

Advanced Foundation Engineering
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Lecture - 1
Introduction

Hello. So, today I will start the first lecture on advanced foundation engineering. So, in this lecture I will be covering different design aspects of various geotechnical structures like shallow foundation, deep foundation, the retaining wall reinforced retaining wall, then what would be the soil structure interaction, then how we will design the different reinforced structure in geotechnical aspect. So, these things will be discussed in this lecture, and before we discuss about the various design aspects of foundation and the geotechnical structure foundation of geotechnical structures, then we will start about our different modules. So, what are the different modules that we will discuss?

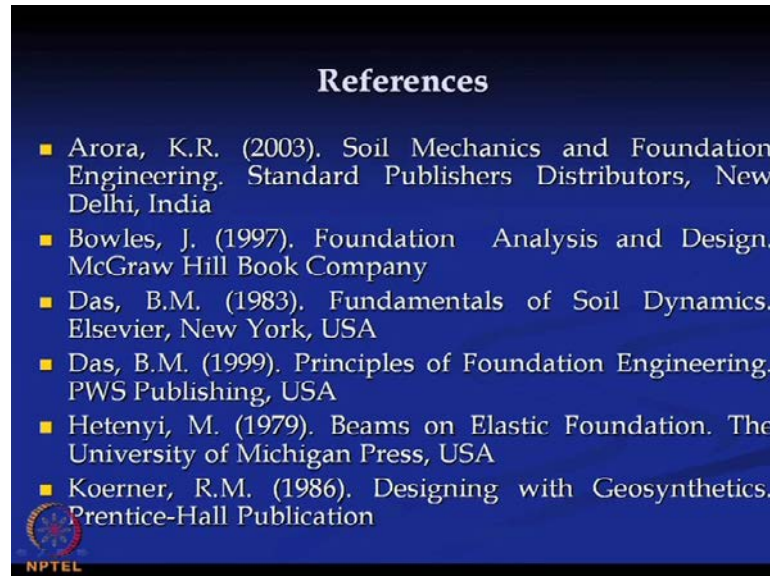
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So, first here the course has been divided into five modules; that is module one there will be soil exploration, then the module and in the soil exploration there will be three lectures, and then the shallow foundation that is module two there will be total eleven lectures, and then in the deep foundation module three there will be total seven lectures and the retaining structures and the reinforced earth design, so that is module four there will be total ten lectures, and the soil foundation interaction then that will be module

five; there will be total eight lectures. So, including the introduction today's lecture there will be total forty lectures in this course.

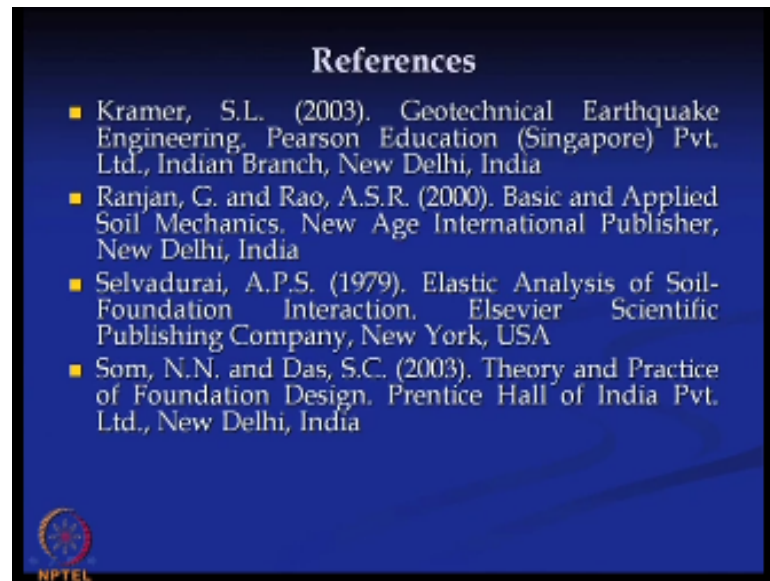
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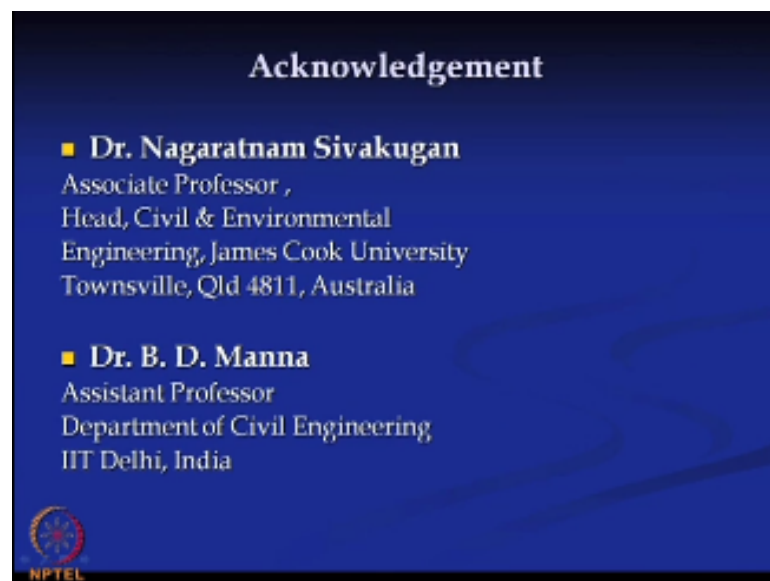
Now the books that will be that is the reference books and this will be followed in the lectures. Those are the Arora 2003 which is soil mechanics and foundation engineering that is the Standard Publishers Distributors. Then Bowles in 1997, then B. M. Das 1983, then one is Foundation of Soil Dynamics, another is B. M. Das 1999 Principles of Foundation Engineering, then Hetenyi books that is Beams on Elastic Foundation 1979, then Koerner's books for the Design with Geosynthetics that is 1986.

Then the Kramer books for the Geotechnical Earthquake engineering part because some part of the earthquake engineering design or design of the retaining wall under earthquake seismic condition that will also be discussed in this course. So, that part the reference book is Kramer 2003, then Ranjan and Rao on Basic and Applied Soil Mechanics 2000 and then Selvadurai that is the Elastic Analysis of Soil Foundation Interaction 1979 that is the reference books for the soil foundation interaction part, then N. N. Som and Das 2003 the Theory and Practice of Foundation Design. So, these are the reference books which will be followed in these lectures.

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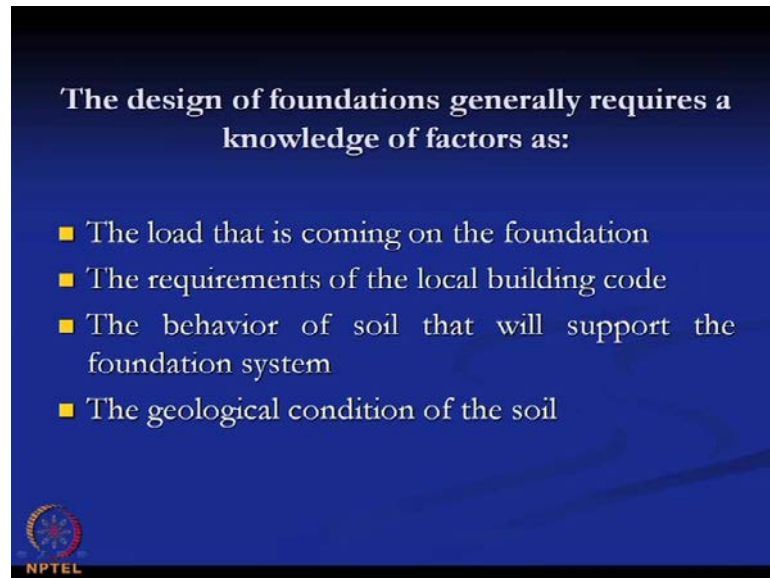


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Now the acknowledgment is given to the professor N.Sivakugan, Associate Professor and Head, Engineering College, James Cook University, Australia, and Professor B. D. Manna, Assistant Professor, Department of Civil Engineering, IIT Delhi, and they have also given some lectures note which will help me to prepare these lectures.

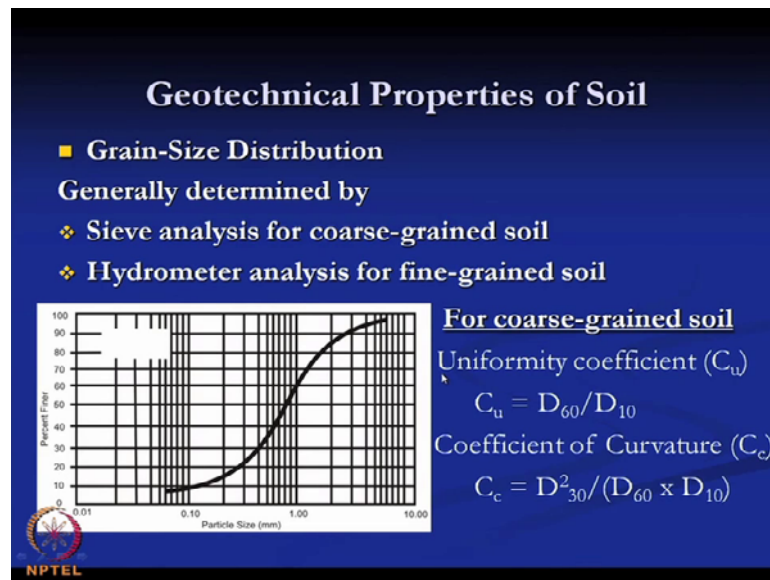
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Now first we start that the design of foundations generally requires knowledge of factors as the load that is coming on the foundation. So, the first is what is the load which is coming on the foundation; the requirements of the local building codes; the behavior of soil that will support the foundation system, and geological condition of the soil. So, these things are very important when we design a foundation that how much load is coming on the foundation. So, we should know how much load is coming on the foundation, then what are the required design codes building codes of the area where we are designing the foundation.

And the behavior of soil that will support the foundation system, what will be the soil properties? So, we should know the soil properties before we know start the foundation design, then what is the soil property, what is their behavior? We should know before we start the foundation. So, to know that soil properties, we have to go for soil exploration for the laboratory as well as field testing to know the soil properties and then the geological condition of the soil that is also required.

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Next part is if you start the geotechnical properties of the soil, so before we go for the foundation aspect part, so in the introduction lecture basically I will discuss about some geotechnical properties and soil properties also that will be required for our design purpose. So, those are the very important properties. Those things I will discuss in the introductory lecture, and for the next lecture, lecture two I will start about the different components of this course of the foundation advanced foundation engineering.

So, before we go for that part we should know the geotechnical properties of the soil. So, first important property is the grain size distribution. So, grain size distribution is determined generally by the sieve analysis for the coarse-grained soil and for the hydrometer analysis for the fine-grained soil. So, this is a typical grain-size distribution curve, and so here the x axis is the particle size and y axis is the percent finer. So, fifty percent finer means the fifty percent particle is fifty percent of this particle size, say, fifty percent finer means suppose say this is particle size is 0.8, so 0.8 millimeter particle is amount of the point less than 0.8 millimeter particle is 50 percent. So, that is the percent finer is y axis.

So, from this graph we can determine the two coefficient for coarse gained soil, one is uniformity coefficient C_u , another is coefficient of curvature C_c . So, C_u is basically D_{60} by D_{10} whereas D_{60} denotes that the particle size which corresponds to 60 percent particle percent finer, and similarly D_{10} is the particle size corresponding to 10 percent

finer. So, from this curve we can determine what is the particle size for 60 percent particle finer, and what is the particle size for 10 percent finer. So, if we know these two values from this graph then you will get the uniformity coefficient of the soil. Similarly, the coefficient of curvatures defined by the D_{30}^2 divided by $D_{60} \times D_{10}$ so from here you also get the two coefficient.

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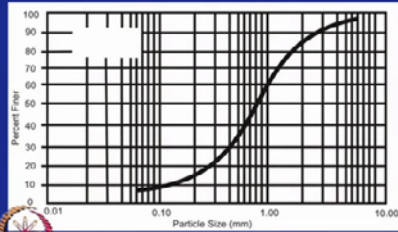


Now the purpose of this two coefficient, so from this two coefficients we can identify whether this soil is the well-graded soil or soil is the poorly-graded soil. So, well graded soil if C_u is greater than 6 for the sands and is greater than 4 for the gravels and C_c must lie between 1 to 3, then that type of soil is called a well-graded soil. And if it is not satisfying this condition then that soil is called poorly-graded soil, and third type of soil is gap graded soil. Now what is well-graded soil, what is poorly-graded soil, what is gap graded soil. Now well-graded soil that the soil where the different particle size is present in the soil in almost the equal amount, so that there is proper distribution of the soil.

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Geotechnical Properties of Soil


- **Grain-Size Distribution**
Generally determined by
 - ❖ Sieve analysis for coarse-grained soil
 - ❖ Hydrometer analysis for fine-grained soil



For coarse-grained soil

Uniformity coefficient (C_u)
 $C_u = D_{60}/D_{10}$

Coefficient of Curvature (C_c)
 $C_c = D_{30}^2/(D_{60} \times D_{10})$



That means here this is the proper distribution of the soil where the amount of the different sizes of particle are present in the soil, and they are more or less equal amount is present in the soil.

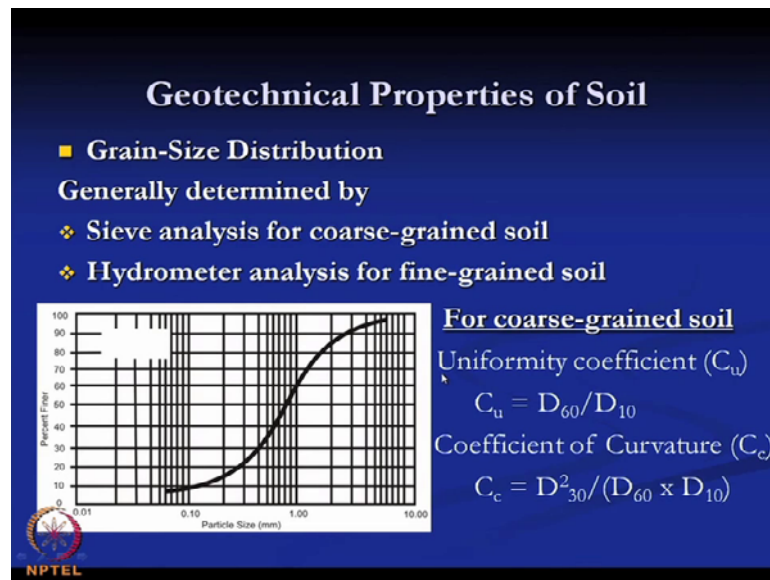
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- **Well-graded soil**
 $C_u > 6$ for sands
 > 4 for gravels
and C_c must lie between 1 and 3
- **Poorly-graded soil**
- **Gap graded soil**



Whereas for the poorly-graded soil for one particular range of the particular size of soil is excessively present in the soil.

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So, that means there will be this curve will not be a flat one; it will be a straight one if it is a poorly-graded soil because one particular range for a particular particle size is excessively present in the soil; that type of soil is called the poorly-graded soil.

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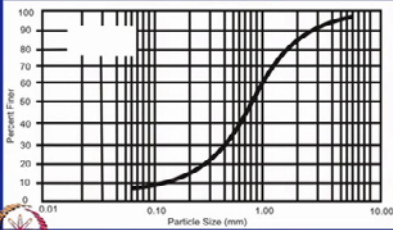


And in gap-graded soil means one particular range of the particles size is missing in the soil.

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Geotechnical Properties of Soil

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For coarse-grained soil

Uniformity coefficient (C_u)
 $C_u = D_{60}/D_{10}$

Coefficient of Curvature (C_c)
 $C_c = D_{30}^2/(D_{60} \times D_{10})$

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So, there the graph will be like this will start from here, then there is gap, then it will start from again. So, there will be particular range of the particle size missing in the soil.

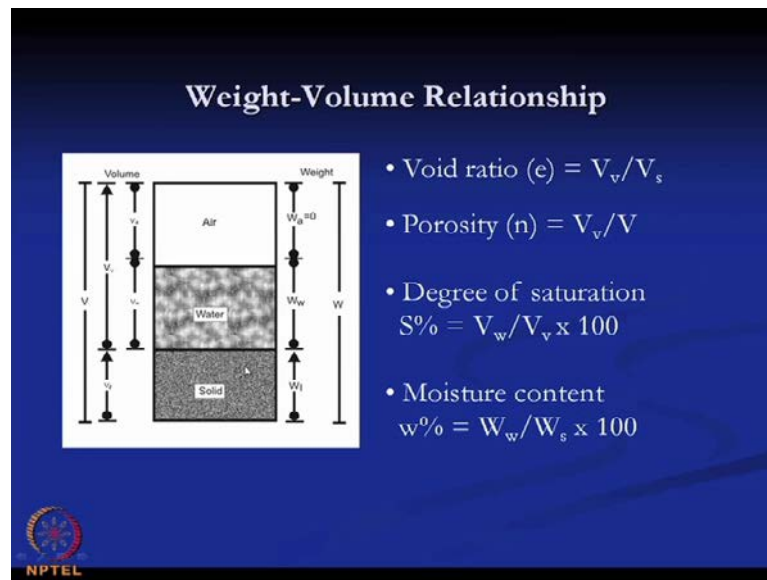
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- **Well-graded soil**
 $C_u > 6$ for sands
 > 4 for gravels
and C_c must lie between 1 and 3
- **Poorly-graded soil**
- **Gap graded soil**

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So, in that type of soil is called gap-graded soil.

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Now next one is the weight-volume relationship of the soil. So, as we know that soil is a three phase system that is air, water and solid. So, from these three phase system we can determine different soil properties and those properties are very important for the foundation design. So, if we consider the V_a is the volume of the air and V_w is the volume of the water and V_s is the volume of the solid. Now here this water and this air they are present in the voids in between the solids. So, that gives the volume of the water and volume of the air if we sum these two volume that will give us the volume of the voids. So, that is V_v will be V_w plus V_a and total volume is V .

Similarly, we can total weight of this soil is considered w , then W_s is the weight of the solid, then W_w is the weight of the water and W_a is weight of the air generally it is taken as zero. So, we can neglect the air weight in the soil during the calculation. So, from this graph we can say that if it is a totally saturated soil that means all the voids are filled with water then this system become a two phase system; that means the solid and the water only because that is the fully saturated soil, there will be no air. Now similarly if the soil is a dry soil completely dry soil then this total void will be filled by the air, so that means that will also become a two phase system, because all the voids will be filled by air, there will be no water. So, in that case we have to consider the weight and the volume accordingly.

Now then the different definition of this one is the void ratio e ; void ratio is defined by volume of void divided by volume of solid. Similarly, porosity is defined as volume of void divided by total volume. So, we can say here that the void ratio e is the volume of void divided by volume of solid. So, e value can be greater than 1, but porosity if you look at the definition of the porosity that is volume of void divided by total volume. So, the volume of void cannot be greater than the total volume, so the porosity cannot be greater than one. Now similarly, degree of saturation s which is expressed in percentage is defined as volume of water divided by volume of voids into 100 because it is expressed in percentage. Similarly, moisture content w in percentage is weight of water divided by weight of solid expressed in percentage.

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The unit weight of the soil at any water content or any degree of saturation can be written as:

$$\gamma = (G_s + Se) \gamma_w / (1+e)$$

where G_s is the specific gravity of the soil, γ_w is the unit weight of the water ($9.81 \text{ kN/m}^3 \approx 10 \text{ kN/m}^3$)

$$\gamma_{\text{dry}} = G_s \gamma_w / (1+e) \quad (\text{in case of dry soil } S = 0)$$

$$\gamma_{\text{dry}} = \gamma_{\text{bulk}} / (1+w)$$

$$\gamma_{\text{sat}} = (G_s + e) \gamma_w / (1+e) \quad (\text{in case of dry soil } S = 1)$$


Now the unit weight soil at any water content or any degree of saturation can be written as because what as I have mentioned that soil can be in the different stage; this can be in the completely dry stage, it can be in the completely saturated stage, or it can be in some normal stage, it is not it is partially saturated, this is not completely saturated. So, at different condition how we will determine the unit weight of the soil, then if we denote unit weight of the soil is γ then for γ_{bulk} or the unit weight at any condition is given by $G_s + Se$ divided by one plus e into γ_w . So, γ_w is the unit weight of water; it can be taken as equal to 10 kilo Newton per meter cube. G_s is the specific gravity of the soil and S is the degree of saturation, e is the void ratio.

Now if the soil is completely dry; that means the s is equal to zero, that means saturation is zero then degree of saturation then the equation of γ_{dry} will be G_s into γ_w by $1 + e$. So, that is because here s is equal to zero, so this equation becomes this one for the γ_{dry} . And then we can write that γ_{dry} is equal to γ_{bulk} divided by $1 + w$; w is the water content of the soil. Bulk density means bulk unit weight means the unit weight at any condition with any water content, so that is γ_{bulk} , γ_{bulk} is equal to this one. Similarly, γ_{sat} if I put for the γ_{sat} saturation if it the soil is completely saturated then S value will be equal to 1. So, if in that case S value is equal to 1 then this equation become this one if it is a completely saturated soil. So, for the saturated soil this equation become G_s plus $e \gamma_w$ divided by $1 + e$ because in that case S is equal to 1.


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Relative Density

In granular soils, the degree of compaction in the field can be measured by relative density ($D_r\%$)

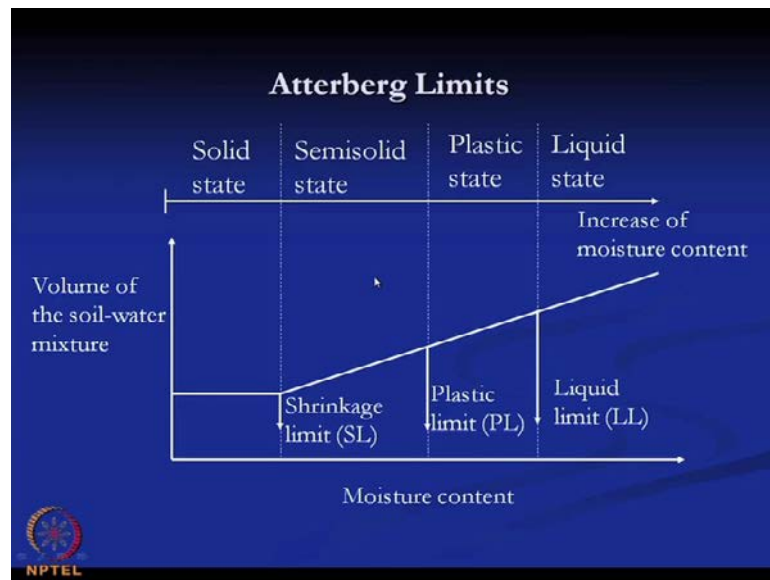
$$D_r(\%) = (e_{max} - e) \times 100 / (e_{max} - e_{min})$$

where e_{max} = void ratio of the soil in the loosest state
 e_{min} = void ratio in the densest state
 e = in situ void ratio



The next one is the relative density of the soil. In a granular soil the degree of compaction in the field can be measured by relative density r_d in percentage. So, relative density can be expressed is e_{max} minus $e_{natural}$ divided by e_{max} minus e_{min} into 100, because it is expressed in terms of percentage where e_{max} is the void ratio of the soil in the loosest state, and e_{min} is the void ratio in the densest state, and e is the in situ void ratio on the natural void ratio. So, if we know the e_{max} , e_{min} and e at any condition then we can determine what is the degree of relative density of the soil at that situation.

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Now next important properties are the Atterberg limits. So, first we will define what are the Atterberg limits?

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- **Well-graded soil**
 $C_u > 6$ for sands
 > 4 for gravels
and C_c must lie between 1 and 3
 - **Poorly-graded soil**
 - **Gap graded soil**
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So, previous the properties that we have discussed that are the well-graded soil, poorly-graded soil, gap graded soil, these properties are basically properties for the coarse grained soil that is for the sand, mille sand, and this is the common thing.


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Relative Density

In granular soils, the degree of compaction in the field can be measured by relative density ($D_r\%$)

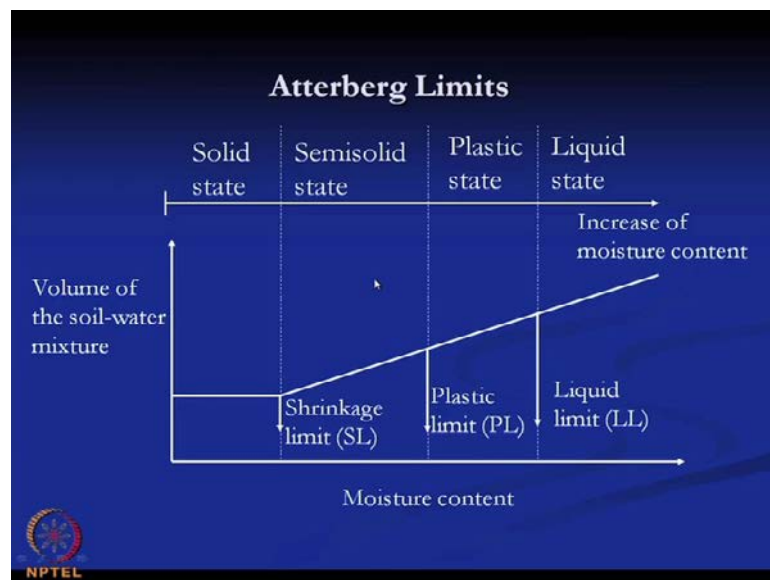
$$D_r(\%) = (e_{\max} - e) \times 100 / (e_{\max} - e_{\min})$$

where e_{\max} = void ratio of the soil in the loosest state
 e_{\min} = void ratio in the densest state
 e = in situ void ratio



And again relative density is also very important properties for the granular soil or the coarse grained soil.

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Similarly, the Atterberg limits these limits are very important properties for basically for the fine grain soil or the clayey soil. So, that means here we can say from this curve the soil has four different state; that is the solid state, semisolid state, plastic state and liquid state. Now we can say in this way that if we take a completely dry soil soil-soil that means that is soil solid soil in the solid state. Now if we add some percentage over some

amount of the water then the solid state becomes semisolid state. If we add more water then this semisolid state will become the plastic state; then in the plastic state if we add more water then it will go to a state which is called the liquid state.

Now here we can say that there is a limit or there is a junction between every state; that means there is four states and there is three junctions. And if I see that part that is the moisture content, so as the moisture content increases then soil go from solid state to semisolid, plastic and liquid and vice versa. From the liquid state if we reduce the water content in the soil then it will go to plastic state, and from the plastic state it will go to semisolid state, and from the semisolid state it will go to solid state. Now from this graph if I draw a graph with this moisture content, first is volume in the soil water mixture. So, you can see that if we decrease the soil water content amount, then from the liquid state it will go to plastic state, and then it will go to suddenly semisolid state, and as we reduce the water content the volume in the soil water mixture that will also reduce.

But after a certain point or the intersection between the semisolid state and the solid state or the junction of the semisolid state and the solid state, after that if we decrease the moisture content then the volume will not change, volume remain constant. So, that means after this point that if we further reduce the water content, but volume remains constant, volume will not change. Now let us go for what is this junction of this different state; that means the junction of plastic state and the liquid state is called the liquid limit. So these three are the limits, so these are liquid limits, plastic limit and the shrinkage limit; so, the liquid limit is the limit where soil changes its states from liquid to plastic or vice versa. Similarly, the next limit is between the plastic state to semisolid state and that limit is called the plastic limit and third limit is in between semisolid to the solid, and this limit is called the shrinkage limit.

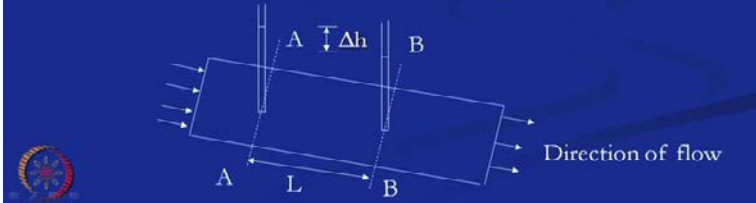
So, we can say if we reduce the water from a liquid state of a solid soil then it will pass the liquid limit it will go to the plastic state, and then if we further reduce it, it will pass the plastic limit and it will go to semisolid, state and if we further reduce the water content then it will pass the shrinkage limit and it will go to solid state. And from this graph we can say that after shrinkage limit the volume of the water soil mixture will not change or does not change if we further reduce the amount of water present in the soil water mixture. So, after the shrinkage limit there is no volume change. So, these three

limits are called the Atterberg limits, and these are very important properties for the fine grain soil.

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Hydraulic Conductivity of Soil

- Darcy (1856) proposed the following equation for calculating the velocity of flow of water through a soil
$$v = ki$$
where v = Darcy velocity (cm/sec)
 k = hydraulic conductivity of soil (cm/sec)
 i = hydraulic gradient ($i = \Delta h/L$)



So, next one is the hydraulic conductivity of the soil. So, what is hydraulic conductivity of the soil? Darcy proposed the following equation for calculating the velocity of flow of water through a soil, and that equation is v equal to k into i where v is the Darcy velocity that is written in centimeter per second, k is the hydraulic conductivity of the soil that is centimeter per second and i is the hydraulic gradient that is Δh by L . Now what is Δh by L ? If the water is flowing in this direction and if we take the two height of the water at two location then it will show some difference; otherwise, this flow will not occur. So, that means if this height difference is Δh and the length of this two point A and B is L then i hydraulic gradient can be defined as Δh divided by L .

So, from this expression we can calculate the velocity of a soil is hydraulic conductivity into hydraulic gradient. So, what is the hydraulic conductivity now? If we consider this i is equal to 1 then this v is becomes the Darcy velocity it is centimeter per second. So, that means k if i is equal to 1 k is equal to v . So, the hydraulic conductivity of the soil is the velocity of the Darcy's velocity at which under the unit gradient. So, that means the hydraulic conductivity of soil is a velocity or the Darcy velocity under unit hydraulic gradient, so that means i is equal to 1.

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In the laboratory hydraulic conductivity can be determined by

- Constant head method (more suitable for coarse-grained soil)
- Falling head method (suitable for soils such as fine sands and silts)

Type of soil	Hydraulic conductivity (cm/sec)
Medium to coarse gravel	$>10^{-1}$
Coarse to fine sand	10^{-1} to 10^{-3}
Fine sand, silty sand	10^{-3} to 10^{-5}
Silt, clayey silt, silty clay	10^{-5} to 10^{-6}
Clays	10^{-7} or less

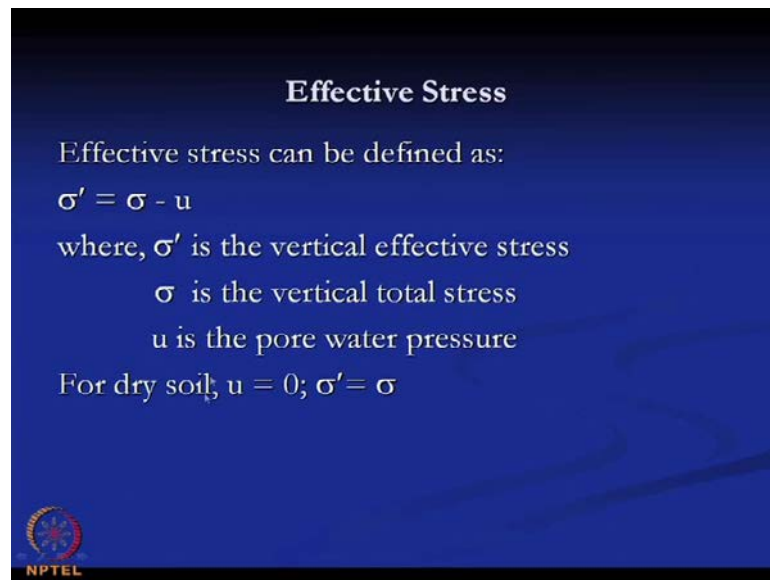
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Das, B. M., 1999

Now in the laboratory hydraulic conductivity can be determined; in the laboratory we can determine hydraulic conductivity by two methods. One is constant head method more suitable for coarse-grained soil and falling head method suitable for soil such as fine sand and silt. So, that means it is not suitable for the fine soil that is falling head method. Now in the field also we can determine the hydraulic conductivity of the soil; these two are the latest that we are discussing here.

Now the type of soil and the hydraulic conductivity in centimeter per second that medium to coarse gravel the hydraulic conductivity is greater than 10 to the power minus 1 ; for coarse to fine sand that is 10 to the power minus 1 to 10 to the power minus 3 , for fine sand silty sand that is 10 to the power minus 3 to 10 to the power minus 5 . For silt clayey silt and silty clay that value is 10 to the power minus 5 to 10 to the power minus 6 , and for the clays the value of k or hydraulic conductivity is 10 to the power minus 7 or less than that.

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Effective Stress

Effective stress can be defined as:

$$\sigma' = \sigma - u$$

where, σ' is the vertical effective stress
 σ is the vertical total stress
 u is the pore water pressure

For dry soil; $u = 0$; $\sigma' = \sigma$

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So, next concept or the next thing is the effective stress concept. Now what is effective stress? Now effective stress can be defined as the total stress minus the pore water pressure. Now where sigma dash is the vertical effective stress and sigma is the vertical total stress, u is the pore water pressure. So, that means when we apply weight or the load on a soil stress on a soil, initially that stress this stress is taken by the initial time is taken by the water. And now if we do not permit any flow of the water that means this stresses will be taken by the water initial stresses. Now if we permit the water to flow then gradually this water will flow, and the stress which was taken by the water initially will be transferred to the soil skeleton.

So, now as time progresses this water goes out then this stresses will be transferred to the soil skeleton. Now soil will take the stress in that fashion. So, that means when the soil is totally dry; that means there is more water. Now if we apply the stress on a soil water system then the stress will be taken by the water if we apply the stress on this condition; that means this water pore water pressure will be developed. Now if the soil is totally dry that mean no pore water pressure will be developed in that case u is zero, in that condition the effective stress will be equal to the total stress. So, that means if u is the dry condition u is zero that means the sigma dash is equal to sigma and that means dry means there is no water present in the soil.

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Diagram illustrating the calculation of effective stress in a soil medium. The soil is divided into two layers: an upper layer of height h_1 with unit weight γ , and a lower saturated layer of height h_2 with saturated unit weight γ_{sat} . The ground water level is indicated by a horizontal line with a downward-pointing triangle. A point A is marked in the saturated layer. The effective stress σ' is calculated as follows:

$$\begin{aligned}\sigma' &= \sigma - u = (h_1 \gamma + h_2 \gamma_{sat}) - h_2 \gamma_w \\ &= h_1 \gamma + h_2 (\gamma_{sat} - \gamma_w) \\ &= h_1 \gamma + h_2 \gamma'\end{aligned}$$

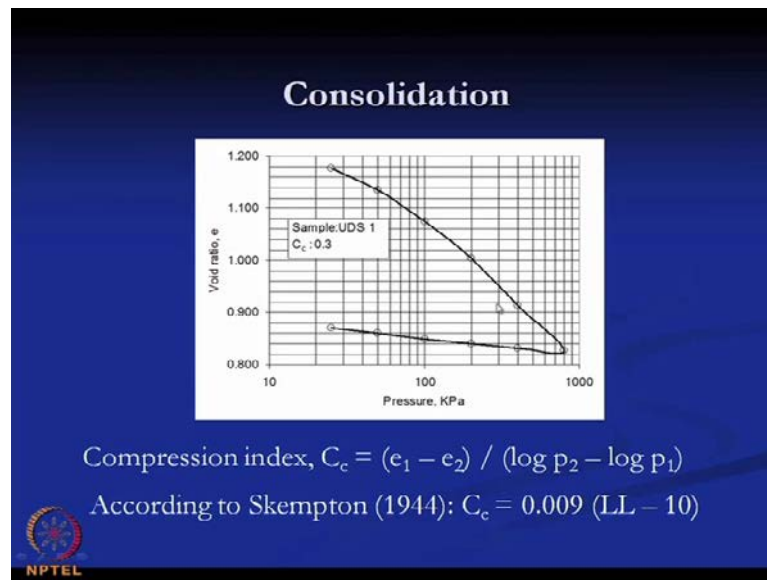
Where γ' is the submerged unit weight of the soil $= (\gamma_{sat} - \gamma_w)$

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Now how we will calculate the total stress or effective stress in a soil medium. Suppose this is the soil medium where the water table is at a depth of h_1 from the ground surface, and this is the unit weight of the soil above the ground water table is, say, γ and unit weight of the soil below the ground water table that is saturated because it is below the water table. So, saturated unit weight of the soil is γ_{sat} . Now the total stress at a point can be calculated as h_1 into γ plus h_2 into γ_{sat} , and pore water pressure at a depth at a point A and this A point is at a depth of H_2 from the water surface. So, at this point the pore water pressure can be determined as h_2 into γ_w where γ_w is a unit weight of the water.

Now here if we take this is γh_1 into γ plus h_2 , if we take h_2 common so this will be γ_{sat} minus γ_w . So, $h_1 \gamma$ plus $h_2 \gamma_{sat}$ minus $h_2 \gamma_w$; this $\gamma_{sat} - \gamma_w$ is called as submerged unit weight of the soil that is equal to γ_{sat} minus γ_w . So, when you calculate the effective stress at any point of below the water table then the effective stress will be equal to the height of the soil or depth of the soil into the unit weight of the soil above the water table plus the depth of that point from the ground water table into the submerged unit weight of the soil that is γ_{sat} minus γ_w . So, this way we can calculate the effective stress of the soil at any depth within the soil medium.

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The next thing that I will discuss about the consolidation, consolidation is also very important properties for the fine grained soil. Now as I have mentioned that soil voids are filled by either air or water or both. So, if we want to remove this voids, there are basically two methods by which we can remove this voids; one is compaction another is consolidation. So, the major difference between these two methods that by compaction we can remove the air voids but by consolidation we can remove the water voids; so there are other differences also there based on this two methods, but this is the major difference. So, here consolidation means we can remove the water voids or water present with in the soil pores.

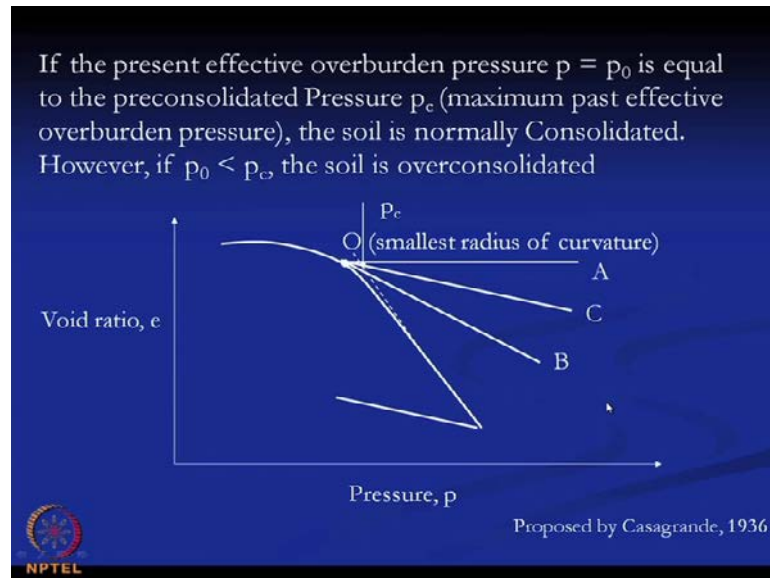
So, now this consolidation once we have done the consolidation, this consolidation can be done in the laboratory and there are some properties which are very important for our foundation design basically for the settlement because consolidation is very important properties for the fine grained soil or the clayey soil, because in the sand grained soil permeability of the soil is very high. So, once we apply the load all the soil or the water can dissipate within very short duration of the time. So, long term settlement all the settlement that we will get for the coarse grained soil is the immediate settlement. The long time settlement is very negligible in case of coarse grained soil, but for the fine grained soil likely where the permeability is very low.

So, once we apply the load there will be very negligible amount of the immediate settlement all that depending upon the type of clay, but the most of the settlement will come because of the consolidation because as time progresses the water will dissipate from the clayey soil slowly slowly, and then the settlement will occur. So, that is the time dependent phenomenon and it will take the long time to complete the total settlement. So, that is why consolidation and that settlement is called the consolidation settlement, and that consolidation settlement is very important properties for a fine grained soil during the foundation design.

So, in the consolidation after what we can do we can apply the load on a soil sample or apply the pressure on a soil sample, and we can determine what is the amount of void in the soil or we can determine the void ratio. So, it is expected as we apply the more pressure the void ratio will decrease. So, here a typical consolidation I mean void ratio versus $\log p$, p means the pressure graph is presented. Now this pressure is plotted in the logarithm scale and void ratio in the normal scale. So, this is $\log p$. So, here we can see as we apply the more pressure the void ratio decreases. This is the loading curve and this is the unloading curve, so once we remove the pressure so there will be some rebound of the soil voids. So, it will further go up.

Now here the slope we can determine the compression index that is the slope of this loading curve. So, this slope of loading curve so the compression index C_c is equal to $e_1 - e_2$ divided by $\log p_2 - \log p_1$. Now e_1 is the void ratio corresponding to pressure p_1 , and e_2 is the void ratio corresponding to pressure p_2 . So, this is basically C_c is the slope of this loading path. Now according to Skempton we can determine the C_c also that is $0.009(LL - 10)$; in this way also we can determine what is the value of C_c .

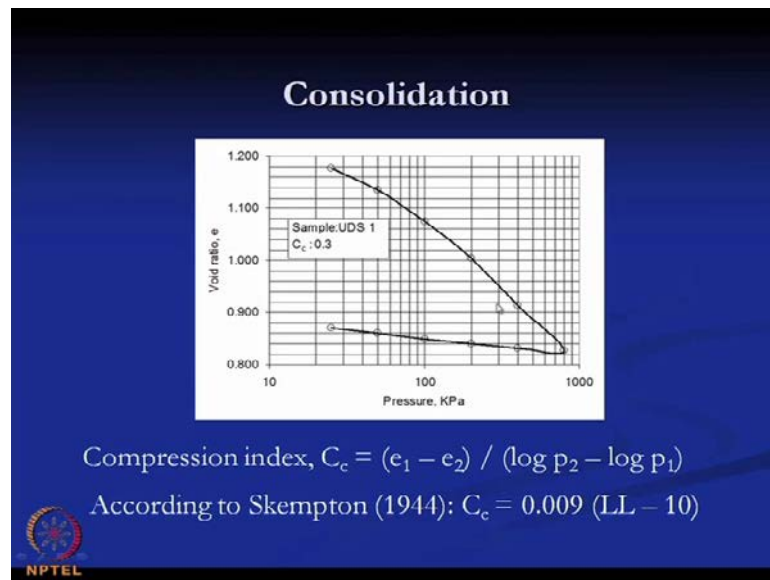
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Now there is another very important thing that the over consolidated soil. Now what is over consolidated soil? Now if the natural pressure or the current pressure which is applied on the soil is less than the pressure which is previously subjected to the soil or the soil has experienced the more pressure which is currently applied on the soil then that soil is called the over consolidated soil. Now for example that if the landslide is there now previously that soil before landslide is suffering more stresses or more pressure. Now after the landslide some soil on that point is removed and it will wash away, so that means the stresses now currently on that location is less than the stress which is previously subjected to on that point. So, in that case that soil is called as the over consolidated soil.

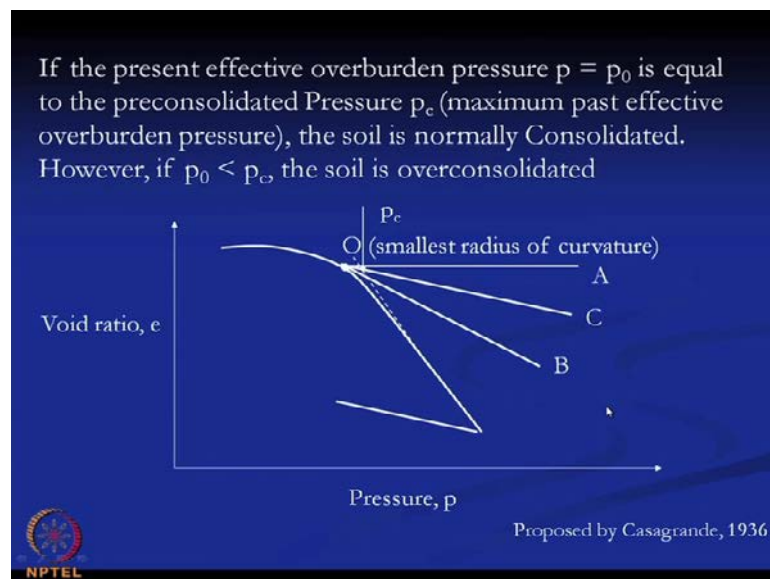
So, form this over consolidated soil how will you calculate the over consolidated ratio that is over consolidated ratio or the over consolidated stress. So, that over consolidated stress how we calculate that is proposed by the Casagrande in 1936. Now form this e void ratio versus log p graph e versus log p graph also we can determine this over consolidated pressure p_c . Now this is the typical loading path and this is unloading plot.

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Similar to this graph is loading and unloading path.

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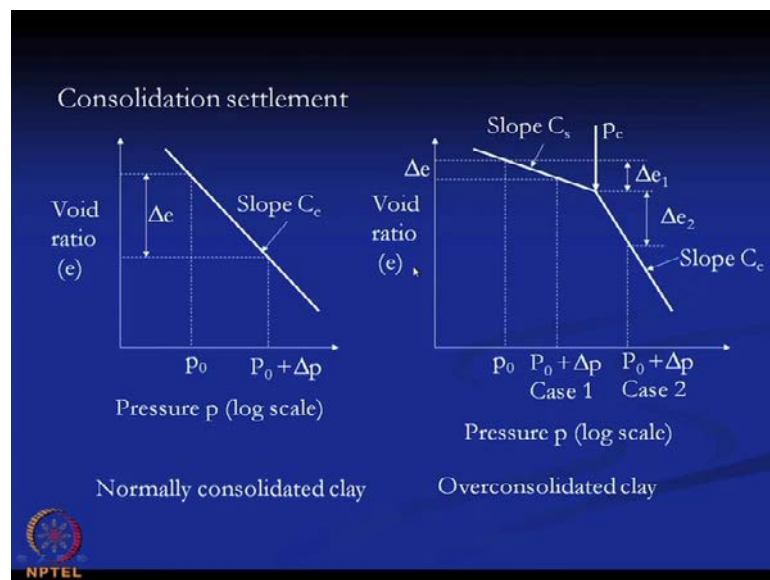


Now from this loading path you have to identify a point to which as the smallest radius of curvature. Now from here, here we can get the different curvature and we will get a point O here which has the smallest radius of curvature. Now once you select the point O then we can draw a line OA which is parallel to x axis. Now from first select the point to which has the smallest radius of curvature. Now from point O draw a line OA which is parallel to pressure p x axis.

Now from this point A draw a line OB such that this OB is a tangent at O. So, draw a line OB such that OB is a tangent at O; then draw another line OC such that it bisects this angle AOB, and once we get the OC line the next step is to extend this straight portion of the loading curve. Now extend this state portion of the loading curve, and identify the point where the straight portion of the loading curve and this bisection curve intersects. Now identify that point and pressure corresponding to that point is called the over consolidated pressure or maximum past effective overburden pressure.

So, that the present if the present, so this way we can determine the P_c which is maximum past effective overburden pressure; now if present effective overburden pressure p_0 is equal to preconsolidated pressure P_c then the soil is called normally consolidated soil; that means the present effective overburden pressure is equal to this preconsolidated maximum past effective overburden pressure p_c , then that soil is called normally consolidated soil. Now if this p_0 that means the present effective overburden pressure is less than the P_c or the past effective overburden pressure as I have mentioned then that soil is called over consolidated soil. So, this way from this log e versus log p curve also we can determine the p_c value.

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Now how we will calculate the consolidation settlement of a soil, because as I have mention that the foundation design this settlement calculation is very important issue for the clayey soil. Now here how we will calculate the settlement for the consolidation

settlement? So, there is two type of soil we have considered; one is normally consolidated clay, another is over consolidated clay. So, now in the normally consolidated clay this is the typical loading path that we will consider that is the straight portion we can consider for the normally consolidated clay. And here that slope of this curve will give us the C_c as I have mentioned the slope of this curve the compression index, so that means this is the difference between stress is Δp and p_0 plus Δp that is the difference between stress, and because of this stress difference this is the difference between the void ratio Δe , and as expected as we increase the pressure I the void ratio will decrease.

So, similarly then similar curve we can draw for the over consolidated clay, for the over consolidated clay so this is the typical curve $\log e$ versus $\log p$ curve. And here this is the point where we got the p_c value, and then we will locate this point, how we will get this P_c value we have already explained, and then there is two parts. One is this one whose slope will give us the C_c composition index and another is this part this above this P_c value portion that is the C_s , and here also P_0 plus Δp there will be the Δe and here also p_0 plus Δp that portion there also we will get that. So, that means here we will get the Δp Δe_1 and Δe_2 . So, there basically we have two different portions.


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Normally consolidated clay
Settlement $S = \frac{C_c}{(1+e_0)} H \log \left(\frac{p_0 + \Delta p}{p_0} \right)$

Over-consolidated clay
Case 1: $p_0 + \Delta p < p_c$
Settlement $S = \frac{C_s}{(1+e_0)} H \log \left(\frac{p_0 + \Delta p}{p_0} \right)$

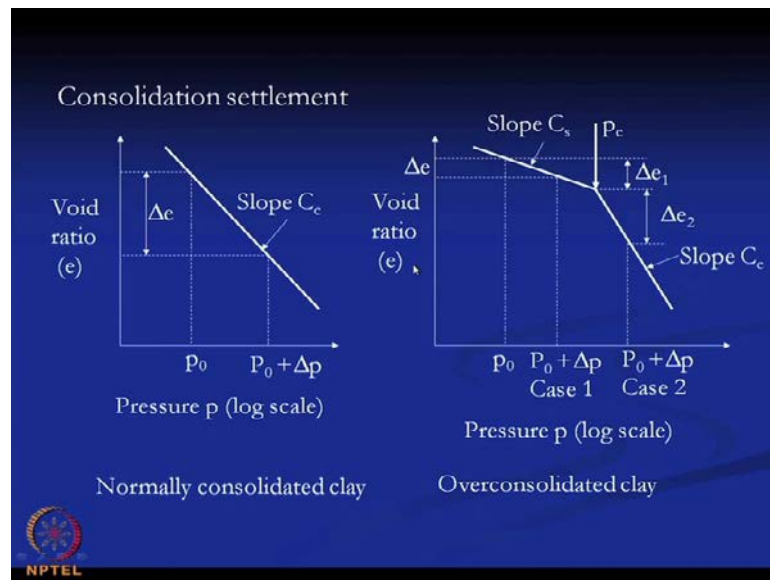
Case 2: $p_0 < p_c < p_0 + \Delta p$
Settlement $S = \frac{C_s}{(1+e_0)} H \log \left(\frac{p_c}{p_0} \right) + \frac{C_c}{(1+e_0)} H \log \left(\frac{p_0 + \Delta p}{p_c} \right)$

where C_s is swelling index



Now for the normally consolidated clay how we will calculate that for the settlement S is C_c $1 + e_0$ into $H \log p_0$ plus Δp divided by p_0 .

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So, this is the settlement calculation for typical this portion.

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Normally consolidated clay

$$\text{Settlement } S = (C_c / (1 + e_0)) H \log ((p_0 + \Delta p) / p_0)$$

Over-consolidated clay

Case 1: $p_0 + \Delta p < p_c$

$$\text{Settlement } S = (C_s / (1 + e_0)) H \log ((p_0 + \Delta p) / p_0)$$

Case 2: $p_0 < p_c < p_0 + \Delta p$

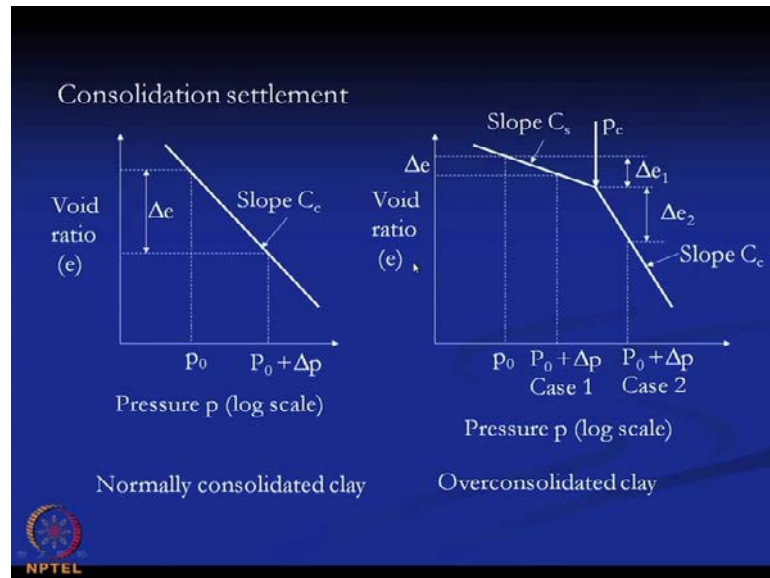
$$\text{Settlement } S = (C_s / (1 + e_0)) H \log (p_c / p_0) + (C_c / (1 + e_0)) H \log ((p_0 + \Delta p) / p_c)$$

where C_s is swelling index

Now where C_c is the compression index, e_0 is the initial void ratio, H is the thickness of the soil layer for which we are determining the settlement, and p_0 is the initial applied stress and Δp is the stress or additional stress; that means for example, the p_0 is equal to effective overburden pressure, and Δp is the additional stress due to the applied external load on the foundation. So, later on when you talk about the foundation settlement calculation, you will show how this p_0 and Δp can be calculated. So, that

part will be shown later on during the settlement calculation of the foundation. Now similarly for the over consolidated case for the case one if $p_0 + \Delta p$ is less than p_c .

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That means if $p_0 + \Delta p$ is less than p_c in this condition in that case.

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Normally consolidated clay

$$\text{Settlement } S = \frac{C_c}{1+e_0} H \log \left(\frac{p_0 + \Delta p}{p_0} \right)$$

Over-consolidated clay

Case 1: $p_0 + \Delta p < p_c$

$$\text{Settlement } S = \frac{C_s}{1+e_0} H \log \left(\frac{p_0 + \Delta p}{p_0} \right)$$

Case 2: $p_0 < p_c < p_0 + \Delta p$

$$\text{Settlement } S = \frac{C_s}{1+e_0} H \log \left(\frac{p_c}{p_0} \right) + \frac{C_c}{1+e_0} H \log \left(\frac{p_0 + \Delta p}{p_c} \right)$$

where C_s is swelling index

The settlement is calculated as C_s divided by $1 + e_0$ $h \log p_0 + \Delta p$ divided by p_0 ; that means in that case instead of using C_c we will use the C_s where C_s is the swelling index, and in the case two if the point is in this condition that means here p_0 is

less than p_c , p_0 plus Δp is greater than p_c . In that condition settlement we can calculate the c_s plus 1 plus e_0 into $h \log p_c$ divided by p_0 plus C_c divided by 1 plus e_0 into $h \log p_0$ plus Δp divided by p_c . So, in these two conditions how we can determine the consolidation settlement? So, one is normally consolidated soil, this is the expression. If it is over consolidated soil if case one this is the expression; if it is case two this is the expression.

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Shear Strength

The shear strength, τ_f , of a soil, in terms of total stress is

$$\tau_f = c + \sigma \tan \phi$$

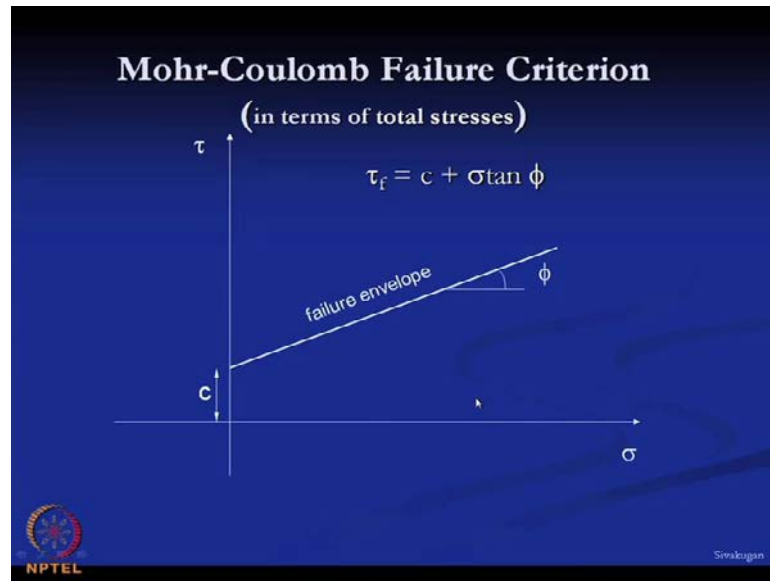
where σ = total normal stress on plane of shearing
 c = cohesion or apparent cohesion
 ϕ = angle of friction

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The next one is very important is the shear strength of the soil. Now shear strength is generally determined by this expression, the strength is cohesion plus σ_n into $\tan \phi$ or σ_n . This is in terms of total stress, so the c plus σ total normal stress on the plane of shearing. So, σ is the total normal stress into $\tan \phi$. So, ϕ is the friction angle, c is the cohesion of the soil.

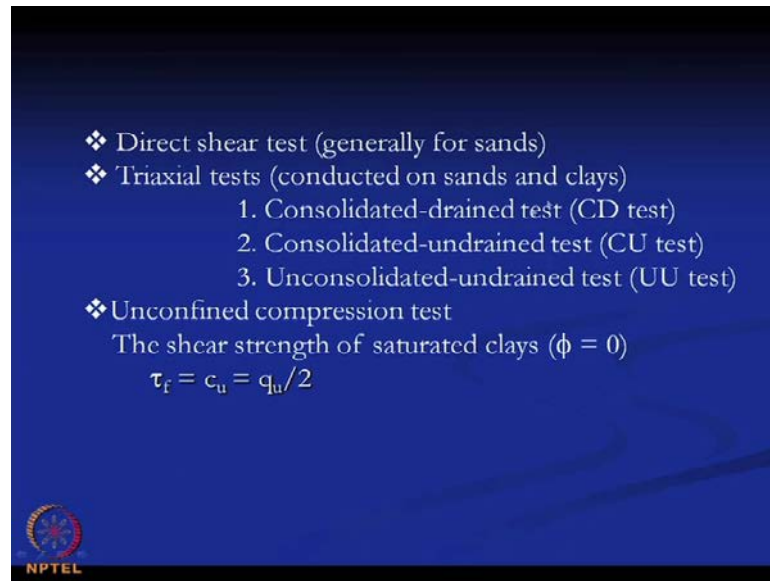
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Now these things we can draw which is the Mohr-Coulomb failure criteria or Mohr-Coulomb failure envelope is there. So, this is the envelope, and this is the sigma axis normal stress axis and this is the shear stress axis. Now if any Mohr-Coulomb touches a Mohr circle touches this envelope; that means that failure will occur and anything so that means here this expression shear strength expression is c plus σ into $\tan \phi$, ϕ we can determine by $\tan \phi$ is the slope of this angle. So, if we know the slope of this angle we can determine the slope of this line; if we know the slope of this line you can determine the angle ϕ here also.

So, τ_f is the maximum shear stress in soil that can take without any failure under normal stress σ . Now this is the same expression we can write in terms of effective stress. So, in terms of effective stress this will be c' effective coefficient then the σ' or τ_f' . So, σ' will be $\sigma - u$, u is the pore water pressure and similar envelope you can determine but only this in terms of effective stress. So, τ_f is the maximum shear stress the soil can take without failure under normal effective stress of σ' .


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- ❖ Direct shear test (generally for sands)
- ❖ Triaxial tests (conducted on sands and clays)
 1. Consolidated-drained test (CD test)
 2. Consolidated-undrained test (CU test)
 3. Unconsolidated-undrained test (UU test)
- ❖ Unconfined compression test

The shear strength of saturated clays ($\phi = 0$)

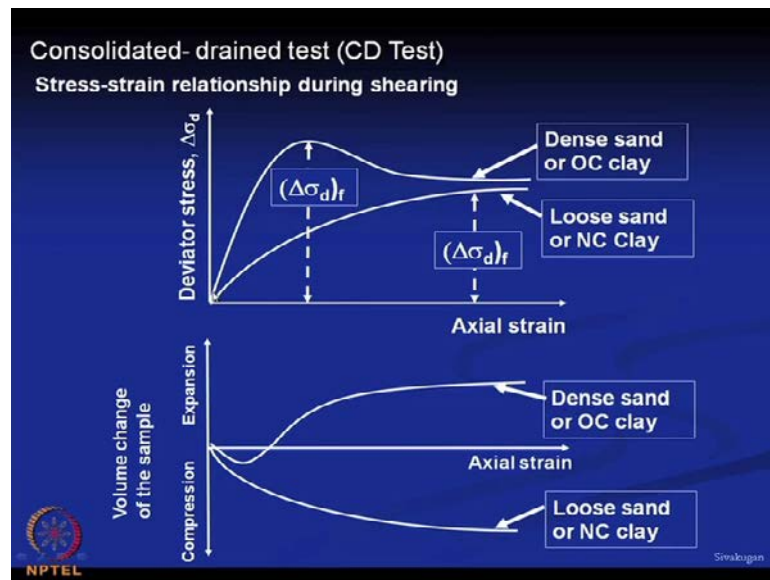
$$\tau_f = c_u = q_u/2$$

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Now these properties, so that means here we can see the c and ϕ these are the strength properties of the soil. So, those are very important things for the and this c and ϕ these two parameters very important for the foundation design for the foundation bearing capacity design; that means how much amount of load foundation can carry this, we can determine this based on these two parameters. So, these two parameters we have to determine; in the laboratory we can determine these two parameters in different by this different test. One is direct shear test generally for the sand then triaxial test conducted on sands and clay both, and these are three types of test depending upon the drainage condition, depending that is the consolidated-drained test CD, consolidated-undrained test, unconsolidated-undrained test UU.

So, depending upon whether it is a consolidated or unconsolidated drained or undrained these are three types of triaxial test. Another test which is conducted is unconfined compression strength. This is suitable for the soil whose saturated clay; that means ϕ value is equal to zero; that means the shear strength of the saturated clay can be calculated for this type of test τ_f equal to c_u . c_u is the undrained coefficient of the soil and here if the unconfined compression strength is q_u then if you divide it by 2; that means there you will get the c_u . So, half of the q_u will give you the c_u . So, that is the unconfined compressive stress divided by 2 that will give us the c_u for unconfined compressive strength test.

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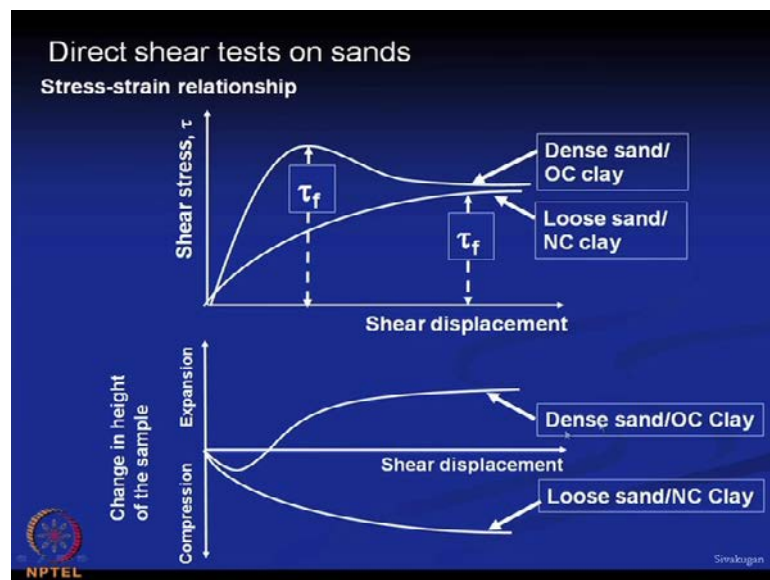


Now so these are the typical sand or the clay consolidated-drained test CD stress-strain relationship during shearing. So, in the triaxial test if I take this x is the axial strain axis and this is the deviator stress then this curve will give us for this curve is for the loose sand or normally consolidated clay and this curve is for the dense sand or over consolidated clay. Now from these two curves we can see that for the loose sand or normally consolidated clay we will not get any prominent failure peak in the curve, but in the dense sand or over consolidated clay will get a permanent peak in the stress-strain curve. But ultimately we will get this two values will approach a same condition a same level, and this thing after this stress that is called the residual stress. And now so similarly if I get the axial strain and the volume change curve then for the loose sand or normally consolidated clay volume will decrease and it will decrease always as we apply the load; as we apply the load volume will decrease.

But for the dense sand or over consolidated clay as we apply the load initially the volume will decrease but after that the volume will increase. So, here after certain point the volume will increase or this is due to the reason that for the loose sand as we apply the load the voids in between the soil grains that will reduce, and it will reduce continuously, but in case of dense sand because this void is already in a packed condition the void in the soil grains between the soil grains already is in very less amount it is in the packed condition. So, if we further apply the stress there this volume will slightly reduce again. It will be come a very dense condition but again if we apply the load then these dense

conditions will become a loose condition; that means the loose means the void in between the soil particles that will increase. So, once it becomes very dense then after that if we apply the stress it is become again the force volume will increase. So, that is why this volume will change for the dense sand.

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Some Corrections

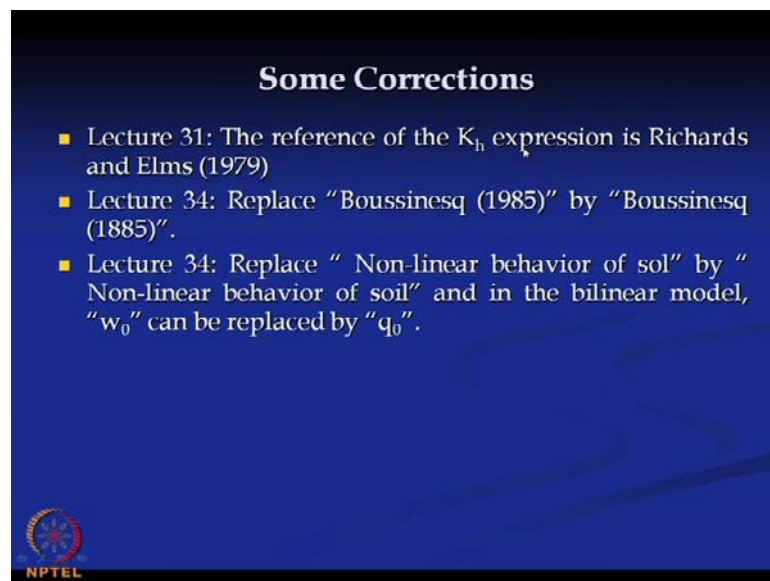
- Lecture 3: at 57.16 minutes, it is recorded as soil rather it should be in-situ tests. Replace Baguelin et al., (197) by Baguelin et al., (1978).
- Lecture 4: at 19:20 minutes, replace "refacted ray" by "refracted ray".
- Lecture 9: at 52.40 minutes, it is foundation on layered soil instead of raft foundation.
- Lecture 15: Unit of unit weight is kN/m^3 not kN/m^2
- Lecture 29: it tells to discuss about the braced cut, but not discussed there. At 2 minutes, it is reinforced foundation instead of RCC foundation as said.
- Lecture 30: Modulus of subgrade reaction is stress per unit deflection not stress per unit area.

For similar curve we will get for the direct shear stress also this is for the dense sand and this is for the loose sand. Hence we will have volume versus shear strength. So, this is

the shear displacement and shear stress and previous curve was axial stress and deviator stress axial strain and deviator stress but the similar nature of the curve we will get.

Now so this in the successive lectures you will get some corrections required so that in the different lectures. So, this is the additional slide that is put here. So, in the lecture 3 in this time 57.16 minutes it is recorded the soil as soil rather that it should be in-situ test replaced this reference by this difference. So, in lecture 4 at this 19.20 minute replace refracted by refracted rays, lecture nine 52.40 minute it is foundation on layered soil instead of raft foundation. In lecture 15 unit of unit weight is kilo Newton per meter cube not kilo Newton per meter square, lecture 29 it tells to discuss about the braced cut but not discussed there; at two minute it is reinforced found instead of RCC foundation as said. In lecture 30 modulus of subgrade reaction is stress per unit deflection and not stress per unit per area.

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In lecture 31 the reference of K_h expression is Richards and Elms 1979, lecture 34 Replace 'Boussinesq 1985 by Boussinesq 1885', in the spelling yes you have to change there. And in lecture 34 Replace 'Non-linear behavior of soil by non-linear behavior of soil, and in the bilinear model 'w 0' can be replaced by 'q 0'. So, these are the few corrections in the different lectures that we will follow in the coming series of lectures. So, this is the introductory lecture that I have taken. So, from the next lecture onward I will start the different models; that means first I will start about the module one, that

means the soil exploration, then we will start module two, three, four and five. So, in the next class I will start about the soil exploration.

Thank you.