

Foundation Design
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Lecture - 8B
Settlement Analysis- Part 2

Last class, I have started settlement analysis example before application of building load. Actually total settlement is settlement due to heave it may be negative if I am considering settlement of immediate as well as consolidation settlement downward is positive. So, total settlement is settlement due to heaves immediate settlement and consolidation settlement considering heave settlement is very small it has been neglected.

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$s_f = s_i + s_c$

Immediate Settlement

(A) clay $s_i = \frac{q_n B}{E} (1-\nu^2) I_p$

I_p = Influence factor at center/at edge

m/L/B	I_p	
	center	corner
1.0	1.12	
1.5	1.36	
2.0	1.52	
↓		
10.0	2.53	

$\frac{1}{2}$ value at center

Depth correction factor
 $= \frac{\text{Settlement of Foundation at } D}{\text{Settlement of corresponding surface foundation}}$

Diagrams: A rectangular foundation and a triangular foundation.

So, it is immediate as well as consolidation settlement then immediate settlement for cases of clay.

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B Sand (Buisman, 1948)

$$s_{\text{sand}} = \sum \frac{2.3 P_0}{E} \log_{10} \frac{P_0 + \Delta P}{P_0} dz$$

P_0 = Initial effective overburden pressure before loading

ΔP = Increase in vertical stress at the center of layer due to Foundation Loading

E = Modulus of elasticity

$$E = C_1 + C_2 N \text{ (kg/cm}^2\text{)}$$

Soil type	$C_1 \text{ (kg/cm}^2\text{)}$	$C_2 \text{ (kg/cm}^2\text{)}$
1) Fine Sand above W.T	52	3.3
2) Fine Sand below W.T	71	4.9
3) Sand Medium	39	4.5
4) coarse Sand	38	10.5
5) Sand + Gravel	43	11.8
6) Silty Sand	24	5.3
7) Silt	12	5.8

And for sand we have considered 2 theories Buisman 1948. Then another one is your Schmertmann and Hartman 1978.

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Schmertmann and Hartman (1978)

$$s_i = C_1 C_2 (\bar{q} - q) \sum_0^{\bar{z}} \frac{I_z}{E_s} dz$$

I_z = Strain Influence factor

C_1 = correction factor (Depth)

$$C_1 = 1 - 0.5 \left[\frac{q}{q_c} - 1 \right]$$

C_2 = correction factor for creep

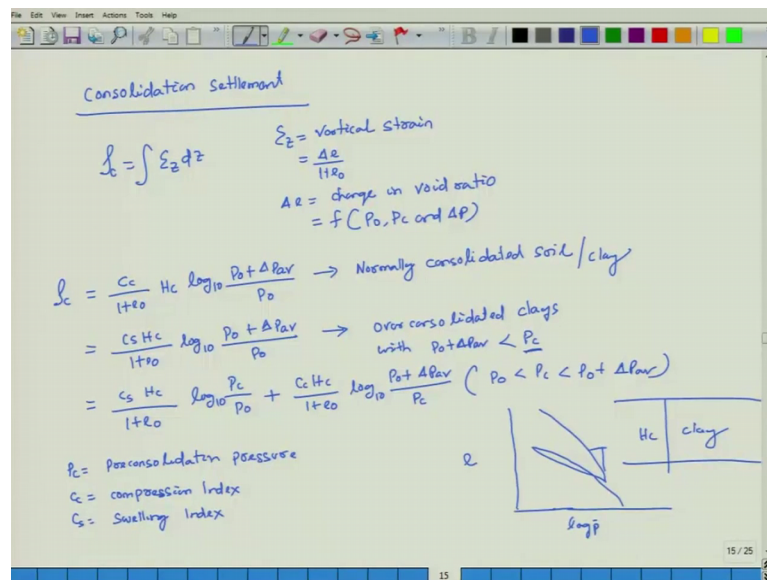
$$C_2 = 1 + 0.2 \log \left(\frac{t \text{ (years)}}{0.1} \right)$$

$\bar{q}$ = stress at the level of Foundation

$q = \gamma D_f$

So, these we have covered. Now come to consolidation settlement consolidation settlement. Consolidation settlement if I write it rho c is equal to epsilon z into d z integration.

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Epsilon z is equal to your vertical strength, which is equal to delta e by 1 plus e 0. And delta e is your change in void ratio, change in void ratio which is equal to a function of P 0 pc pre consolidation pressure and increase in stress due to external loading that is your delta p. So, consolidation settlements general it is Cc by 1 plus e 0, Hc log 10 P 0 plus delta P average divided by P 0. It is for normally consolidated soil. And which is equal to also Cs Hc by 1 plus e 0, log 10 P 0 plus delta P average divide by P 0. This is for over consolidated clays, with P 0 plus delta P average is less than pre consolidation pressure. Pre consolidations pressure how we will get it.

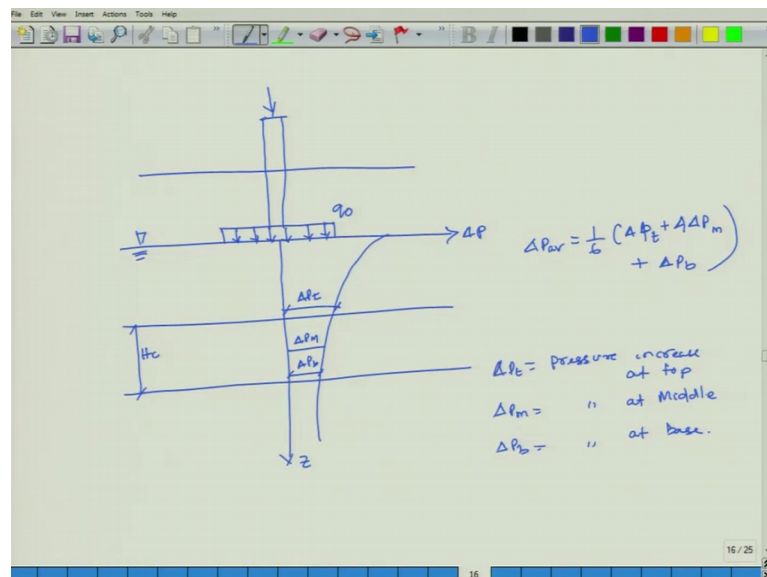
So, that part is has been covered in consolidation in soil mechanics also. Again it is Cs Hc by 1 plus e 0, log 10 pc by P 0 plus Cc Hc by 1 plus e 0 log 10, P 0 plus delta P average divided by pc. So; that means, in this case P 0 less than pc less than P 0 plus delta P average. So, pc is your pre consolidation pressure. Cc is equal to compression index and Cs is equal to swelling index.

Now, if you look at the consolidation theory e versus log p. So, for normally consolidated soil it is Cc by 1 plus e, 0 Cc is your slope of your origin curve right. So, swelling index coefficient of compression, this is a compression curve this is excavations swelling then this is recompression curve. So, s is your height of the layer height of this soil total height of the soil it is your Hc compress layer, if it is a clay log 10 P 0 plus delta P average by P 0 delta P average I will I will get back to you.

This is for your normally consolidated soil or clay normal consolidated soil or you can write it clay. Similarly, for this part from here to here, it is C_s sc by $1 + e_0 \log_{10} \frac{P_0 + \Delta p_{av}}{P_0}$. This is over consolidated clays particularly when $P_0 + \Delta p_{av}$ is less than P_c pre consolidation pressure, then if P_c is lying between P_0 over burden and $P_0 + \Delta P$ average. In that case it is C_s sc by $1 + e_0 \log_{10} \frac{P_c}{P_0}$ plus C_c by sc divided by $1 + e_0 \log_{10} \frac{P_0 + \Delta p_{av}}{P_0}$.

Let me draw layer here, this is your clay layer and there is some errors here it is your ground water table. Then footing is resting here.

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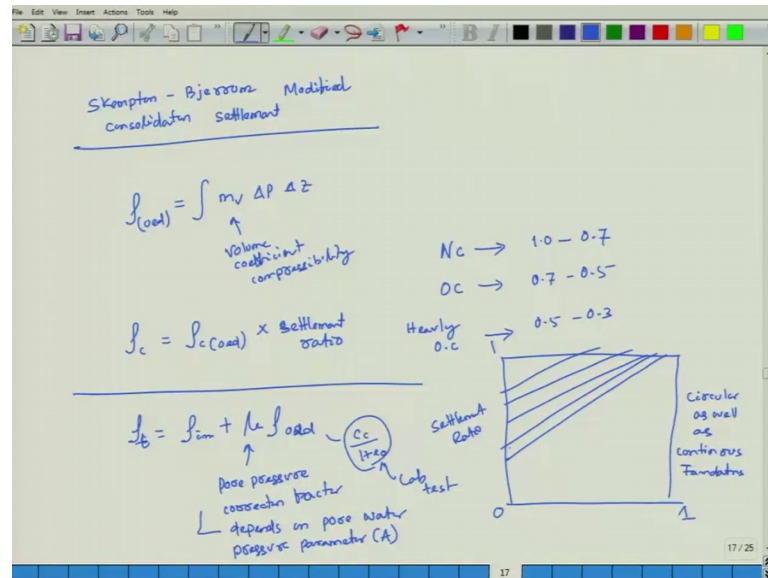


So, this will be q_0 , and this layer particularly this layer is your sc or clay soils. Here if I draw it here, load intensity and this is your ΔP , then this comes out to be here. This part is your ΔP L ΔP_m . This is you ΔP_b . And this is your depth Z . So, from how do get the average value generally average increase in increase of pressure may be approximated ΔP average is equal to one-sixth of ΔP L , ΔP top ΔP top, plus 4 ΔP middle, plus ΔP bottom. The increase in stress particularly in this soil layer it is not a constant with your depth. Rather it is decreasing at the bottom if I write it ΔP t is your pressure increase, pressure increase at top. And ΔP_m is your pressure increase at middle, then ΔP_b is your pressure increase at base.

So, ΔP average you can calculate considering increase particularly if this is your clay soil. This layer you want to find it out consolidation settlement, then find out in increase

in stress at the top of the layer, at the middle of the layer, at the bottom of the layer; that means, then you can find it out ΔP average is our $\frac{1}{6} \Delta P$ top plus $\frac{4}{6} \Delta P$ middle plus ΔP at the base.

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Next part is your Skempton, modified your coefficient (Refer Time: 10:34) means particularly consolidation settlement this is your skempton and Bjerrum modified consolidation settlement. So, it will be rho odometer. That means, consolidations settlement from your odometer test; that means, from your consolidation test suppose to be integration of $m_v \Delta P$ into Δz m_v is your m_v is your volume coefficient compressibility volume coefficient compressibility.

So, then you can find it out in the field taking into consolidation of in the consolidation settlement in the field, it will be consolidation settlement in odometer in to settlement ratio. So, you can get it this m_b from your consolidation test, I hope this as covered primarily in soil mechanics particularly in our consolidation part. So, he further said they further particularly based one their laboratory study they further said consolidation settlement is your immediate settlement plus your μ into rho odometer. Rho odometer test from consolidation test μ is called pore pressure correction factor, μ is your pore pressure correction factor pore pressure correction factor and it depends upon your pored pore pressure parameter A, depends on pore water pressure parameter A.

So, they have given graphical values also from there you can take it, generally for rough design per n_c normally consolidated clays the value of the correction factor is taken as 1.0 to 0.7 for over consolidated clay the μ value has been taken as 0.7 to 0.5. Then for heavily over consolidated clay over consolidated clay this value will be 0.5 to 0.3. They have given certain chart you can collect it in a book foundation design in a analysis by Bowles as I said. From there it is your settlement ratio, and this is varying from 0 to 1. Here also settlement ratio this is varying from 0 to 1. And they have given for this chart is there it is for circular foundation circular as well as for continuous foundations.

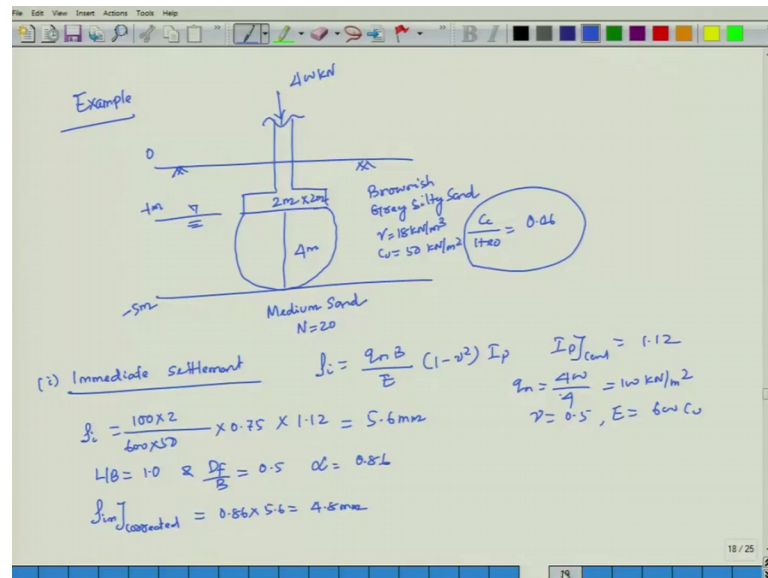
So, this is how it has been modified in the consolidation settlement if I put it in summary. The consolidation settlement ρ_c is your ϵ_z into d_z . And this is your vertical strength and it is Δe by $1 + e_0$; that means, change in void ratio Δe is your change in void ratio it is a function of over burden pressure, pre consolidation pressure and increase in your stress. And consolidation settlement has been given for normally consolidated soil over consolidated clay and over consolidated clay particularly $P_0 + \Delta p_{av}$ is less than p_c . If p_c is lying between P_0 to this $P_0 + \Delta p_v$, and these are all 3 sets of equations.

And from there this is your compression index C_c is your compression index C_s is your swelling index. C_c this compression index you can get it from your origin curve C_s you can get this slope of swelling and recompression index you can get it slope from here. You can write it C_s sorry C_c , C_s recompression or C_s some time z . This you can get it from your consolidation graph e versus $\log P$.

Then how to calculate ΔP average it is one-6th of increase in stress at top then 4 times increases in stress at middle, then increase in stress at the bottom then again it has been modified by Skempton considering your m_b , this is your volume coefficient compressibility you can get it directly from your consolidation odometer test and finally, they have suggested total settlement total settlement is your immediate settlement plus μ into odometer settlement considering consolidations means your pore water pressure correction factors. Whatever the value you are getting for these case C_c by $1 + e_0$ this is from your laboratory test.

So, from the odometer test you can find it out a settlement that is basically from your laboratory test and the pore water pressure corrections has been applied to simulate into true fact of your field for normally consolidated clay it is varying between 1 to 0.7 for over consolidated clay it is 0.7 to 0.5. Heavily over consolidated clay it is varying 0.5 to 0.3. Before I go to your stress part and other part settlement by these stress part methods.

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Let us solve one problem, and then only try for different methods one example. There is a case here; 0 meter here this is your ground surface. And there is a footing. Here it is your minus 1 meter water table is lying here. This is your minus 5 meter and beyond this it is a medium sand, n is equal to 20. And this width is your 2 meter. And this soil is brownish grey silty sand, silty sand γ is equal to 18 kilonewton per meter q . Ogden coefficient is your 50 kilonewton per meter square from laboratory test C_c by 1 plus e_0 this parameter getting 0.06. And find it out your settlement total load coming one to the footing is your 400 kilonewton. This is what is your example: there is a proposed side of 0 to 5 meter water table is located at 1 meter below your ground surface footing size is 2 meter.

So, then the load excepted load from the column is your 400 kilonewton. And it is a brownish grey silty sand γ is given 18 kilonewton per meter q ; Ogden coefficient 50 kilonewton per meter square. C_c by 1 plus e_0 from your consolidation test it comes out to be 0.06. Now calculate because this is a silty sand calculate immediately

settlement part one, immediate settlement. In these immediate settlement what is your formula, q_n into b by $e^{1-\mu^2}$ into i_p , i_p is given, i_p at the center i_p at the center it is your 1.12 then you calculate your values calculate your values.

So, this is your ρI is equal to q_n what is the value of q_n . So, q_n you can always find it out 400 by 4. It is a 2 meter by 2 meter, it is a square footing 400 by 4, it is hundred kilonewton per meter square. μ value is given 0.5, e you assume 600, c_u based on the c_u you can calculate e modulus of elasticity. And from there this is your 100 into 2 divided by 600 into c_u value is your 50 into 0.75 into 1.12.

So, this is coming about to be 5.6 mm. Then depth correction factor has to be calculated. So, this is your L by b is equal to 1.0 and d_f by b is equal to 0.5. So, depth correction factor α is equal to 0.86. So, immediate settlement corrected, it is your 0.86 into 5.6 which is your 4.8 mm.

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consolidation settlement

$$P_0 = 1 \times 18 + 8 \times 2 = 34 \text{ kN/m}^2$$

$$\Delta P = 0.34 \times 100 = 34 \text{ kN/m}^2$$

$$S = \frac{C_c}{1+e_0} \log_{10} \frac{P_0 + \Delta P}{P_0} = 72 \text{ mm}$$

$$K_c = 0.86 \text{ (pore water pressure correction)}$$

$$S_c = 0.86 \times 72 = 62 \text{ mm}$$

$$S = S_s + S_c = 48 \text{ mm} + 62 \text{ mm} = 110 \text{ mm}$$

Now, come to your consolidation settlement. So, calculate P_0 if you look at here P_0 water table is at 1 meter and below 1 meter, 1 to 5 meter how long your pressure ball you can calculate you can take it into 2 times b . So, it will be 2 into 2 times it will be here 4 meter exactly it is at here. So, then calculate P_0 . So, P_0 is equal to 1 into 18, 1 into 18 above of the water table bulk unit weight consider plus 8 into 2, where is your 8 into 2 submerged unit 8 minus 10. Gamma saturated assuming this is your gamma

saturated. So, $\gamma_{\text{saturated}} - \gamma_w$ or 9.81, it comes out to be 8 then here it is 18 plus 16, 34 kilonewton per meter square.

ΔP increase in stress because of your rectangular loaded because I have not covered that one stress increase in stress because of your external loaded that will be after your settlement. I just put it here for rectangular loaded ΔP is equal to 0.34 into 100. 100 is your load intensity hundred kilonewton per meter square it is your 400 kilonewton here it is 2 meter by 2 meter. This part I will discuss after your settlement then again I come back to this problem.

So, this comes out to be 34 kilonewton per meter square. So, Δ is equal to $C_c \cdot \frac{1}{1 + e_0} \cdot \log_{10} \frac{P_0 + \Delta P}{P_0}$, which comes out to be 72 mm. Then you are considering pore water pressure corrections μ is equal to 0.86 this is your pore water pressure correction, then it comes out to be ρ is equal to 0.86 into 72 which is your 62 mm. Now, immediate settlement is your 4.8 mm. So, total settlement is equal to immediate settlement plus consolidation settlement 4.8 mm plus 62 mm: so 66.8 mm. So, I will stop it here.

Next class I will go by means of stress path method to find it out your settlements.

Thank you.