find out over here.

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## Example : calibration of partial safety factors(contd...)

- Determine the  $\{G\}$  vector:

$$G_1 = -\frac{\partial G}{\partial R}\sigma_R = -\sigma_R = -V_R\mu_R = -0.1\mu_R = -0.1\mu_Q \quad (20)$$

$$G_2 = -\frac{\partial G}{\partial Q}\sigma_Q = \sigma_Q = V_Q\mu_Q = 0.12\mu_Q$$

- Note that  $\mu_R = \mu_Q$  is used to evaluate  $G_1$

So as usual I can take  $G_1$  we can just take the derivative and you can find out these  $-0.1 \mu_r -0.1 \mu_q$ .  $G_2 = G_1$ , and then it is used to evaluate  $G_1$ . So you can consider that the  $\mu_1$  and  $\mu_r$  to evaluate  $g_1$ .

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## Example : calibration of partial safety factors(contd...)

- Calculate  $\alpha$ . The correlation matrix  $[\rho]$  is the identity matrix. This means that variables are uncorrelated

$$\begin{aligned} \{\alpha\} &= \frac{[\rho]\{G\}}{\sqrt{\{G\}^T[\rho]\{G\}}} \\ &= \frac{1}{\sqrt{(-0.1\mu_Q)^2 + (0.12\mu_Q)^2}} \begin{Bmatrix} -0.1\mu_Q \\ 0.12\mu_Q \end{Bmatrix} \quad (2) \\ &= \frac{1}{0.156\mu_Q} \begin{Bmatrix} -0.1\mu_Q \\ 0.12\mu_Q \end{Bmatrix} \\ &= \begin{Bmatrix} -0.641 \\ 0.769 \end{Bmatrix} \end{aligned}$$

Then calculate  $\alpha$   $\rho$   $G$  this particular over here and this is over here and then I can get  $\alpha=-0.641$  and 0.760. This is the one we can get it.

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## Example : calibration of partial safety factors(contd...)

- Determine a new design point for n-1 variables. Calculate  $z_Q^*$  in this way

$$z_Q^* = \alpha_Q \beta_{target} = 0.769(3.0) = 2.31 \quad (22)$$

- Determine  $q^*$  using

$$q^* = \mu_Q + z_Q^* \sigma_Q = \mu_Q(1 + z_Q^* V_Q) = \mu_Q(1 + 2.31(0.12)) = 1.28\mu_Q \quad (23)$$

- Determine  $r^*$  by solving  $g=0$ . Thus  $r^* = 1.28\mu_Q$ .
- Before iterating again, get an improved estimate of  $\mu_R$  in terms of  $\mu_Q$  for use in calculating  $\{G\}$  and  $\{\alpha\}$ .

$$\mu_R = \frac{r^*}{(1 + \alpha_R \beta_{target} V_R)} = \frac{1.28\mu_Q}{1 - 0.641(3.0)(0.10)} = 1.58\mu_Q \quad (24)$$

So  $z^*q =$  this one that is 2.31  $q^*$  using this particular formula we can use  $1.28\mu_Q$ . Determine  $r^* = 0$ ,  $r^* = 1.28\mu_Q$  and then you are putting this one then I get  $1.58\mu_Q$ . so this the one that step by step if you do it than I can get the value.

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## Example : calibration of partial safety factors(contd...)

- The results of subsequent iterations are shown in Table-2

	Iteration number		
	1	2	3
$r^*(start)$	$\mu_Q$	$1.28\mu_Q$	$1.22\mu_Q$
$q^*(start)$	$\mu_Q$	$1.28\mu_Q$	$1.22\mu_Q$
$\mu_R(start)$	$\mu_Q$	$1.58\mu_Q$	$1.60\mu_Q$
$\alpha_R$	-0.641	-0.796	-0.800
$\alpha_Q$	0.769	0.605	0.600
$r^*(end)$	$1.28\mu_Q$	$1.22\mu_Q$	$1.22\mu_Q$
$q^*(end)$	$1.28\mu_Q$	$1.22\mu_Q$	$1.22\mu_Q$
$\mu_R(end)$	$1.58\mu_Q$	$1.60\mu_Q$	$1.60\mu_Q$



And so it is nothing but actually 1<sup>st</sup> one we will get like this and 2 set we will get like this and 3<sup>rd</sup> one we will get like this. So this the way we can find out, so if you start with the value  $r^*, q^*, \mu_Q$  apply the value you get the value then this one I am getting it over here this one I am using it over here. From here to here I am getting 3 equations and I am getting the exact value of the particular one.

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## Example : calibration of partial safety factors(contd...)

- Assuming the mean values are the nominal design values, the design factors are

$$\gamma_R = \frac{r^*}{\mu_R} = \frac{1.22\mu_Q}{1.60\mu_Q} = 0.763 \quad *$$

$$\gamma_Q = \frac{q^*}{\mu_Q} = \frac{1.22\mu_Q}{\mu_Q} = 1.22 \quad (25)$$

- Assume  $\mu_R = 10$ . From the design equation,  $\gamma_R\mu_R \geq \gamma_Q\mu_Q$ , the minimum required  $\mu_R$  to achieve  $\beta = 3$  would be

$$\mu_R = \frac{\gamma_Q\mu_Q}{\gamma_R} = \frac{(1.22)(10)}{0.763} = 16.0$$



So  $\gamma_r = r^*/\mu_r = 0.763$   $\gamma_q = q^*/\mu_q = 1.22$   $\mu_q$ , so that means I am getting this value as this 0.763 and 1.22 that particular one we are getting this value that we can find out and then we can  $\mu_r = 10$  that would be 16. That means we have got the particular one here 16.10 so these two achieve  $\beta=3$  I required the particular one is 16 that particular one we can consider over here.  $1.22 \times 10/0.763$  then I am getting the 16 that I can find out over here.

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## Example : calibration of partial safety factors(contd...)

- If the partial safety factors are calibrated correctly, a nominal resistance of 16 will ensure a target  $\beta = 3$  is achieved if the nominal loading is equal to 10.
- For this simple case of a linear limit state function, it can be checked with the following equation

$$\beta = \frac{\mu_R - \mu_Q}{\sqrt{\sigma_R^2 + \sigma_Q^2}} \quad (27)$$

- Substituting all the variables determined into this expression and noting that  $\sigma_R = V_R \mu_R$

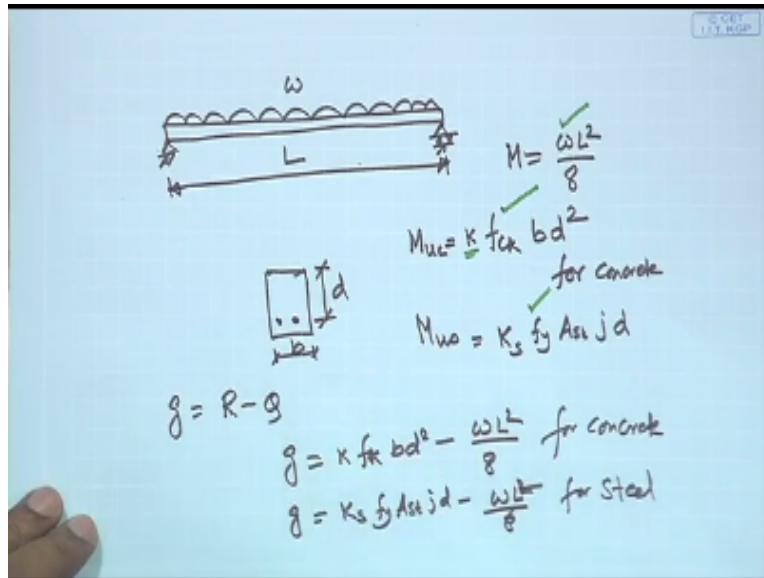
$$\beta = \frac{\mu_R - \mu_Q}{\sqrt{\sigma_R^2 + \sigma_Q^2}} = \frac{16.0 - 10}{\sqrt{[(0.1)(16.0)]^2 + [(0.12)(10)]^2}} = \frac{6.0}{2.00} = 3.0 \quad (28)$$

So even the partial safety factors are calibrated correctly, a normal resistance of 16 will ensure the target  $\beta=3$  is achieved if the nominal loading is = 20. So that means I can get the particular one here 16 and that one is 10 that we can find over here. So as I have shown you earlier  $\beta = \frac{\mu_R - \mu_Q}{\sigma_R^2 + \sigma_Q^2}$ , so then we can find out from this  $\beta=16, 10, 0.1(16)^2$  so which I am getting it = 3.

So I can get the value of three that we can find out whatever the target we have taken 16 and 10 we got it as it here. This is the one how do we calculate calibration factor because I thought this is what I have to show then I can show the different in state, that you say service limit state extreme limit state there are different kind of living state. Each of them having their certain objective that we consider.

On the basis of that we can find out. So coming to this one here one may say that one just to give you an idea that how it works with the calibration method and this is the simple one you can try these the same thing you can try with the other load cases, say for example that one I have shown you this particular one here.

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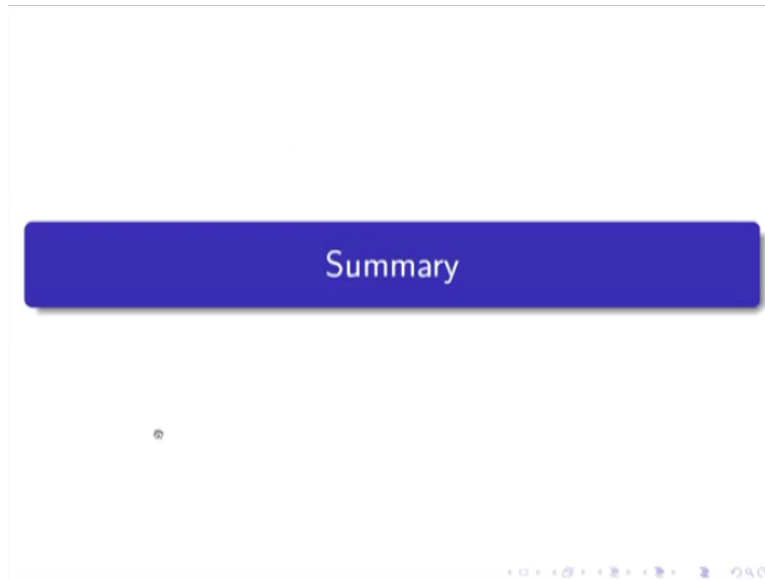


This is very intelligent interesting one from the we are talking from the design quetes from the interview for that is equally possible to make it for the health monitring then means thsat you having the particular structure for that and what the lability of the structure that also you can find out in that one .

In this case we will actually fore or method in this case what you are giving we are  $\beta$ =to 3 and you are trying to find the corresponding factor so that I can get that so the abilty is but in the other case when ever we are intrested the particular structure in the gone for the inspection the monitoring you have done they are finding the distuinsh of the stage of the quaslity .

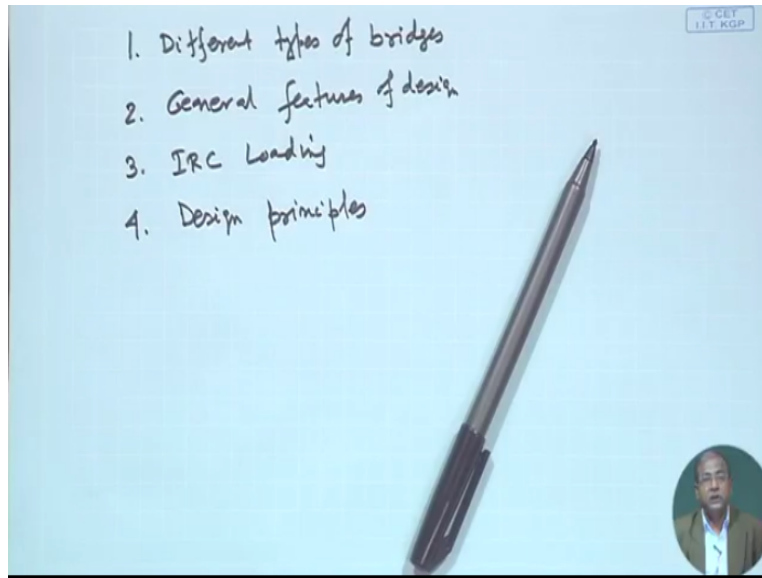
And the other thing bending on the quality is the system we are calculating the  $\beta$ follow are m,ethod that what ever the value we got it we say our the  $\beta$ is greater than 3 that means it is alright if the  $\beta$ is less than 3 then it is not alright then we will go for the  $\beta$ =to 2  $\beta$ =to 4 that way you can find outin the changes in the loadside of that.

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So this is the one I would like to say the the particularly here that would like to conclude that is one do so that particular one will be good one is the .

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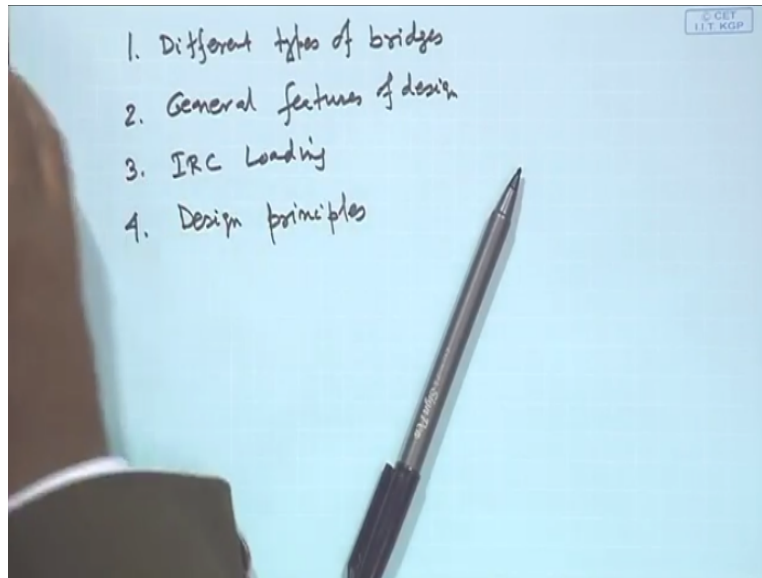


And this is different types of bridges then we are considering the particular loads we have say the general features of design number three I have seen the the loading the design code and the design principles and how could be it calibrated I have you told you the design principles that how to calibrate the load in the factor actually in the more important that one then we will find the different states again I like to say that the limit states that one we will do.

The design equally in the really see that working states is nothing but the another kind of living state but it longally considering stress similarly we are having the state method of collapse method visibility like that I can have in the kind of things and what else we do now in that in the next week that from 6 lecture number 6 onwards we shall concentrate on that the design of complete elements and we can go through the different elements concisely.

First of all you told the particular one the not the only one method it is solved it by in the method then what happens if we decide it by the living method let us say the high score then how I can see through it if you design as per IRC so that the new code then also what will happen different aspect consider and which we shall find out define aspects find out coming through these spectrum here .

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I have like to say that here the basic thing things of design codes are disussed here and in the whole week we have discussed types of bridges vand finally you an focused on the rein force concrete and the road bridges and that on and RCC T beam thank you very much.