

Geotechnical Measurements and Explorations

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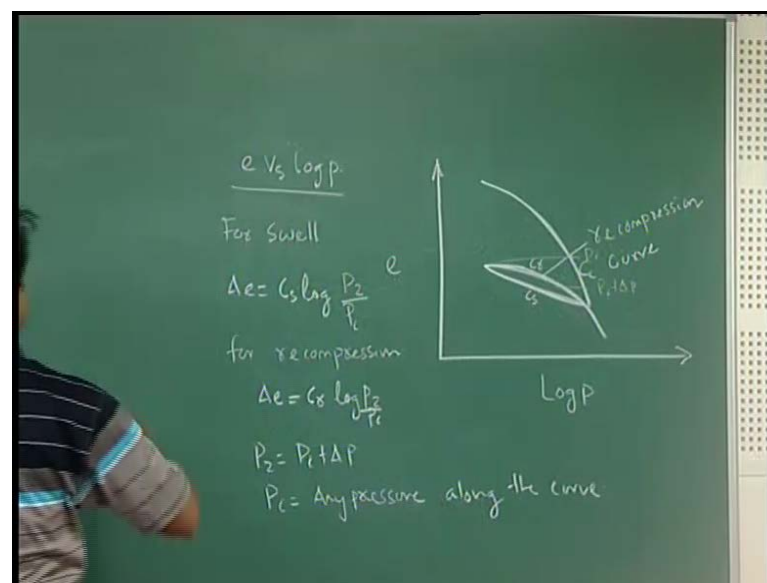
Department of Civil Engineering

Indian Institute of Technology, Kanpur

Module No. # 01

Lecture No. # 03

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Now we start with this e versus $\log p$ again. So this as I explained earlier; this is your compression curve, this is your swelling curve and this is your recompression curve. For swell if interested to find it out what is the swell? For swell change in void ratio Δe is your $c_s \log p$ two by p_1 . For recompression curve; this is your recompression curve **for recompression curve** Δe is equal to $c_r \log p$ two by p_1 c_r is your recompression index so p_2 is equal to p_1 plus Δp p_1 is your any pressure along the curve. If you look at here p_1 is your any pressure, this is my p_1 and this is your p_1 plus Δp . p_1 is your any pressure along this curve.

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$\Sigma V_s \log p$

$$\Delta \varepsilon = c_s' \log \frac{P_2}{P_1}$$

$$\Delta \xi = c_s' \log \frac{P_2}{P_1}$$

$e \text{ Vs } \log p$

For Swell

$$\Delta e = c_s \log \frac{P_2}{P_1}$$

for recompression

$$\Delta e = c_r \log \frac{P_2}{P_1}$$

$$P_2 = P_1 + \Delta P$$

$$P_1 = \text{Any pressure}$$

Now similarly, if this curve is there for strain versus log p then what parameter you are going to get? In terms of change in strain particularly swelling $c_s \text{ prime} \log p_2 \text{ by } p_1$. Similarly, for recompression it is $c_r \text{ prime} \log p_2 \text{ by } p_1$.

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Relationship between C_c & C_c'

$$\Delta e = \frac{\Delta V_v}{V_s} = \frac{\Delta H}{H_s} \approx \Delta H \rightarrow H_s = V_s = 1.0 \text{ (Taken) } H$$

$$\Delta H = C_c \log \frac{P_2}{P_1}$$

For initial void ratio e_0 ,

$$\Delta \xi = \frac{\Delta H}{1+e_0} = \frac{\Delta H}{H_s + H_v}$$

During compression, voids compress (Assumption)

$$\Delta \xi = \frac{\Delta H}{H_{e0}} = \frac{\Delta H}{1+e_0}$$

$$\frac{\Delta H}{1+e_0} = C_c' \log \frac{P_2}{P_1}$$

$$\Delta H = (H_{e0}) C_c' \log \frac{P_2}{P_1}$$

$$C_c \log \frac{P_2}{P_1} = (H_{e0}) C_c' \log \frac{P_2}{P_1}$$

Initial Void Ratio

$$C_c' = \frac{C_c}{1+e_0}$$

Now, come back to what is the relationship between **relationship between** C_c and C_c' . C_c compression index and C_c' compression index prime; now as you know the void ratio Δe , change in void ratio or void ratio you can say volume of voids by **by** definition volume of voids by volume of solids. So, it is Δv volume of voids change

in volume of voids change in void ratio is equal to change in void ratio is equal to change in volume of voids divided by volume of solids which is equal to $\frac{\Delta h}{h_s}$.

h_s is nothing but, your height of soil and Δh is your change in void. How do you find it out? Change in void; it will as the sample compress. As the sample compress by means of consolidation test what will happen in the compression? Expulsion of air and water will occur. Once expulsion of air and water will occur so suppose sample is initial height is h , now it has been compressed during consolidation. So voids will go, means air and water will go out. So slowly, slowly sample will change its positions that means Δh is your change in length or change in height $\frac{\Delta h}{h_s}$ divided by h_s your height of solid. Height of solid is your volume of solid. So, this is equal to $\frac{\Delta h}{h_s}$. That means this condition when it is applicable? When h_s is equal to v_s is equal to one that means we assume that maximum it will change in height will occur so that after that no further change in volume or no further change in height. That means if I take h_s means height of solid and volume of solid is equal to one. This is assumed or may be taken then is your change in void ratio is equal to change in $\frac{\Delta h}{h_s}$ is your height or change in your strain.

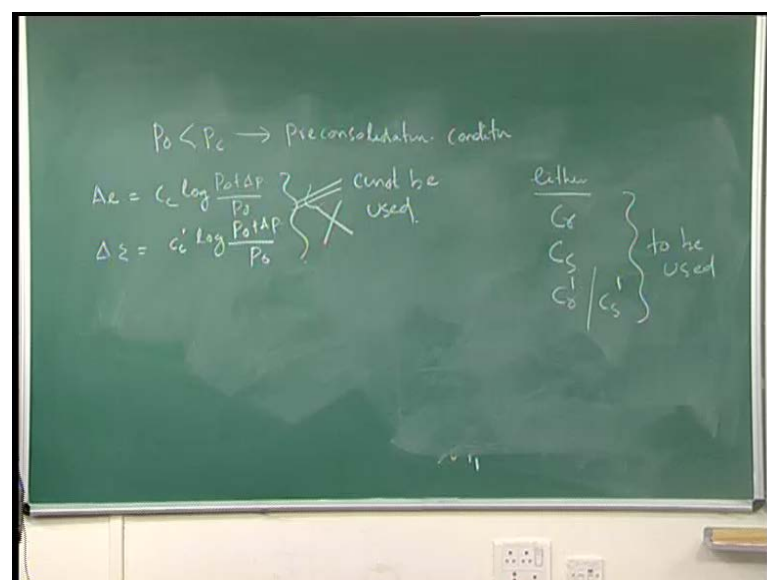
Then $\Delta h = c_c \log \frac{p_2}{p_1}$ or p_1 whatever you say for $\frac{\Delta h}{h_s}$ this compression curve Δe is equal to $c_c \log \frac{p_2}{p_1}$ whatever. So, $\frac{\Delta h}{h_s}$ now as Δe is equal to Δh now Δh I put it here $c_c \log \frac{p_2}{p_1}$ and p_1 . Now, for initial void ratio e_0 ; e_0 change in strain Δh by one plus e_0 which is equal to Δh by h_s plus h_v height of solid plus height of volume. Now, during compression only voids compress. This is our assumption in one dimensional consolidation theory. We assume that during compression that means $\frac{\Delta h}{h_s}$ in one direction suppose this a z direction may be y may be x in one direction particularly in vertical direction it compresses. Once one direction it compresses, the assumption is it only compresses voids. That is it $\frac{\Delta h}{h_s}$ only compresses the voids. This is your assumptions.

Now, change in strain Δh by one plus e_0 which is equal to Δh by one plus e_0 . Now, Δh by one plus e_0 is equal to $c_c \log \frac{p_2}{p_1}$. This is your change in strain, $\frac{\Delta h}{h_s}$ if I plot instead of e if I plot strain per $\log p$ strain per $\log p$, so this c_c from here we are supposed to get c_c , it will become c_c . Now, this is your change in strain is your Δh by one plus e_0 which is equal to $c_c \log \frac{p_2}{p_1}$. Now Δh by one plus e_0 if you look at here, it is coming Δh is equal to one plus e_0 $c_c \log \frac{p_2}{p_1}$. Now, Δh is

nothing but, if I write it here equation one Δh is nothing but, $c_c \log p_2$ by p_1 one which is equal to one plus $e_0 c_c' \log p_2$ by p_1 . Now, if you cut it means cancel all equal terms both the sides. Now, c_c' is equal to c_c by one plus e_0 . That means compression index what you get by plotting change in strain with your $\log p$ by plotting strain or e versus $\log p$? Suppose you are plotting e versus $\log p$; the compression index curve it is giving you c_c . If I plot strain versus $\log p$ the compression index curve will give me c_c' .

Now what is the relation between c_c and c_c' ? If somebody wanted to change from change in strain versus $\log p$ to e versus $\log p$, that means compression index c_c' due to strain versus $\log p$ is equal to c_c compression index, you are getting from e versus $\log p$ divided by one plus e_0 . e_0 is nothing but, it is your initial void ratio. This relationship if you know from there if you know h you can find it out e , if I know c_c I can find it out c_c' . Suppose there is a curve has been plotted e versus $\log p$, so once you get e versus $\log p$ from there you can get it c_c because from this slope of this curve you can get c_c compression index. Once you get c_c then you can get what is your compression index for a curve change in strain or strain versus $\log p$. From this relation you can get it c_c' .

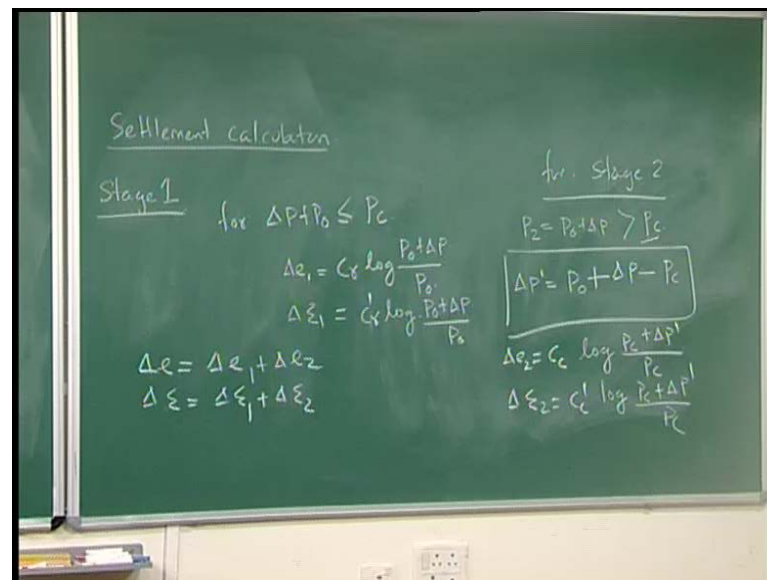
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Now move to when p_0 less than p_c . That means this condition is called for pre consolidation pressure, pre consolidation condition. In this case **in this case** these two

equations change in void ratio $c_c \log \frac{p_0 + \Delta p}{p_0}$ or change in strain $c_{\alpha} \log \frac{p_0 + \Delta p}{p_0}$. These two equations cannot be used for pre consolidation conditions. To find it out change in void ratio or change in strain by means of conventional formula. This is a conventional formula. It cannot be used the condition where p_0 is less than p_c . That means in case of pre consolidation conditions these two cannot be used. Now for these conditions **for these conditions** either c_{α} or c_{α}' to be used. Why? Because this pre consolidation condition means earlier whatever pressure is there it is less than your p_c . This pressure has been eroded away that means the pre consolidation conditions has been from recent past it is continuing. So, in this conditions settlement can be calculated in two stages.

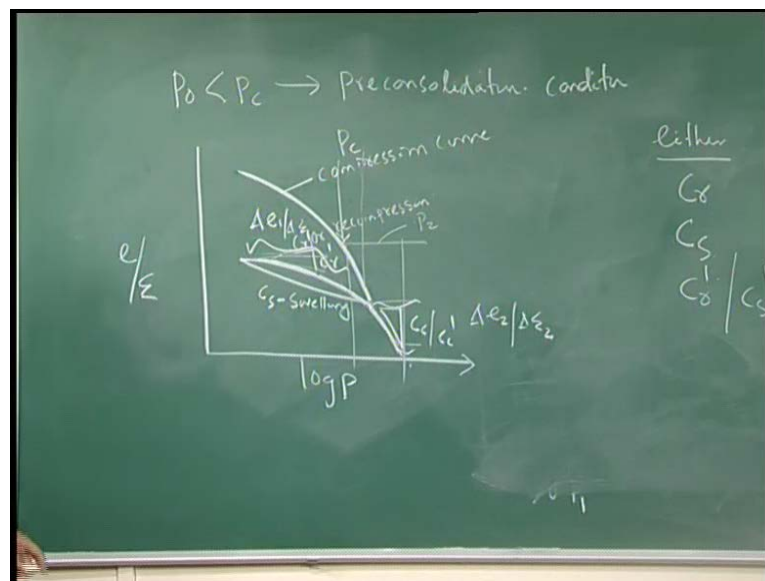
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Stage one; for $\Delta p + p_0$ less than equal to pre consolidation pressure, p_c is your pre consolidation pressure then, Δe one is equal to $c_r \log \frac{p_0 + \Delta p}{p_0}$ by p_0 . Then Δe one is equal to $c_c \log \frac{p_0 + \Delta p}{p_0}$. For stage two that means, increase in $\Delta p + p_0$. That means this is your over burden pressure, increase in stress and the present stress if less than your pre consolidation may or consolidation pressure p_c then, Δe and $\Delta \epsilon$ means change in void ratio and change in strain in terms of c_r and c_r' to be calculated. So here, recompression curve **here recompression curve** for strain.

For stage two; suppose say p_2 is equal to $p_0 + \Delta p > p_c$ that means, stage one $p_0 + \Delta p < p_c$. p_c is your pre consolidation pressure. If stage two $p_0 + \Delta p$ is greater than p_c that means pre consolidation pressure, in that case you can find it out $\Delta p'$ is equal to $p_0 + \Delta p - p_c$. As it is greater than your pre consolidation pressure that means, increase in stress because of this is $p_0 + \Delta p - p_c$. So now, we can find it out Δe_2 is equal to c_c . In this case it will come $c_c \log p_c + \Delta p'$ by p_c and Δx_2 is equal to $c_c \log p_c + \Delta p'$ by p_c . Now the total change, if I say total change in void ratio because of condition one, stage one and stage two what will happen? So in this case, Δe is equal to $\Delta e_1 + \Delta e_2$, that means change in strain is equal to $\Delta x_1 + \Delta x_2$. Now, look at a in figure this is **this is this is** what I have written in terms of calculation point of view.

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If you want to understand then draw e versus $\log p$. Stage one; in stage one if you look at here, we are using recompression index. If this is my once again I am saying this is compression curve, this is c_s or swelling, this is c_r or recompression. Now, p_0 is less than p_c that means pre consolidation condition. That means the consolidation has already been done in the **past** recent past that means stage one whatever I am applying increase in pressure plus whatever the pressure is there is less than p_c . That means already this compression part is over, means already the compression or may be consolidation has been occurred in recent past. That is the physical significance.

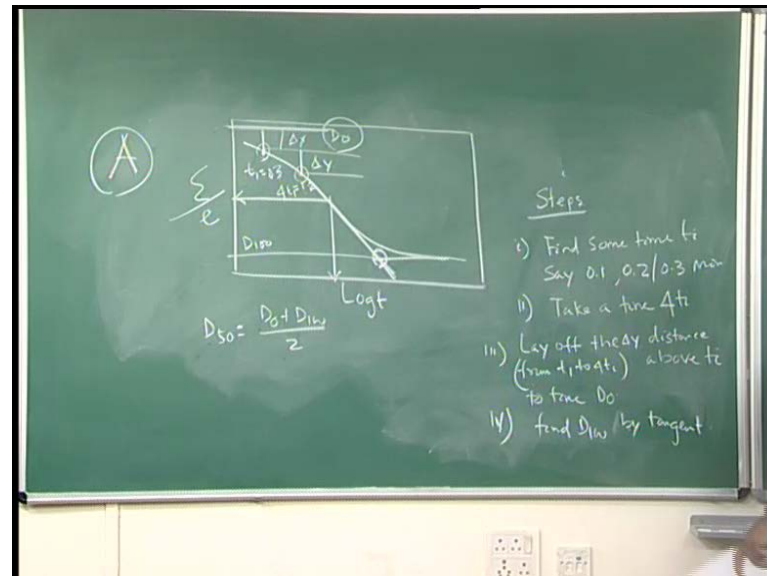
Now, we are here when Δp and p_c is less than p_c . That means once I am applying Δp , because the condition is p_0 is less than p_c . That is your pre consolidation condition. In pre consolidation condition means, as I explained last class this is your pre consolidation condition. Means already consolidation occurred in recent past that means this part is already over. Consolidation occurs in the recent **part** past that means the compression part is already over. Now, once you applied increase in stress Δp that means we are here we are applying increase in stress Δp . So, that means it is nothing but, you are using your recompression curve c_r or recompression curve from here you can get your recompression index by means of your slope. You can get it from slope recompression index. So, that is why for stage one increase in, means change in void ratio you can find it out c_r , change in strain you can find it out $c_{r'}$.

Now for stage two; the moment you say that what will happen? The moment you say that $p_0 + \Delta p$ is greater than p_c suppose p_c is lying somewhere else here. Pre consolidation pressure is lying somewhere else here. Now, you are saying stage two p_2 is equal to $p_0 + \Delta p$ greater than p_c that means $p_0 + \Delta p$ greater than p_c means, pre consolidation pressure means it will cover up reconsolidation means recompression curve and again it will come back to your compression curve. It will again come back to your compression curve or slope so this is nothing but, your c_c or $c_{c'}$. So, that means for stage two if p_2 is equal to $p_0 + \Delta p$ greater than p_c that means p_c is here. Whatever I am applying Δp increase in stress is more than p_c that means this curves here, it will start from here.

In this case you find it out how much is your increase in pressure, how much is your increase in pressure Δp . That means initial pressure initial over burden zero whatever you applied increase in stress Δp minus pre consolidation pressure, your pre consolidation pressure is your minus here. That means whatever is here from here to here in terms of you can say from here to here, this is your p_2 after p_c . So, from there Δp increase in stress you find it out. Once the p_2 has been applied the curve from recompression, it comes to again compression **it comes to again compression**. From this compression curve you can find it out c_c or $c_{c'}$ by slope. So, you can get change in void ratio or change in strain in this conditions. That means here to here you are getting Δe_1 or $\Delta \epsilon_1$. From here to here you are getting Δe_2 or $\Delta \epsilon_2$. That means total change in void ratio or total change in strain you can find it out

delta e one plus delta e two or total change in strain delta xi one plus delta xi two. For stage one and stage two. Now, move to, this is all about your c c **this is all about your c c**.

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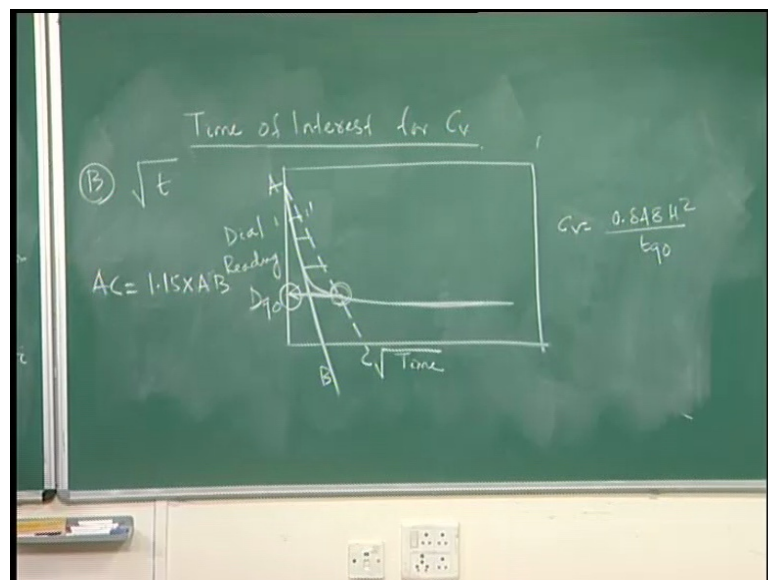
Now, we are moving to c v, time of interest **interest** for computing **for computing** c v. One is your log t plot, **log t plot** b is your root two root time plot. So, case one; a strain versus log t. This is called logarithmic time plot. This one so plot it. Now what are the steps? Find sometime t I say 0.1 0.2 or 0.3 minute. Then second step is your take a time four t I. Now, I take certain time let us say arbitrarily say t one is equal to 0.3 minute, then find it out what is your four t I. Suppose four t I is here, suppose t one is 0.3 minute, four t I means four into 0.3. So, 1.2 minutes. So this is your four t one is equal to 1.2. Now, find it out what is your lay off this delta y. Now, this delta y between t one and four t one it should be lay off above t one. So, this is your delta y to get e zero or d zero. This is my d zero. Now, d hundred to be you can get it draw a tangent of from this part of this where the curvature and the bottom of your where it is asymptotic towards your time curve wherever the intercept is there, you will get d hundred. This is your initial reading d zero. So, from there you can find it out d fifty is equal to d zero plus d hundred by two.

Now third step is your lay off. The delta y distance from t one to four t one above t I to find d zero, find d hundred by tangent. Now, if it is not a strain versus log t; it may be a e versus also log t. Void ratio versus also log t. In case of void ratio versus log d this will be your e zero, d zero means initial. General trend of this curve is like this. Once again I

am repeating these steps. So, arbitrarily you choose any time. Suppose t_1 I can say choose .1 .2 .3. In this case my first part is your t_1 one, first you have to find it out d_0 where is your d_0 ? Locate. First time I have arbitrarily chosen say t_1 is equal to 0.3 minute.

Now, with this t_1 find it out four t_1 . That means where it locate four t_1 is locating here. That is your one point two minutes. Now lay off this from t_1 to four t_1 one how much is your this? This is your Δy with this Δy from t_1 you can put it above the t_1 . So, this Δy I put it here so whatever we are getting from here this is my initial d_0 or e_0 sometimes it is called, if it is e versus $\log t$ plot you can find it out d_0 point here. d_{100} point you can get it you draw a tangent from here and the bottom part where it is asymptotic towards your time axis where it intercept that is your d_{100} . Now from this d_0 to d_{100} you can get d_{50} that is that means d_0 plus d_{100} by two that is your d_{50} . That means this is my d_{50} or t_{50} . d is nothing but, you can say that d_{50} is your up to the degree of consolidation, fifty percent degree of consolidation. This is your zero degree of consolidation. This is your hundred degree of consolidation. From there you can get time t_{50} for fifty percent of consolidation. Now come back to second method root two time plot b.

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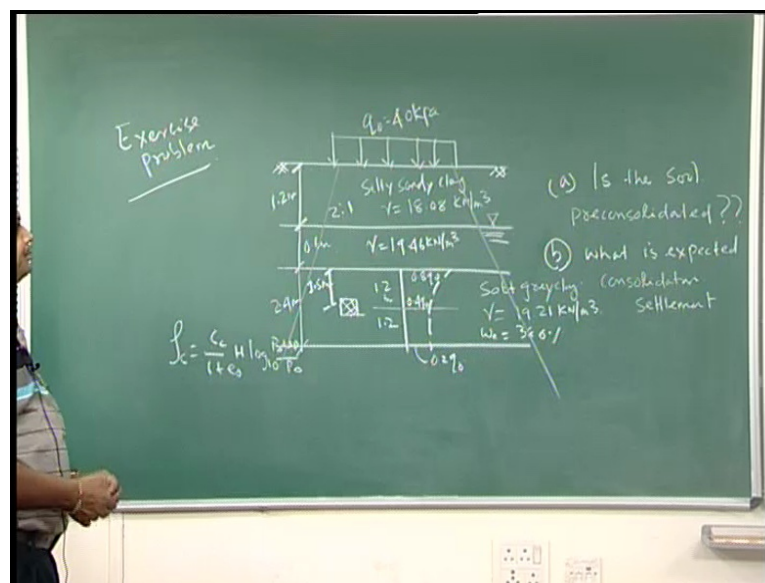
Now, plot this curve say dial reading **dial reading** whatever from consolidation, dial (()) reading versus time time interval in terms of root **root** time, you draw the curve this is

your curve general trend is like this. Now, initial part draw a tangent from the initial part where it curve generally starts with moving straight line draw a tangent. From this initial part and extend it.

With this tangent draw whatever line mark it a b. Now with this line a b you can extrapolate a c. Suppose this coordinate is how much? This is your coordinate from there. Suppose this is your a one. So, this coordinate will be a one prime. So, it will be exactly 1.15 times of a b, 1.15 times of a b. Now, each coordinate you mark it, each coordinate you find it out and plot a c. a c is nothing but, your 1.15 times of a b. The a c where it intersect your consolidation curve that is your dial gauge reading versus time. This part it **it** intercepts at this position from here. You extend this gives your ninety percent degree of consolidation, ninety percent degree of, that is your d 90 **ninety percent degree of consolidation**. Now, once you get d ninety or d fifty then, from here once you get d ninety you can find it out c v is equal to 0.848 by t ninety. For this case for here you can find it out c v is equal to 0.197h square by t 50.

These are the two methods used particularly to find it out c v. These two methods called time of interest. What time of interest you are, you want degree of consolidation should be ninety percent or you want a degree of consolidation at fifty percent? What would be your coefficient of consolidation c v? So, these are the all two time plots; one is your logarithmic time other is your root two time.

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Now one exercise problem I am giving. Silty sand this is a field problem, silty sandy clay, γ is equal to 18.08 kilo Newton per meter and water table is located below 1.2 meter of the ground surface. This is your water table located below 1.2 meter here γ is equal to 19.46 kilo Newton per meter and soil is expected to take out from the ground surface. So, this distance is say 1.5 meter. Now, this is your 1.2 meter. This is your 1.2 meter and this is 0.8 q_0 , 0.4 q_0 and 0.2 q_0 and this is soft gray clay, γ is equal to 19.21 kilo Newton per meter cube. Natural moisture content is equal to 30.0 percent. Now, this is your field condition where the surcharge is forty k p a. Initially this is a silty sand clay first 1.2 meter, 10.6 meter below 1.2 meter this is water table and the soil is γ is 19.46. This soil is also silty sand below 1.8 meter soft grey clay is there and with this below 1.8 meter another 1.5 meter soil sample has been collected for your consolidation laboratory, from field.

Now the question is; there are two questions. One is your is the soil pre consolidated? Now b is equal to second part, what is expected consolidation settlement? Now this is your consolidation pressure or this is this is varying from 0.89 q , 0.49 q , 0.29 q_0 . From these, there are two **two two** questions; one is your is the soil pre consolidated, that means you have to check whether p_0 is less than p_c , pre consolidation pressure or if it is less than then it will be pre consolidated.

Second part what is your expected consolidation settlement in this layer? Expected consolidation settlement in this layer means consolidation settlement c_c by one plus e_0 $\log_{10} \frac{p_0 + \Delta p}{p_0}$. Find it out p_0 . Stress at this distance because γ into γ is your 18.08 into 1.2 γ into 0.6 γ into this. Δp increase in stress because of your forty k p a. That you can find it out by means of I am giving this is hint. This is an exercise problem because your fear external load forty k p a increase in stress, you can find it out by means of two is to one method. Two is to one distribution method at this layer what is your increase in stress Δp you can get it and c_c one plus e_0 natural moisture content is given and from there you can find it out e_0 and c_c you can assume it. There are correlations. Next class I will say different correlations of c_c available for soft clay, c_c is equal to 0.07 into one minus e_0 . From there you can find it out c_c . With this hint please complete this problem.

Thank you