

Geology and Soil Mechanics
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Lecture - 13
Soil Compaction- C

Welcome back. So, in the last lecture we just talked about the different procedures by which you can measure the unit weight in the field. So, what are those procedures, what are those methods?

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Soil Compaction

Determination of field unit weight of compaction

- **Procedures for determining the field unit weight**
 - Sand cone method
 - Rubber balloon method
 - Nuclear method

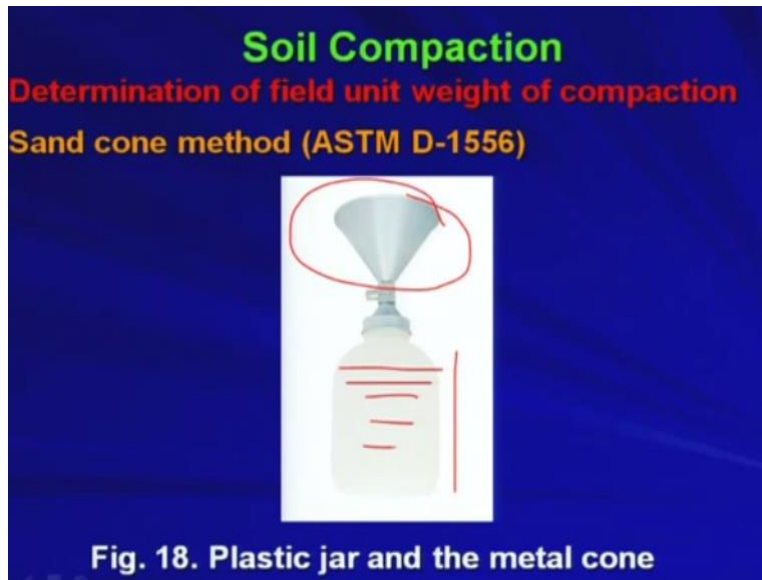
Sand cone method (ASTM D-1556)

- Sand cone device consists of a glass or plastic jar with a metal cone attached at its top
- Let, the combined weight of jar+cone+sand = W_1

First one was the sand cone method, then rubber balloon method, and nuclear method. So, among these 3 we will be talking about the sand cone method which is as per (ASTM D-1556). So, basically in the sand cone device consists of a glass or plastic jar with a metal cone attached at tips right. So, you will be having one jar which will be made of glass or plastic and on top of that you will be having some metal cone.

So, I will show you the figure how it will look like. So, now let the combined weight of jar plus cone plus sand. So, you will be filling some sand inside the jar. Now the combined weight of the jar, jar itself plus cone which will be attached at the top and the sand whatever you have put inside the jar, the combined weight is a W_1 , capital W_1 okay.

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The plastic jar or and the metal cone will look like this so this is the sand cone method device. So, as you can see so basically this is the jar which can be made of glass or say plastic and this is the metal cone okay which will be attached on top of the jar. Now you can put sand in inside the jar okay and then the combined weight of the jar plus cone plus the sand whatever you have filled inside the jar so that say that is W_1 whatever we have decided now and now in the field what exactly we are doing with this sand cone device.

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Soil Compaction
Determination of field unit weight of compaction
Sand cone method (ASTM D-1556)

- In the field a small hole is excavated
- Say, the weight of moist soil excavated from hole
 $= W_2$
- If the water content of excavated soil is known then the dry weight of soil is
 $W_3 = W_2 / [1 + w(\%) / 100]$
- After excavation, the cone with the sand filled jar is inverted and placed over the hole; sand is allowed to flow out to fill the hole and the cone

Now in the field where you have compacted the soil and where actually you need to find out the unit weight, so basically in the field you excavate a small hole okay that is I mean comparatively reasonably small hole you just excavate okay and say the weight of moist soil excavated from

hole is W_2 . So, whatever soil you have excavated from the hole, say the weight of that moist soil is W_2 because you have compacted so the soil will be moist.

So, now if the water content of excavated soil is known which is possible right so you are excavating the soil from the hole whatever you have excavated in the in the site and then you are collecting the soil and then you can find out the water content from the laboratory experiment. Then the dry weight of the soil is given by this expression where W_3 is equal to W_2 whatever is already explained.

So, as you can see here so the weight W_2 is the weight of the moist soil divided by the $1 + w$ where small w is the water content which you have determined from the laboratory experiment by 100. So, if you express the water content in percentage so it will be coming as w in percentage by 100. So, that will give me the dry weight of the soil, so that is W_3 .

Now after excavation, the cone with the sand filled jar is inverted and placed over the hole; sand is allowed to flow out to fill the hole and the cone. So, now what you do, so you have excavated the soil, you have taken out the soil, and you have done whatever experiments are required to find out the water content and other things. So, that you have done. So, in the I mean you take the jar which is filled with sand.

Now you invert the jar on top of the hole okay, excavated hole and then you allow the sand to fill in the hole itself. So, now the what will happen? The sand will come out from the jar. It will fill the cone as well as the hole. Now based on that you will be getting some jar some sand will be remaining in the jar itself and some sand will be remaining in the cone as well as the it will be filling the excavated hole.

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Soil Compaction

Determination of field unit weight of compaction

Sand cone method (ASTM D-1556)

- If the combined weight of jar+cone+remaining sand in the jar = W_4
- The weight of sand to fill the hole and the cone is

$$W_5 = W_1 - W_4$$
- The volume of excavated hole is

$$V = (W_5 - W_c) / \gamma_{d(\text{sand})}$$

Where, W_c = Weight of sand to fill the cone only

$\gamma_{d(\text{sand})}$ = Dry unit weight of sand

Now if the combined weight of jar plus cone plus remaining sand, now whatever sand has gone out from the jar, so whatever is remained okay. So, jar plus cone plus remaining sand in the jar if it is W_4 then the weight of sand to fill the hole and the cone is W_5 which is nothing but W_1 what was W_1 that is the combined weight of jar plus cone plus the total sand which was filled in the jar. Now the W_4 is nothing but the weight of jar plus cone plus the remaining sand. So, whatever sand has gone out from the jar and which has filled basically the hole as well as the cone that is nothing but W_5 which is equal to $W_1 - W_4$ as simple as that.

The volume of excavated hole is the V is given by W_5 , W_5 is the weight of sand which has filled the hole as well as the cone minus W_c by the $\gamma_{d(\text{sand})}$. But W_c is the weight of sand to fill the cone only because W_5 was the weight of sand which was filled in the cone as well as the hole. Now if you want to find out the weight of sand which is filled only in the hole then W_c must be deducted or must be subtracted from W_5 .

So, $W_5 - W_c$ will give you the sand which is filling the hole divided by $\gamma_{d(\text{sand})}$ if you talk about or if you that is nothing but your dry unit weight of sand if you divide the $W_5 - W_c$ by $\gamma_{d(\text{sand})}$ you will be getting the volume of excavated hole. So, whatever hole you have excavated, the volume of excavated hole can be obtained by this expression.

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Soil Compaction

Determination of field unit weight of compaction

Sand cone method (ASTM D-1556)

- The values of W_c and $\gamma_{d(\text{sand})}$ are determined in the lab
- The dry unit weight of compaction is given by,

$$\gamma_d = W_3/V$$

Then the values of W_c and $\gamma_{d(\text{sand})}$ are determined in the laboratory okay. So, there is no issue $\gamma_{d(\text{sand})}$ that is the dry unit weight of the sand. It can be obtained from the laboratory experiment and W_c also you can find out from the laboratory. Now the dry unit weight of compaction is given by γ_d which is equal to W_3/V okay.

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Problem-6

- A laboratory compaction test on soil having $G_s = 2.68$ gave a maximum dry density of 1.82 gm/cc and water content of 17%. Determine the degree of saturation, air content and percentage air voids at the maximum dry density. What would be theoretical maximum dry unit weight corresponding to zero air voids at the OMC?

Now we will take one example. Now we will be taking a few examples on compaction topic. So, this is the problem 6. The problem says a laboratory compaction test on soil having G_s equal to 2.68 gave a maximum dry density of 1.82 gm/cc and water content of 17%. Determine the degree of saturation, air content, and percentage air voids, so these all terms are known to you from the basic definition when we discussed in very earlier classes, at the maximum dry density.

What would be theoretical maximum dry unit weight corresponding to zero air voids at the OMC okay. So, these things we need to find out. So, we have few parameters and we are going to obtain those other things whatever has been asked in the problem. Okay let us start this problem.

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P.6
 We know, $\gamma_d = \frac{G_s \gamma_w}{1 + \frac{W G_s}{S}} \dots (1)$ $g = 10 \text{ m/s}^2$
 Here, $\gamma_{d, \max} = 1.82 \text{ gm/cc} = 18.2 \text{ kN/m}^3$
 $\times g$
 $\therefore \text{OMC} = 17\%, G_s = 2.68$

Okay, so we have seen the problem. Now we are going to solve this problem. So, problem 6. We know from our basic definition and we can establish these relations that is gamma d is equal to G s into gamma w, already we have seen this expression earlier for several times, W that is your water content G s by S that is degree of saturation right. This equation is or this expression is known to me or else you can establish this relation, there is no issue.

So, here what are the things are known to me, gamma d max which is equal to 1.82 gm/cc which is nothing but 18.2 kilo newton per meter cube, so this multiplied by g right. So, I am considering g as for this problem I am considering g 10 meter per s square okay. So, in some problems we can g basically is 9.8, so anyway so for some simplification we are considering g equal to 10. So, there is no issue.

So, gamma d max equal to 18.2 that is given in the problem and that is happening at the water content 17% so gamma d max will always occur at OMC right. So, the whatever water content is given so that is nothing but your OMC which is 17% and your specific gravity of soil solid is given as 2.68. So, these are the parameters are given in the problem.

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From eq. (1) we get

$$18.2 = \frac{(2.68)(10)}{1 + \frac{0.17 \times 2.68}{s}} \Rightarrow S = 0.96 = 96\%$$

Air content

$$a_c = \frac{V_a}{V_v} \Rightarrow a_c = 1 - S = 0.04 = 4\%$$

Now from equation 1 we get so from 18.2 is equal to 2.68 multiplied by 10 that is the unit weight of water divided by $1 + 0.17$ into 2.68 by s . From this I can get the degree of saturation is equal to 0.96 that means 96% okay. So, by knowing γ_d max so if you plot the compaction curve okay and then basically if you find out γ_d max and OMC you can observe from the compaction curve from this expression you can find out the degree of saturation okay.

Now therefore air content which is given by a_c if you recall we have covered these simple definitions which was given by V_a by V_v right where V_a was the volume of air and V_v was the volume of voids right. So, now a_c if you recall from the definition it is nothing but $1 - S$ that is 1 minus degree of saturation which is coming as 0.04 which is nothing but 4% okay. So, your air content is 4% okay. Now we will be talking about the percentage air void.

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Again it can be established that

$$\gamma_d = \frac{(1 - n_a) G_s \gamma_w}{1 + wG}$$

$$\Rightarrow (1 - n_a) = \frac{(18.2)(1 + 0.17 \times 2.68)}{(2.68)(10)} = 0.99$$

$$n_a = 1 - 0.99 = 0.01 = 1\%$$

Now again it can be established that your gamma d that is the dry unit weight of soil is equal to $1 - n_a$. What is n_a a percentage of air voids right into G_s into gamma w by $1 + wG$ right. So, this expression can be established from the simple definition whatever you have seen so far. So, gamma d is equal to $1 - n_a$ where n_a is the percentage of voids into G_s into gamma w divided by $1 + wG$ where w is the water content.

Now from this expression we can write $1 - n_a$ is equal to 18.2 multiplied by $1 + 0.17$ that is your water content multiplied by 2.68 by 2.68 into gamma w that is 10 which is giving me 0.99. So, therefore n_a is equal to $1 - 0.99$ which is equal to 0.01 which is equal to 1%. So, percentage air void is 1% okay. So, now basically when your percentage air void is say zero that means your degree of saturation is 1. So, at that time you will be considering that zero air void condition is occurring.

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When $n_a = 0$ i.e. $S = 1$
theoretical dry unit wt at $w = 17\%$ is given by

$$\gamma_d = \frac{G_s \gamma_w}{1 + w G_s} = 18.4 \text{ kN/m}^3$$

So, when n_a is 0 that is your S equal to 1 that means degree of saturation is 1 at that time your theoretical dry unit weight at water content 17% is given by that means at zero air void condition what is your γ_d that means dry unit weight. So, that we are going to find out. So, at zero air void condition your percentage air void is zero and that means your degree of saturation is 1 okay so is given by γ_d which is equal to $G \gamma_w / 1 + w$ into G_s .

From this we can find out γ_d is equal to 18.4 kilo newton per meter cube because we know all the values here. So, at the water content 17% that is your OMC your γ_d max that is the practical or the actually observed γ_d max in the laboratory was 18.2 whereas the theoretical maximum is 18.4 which you cannot achieve but this is the theoretical maximum which is happening at zero air void condition. So, now we will take the next problem, again on compaction. So, let us see the problem first.

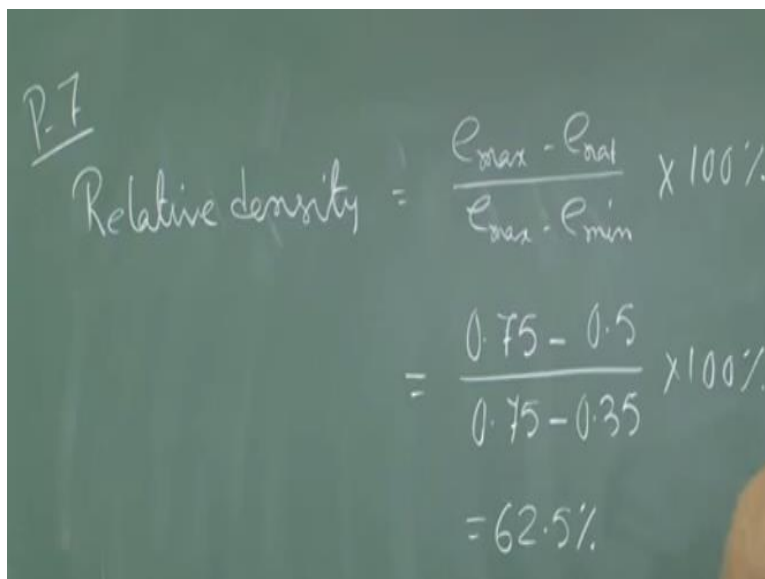
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Problem-7

- The in-situ void ratio of a granular soil deposit is 0.5. The maximum and minimum void ratios of the soil were determined to be 0.75 and 0.35. $G_s = 2.67$. Determine the relative density and relative compaction of the deposit.

Okay, so the next problem says the in-situ void ratio of a granular soil deposit is 0.5 okay. The maximum and minimum void ratios of the soil were determined to be 0.75 and 0.35. Now G_s is equal to 2.67. Determine the relative density and relative compaction of the deposit. So, basically, we are going to find out the relative density and as well as the relative compaction of this particular soil.

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P-7
Relative density = $\frac{e_{max} - e_{nat}}{e_{max} - e_{min}} \times 100\%$
 $= \frac{0.75 - 0.5}{0.75 - 0.35} \times 100\%$
 $= 62.5\%$

So, now basically your relative density, this is your problem 7. Your relative density from the definition you know $e_{max} - e_{natural}$ by $e_{max} - e_{mean}$ into 100%. So, that is your, that is the expression for your relative density and already we have established this relation and we have

seen and we have solved a couple of problems on that. So, what is your e_{max} in the problem? So, that is your maximum void ratio which is 0.75, it is given in the problem.

Now what is $e_{natural}$? What magnitude of $e_{natural}$ is given in the problem? Now in-situ void ratio that means the natural void ratio of the granular soil is 0.5, so that is given, divided by e_{max} is 0.75 again and what is $e_{minimum}$, that is your minimum void ratio which is given in the problem as 0.35. So, if you solve this calculation you will be getting your relative density is 62.5%.

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$$\gamma_{d(max)} = \frac{G_s \gamma_w}{1 + e_{min}} = \frac{(2.67)(10)}{1 + 0.35} = 19.78 \text{ kN/m}^3$$
$$\gamma_{d(min)} = \frac{G_s \gamma_w}{1 + e_{max}} = 15.26 \text{ kN/m}^3$$
$$\gamma_{d(in-situ)} = \frac{G_s \gamma_w}{1 + e_{in-situ}} = \frac{(2.67)(10)}{1 + 0.5} = 17.8 \text{ kN/m}^3$$

So, your γ_d max will be $G \gamma_w$ by so at what situation you will be getting maximum dry unit weight? So, could you please I mean could you please tell me that what should be the maximum unit weight at what void ratio when the soil will be densely packed. So, when the soil will be densely packed, at that time what should be the void ratio, $e_{minimum}$. So, γ_d max will occur at $e_{minimum}$, so from this expression, this expression is already known to me or else you can establish that relation, there is no issue.

So, in that relation, your e value that is the void ratio value should be minimum which will be giving me the γ_d max. So, if you put all the values 2.67 into 10 divided by $1 + 0.35$. So, that is giving me 19.78 kilo newton per meter cube. Similarly, if you can find out γ_d minimum that is the minimum dry unit weight. At what situation γ_d minimum will occur when your void ratio will be becoming maximum that means loosest packing will be giving you the γ_d minimum.

So, that is given by $1 + e_{\max}$. So, if you put the values you will be getting 15.26 kilo newton per meter cube. Now what is the value of γ_d in-situ that means in the field condition. That is $G_s \gamma_w$ by $1 + e_{\text{in-situ}}$ which is nothing but e_{natural} right. So, if you put all the values divided by $1 + 0.5$ which will give me 17.8 kilo newton per meter cube. So, you have got the relative density as well as you have got the different unit weight at different condition.

That means when your soil is densely packed at that time you have got γ_d max which is equal to 19.78 corresponding to e_{minimum} . Then you have got γ_d min that means when the soil is loosely packed or the loosest state that means your void ratio was e_{\max} and at that time you have got γ_d min equal to 15.26. Whereas at the in-situ condition, at the natural condition, your γ_d in-situ is coming as 17.8 okay. So, now with that we can calculate the relative compaction.

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P-7
Relative compaction = $\frac{\gamma_d(\text{in-situ})}{\gamma_d(\text{max})} \times 100\%$
 $= \frac{17.8}{19.78} \times 100\%$
 $= 89.9\%$

So, we can write down the relative compaction. What will be the expression for relative compaction? From the definition, itself we can see that whatever you have achieved and whatever was there, based on that you can calculate the relative compaction. So, that is nothing but γ_d in-situ by γ_d max, or by if you want to express that thing in percentage multiply by 100.

So, γ_d in-situ that means you have achieved that much of compaction. Whereas γ_d max that is the densest packing available in the laboratory. So, in the laboratory basically γ_d max you can achieve okay, but in the field, you have achieved γ_d in-situ. So, the ratio of

these 2 will give you the relative compaction and if you put the values 17.8 by 19.78 into 100, so which will be coming as 89.9%. So, you have achieved 89.9% compaction in the field as compared to the gamma d max available in the laboratory.

So, I will stop here today. So, in the next lecture we will solve another problem which will be very important and I mean there are several aspects and that problem is basically talking about some practical problem or practical situation. Based on some practical situation we have developed that problem and in the next class we will see that problem. So, today I will stop here.

Thank you very much.