

**Course on Design of Steel Structures**  
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**Mod 10 Lecture 47**  
**Laterally Supported Beams**

Today, I am going to discuss about the design procedure of the lateral supported beam. So beam will be designed on the basis of laterally supported or laterally unsupported. So today we will discuss only about the laterally supported beam where, its web will be supported laterally so that the lateral torsional buckling may be prevented.

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**Laterally Supported Beam (Cl. 8.2.1, IS 800: 2007)**

**Design Bending Strength**

➤ If  $V < 0.6 V_d$  *Low shear*

Where,  
 $V$  is the factored design shear force and  $V_d$  is the design shear strength of the cross-section  
The design bending strength,  $M_d$  shall be taken as:

$$M_d = \beta_b Z_{p y} f_y / \gamma_{m0}$$

So in this case we are assuming that lateral torsional buckling is prevented and with this what will be the design criteria that will be discussed and that is given in clause 8.2.1 of IS 800-2007, the detail has been discussed where the design bending strength can be calculated in two cases, one is for low shear another is for high shear. Low shear means when the shear force is less than the 0.6 time that design shear strength then it is called low shear, that means if  $V_d$  is a design shear strength of the cross section then uhh if  $V$  less than  $0.6 V_d$  then we can called as low shear that means shear force is less. So in case of low shear we can find out the design bending strength simply by from this formula that is  $M_d$  is equal to  $\beta_b$  into  $Z_p F_y$  by  $\gamma_{m0}$ , right.

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To avoid irreversible deformation under serviceability loads, following conditions are to be satisfied.

$$\begin{aligned} M_d &\leq 1.2 Z_e f_y \gamma_{m0} && \text{for simply supported beams} \\ M_d &\leq 1.5 Z_e f_y \gamma_{m0} && \text{for cantilever beams;} \end{aligned}$$

Where,

$\beta_b = 1.0$  for plastic and compact sections;

$\beta_b = Z_e / Z_p$  for semi-compact sections;

$Z_p$ ,  $Z_e$  = plastic and elastic section moduli of the cross-section, respectively;

$f_y$  = yield stress of the material; and

$\gamma_{m0}$  = partial safety factor

$M_d$  is equal to  $\beta_b$  into  $Z_p$  into  $F_y$  by  $\gamma_{m0}$  where  $M_d$  is the design bending strength and  $\beta_b$  we can consider as 1 for plastic and compact sections, for plastic and compact section is value  $\beta_b$  can be consider as 1 and for semi-compact section, we can consider  $Z_e$  by  $Z_p$  as the  $\beta_b$  value right where  $Z_e$  is the elastic section modulus and  $Z_p$  is the plastic section modulus. So the ratio of  $Z_e$  by  $Z_p$  can be found as  $\beta_b$  and for semi compact section, this  $\beta_b$  value will be calculated and will be used and for plastic or compact section  $\beta_b$  value will be consider simply 1 and whether the section is plastic or compact or semi-compact that will be decided from the code permissions, because from the thickness of the web and width of the flange, depth of the web and other criteria like flange, thickness flange width etcetera, we can find out whether a section is compact, plastic or semi-compact from the code and from that basis we can find out the  $\beta_b$  value, right and  $F_y$  is the yield stress of the material and  $\gamma_{m0}$  is the partial safety factor.

So  $F_y$  can be found for different material to the the yield stress value will be different which also we can found from the code and  $\gamma_{m0}$  is the partial safety factor which is found in table 5, right and to avoid irreversible deformation under serviceability loads, we have to maintain these condition, like for simply supported beam  $M_d$  should be less than 1.2 into  $Z_e F_y$  by  $\gamma_{m0}$ , so  $M_d$  value whatever you have calculated there, in any case it should be less than this value that means the  $M_d$  value calculated at there, if it is more than this then we will take this value  $M_d$ . So  $M_d$  is 1.2 into  $Z_e F_y$  by  $\gamma_{m0}$  for simply supported beam and for cantilever beam we can consider  $M_d$  as uhh 1.5  $Z_e F_y$  by  $\gamma_{m0}$ , so  $M_d$  value should be less than this or this depending on the support condition.

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➤ If  $V > 0.6 V_d$

The design bending strength  $M_d$  will be taken as,

$$M_d = M_{dv}$$

Where,  $M_{dv}$  is the design bending strength under high shear and it is calculated as,

**(a) Plastic or compact section**

$$M_{dv} = M_d - \beta(M_d - M_{fd}) \leq 1.2 \frac{Z_e f_y}{\gamma_{m0}}$$

Where,

$$\beta = \left( 2 \frac{V}{V_d} - 1 \right)^2$$

$V_d$  = design shear strength as governed by web yielding or web buckling =  $A_v f_v$

$f_v$  = design shear strength

$A_v$  = shear area =  $D t_w$  for rolled sections  
 =  $d t_w$  for welded/built up sections

$V$  = factored shear force

So once we find the value of  $M_d$  then we can go ahead for next; however if we see that the shear force is more than the 0.6 times design shear strength of the beam section then we can use this formula that is  $M_d$  will be equal to  $M_{dv}$  where  $M_{dv}$  can be calculated from this. So when the section is under high shear that means when the beam is under high shear that means when  $V$  greater than  $0.6V_d$  then the design bending strength can be calculated as  $M_d$  is equal to  $M_{dv}$ , where  $M_{dv}$  is a design bending strength under high shear and it can be calculated as  $M_{dv}$  as like this and it can be calculated for plastic or compact section from this formula. If the section is plastic or compact then we can find the  $M_{dv}$  value as  $M_d$  minus beta into  $M_d$  minus  $M_{fd}$ , right and in any case, it should be less than or equal to  $1.2 Z_e F_y$  by gamma  $m_0$ .

So you have to consider this criteria, it has to be less than this and  $M_{dv}$  can be calculated from this, where beta is this beta is  $2$  into  $V$  by  $V_d$  minus  $1$  whole square. So beta is a coefficient, which can be calculated from this formula and then we can find out the value of  $M_{dv}$ , right and here,  $V_d$  the design shear strength can be calculated as governed by the web yielding or web buckling and  $V_d$  is simply  $A_v$  into  $F_v$  where  $A_v$  is a shear area and  $F_v$  is a design shear strength.

So  $A_v$  is the design shear uhh shear area can be calculated as  $D$  into  $t_w$  for rolled section where  $D$  is the overall depth,  $t_w$  is the thickness of web and  $d$  into  $t_w$  for welded or built up sections where  $t_w$  is a thickness and  $d$  is a effective depth, right. Here remember (the) for rolled section, this capital  $D$  is the overall depth, right. So  $A_v$  can be calculated as  $D$  into  $t_w$  for rolled section and small  $d$  into  $t_w$  for welded or built up sections and  $F_v$  is design shear

strength and  $v$  is the factor shear force, which we can calculate from the loading condition and from boundary conditions, right.

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$M_d$  = plastic design moment of the whole section disregarding high shear force effect and considering web buckling effects.

$M_{fd}$  = plastic design strength of the area of the cross section excluding the shear area

$M_{fd} = \frac{d^2 t_w}{4} f_y$  for built up sections  
 $M_{fd} = \frac{D^2 t_w}{4} f_y$  for rolled sections

$d = D - 2t_f$

(b) Semi-compact section

$M_{dv} = Z_e \frac{f_y}{\gamma_{m0}}$

The slide also features a hand-drawn diagram of an I-section with labels  $D$  for overall depth and  $d$  for effective depth.

So once we calculate  $V$  and  $V_d$  then we can find out the value of beta and then we can find out the value of  $M_{dv}$ , right. So  $M_d$  is a plastic design moment of the whole section disregarding high shear force effect and considering web buckling effect. So  $M_d$  already we have calculated as a plastic design moment of the whole section uhh where we are not going to consider the shear force effect and  $M_{fd}$  is the plastic design strength which can be calculated from this formula  $M_{fd}$ ,  $M_{fd}$  is a plastic design strength of the area of the cross section excluding the shear area, right.

So in case of a section we have to find out the  $M_{fd}$  value which is called plastic design strength of the area of the cross section excluding shear area. So  $M_{fd}$  value we can find out as  $D^2 t_w$  by 4 gamma into  $F_y$  for built up section, right and  $M_{fd}$  is equal to capital  $D$  square  $t_w$  by 4  $F_y$  for rolled section where  $D$  is overall depth and small  $d$  the effective depth that capital  $D$  minus  $2t_f$  that means if we have a section like this then we can find out this is as capital  $D$  and this is as small  $d$  which is capital  $D$  minus  $2t_f$ , right. So  $M_{fd}$  can be found from this formula depending on the type of sections and then we can find out the  $M_d$  value and then  $M_{dv}$  and for semi-compact section simply we can find out the value as  $Z_e$  into  $F_y$  by gamma  $m_0$ . So for semi-compact section with high shear the  $M_{dv}$  value can be calculated from this formula which is called  $Z_e F_y$  by gamma  $m_0$ , right.

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**Design for Shear (Cl. 8.4, IS 800: 2007)**

The factored design shear force  $V$  in a beam should satisfy,

$$V \leq \frac{V_n}{\gamma_{m0}}$$

Where  $V_n$  = nominal shear strength of a section

$$V_n = \frac{A_v f_{yw}}{\sqrt{3}}$$

Where  $A_v$  = shear area  
 $f_{yw}$  = yield strength of the web

So after designing the shear bending then we will go for shear right. So regarding (10:29) shear uhh clause 8.4 describes the criteria. In clause 8.4, it says that the factored design shear force should be less than the nominal shear force by gamma m0,  $V_n$  by gamma m0, right. So  $V$  the factor design shear force should be less than or equal to  $V_n$  by gamma m0, where  $V_n$  is the nominal shear strength of a section and  $V_n$  value can be found from this formula  $A_v f_{yw}$  by root 3,  $A_v$  is equal to shear area and we have shown how to calculated shear area and  $f_{yw}$  is the yield strength of the web, right.

So,  $V_n$  the nominal shear strength of a section can be calculated from this formula where  $V_n$  is equal to  $A_v$  into  $F_{yw}$  by root 3, where  $F_{yw}$  is a yield strength of the web and  $A_v$  is the shear area and the factor design shear force  $V$  should be less than or equal to  $V_n$  by gamma m0.

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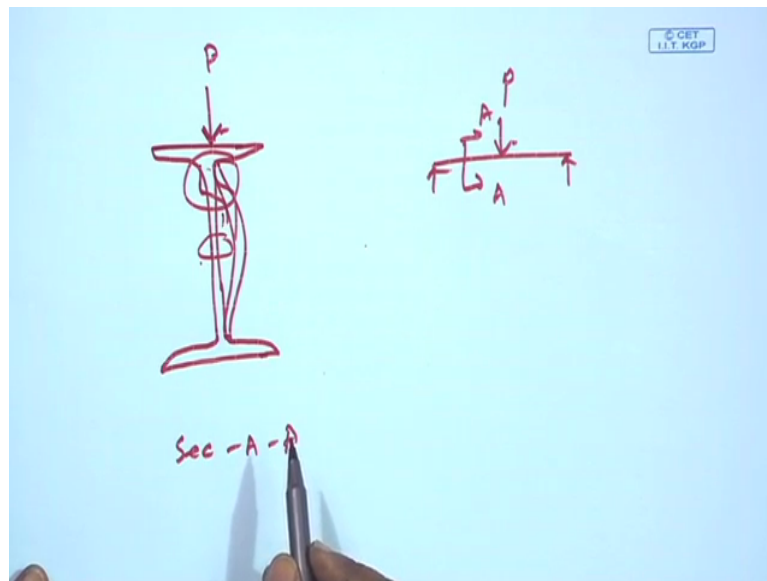
**Shear Areas of different Sections (Cl. 8.4.1.1, IS 800: 2007):**

Section	Shear Area $A_v$
Hot rolled (major axis bending)	$Dt_w$
Welded (major axis bending)	$dt_w$
Hot rolled or Welded (minor axis bending)	$2bt_f$
Rectangular hollow Sections (loaded parallel to height)	$AD/(b+D)$
Rectangular hollow Sections (loaded parallel to width)	$Ab/(b+D)$
Circular hollow tubes	$2A/\pi$
Plates & solid bars	$A$

Now shear areas can be calculated as given in clause 8.4.1.1, where it is told that the shear area  $A_v$  can be calculated for different type of sections like for hot rolled section, if major axis bending is happening then this is  $D$  into  $t_w$ ,  $D$  is a overall depth and for major axis bending for welded section, it will be small  $d$  into  $t_w$  for welded section and similarly, for hot rolled or welded section about minor axis, it will be  $2$  into  $b$  into  $t_f$ , because the flange is in two side. So  $2$  into  $V$  into  $t_f$  right.

So for hot rolled or welded sections about minor axis bending the shear is a there will be  $2$  into  $b$  into  $t_f$ . Similarly, the rectangular hollow section loaded parallel to high will be this,  $A$  into  $D$  by  $b$  plus  $D$ ,  $D$  is the total depth and  $A$  is the shear area and rectangular hollow sections loaded with or loaded parallel to width will be  $A$  small  $b$  by  $b$  plus  $D$ . So one is  $A$  capital  $D$  by  $b$  plus  $D$ , another is  $A$  small  $b$  by  $B$  plus  $D$  and for circular hollow section, it will be  $2A$  by  $\pi$  and for plates and bars it will be  $A$ ,  $A$  is a cross sectional area. So this is how the shear area of a section can be calculated, which has been given in clause 8.4.1.1 from which we can calculate the shear area  $A_v$ .

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Then coming to web buckling, so now for web buckling we can see that the web behaves like a column if placed under concentrated load that means uhh if we have uhh I sections say for example, here then if we have a concentrate load say, this is a beam and if we cut this section, so this is section A-A right. So if we see, now because of the concentrated load on the web at a particular point, so this may buckle depending on the type of member it will buckle. So if the web is thin then it will come to buckling or sometimes it may cripple also, it may cripple because of the concentrated load. So we have to avoid this buckling and crippling we will come in detail, how to restrict this web buckling and web crippling.

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The image is a screenshot of a presentation slide titled 'Web Buckling' in red text. The slide has a light green background and a black toolbar at the top. The toolbar contains various icons for presentation navigation. The slide contains three bullet points:

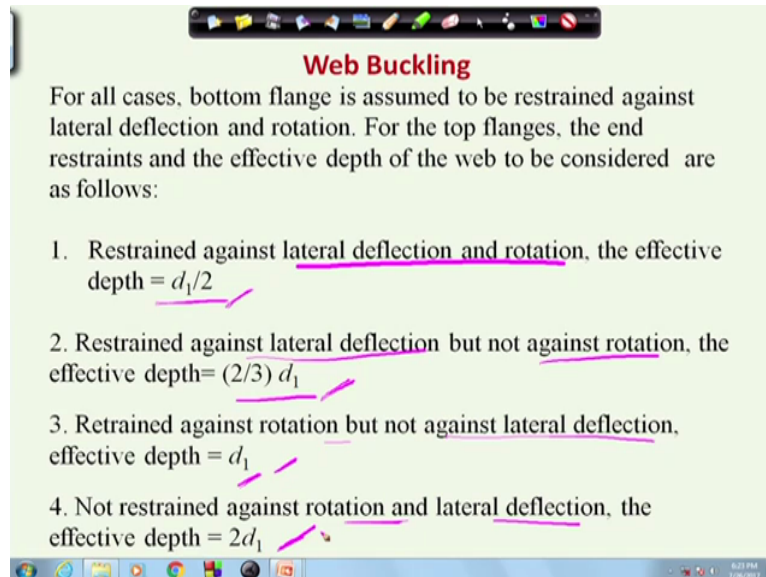
- The web behaves like a column if placed under concentrated load.
- The Web is quite thin and therefore is subjected to buckling.
- Web buckling occurs when the intensity of vertical compressive stress near the center of section becomes greater than the critical buckling stress for the web acting as column.

In the bottom right corner, there is a small circular inset image of a man with dark hair, wearing a light blue shirt, looking towards the left.



So as the web behaves like a column, therefore the web strength we have to calculate the strength means the, but it will compressive strength we have the center of the web we have to calculate and then we have to check whether it is safe or not.

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**Web Buckling**

For all cases, bottom flange is assumed to be restrained against lateral deflection and rotation. For the top flanges, the end restraints and the effective depth of the web to be considered are as follows:

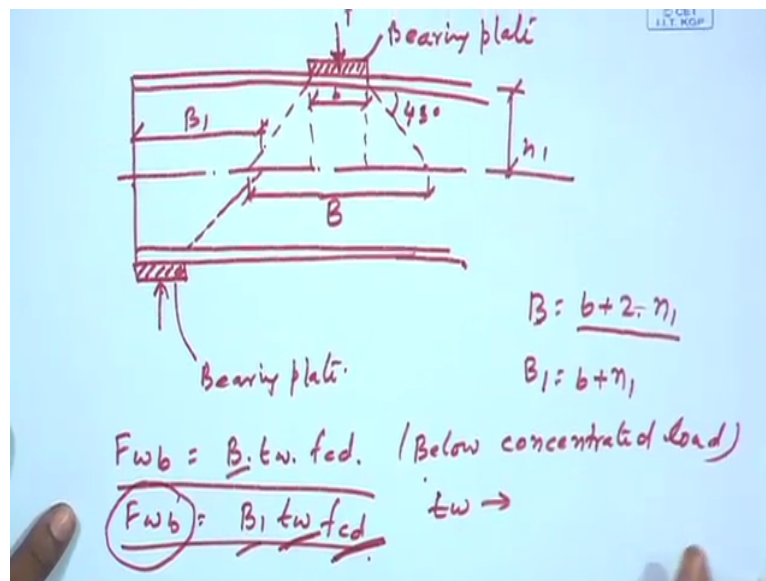
1. Restrained against lateral deflection and rotation, the effective depth =  $d_1/2$
2. Restrained against lateral deflection but not against rotation, the effective depth =  $(2/3) d_1$
3. Restrained against rotation but not against lateral deflection, the effective depth =  $d_1$
4. Not restrained against rotation and lateral deflection, the effective depth =  $2d_1$

So for calculating web buckling, for different cases the effective depth has been given say for example, uhh when the web is restrained against lateral deflection and rotation, the effective depth is considered as  $d_1$  by 2, right where  $d_1$  is a depth of the web and if it is restrained against lateral deflection, but not against rotation then the effective depth will be  $2/3$  rd  $d_1$  and if restrained against restrained against rotation, but not against lateral deflection then effective depth will be  $d_1$  and not restrained against rotation and lateral deflection the effective depth will be  $2d_1$ .

So the effective depth of the web can be calculated on the basis of the restrained condition and that is given here that if restrained against lateral deflection in rotation, it is  $d_1$  by 2, if restrained against lateral deflection, but not against rotation then  $2/3$   $d_1$ , if restrained against rotation, but not against lateral deflection then  $d_1$  and if restrained against both rotation and uhh sorry, if not restrained against rotation and lateral deflection then effective depth  $2d_1$ . So this is required to calculate the compressive stress of the web.



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Now web buckling strength will we will like to calculate. So for calculation of web buckling strength we need to find out how the bearing plate is going to be provided to minimize the web buckling means to reduce the web buckling, say for example, if a member is subjected to concentrated load at certain point, say concentrated load  $p$  is there and this is called bearing plate bearing plate.

Now and if we have a support here then also there is a chance of web buckling here, because of the reaction at the support, so here also we need to provide bearing plate and below concentrated load if we provide the bearing plate then the load will be dispersed with 45 degree angle. This is the flange and if this is neutral axis depth, then this will be the width for which we have to calculate. This is  $B$  right and this  $B$  value will be  $B$  plus 2 into  $n_1$ ,  $n_1$  means if the angle of dispersion is 45 degree then this value is called  $n$ . So  $n_1$  is the length from dispersion at a 45 degree angle to the level of neutral axis.

So so we can find out  $B$  as a  $b$  plus  $2n_1$  where small  $b$  is the uhh bearing length, this is small  $b$  right. So this is  $n_1$ , so  $b$  plus  $2n_1$  right. So and in this case if it is like this, so if I consider this is as  $B_1$  then at the support  $B_1$  will be simply  $B$  plus  $n_1$ , right. So the buckling strength below the concentrated load  $F_{wb}$ , I can calculate it as  $B$  into  $t_w$  into  $F_{cd}$  buckling strength can be calculated as this below concentrated load, right and at support buckling strength ((20:52)) will be  $b_1$  into  $t_w$  into  $F_{cd}$ , right. So where  $F_{cd}$  is the allowable compressive stress corresponding to the assumed web strut ((21:05)) according to buckling curve C ((21:07)), right. So  $F_{cd}$  value is the allowable compressive stress and it can be calculated corresponding to it the buckling class C.

So if we know  $t_w$  is the uhh thickness of web  $t_w$  is a thickness of web, so if we know the value of  $F_{cd}$  value of  $t_w$  and value of  $B$  or  $B_1$  then we can find out the buckling strength of the member right.

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**Web buckling strength**

$$F_{wb} = B t_w f_{cd}$$

(below concentrated load)

$$F_{wb} = B_1 t_w f_{cd}$$

(at support)

Where,

$F_{wb}$  = web buckling strength at the support  
 $B = b + 2n_1$ ,  $B_1 = b + n_1$   
 $n_1$  = length from dispersion at  $45^\circ$  to the level of neutral axis  
 $t_w$  = thickness of the web  
 $f_{cd}$  = allowable compressive stress corresponding to assumed web strut according to buckling curve  $c$ .

Now here the when we are going to calculate the uhh design compressive stress  $F_{cd}$  we need to know what is the value of lambda, right.

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$$\lambda = \frac{l_e}{r_y} = \frac{0.7d}{\sqrt{\frac{I_y}{A}}} = \frac{0.7d}{\sqrt{\frac{bt^3}{12 \times b \times t}}} = \frac{0.7d}{t/\sqrt{12}}$$

$$\lambda = \frac{0.7d \times \sqrt{12}}{t} \approx 2.5 \frac{d}{t}$$

$$\lambda = 2.5 \frac{d}{t}$$

$c \rightarrow$   
 $f_y \rightarrow$

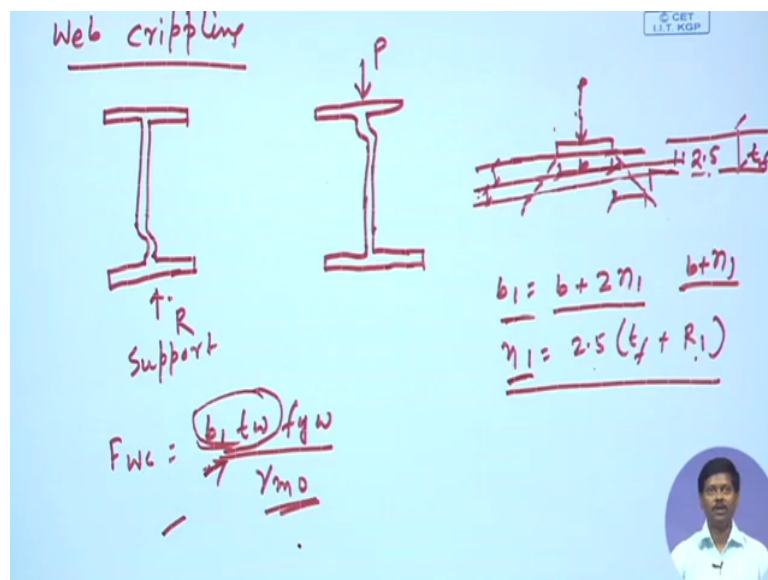
$f_{cd} = F_{wb}$

So lambda means the slenderness ratio. So slenderness ratio we know we can find out  $l_e$  by  $r$ ,  $r$  means in this case  $r_y$ , right. So  $l_e$  the effective length of the strut (())(22:09)  $l_e$  will be  $0.7d$ , so if we consider this  $0.7d$  by  $r_y$   $r_y$  means  $I_y$  by  $A$ . So I can find out  $0.7d$  by uhh, this is  $I_y$  by

A,  $I_y$  means  $bt^3$  by 12 into  $b$  into  $t$ . So this will be  $0.7d$  by  $t$  by root 12, right. So  $\lambda$  we can find out as this.

So after calculation  $\lambda$  will be  $0.7d$  into root over 12 by  $t$ . This will be around  $2.5d$  by  $t$ . so for an idealized web strut the slenderness ratio  $\lambda$  can be found as  $2.5$  into  $d$  by  $t$  from which (23:22) the slenderness ratio can be found and for buckling class C, we can for a particular grade of steel we can find out the value of  $F_y$ , we can find out the  $F_{cd}$  value from this parameters. So  $F_{cd}$  value we can find out the compressive stress allowable compressive stress. Once we can find out the  $F_{cd}$  value I can find out  $F_{wb}$  that is the uhh buckling strength web buckling strength can be found.

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Now we will discuss about the web crippling for which it may fail. Web crippling means when a member is under concentrated load, say for example, we have a support condition here we have a support condition here, so it may fail at the root like this. So web crippling may occur due to concentrated force at the support due to concentrated force, right otherwise in other case also, it may fail like say if a concentrated force is applied at the beam at certain point then also web crippling may happen.

So now we have to find out the web crippling strength so that we can design accordingly, right. So here it is uhh the concentrate force is  $p$  right. Now to know this we have to find out the  $F_{wc}$ ,  $F_{wc}$  is uhh basically  $b_1$  into  $t_w$  into  $f_{yw}$  by  $\gamma_{m0}$  right. So  $b_1$  into  $t_w$  is a area and  $f_{yw}$  is the yield strength of the web, right. So  $b_1$  into  $t_w$  we have to find out, this is the area. So this  $b_1$  is what  $b_1$  is the bearing length. So  $b_1$  we can find out uhh considering an

empirical dispersion that the through flange to the web flange uhh connection at a slop of 1 is to 2.5 that means if we have a load here with a bearing length of  $b$  say, this is bearing length  $b$  and we assume that a dispersion of 1 is to 2.5 slop, it is dispersing.

So at the uhh if we consider this, if this is a flange and if this is the root radius then this value will be basically  $t_f$  plus  $R_1$  root radius  $t_f$  plus  $R_1$  and this  $b_1$  will become  $b$  plus  $2n_1$  right  $2n_1$  and  $n_1$  is basically, 2.5 into  $t_f$  plus  $R_1$ , right. So what we can see that we have to find out the uhh dispersion length which is  $b$  plus  $2n_1$  for concentrate load and if it is under uhh support condition then it will be  $b$  plus  $n_1$ , right. Now  $n_1$  is 2.5 into  $t_f$  plus  $R_1$ , because uhh this is  $t_f$  and this is  $R_1$ . So  $t_f$  plus  $R_1$  will be the depth, so dispersion will be  $t_f$  plus  $R_1$  into 2.5.

So once we find the dispersion length then we can find out the total length  $b_1$  and  $b_1$  if we find out we can find out the  $F_{wc}$ , the crippling uhh web crippling strength. So if tis web crippling strength is more than more than the load coming into uhh into the member at that point then it is find otherwise we have to uhh increase the section uhh or increase the web width so that web crippling can be avoided, right.

So you today discuss what we have seen that primarily the beam has has to design due to the moment and then we have to design due to shear and then criteria. So moment uhh carrying capacity, the design bending strength of the member can be found for two criteria, one is for low shear, another is for high shear. So in the codal permission, it is given you for low shear how to calculate the design bending strength and for high shear how to calculate design bending strength.

Then once design bending strength is calculated we will go for calculation of the shear strength and the design shear strength if it is more than the design if it is more than the shear force acting on the member then it is find otherwise again we have to redesign by increasing the section size, right and also we have to check whether it is uhh means it is safe under web crippling and web buckling. So those criteria has to be also fulfilled.

Of course we have not discussed about that deflection criteria, which also need to be fulfilled that means we we will find out what is that maximum deflection coming on the member due to the load and support condition avoiding (( ))(30:16) limiting deflection and if the criteria is satisfying then fine otherwise again we have redo. So this is how we can design a beam which is supported laterally. So laterally supported beam how to design has been discussed.

In next class we will go through one example of the laterally supported beam and we will see how to design that beam, okay. Thank you.