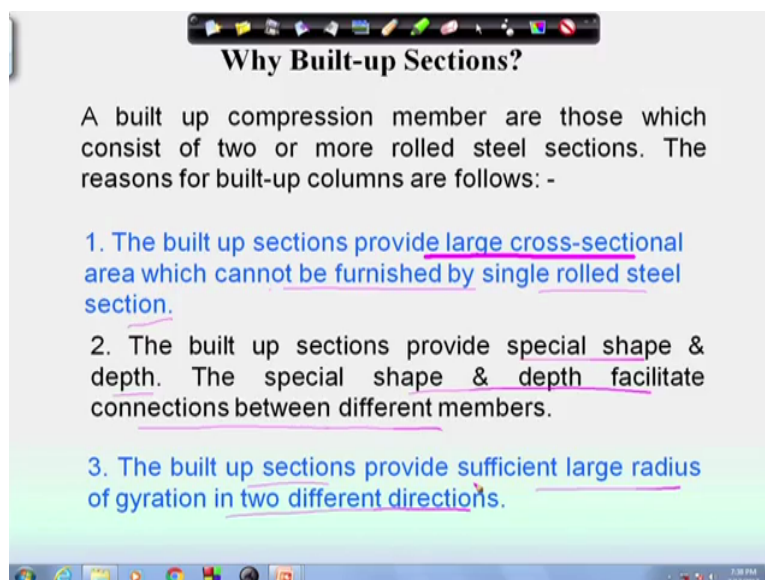


Course on Design of Steel Structures
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Lecture 35
Module 7
Design of Built up Compression Member

Today I am going to discuss about the design procedure of built up members, built up members comprises of two or more rolled steel section, in fact when a load when a compressive load is coming into picture sometimes the load is so heavy that a single rolled section cannot (0:41) that much load because there is a limitation of maximum size of the rolled section. Therefore when load becomes very high we may have to go for built up section comparison of two or more number of sections.

This is not only because of the high load but also sometimes we need equal radius of gyration in both the direction because in rolled steel section we generally see that radius of gyration in one direction is much higher than the other direction. Therefore the buckling will happen about the weaker section first and as a result the load carrying capacity of the member, member means the steel rolled section member will be less about a particular direction, to (1:36) that generally we provide a built up section where higher radius of gyration can be achieved in both the direction and thereby we can increase the load carrying capacity by providing such type of built up members.

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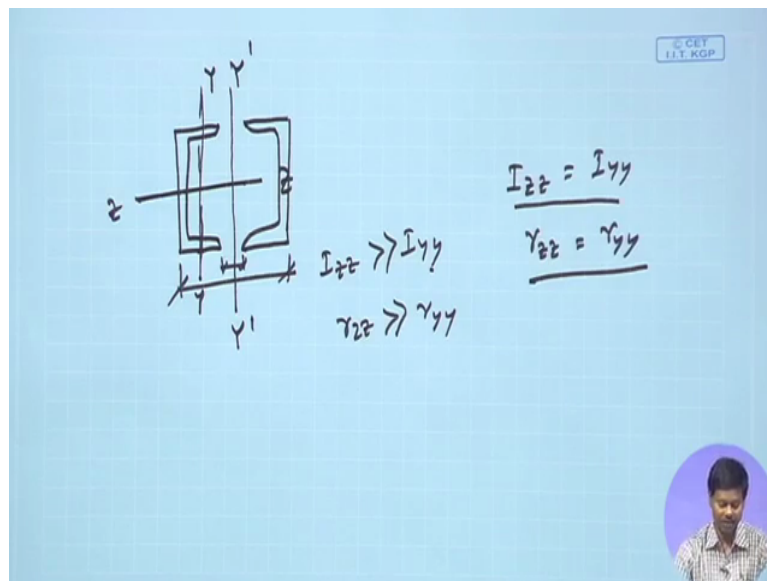
Why Built-up Sections?

A built up compression member are those which consist of two or more rolled steel sections. The reasons for built-up columns are follows: -

1. The built up sections provide large cross-sectional area which cannot be furnished by single rolled steel section.
2. The built up sections provide special shape & depth. The special shape & depth facilitate connections between different members.
3. The built up sections provide sufficient large radius of gyration in two different directions.

Now coming to reason as I told that one is that the built up section provide large cross-sectional area which cannot be furnished by single rolled steel section, right. Then built up section provide special shape and depth. The special shape and depth facilitated connections between different members. And another important thing is that the built up section provide sufficient large radius of gyration in two directions. Therefore we generally prefer built up members in case of long length of column and with high load.

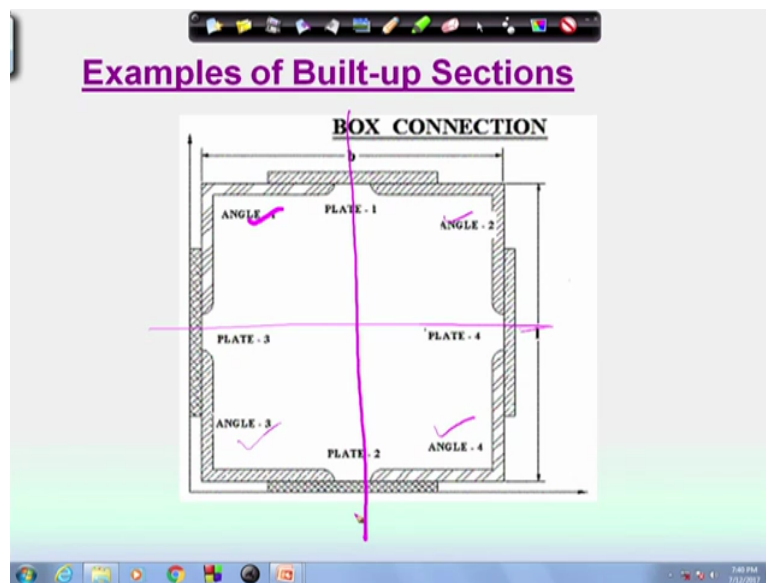
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Say for example if we consider a channel section as a compression member, then we know if this is z-z and if this is y-y axis if we consider, then I_{zz} is much higher than I_{yy} , right or r_{zz} is much higher than r_{yy} much higher than r_{yy} . Therefore the chances of buckling about y-y axis will be much earlier than about z-z axis. So if we provide built up member then what we can do we can increase the radius of gyration by providing another member and with a certain spacing.

So if we do that then we can see that I_{yy} the new I_{yy} of the section will become much higher and the built up member generally we provide in such a way that I_{zz} become I_{yy} means we will vary this spacing between two members to such an extent that when I_{zz} become I_{yy} upto that we will vary, right or r_{zz} become r_{yy} . So in this way we provide the configuration of the built up member.

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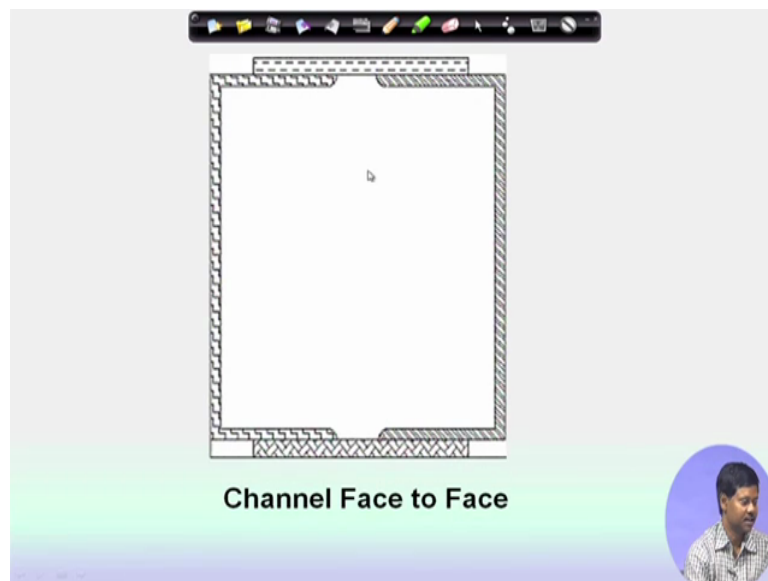
Now now examples of built-up member if we see, here we can see that we can use 4 angle section 4 angle section and to make a box type of cross section by the use of certain tie plate which is called generally lacing or battening that I will come later. So this is one example where we can use built up section to increase the I_{xx} and I_{yy} of the section.

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Another different type of built-up members are used another example is that when two channel sections are placed back to back, then also the built-up members means are connected with the lacing or battening member, so this is one example.

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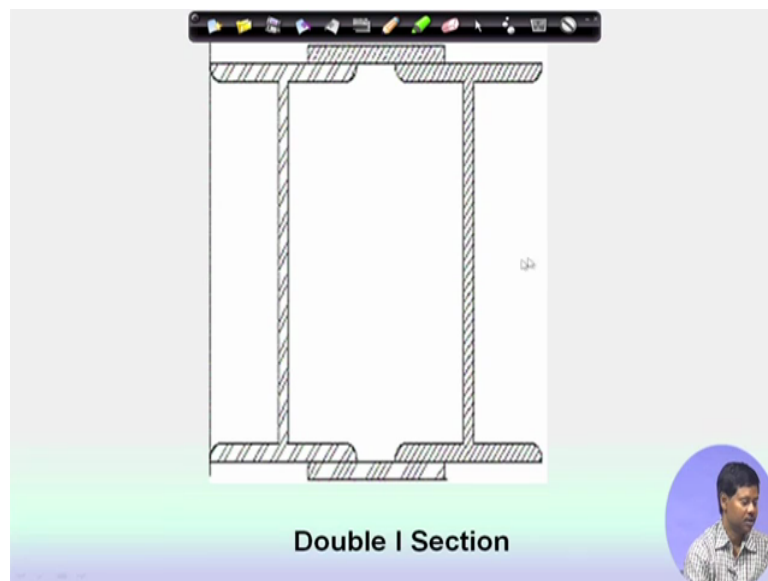
Next is channel section when facing face to face this way also we can provide a built-up member.

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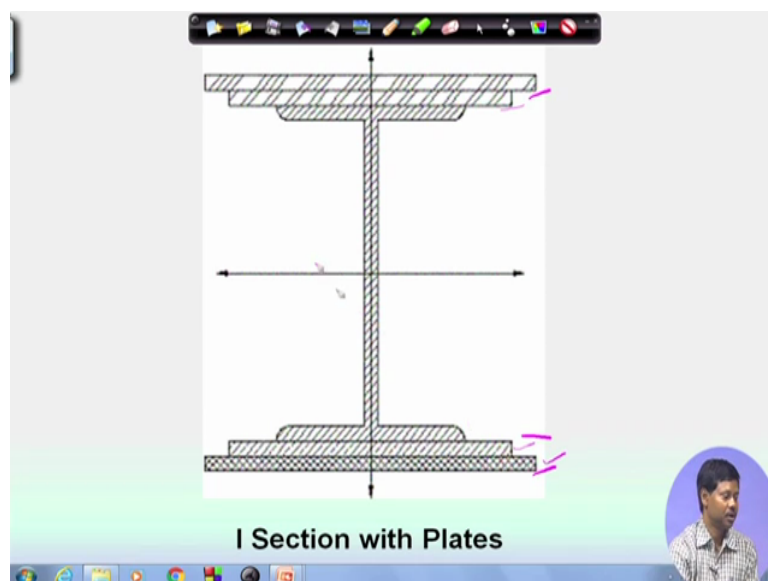
Then I section with channel section at the top as per the requirement, sometimes we see the requirement and according to that requirement we may have to provide that I section with a channel section at the top.

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Sometimes two I sections are provided to share the load.

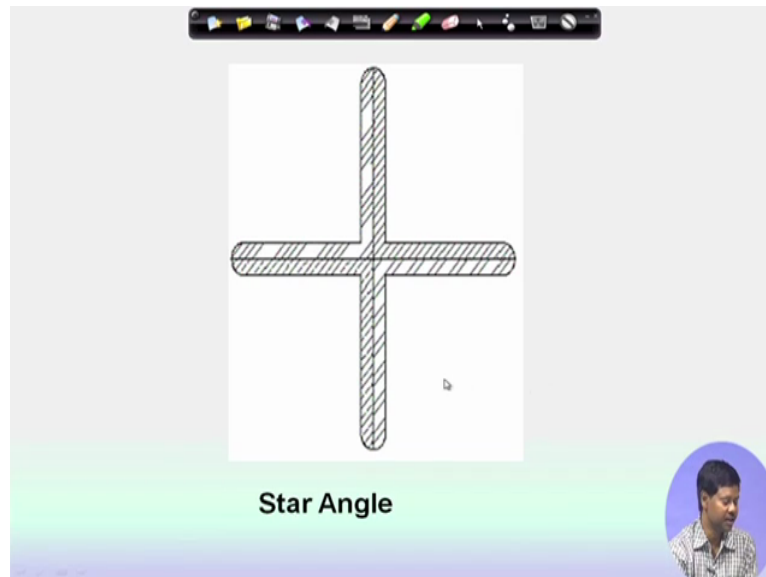
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Sometimes in place of plate girder we generally see that I sections are provided with additional plates. So number of plates are added as per the requirement and in this way we increase the load carrying capacity of the member. Generally I section with plate girder means with plates, we generally provide when the bending moment of the member is become becomes high. That means when a member is under flexural action then because of bending stress may be the single I section is not capable of taking that much load.

So in that case we may have to provide the additional plates as per requirement. So this is another type of means another example of built-up member.

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This is an another type of built-up member which is consisting of 4 angles which is called star angle.

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Design of built-up compression member

Step1: -
Find the effective length from the actual length & end conditions $l_e = K L$

Step2: -
Assume value of λ between 30-60 for the built section.

Step3: -
Find design compressive stress (f_{cd}) from Table 9(C) of IS:800-2007 for the given value of λ

Step4: -
Find the area as $A = \frac{P}{f_{cd}}$

Now coming to design of built-up compression member, so now if we see that design of built-up compression member the steps first we provide the means we find out the effective length. The step 1, what we do is we find out the effective length from the actual length and

end condition that means we can find out from actual length and the end condition from that first we will find out what is the effective length.

Then we generally assume certain value of slenderness ratio λ as 30 to 60 for built up section, generally we consider less value of λ because because of the built up section the radius of gyration is quite high and therefore the slenderness ratio we can consider quite less means it may be from 30 to 60 which will be sufficient.

Then in step 3 we find the compressive stress f_{cd} from table 9C because the buckling class for built-up member is C, therefore we can use table C and corresponding to table C for a particular value of λ whatever we consider we can find out the f_{cd} value for a given grade of steel. So once we get the f_{cd} value we can find out the required area A which is P by f_{cd} , where P is the axial compressive force which is acting on the member.

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Step5: -
Choose a built-up section so that the total area becomes more than the required area calculated in step 4. Also, arrange the members in such that the values of I_{zz} will become close to I_{yy} .

Step6: -
With the above arrangement, find r_{min} and then calculate λ .

Step7: -
From Table 9(C) find the value of f_{cd} and then the design compressive strength (P_d). If $P_d > P$ then OK, otherwise chose a higher section & repeat the Steps 5-7

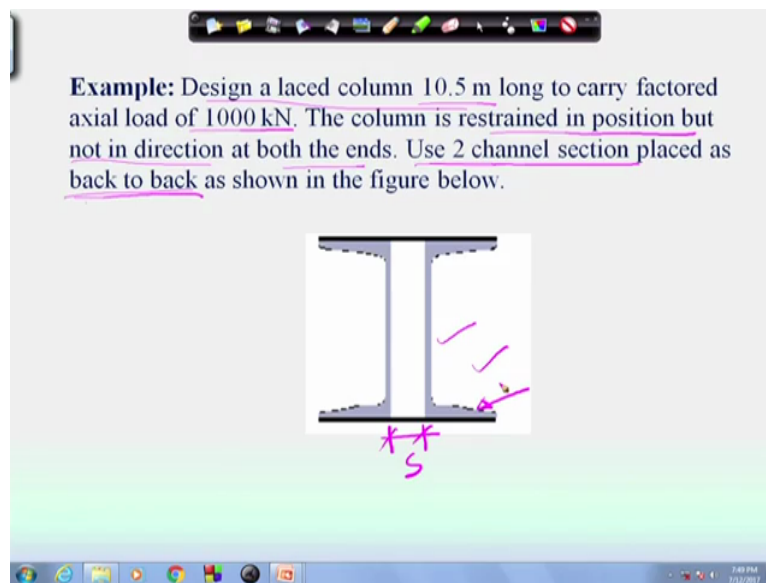
So once we get the area of the compressive member then we can choose a built-up section as per the requirement it may be channel section back to back, it may be channel section face to face, it may be I section. As per the requirement we have to decide what type of sections we are going to provide and what is the arrangement. So accordingly we will find out the required area means we will find out the area from from that considered section and then we will arrange the section in such a way may be if we use two channel section back to back, then we will arrange the section in such a way that the I_{xx} or I_{zz} become I_{yy} , so that we can find out the value of S , S is the spacing between two section.

So here our job is to find out the value of S in such a way that I_{zz} will become I_{yy} , once this is found we can find out the r minimum value which will be practically more or less equal r_{zz} and r_{yy} . So from the minimum value of r the radius of gyration we can calculate the λ the slenderness ratio that is l_e by r .

So from the slenderness ratio again we can go back to table 9C and we can find out the value of f_{cd} corresponding to particular λ and grade of steel, right. So once we get f_{cd} value we can find out the design compressive strength P_d which is A_e by A_e into f_{cd} . So design compressive strength we can find out and if we see the design compressive strength is more than the axial compressive strength acting externally then it is okay, otherwise we can go for a higher section and we can repeat from step 5 to step 7.

That means if we see the design strength is less than the actual load then we have to go for next higher section and we have to repeat the steps so that we get P_d as greater than P and then we can stop. So this is how we can find out the section size of the member and then we can find out the distribution of the means the arrangement of the section that what what will be the spacing between two members, this is what in the built-up section we do after that we have to design the lacing system or batten system as we provide because lacing system or batten system along the length we provide to tie the members the compression members in a proper way so that the members become discompression member the built-up members become parallel to each other, it has equidistance throughout its length and the force coming into the member become means even way means evenly distributed, so this is what we will do.

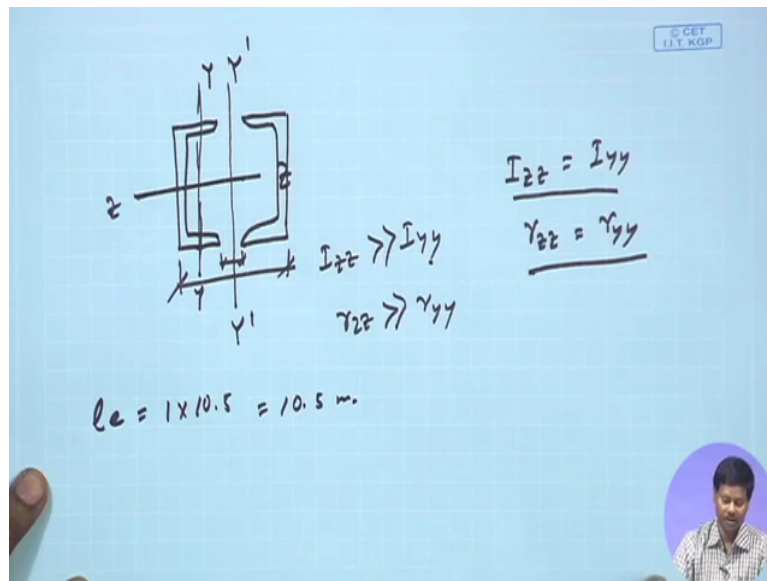
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Now we will go through one example through which we will be able to understand how to design a built up section. Say for example in this case we have to design a column laced column of 10.5 meter long to carry a factored load of 1000 kilonewton. The column is restrained in position but not in direction at both ends. Now it has been told that use 2 channel sections because we have lot of options we can use I section, we can use angle section and also it has been told that use 2 channel section placed back to back we may unless it is told we may use also face to face, or other way we can use. So these are the constraint has been given that we have to use channel section and back to back.

So what we need to do here is we have to find out what is the section size of the channel and what will be the distance between these 2 channel section that is S , spacing between these 2 channel section this is what we have to find out at the moment after that lacing design we will do later. So so to do this what we will do as per the steps we can first find out what is the effective length and then what will be the what is the approximate area as per the requirement of the λ , so this this is what we will try to find out.

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So first from the given problem we can find we know that the l_e the effective length is 1 into 10.5 that is 10.5 meter, right.

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Solution:
 For steel of grade Fe 410:
 $f_u = 410 \text{ MPa}$, $f_y = 250 \text{ MPa}$

Design of column:

$P = 1000 \text{ kN} = 1000 \times 10^3 \text{ N}$
 $L = 1.0 \times 10.5 = 10.5 \text{ m}$

Let the design axial compressive stress for the column be 150 MPa

Required area = $\frac{1000 \times 10^3}{150} = 6666.67 \text{ mm}^2$

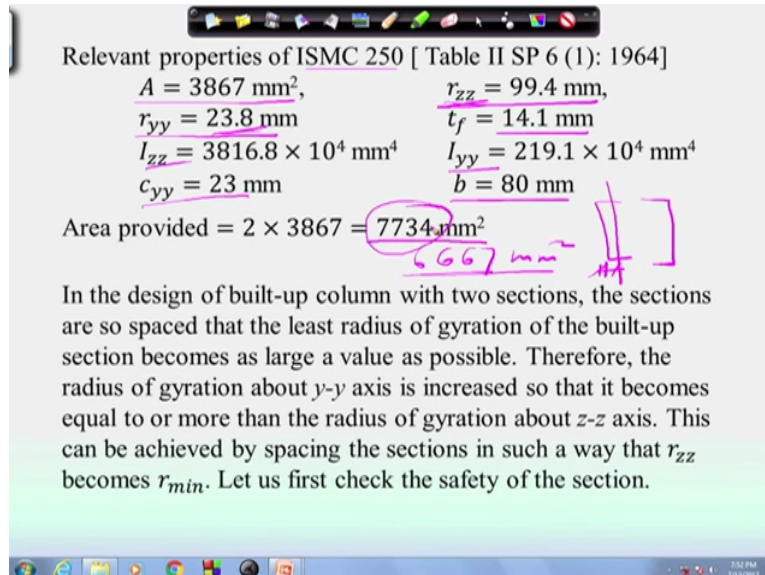
Let us try two ISMC 250 @ 298.2 N/m.

Handwritten notes: $\lambda = 30-60$, f_{cd}

So that can be shown here that that effective length we can find out as 1 into 10.5 that is 10.5 meter and we can consider either some λ as say 30 to 50 or 60 or directly we can consider some compressive stress design axial compressive stress that also we can assume. In steps I have shown that we can assume some λ value and then we can find out the f_{cd} value but directly also we can assume some f_{cd} value and we can find out the required area. So if we assume some f_{cd} value so for example in this case 150 MPa, then required area A

will be 1000 kilonewton divide by 150 that will be this 6666.67 millimetre square. So to accommodate this area we need to provide ISMC 250 to ISMC 250.

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Relevant properties of ISMC 250 [Table II SP 6 (1): 1964]

$A = 3867 \text{ mm}^2$,	$r_{zz} = 99.4 \text{ mm}$,
$r_{yy} = 23.8 \text{ mm}$	$t_f = 14.1 \text{ mm}$
$I_{zz} = 3816.8 \times 10^4 \text{ mm}^4$	$I_{yy} = 219.1 \times 10^4 \text{ mm}^4$
$c_{yy} = 23 \text{ mm}$	$b = 80 \text{ mm}$

Area provided = $2 \times 3867 = 7734 \text{ mm}^2$

In the design of built-up column with two sections, the sections are so spaced that the least radius of gyration of the built-up section becomes as large a value as possible. Therefore, the radius of gyration about y-y axis is increased so that it becomes equal to or more than the radius of gyration about z-z axis. This can be achieved by spacing the sections in such a way that r_{zz} becomes r_{min} . Let us first check the safety of the section.

So if we provide 2 ISMC 250, let us see what will be the combined area and its properties. So if we see that relevant properties are given here that one is the for ISMC 250 area is 3867 millimetre square, r_y is 23.8 and r_z is 99, so here you see r_z is much greater than r_y . So if we use a single section single section then it will buckle about weaker axis that is y-y axis. So to resist that we use 2 section, right.

Now thickness of flange of this channel is 14.1 which will be required for calculation, then I_{zz} and I_{yy} is also given in SP: 6 from which it has been taken, then C_{yy} is (23 point) 23 millimetre C_{yy} means the C_g distance and b the width of flange is 80 mm. So area provided will be 7734 millimetre square, we need 6667 millimetre square means as per the assumptions we can try with this, so we are trying little higher of this section and that is 7734.

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$$\left\{ \frac{L}{r_{zz}} = \frac{10.5 \times 10^3}{99.4} = 105.63 \right.$$

As per clause 7.6.1.5 of IS 800:2007,

The effective slenderness ratio, $\left(\frac{KL}{r}\right)_e = 1.05 \times 105.63 = 110.91 < 180$

For $\left(\frac{KL}{r}\right)_e = 110.91$, $f_y = 250$ MPa and buckling class c, the design compressive stress from Table 9c of IS 800 :2007

$$f_{cd} = 94.6 - \frac{94.6 - 83.7}{10} \times 0.91 = 93.61 \text{ MPa}$$

Therefore load carrying capacity = $A_e f_{cd}$

$$= 7734 \times 93.61 \times 10^{-3}$$

$$= 723.98 \text{ kN} < 1000 \text{ kN}$$

Which is not safe. *Pa*

Now if we try to calculate the slenderness ratio then we can see that L by rz will be this one.

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$$I_{zz} = I_{yy}$$

$$r_{zz} = r_{yy}$$

$$I_{zz} > I_{yy}$$

$$r_{zz} > r_{yy}$$

$$l_e = 1 \times 10.5 = 10.5 \text{ m.}$$

$$r_{zz} \sim r_{yy}$$

Why we are calculating L because rz, if we see when 2 channel sections are placed say back to back, then this rz will not increase rz will be rzz will be constant this cannot be increased that will be same. But we can increase the ry, ry will be increased ry was quite less which can be increased for the combined section upto rzz, so ry will be means assuming that the spacing of these 2 sections will be such that ryy will become rzz and as we cannot increase the value of rzz for this particular section by the change of S, so we first calculate the rzz value and then slenderness ratio value and then we will find out the design compressive stress.

So as per clause 7.6.1.5 if lacing member is used then its slenderness ratio is increase by 5 percent, so if we increase by 5 percent then slenderness ratio is coming 110 which is less than 180 so this is okay means from slenderness ratio point of view the member is fine. Then what we can do for for this slenderness ratio and for a particular grade of steel for this case this is f_y is equal to 250 MPa and buckling class c, as it is built up section we can find out the value of f_{cd} , f_{cd} value we can find out from table 9C and in table 9C for 110 the f_{cd} value is 94.6 and for 120 f_{cd} value was 83.7. So by interpolation we can find out the f_{cd} value for 110.91 which is coming 93.61.

Therefore the load carrying capacity we can find out which will be the area of the combined section into f_{cd} value which is coming 723.98 kilonewton and this is less than 1000 kilonewton that means it is not safe because the design strength P_d we are getting this value and the axial compressive force coming on the column is 1000 kilonewton, so the section whatever we have chosen is not safe. So what we need to do, we have to try with other section other section means the next higher section we can try.

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Try two ISMC 300 @ 351.2 N/m

Relevant properties of ISMC 300 [Table II SP 6 (1): 1964]

$A = 4564 \text{ mm}^2$,	$r_{zz} = 118.1 \text{ mm}$,
$r_{yy} = 26.1 \text{ mm}$	$t_f = 13.6 \text{ mm}$
$I_{zz} = 6362.6 \times 10^4 \text{ mm}^4$	$I_{yy} = 310.8 \times 10^4 \text{ mm}^4$
$c_{yy} = 23.6 \text{ mm}$	$b = 90 \text{ mm}$

Area provided = $2 \times 4564 = 9128 \text{ mm}^2$

$$\frac{L}{r_{zz}} = \frac{10.5 \times 10^3}{118.1} = 88.91$$

As per clause 7.6.1.5 of IS 800:2007,

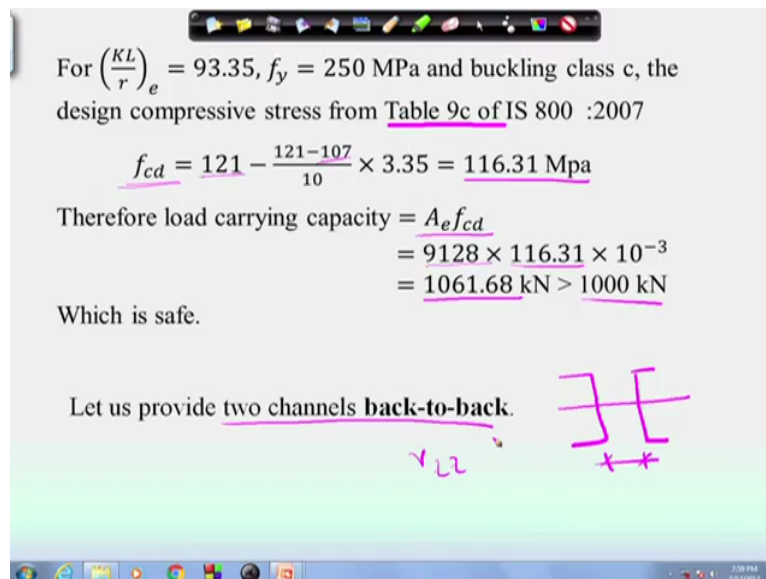
The effective slenderness ratio, $\left(\frac{KL}{r}\right)_e = 1.05 \times 88.91$

$$= 93.35 < 180$$

So next higher section is ISMC 300, so if we choose ISMC 300 then we can see the relevant properties of the section as the cross-sectional area of individual section is this, r_{yy} is this, r_{zz} is this, remember that r_{zz} is increasing from the earlier one also A is increasing, so load carrying capacity will definitely increase. Then I_{zz} is this, I_{yy} is this and C_{yy} , b from table 2 of SP: 6 we can found as this.

Now area of the combined section will become 2 into the area of individual section which will become 9128 millimetre square. So the slenderness ratio of the section will become L by r_{zz} , that is becoming 88.91, right. So slenderness ratio is coming 88.91 and the effective slenderness ratio will be 5 percent more than the original one, so that is becoming 93.35 and this is less than 180, so from slenderness ratio point of view the section chosen is okay, right. So the effective slenderness ratio we could find.

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For $\left(\frac{KL}{r}\right)_e = 93.35$, $f_y = 250$ MPa and buckling class c, the design compressive stress from Table 9c of IS 800 :2007

$$f_{cd} = 121 - \frac{121-107}{10} \times 3.35 = 116.31 \text{ Mpa}$$

Therefore load carrying capacity = $A_e f_{cd}$


$$= 9128 \times 116.31 \times 10^{-3}$$

$$= 1061.68 \text{ kN} > 1000 \text{ kN}$$

Which is safe.

Let us provide two channels back-to-back.

r_{zz}



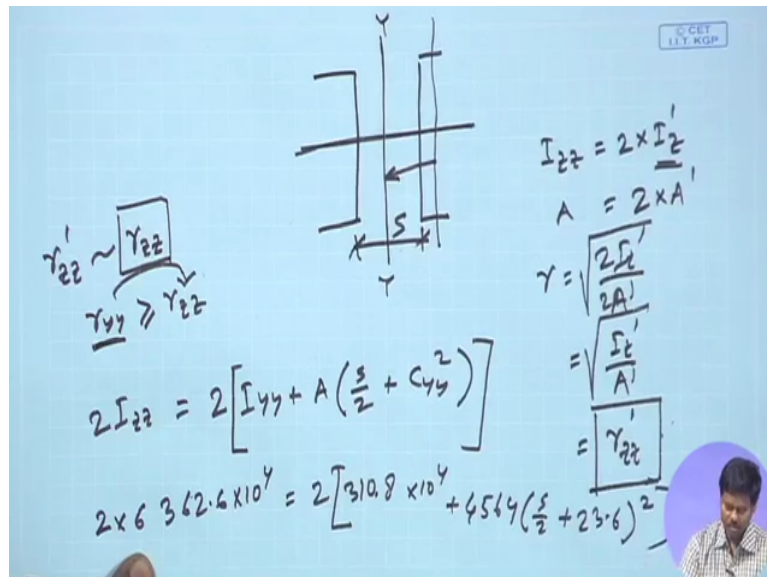
Now once we find the effective slenderness ratio we can find out the f_{cd} value, that is found from IS: 800-2007 of table 9c table 9c is for buckling class c and for f_y is equal to 250 the f_{cd} value is given as 121, for λ is equal to 90 and 107 for λ is equal to (10) 100, so by interpolation we can find out f_{cd} value as 116.31 MPa, right.

Now the load carrying capacity we can find out load carrying capacity will be the area of the section combined section into f_{cd} value. So if we put those value the area of cross section of the combined section into the design compressive stress 116.31, then we can find out the load as 1061.68 kilonewton which is more than 1000 kilonewton, so the section whatever we have chosen is okay, right. So we can provide two channels section back to back and channel section will be the section whatever we have chosen that ISMC 300, right.

Now next question is that what will be the spacing what will be the spacing of these two channel, so as I told the spacing will be decided on the basis of the equal strength from each direction. Now as we have seen that I_{xx} or I_{zz} cannot be increased that means r_{zz} cannot be

increased, so maximum strength can be achieved with respect to rzz maximum strength can be achieved with respect to rzz.

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So coming to this if we see here that if we have two section, now here I_{zz} will be say 2 into I_z individual I_z and A combined A will be 2 into A dash, right. So r will be the combined r will be basically $2I_z$ dash by $2A$ dash because I by r , so this is becoming I_z dash by A dash which is the r_{zz} dash, this is the radius of gyration of the individual section. That means the radius of gyration of the individual section if it is r dash zz then this will become r_{zz} the radius of gyration of the combined section as well, right.

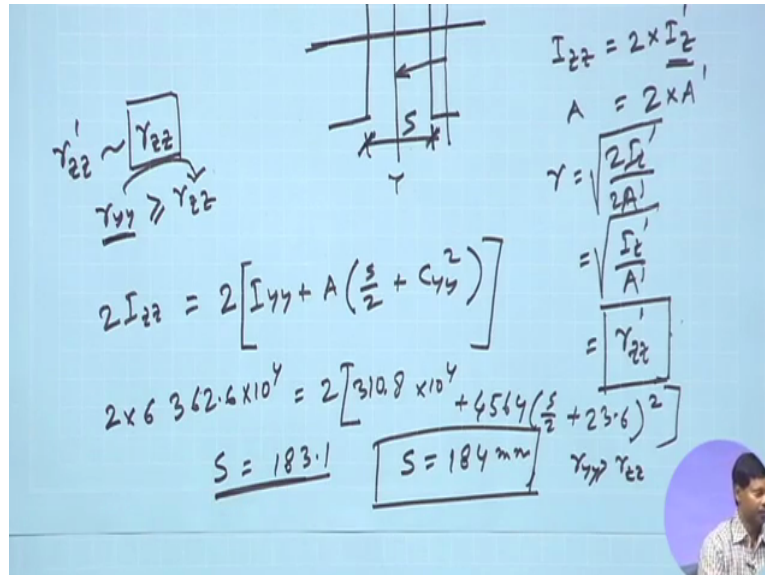
So there is no scope of increasing the value of r_{zz} that means maximum strength can be achieved with this radius of gyration. Now what will be the radius of gyration of I_{yy} means about y - y that we have to find out, right.

Now radius of gyration about y - y will be we will make we will make in such a way that it will be more than or equal to r_{zz} that means the the weaker section which was y - y about y - y that can be increased by the use of particular spacing and r_{yy} can be increased upto r_{zz} . So r_{yy} varies and it can be increased by the increase of spacing and that is so what will be the spacing, so spacing we can find out if we make equal I_{yy} of the combined section and I_{zz} of the combined section as equal.

So I_{zz} of the combined section will be $2I_{zz}$, right and I_{yy} of the combined section will be I_{yy} plus A into if this is S , then S by 2 plus C_{yy} square, right because I_{yy} we could find out from this and we are transferring to this $A r$ square. So from this if we put the value we can find out

the value of S by putting the value I_{zz} as 6362.6 into 10 to the power 4 and I_{yy} value is 310.8 into 10 to the power 4 plus $A r^2$ 4564 into S by 2 plus 23.6, this is the C_g distance.

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Handwritten derivation of the spacing S for two channels:

$$I_{zz}' = 2 \times I_{zz}$$

$$A = 2 \times A'$$

$$r = \sqrt{\frac{I_{zz}'}{A}}$$

$$= \sqrt{\frac{2I_{zz}}{2A'}}$$

$$= \sqrt{\frac{I_{zz}}{A'}}$$

$$= r_{zz}$$

$$r_{yy} \geq r_{zz}$$

$$2I_{zz} = 2 \left[I_{yy} + A \left(\frac{s}{2} + C_{yy} \right)^2 \right]$$

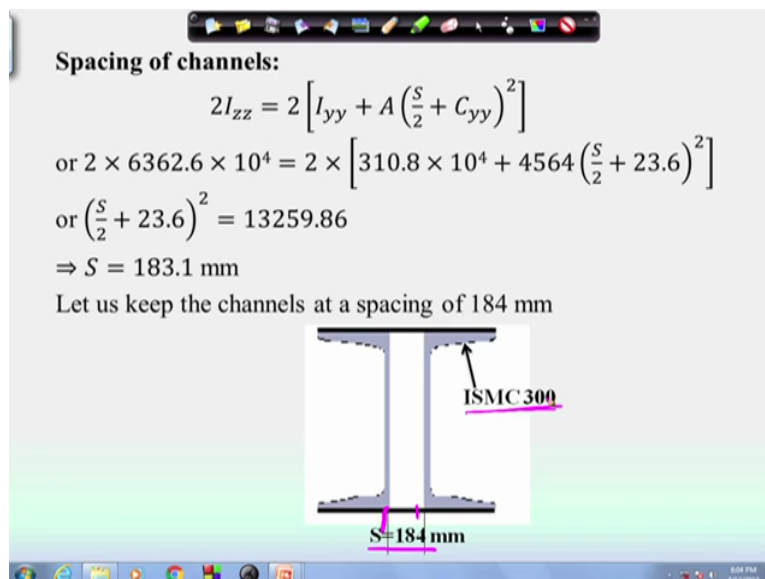
$$2 \times 6362.6 \times 10^4 = 2 \left[310.8 \times 10^4 + 4564 \left(\frac{s}{2} + 23.6 \right)^2 \right]$$

$$S = 183.1$$

$$S = 184 \text{ mm}$$

So from this I can find out value of S as 183.1 that means if I put S the spacing between two section as 183.1 then equal strength can be achieved. So we can provide say S is equal to little higher say 184 that means r_{yy} be little higher than r_z , right. So the spacing between these two members should become 184.

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Spacing of channels:

$$2I_{zz} = 2 \left[I_{yy} + A \left(\frac{s}{2} + C_{yy} \right)^2 \right]$$

$$\text{or } 2 \times 6362.6 \times 10^4 = 2 \times \left[310.8 \times 10^4 + 4564 \left(\frac{s}{2} + 23.6 \right)^2 \right]$$

$$\text{or } \left(\frac{s}{2} + 23.6 \right)^2 = 13259.86$$

$$\Rightarrow S = 183.1 \text{ mm}$$

Let us keep the channels at a spacing of 184 mm

Diagram showing two ISMC 300 channels spaced at $S = 184 \text{ mm}$.

This is what we have calculated in this slide, so the spacing between these two member will become 184 and ISMC 300 section will be used. So in today's lecture what we could see is

that the design steps design procedure of built up section and a work out example has been done to demonstrate the procedure for designing a built up section. In this example we have restricted upto the calculation of the section size that means what will be the section size and its spacing spacing between two section, right upto this we have discussed today. Next day we will discuss about the lacing member, thank you.