

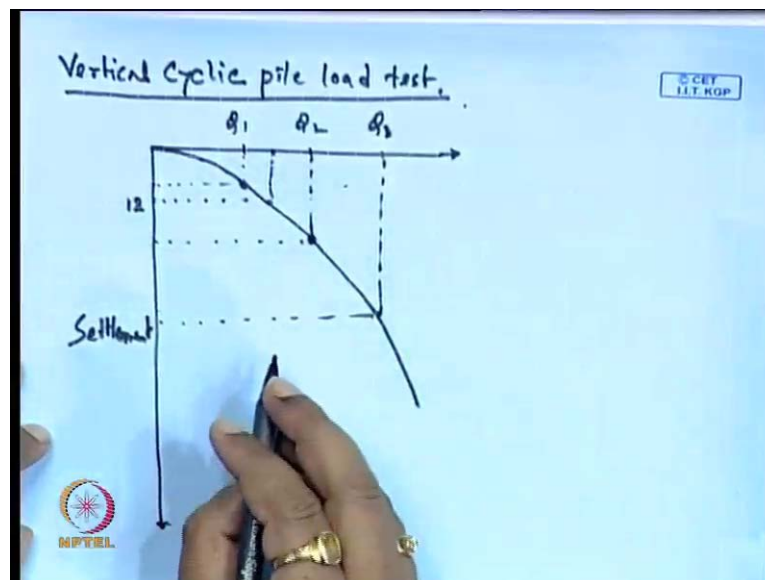
Advanced Foundation Engineering
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Lecture - 18
Pile Foundation- Load Carrying Capacity-II

In last class I have discussed about the how to calculate the pile load capacity by using pile load test, so now in that class I have discussed about the total load carrying capacity of the pile, I will calculate the total allowable load carrying capacity of the pile by using pile load test.

Now, if we want to know the contribution from the tip resistance, and the friction resistance friction part separately, then we have to go for the cyclic pile load test. Now, in this section I will discuss about the cyclic pile load test, and how to determine the frictional resistance of the pile, in the tip resistance of the pile based on this cyclic pile load test.

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Now, this sectional width or vertical cyclic pile load test, now here this is carried out to to separate the pile load in to the skin friction and point bearing on single pile of uniform diameter. Now, suppose if we to the load test this, if I draw the graph, so for the static

load we will draw we will get say these are the different load Q_1 , this is Q_2 , and the say this is Q_3 , so these are the increment, different increment Q_1 , Q_2 , Q_3 .

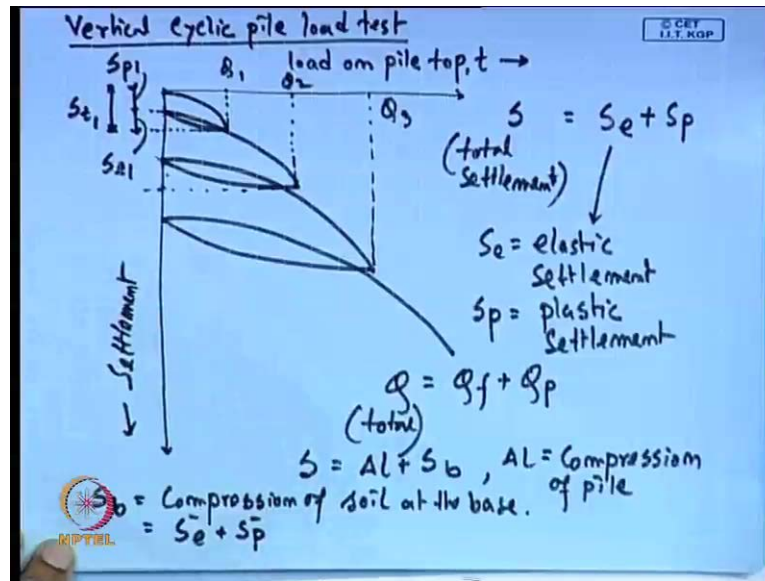
And there, because we are applying the load in 20 percent of increment, so there this is the load corresponding settlement, that I will measure; similarly this is the load and corresponding settlement that we will measure, so this is the value and this is the load and corresponding settlement this will measure (Refer Slide Time: 02:15). So, this is our if I join this point, so this will give us the static pile load test, and there so this will give up the this is the load and this is the settlement; so this settlement this will give us the static load pile load test curve.

Now, similarly here once we get this, this type of graph, so and then the others Q_4 and Q_5 then we will get the complete the graph, and then if we want to determine the allowable load carrying capacity of the pile, then we have to apply those conditions. Suppose, 1 is a 2/3rd of the load by which the settlement attains a value of 12 millimeter, suppose this is 12 millimeter then we will calculate suppose this is the load 12 millimeter, then we will calculate the q value corresponding 12 millimeter, and then we will take the 2/3rd of that load (Refer Slide Time: 03:27).

Similarly, we go for the second condition, then we will go for 50 percent of pile diameter, then we will get one settlement corresponding load 10 percent of the pile diameter for the uniform loaded pile, and then we will go for the that Q and take the 50 percent of that. Then similarly, we have to consider the all the condition and the minimum of that Q will consider that is the allowable load carrying capacity of the pile, but there we cannot know what the contribution from the skin friction is, and what the contribution from the tip resistance.

Where we there we are getting another total load carrying capacity or allowable load carrying capacity of the pile. Now, here by the cyclic test, we will calculate, we will know what would be the contribution from the friction resistance, and what would be the contribution from the tip resistance.

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Now, in the case of cyclic load what will do, so the this is the previous graph for the for the static pile load test, and this is for the vertical cyclic pile load test, now this test is limited only to the initial test not in the routine test. Now, here the graph that we will get suppose, this is the Q or the load on pile top it is in ton, and this is the settlement in millimeter, so this is the first increment say Q_1 ; so we will apply the loading up to Q_1 , then we apply the unloading, so this is the Q_1 and here we will get two settlement.

The next one we will start the Q_2 , and here we apply the loading curve, and then this is the unloading part, this is corresponding to Q_2 , similarly for the Q_3 we will go for the Q_3 , and then we apply the loading and the unloading (Refer Slide Time: 05:45). And then we will go on for the Q_4 and so on, so now here if I go for the every step, now here we will get the, this is our total settlement or S_{t1} , this is the total settlement for the first loading increment.

So, there is a two part, one part is we can see, so this portion is the permanent settlement, and this is the recovery part, so that means this portion is the elastic settlement, and this portion is the plastic settlement (Refer Slide Time: 06:40). So, there is a permanent set of the curve then it is when we unload the this portion this the last point is not the in first point of the of the starting point there is a permanent safe, so that safe is the plastic settlement S_{p1} , and the recovery portion is elastic settlement S_{e1} .

Similarly, for the second set also this there is a two part one is the total, so from this is the total, and then this is the plastic settlement, and this is the elastic settlement (Refer Slide Time: 07:33). So, now every increment of loading will get one plastic settlement, one elastic settlement that is for every increment.

Now, if I write the settlement of the total settlement if S is the total settlement, so that is total settlement is the summation of elastic settlement plus summation of plastic settlement, so S_e is the elastic settlement, where S_e is the elastic settlement and S_p is the plastic settlement. Similarly, the total Q that we are getting that is the combination of friction resistance and the tip resistance. And we can write, so that elastic settlement and the combination of the summation of elastic settlement, and plastic settlement is the, is the total settlement, total load is the summation of friction resistance plus the tip resistance.

In other hand, we can write the total settlement is the summation of ΔL plus S_b , so now where ΔL is equal to compression of pile material, pile or pile material. And S_b is compression of soil at the base (No audio from 09:43 to 09:56), so that this is also S_b have two component elastic part and plastic part, so this is the elastic part and the plastic part.

So, we can say this is the S is the total settlement that is the elastic settlement total elastic settlement and total plastic settlement, and here if that will get the compression of the pile material, because that class the compression of the soil at the base (Refer Slide Time: 10:21). So, at the base soil also so that means, the the total settlement it is due to the summation of the, the soil settlement at the base, so base soil that will settle, because of that we will get the settlement of the pile, and the pile material that may also compress.

So, that is the summation of the compression of the pile material, and the compression of the base soil, similar the base soil also there is two types of settlement, one is elastic settlement, another is the plastic settlement. So, and in the pile material also we can consider two types of settlement, one is the plastic settlement and the elastic settlement. So, the total elastic settlement is the summation of elastic settlement of the pile material, and the elastic settlement of the base soil. And total plastic settlement is the plastic settlement of the pile material, and plus the plastic settlement of the base soil.

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\bar{S}_e = elastic compression of the soil at base
 \bar{S}_p = plastic " " " " "

$S = AL + \bar{S}_e + \bar{S}_p$
 Again $S = S_e + S_p$
 $S_e + S_p = AL + \bar{S}_e + \bar{S}_p$ (1)

$\bar{S}_e = (S_p - \bar{S}_p) + \bar{S}_e - AL$
 $AL = \frac{(Q - Q_f/2)L}{AE}$

if $S_p = \bar{S}_p$ (as plastic settlement of pile material is neglected)

$S_e = \bar{S}_e - AL$

Q = total load on pile
 Q_f = frictional load
 L = Length of the pile
 A = average c/s area of the pile
 E = Modulus of Elasticity of the pile material.

Now, here if I further write this expression in different form, then we will get that again we can write this S_p is the plastic compression of the soil at the base, S_e elastic compression of the soil at base, and S_p is the elastic compression of the soil, this is the plastic compression of the soil at the base. So, finally we can write the total settlement is ΔL plus S_e plus S_p , and again we have written that S is total elastic settlement plus total plastic settlement.

So, if I compare this to expression, so S_e plus S_p that will be ΔL plus S_e plus S_p . So, you can write that S_e elastic settlement at the base is S_p minus S_p plus S_e minus ΔL , now this S_p and S_e that we can determine from the figure or the pile load test that load versus settlement figure. And this if I this ΔL we can calculate by this expression that Q minus Q_f by 2 into L divided by $A E$, where Q is equal to total load on the pile Q_f , the frictional resistance, frictional load or resistance (Refer Slide Time: 13:30).

This is the length of the pile (No audio from 14:14 to 14:21) (Refer Slide Time: 14:14), this is the average cross section area of the pile, E is the modulus of elasticity of the pile material of the pile material, so this is the modulus of elasticity of the pile material. Now, if we consider that the plastic settlement of the pile material is negligible, because the plastic settlement, total plastic settlement we are taking the summation of plastic settlement of the pile material, and plastic settlement of the base soil.

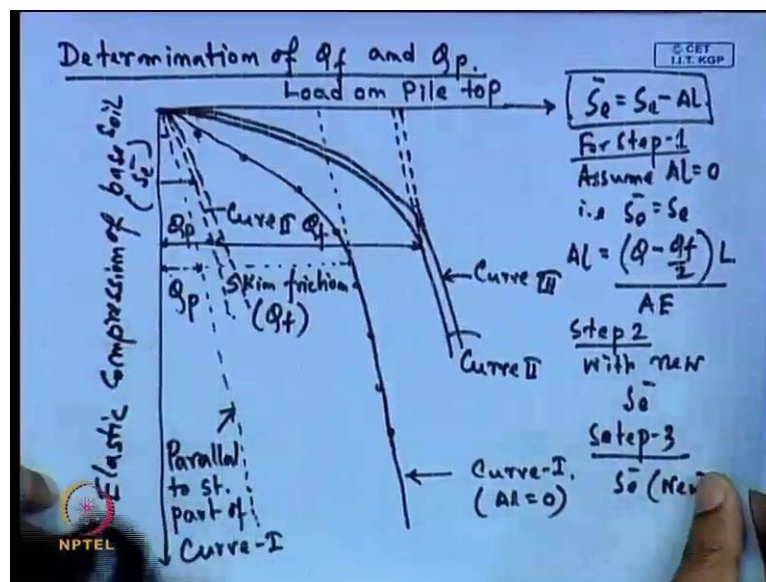
So, here we assume the plastic settlement of the pile material is negligible, so we are taking the all the settlement of the pile material is elastic, because the pile material is very steep compare to the soil. So, the plastic settlement is, plastic settlement of the pile material is negligible, so total settlement will be total plastic settlement will be plastic settlement of the base soil, because plastic settlement of pile material is neglected as (No audio from 15:59 to 16:13) is neglected, in that case S_p will be S_p dash.

So, from this expression, so if I write this is equation 1, so from equation 1 we can write, or equation this is 1 we can write that \bar{S}_e is S_e minus ΔL , so this is the expression or the final expression. So, here ΔL we will calculate by this expression, and S_e we have to determine from the pile load load versus settlement graph, and then we will calculate the S_e part.

Now, the next step how to determine the Q_f and Q_p ; the next step determination of Q_f and Q_p ...

(No audio from 17:20 to 17:36)

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Q_f is the friction resistance, and Q_p is the base resistance, so here first what we will do, so we draw a graph, so this is load on pile top, and this side this is the elastic compression of soil or sub grid, so this is the elastic (No audio from 18:14 to 18:25) base soil. So, you can write this is S_e bar, so this side is S_e bar and this side is load on the

pile, so first step we assume that ΔL is 0, so what we will get from this load versus settlement curve or the first curve, so that I have drawn this for the pile.

So, from this first curve we will get what is the S_e for a particular loading density, for a particular loading density what is S_e (Refer Slide Time: 19:01). Now, if we consider that because the our expression is \bar{S}_e equal to S_e minus ΔL , so that is the expression and for the first step, for the step 1 assume ΔL is equal to 0, so this S_e for any load increment will get from the previous curve or load versus settlement curve, and then we will get the S_e .

So, in that case S_e that is \bar{S}_e is equal to S_e for the first step, this is for the first step only, so what we will do now we will draw this graph, corresponding to different loading point (No audio from 20:12 to 20:22), so we will draw this graph, so this is say curve I, this is for the first step where we assume that ΔL is equal to 0 (Refer Slide Time: 20:00).

Under next step that what we will do that, we will draw one line which is parallel to this straight portion, now this is the straight portion of the graph, so here we will get one non-linear portion, then is a straight portion of the graph. And we draw one parallel line which is passing through this origin, and parallel to this straight portion of this curve I (Refer Slide Time: 21:16). So, which is passing through the origin, and this is this graph is parallel to the straight line portion of curve I, so this is parallel parallel to straight part of curve I.

Now, from this graph we will determine what would be the value of here, from this graph, so this part will give you the point resistance of any loading increment for this loading increment say (Refer Slide Time: 22:00). So, this will give the point resistance and this part will give the friction resistance, this is the skin friction or Q_f , and this is the Q_b part Q_b or Q_p part. So, or any loading position say from this portion, here this portion is Q_p and for this is the friction resistance part, so here that we will determine.

So, once we get this any loading condition will get the Q_p and Q_f , in the second step once we know the Q_a value, because that expression of ΔL , ΔL we are giving that is the Q minus Q_f divided by 2 into L divided by $A E$. So, E is material property L is the length of the pile, and Q and Q is the total load at load or the load increment at any point, and once we get the Q_f from this part, because this step portion this step portion left

hand side will give you the Q_p and this is the right hand side will give us the Q_f (Refer Slide Time: 23:29)

So, once we get the Q_f at any loading increment from this graph, will get the ΔL , so for the any loading increment we will calculate the ΔL , and that ΔL we will put here, and S_e is previously we can calculate from the load (()) displacement curve and that is the same as the step I. So, now we will get the new S_e bar, so once we get a new S_e bar then we will draw another curve by using the new S_e bar, suppose that is this curve is the new S_e bar or the step II (Refer Slide Time: 24:16).

So, this is our step II, how do we calculate new S_e with new S_e bar, so this is say curve II similarly, this curve also we will get one straight portion we extend this, straight portion of the curve, and again we will draw the parallel line of this straight portion, so this is the parallel line for curve II (Refer Slide Time: 24:39). And similarly, we will repeat the something here also we will get the Q_p and Q_f separately from this, the left hand side of this part, so this portion is basically this portion is Q_p , and this portion is Q_f .

So, this here also this is Q_p , the Q_f the Q_p and Q_f for the first part and this is this portion is Q_f and this portion that means, the right hand side of this straight line which is passing through the origin straight parallel to the straight portion of the curve, right hand side of this curve is Q_f , and left hand side of this curve is Q_p . So, once we get this value then we will calculate the new ΔL , and then we will get the new again in the step 3, we will get another S_e bar or the new S_e bar, then will get another we will calculate another curve (Refer Slide Time: 25:59).

So, this is our curve III and again we will extend this the straight portion, and then we will again draw this parallel line for the straight portion of this third curve, and again we calculate the Q_p and Q_f , again we repeat the something, we will calculate new ΔL we will calculate the new S_e bar. And we will repeat the thing unless the two curves are (()) curve were matching each other, and generally it is observed the after the three trails this curves are matching each other.

So, this so when this curves are matching say suppose curve III and curve IV are matching each other, then we will stop there. And then from that curve itself, similarly from this straight portion right left hand side will give us the contribution from the Q_p

that means, this is left hand side. And the right hand side of this straight portion which is passing of the of the line which is passing from this origin, right portion right hand side of this curve up to the origin original curve that will give us the friction resistance.

So, one the so for this method we can determine, what is the contribution from the tip resistance, and friction resistance separately. Now, this will give us the ultimate load carrying capacity of the friction or contribution from the friction and the tip separately (Refer Slide Time: 27:45). Now, if we want to find the safe pile capacity, then you have to divide this thing by factor of safety.

Now, for the skin friction resistance, so that we if we divide this part by factor of safety, we will get the safe friction resistance, and safety bearing resistance that we are getting from this pile, by that we can determine from the pile load test. So, by this method the cyclic pile load test, we can separately determine the contribution from the friction part or friction resistance and from the tip resistance of the pile by this pile load test.

Now, the next section that on the, next section we will discuss about the pile load test for the different dynamic pile formula, because this is the third method, because the first method was static expression. Now, this second one data I have discussed from the pile load test, now next one that we will discuss that I will discuss that is five dynamic pile formula.

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Dynamic Pile Formula:

• Engineering News Record (ENR) Formula.

$$Q_a = \frac{WH\eta_h}{F(s+c)}$$

(allowable pile load)

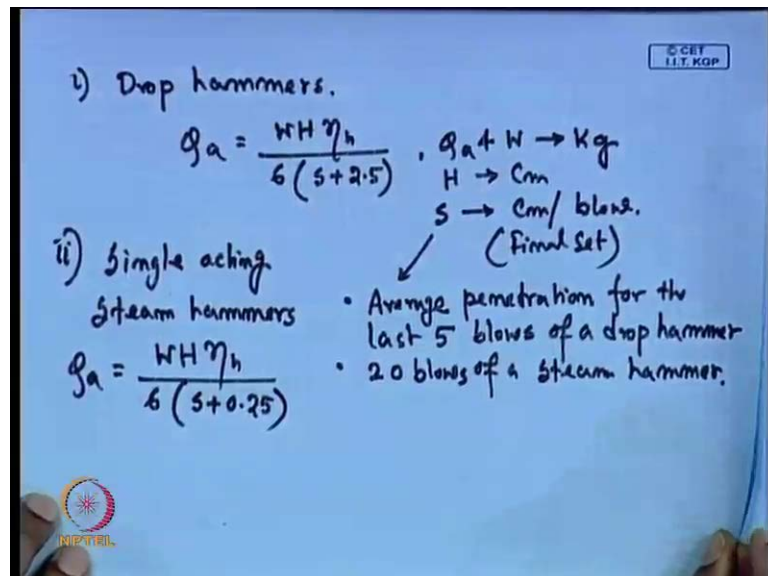
W = wt of the hammer
H = height of falling.
s = real set/blow
c = empirical factor
F = F.O.S (≈6)
 η_h = efficiency (Drop hammer → 0.7 to 0.9
Steam → 0.75 to 0.85)

So, this is the (No audio from 29:01 to 29:12) over that one formula that will given, so first one will giving the (No audio from 29:17 to 29:24) engineering news record or ENR formula. So, these are the based one the pile driven energy or the weight that we are using, based on that we are calculating this allowable load carrying capacity of the pile.

So, Q allowable or the allowable pile load that we can calculate by W into H into η_h into S plus C , where W is weight of the hammer (No audio from 30:22 to 30:37). And H is the height of fall (No audio from 30:43 to 30:53) height of falling, S is the real set per blow, C is the empirical factor, F is factor of safety usually taken as 6 and this is the efficiency.

Now, for the drop hammer this value is 0.7 to 0.9, for steam hammer this value is 0.75 to 0.85. So, now, this equation of this expression is based on the energy that we are applying to or to draw and drive a pile into the soil. So, this is the weight of the hammer this is the free fall height this efficiency and this is a factor of safety, which is generally taken of 6, S is the set real set per blow. Before we apply the load how much is the amount of the real set per blow that is S and C is the empirical factor. Now, this expression we can use for different hammer.

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So, now, for the drop hammer (No audio from 32:46 to 32:55) this Q_a is W into H and this is the efficiency into 6 factor of safety and S plus 2.5. This is for the drop hammer

where q_a , and w this is in $k g$, H in centimeter, S is equal to centimeter per blow that is the final set or the real set or the final set (No audio from 33:34 to 33:45).

So, this final set S we can take, that S value that the average penetration, (No audio from 33:52 to 34:02) for the last 5 blows of a drop hammer or 20 blows of a steam hammer. So, that means this S centimeter per blow, here the final set when last 5 blows average that, we will consider as the S in case of drop hammer. And for last 20 blows of in case of steam hammer, the average of last 20 blows penetration that we will consider the s value in case of steam hammer.

So, similarly for the steam hammer or single acting steam hammer, this Q_a is equal to W into H into efficiency by 6 plus S into 0.25. So, here for the drop hammer c value is 2.5, for the steam hammer this is 0.25. So, this again this W and Q_a is in $k g$ H is in centimeter, S in centimeter per blow this is 0.25.

So, by using this expression also we can determine the pile load carrying capacity of the pile. So, now, there is others other this type of expression are also available, but here I am just giving one expression, which is very popular that is the a ENR formula and by which we can also determine the pile load carrying capacity. The next one the fourth method, that we can determine the pile load test by using the correlation with the penetration test data.

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By using Correlation with Penetration Test value.

Driven Pile in Sand.

- $q_{pu} = 40 N (L/D) \rightarrow KN/m^2 \leq 400 N KN/m^2$

\swarrow SPT (observed)
 \swarrow Ultimate tip resistance
- $q_{pu} = q_c$

\swarrow Come resistance.

$\neq 400 N KN/m^2$, N is observed value without any overburden correction.

\swarrow at least 5D

\swarrow Heavy layer

By using (No audio from 36:31 to 36:41) with penetration test value; that means, by SPT or CPT value we can determine the pile load carrying capacity of the pile. Now first we will give the for the driven pile in sand, so driven pile in sand. So, here q_p that means, the it is the tip resistance ultimate tip resistance (No audio from 37:25 to 37:37).

That this $40 N$ into L by D which is in kilo Newton per meter square, but that should be less than equal to $400 N$ kilo Newton per meter square. That means, this if we use this expression, now that q_p cannot be greater than $400 N$ kilo Newton per meter square. So that means, if it is coming more than 400 kilo Newton per meter square, N kilo Newton per meter square, then we have to consider the $400 N$ kilo Newton per meter square.

So, that means, so this will limited to this value that means, this is the ultimate tip resistance. Similarly, for the driven pile we can find the q_p that is q_c , which is based on the SPT value, this is the SPT value. So, this is SPT value is observed value without any correction. So, this N is observed value without any overburden correction correction.

Now, again by the q_c that means, the cone resistance, this is the cone resistance, we can determine the tip ultimate tip resistance of the pile. Now, q_c is taken as the average value q_c over a distance $3 D$ above and $1 D$ below the level of the pile tip. That means, this q_c value, suppose this is the pile tip portion and this diameter is say D . So, that we can take the average value of this is $3 D$ and $1 D$, then this is the tip.

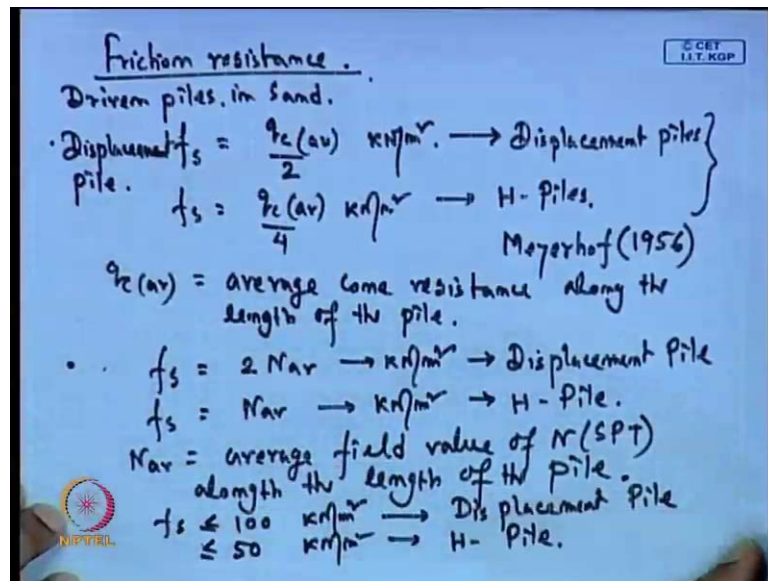
So, the average value of this $4 D$ portion, the $3 D$ above the tip and $1 D$ below the tip that average value of q_c , that we have to consider as this q_c . So, that means, for the pile to attain the it is full bearing resistance it should be driven at least $5 D$ inside the bearing strata. For the pile attain its full bearing resistance; that means, for the pile attains the full bearing resistance it should be driven at least $5 D$ inside the bearing strata. Suppose, if there is a bearing strata is there.

So, this is suppose the bearing strata inside this one is the bearing strata, bearing layer then the pile this has to be penetrated inside the strata at least for the $5 D$ part. Then we will get the full resistance this is the at least. See, if one pile is penetrated that this bearing layer or the bearing strata at least for the $5 D$ length then we will give the full resistance from this strata. Now that means, here the this q_c value will take the average

of this 3 D above the tip and 1 D below the tip this average of this 4 D zone, we will get the q_c .

Average q_c will give the q_c and if we get the full resistance of this any bearing strata, then this bearing strata this pile has to be penetrated at least 5 D below this within this bearing strata. Now, the friction resistance this is the we are talking about the ultimate tip resistance then how to get the friction resistance.

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The friction resistance of the pile, (No audio from 42:08 to 42:17) so for the driven pile here the same thing for the driven pile in sand. So, we are talking about the this pile in sand, the friction resistance f_s we can take the q_c average by 2 that is in kilo Newton per meter square.

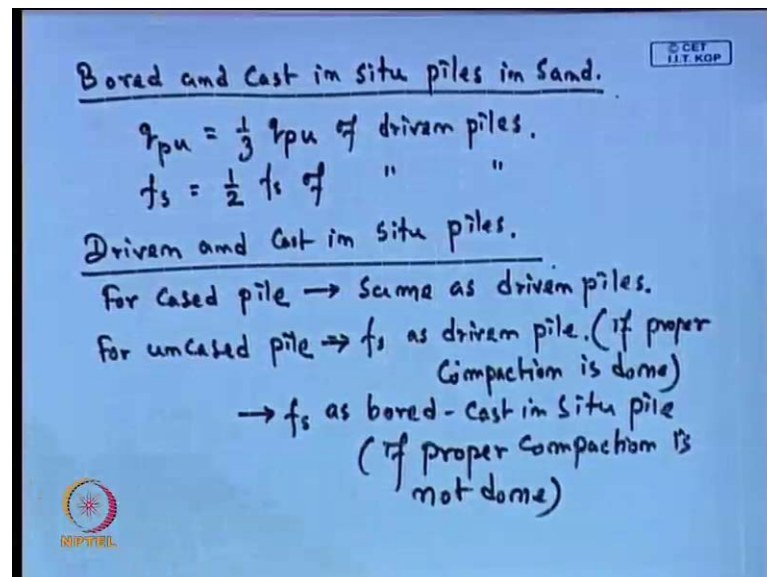
And this is for the, this is displacement pile or this is for the displacement pile and f_s is equal to q_c average by 4, this is kilo Newton per meter square this is for the H pile. This expressions are given by the both the expressions given by the Meyerhof in 1956. Now, q_c average, is the average cone resistance (No audio from 43:35 to 43:45) along the length of the pile, this is the average cone resistance along the length of the pile same way.

Similarly this is in terms of cone resistance, similarly for the in terms of N value this q_s is equal to $2 N$ average this is also kilo Newton N meter square, this is for the

displacement pile or q_s equal to N average that is in kilo Newton per meter square this is for the H pile. Where N average this is the SPT value this is the average field value of N this is the SPT along the length of the pile.

Now, another condition that, here the for the q_p even that means, the tip resistance also that that cannot be greater than 400 N value. Similarly, now for the displace $q_f s$ that is less than equal to 100 kilo Newton per meter square, this is for the displacement pile and that is less than equal to 50 kilo Newton per meter square that is for the H pile. So, this is the another two condition, so these are the expression for the driven pile in the sand.

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Next one we will give the expression for the bored and cast in situ pile in the sand. This is the bored, (No audio from 46:05 to 46:27) now again we will get the $q_p u$ that is equal to 1/3 rd of $q_p u$ that we will get of driven pile. And f_s that is equal to half of the f_s of driven pile. So, first we will calculate the $q_p u$ and f_s for the driven pile, and then we take the 1/3 rd for the bored and cast in situ piles in sand and f_s is half of the f_s of the driven pile.

Next one is the driven and cast in situ pile. Now here for the case pile, case pile it is same as driven pile. And for the uncased pile the f_s as driven pile if a case f_s is same as driven pile. Now, if proper compaction is done or either we can take f_s as bored cast in situ pile, if proper compaction is not done. So, these are the condition or these are the condition by which we can determine the pile load carrying capacity of the pile or as the

tip resistance of the pile or the friction resistance of the pile, based on the penetration test data; that means the cone resistance or the n value or the SPT n value. We can determine this for the driven pile, we can determine bored cast in situ pile, we can determine for the driven cast in situ piles also. And that then in the different pile condition in the case pile uncased pile on all this the cases, we can driven we can determine the pile load capacity of the pile by using this penetration value.

So, there is four different methods by which we can determine the ultimate load carrying capacity of the pile or allowable load carrying capacity of the pile, one first one is the static method or static equation or the formulae. Next one, second one is the by the pile load test, so for the for the static or the cyclic if I go for the for the cyclic pile load test then we can determine separately the section resistance and the tip resistance. And third one by using the dynamic equations or the formulae's and formulae. And the next one in the third expression is by using by using the penetration test data.

So, these are the all different methods by which we can determine the pile load, ultimately pile load capacity of the pile different piles. And then in the in this section I have also discussed, that when we go for the group analysis or group calculation, then how we will calculate this group efficiency of the pile and group ultimate load carrying capacity of the pile.

Now, this in the next section I will discuss about the settlement of the pile, then the how to calculate the load bearing capacity of the under reamed pile in those things, I will discuss in the next section.

Thank you.