

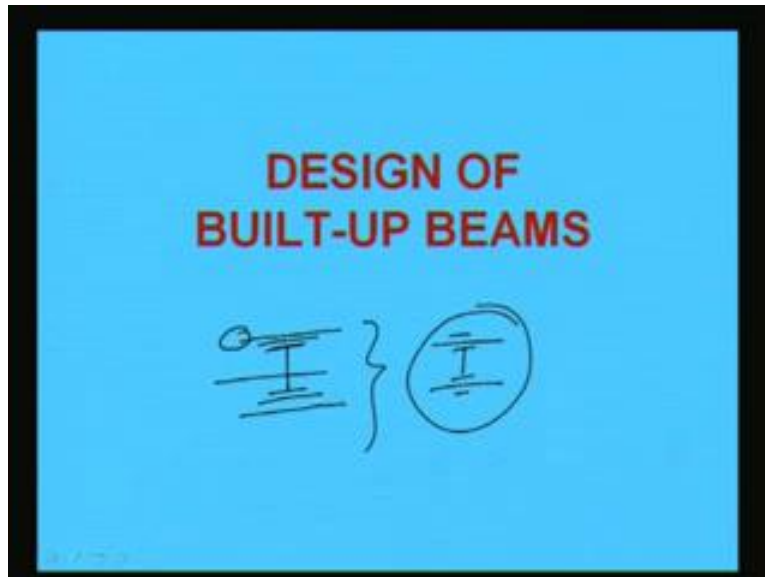
**Design of Steel Structures**  
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**Module - 6**  
**Flexural Members**  
**Lecture - 7**  
**Design of a Built-Up Beams**

Hello, today we will be solving an workout example on design of built-up beam. In last 2 lectures, whatever we have discussed about different aspects of built-up beam those things we will apply through 1 example. When we will go through this example workout example then we will see how to apply the codal provisions and other things step by step.

As we know that built-up section are made only when the load is high or the depth is restricted from architectural or from some other point of view or the span of the beam is very high. And to restrict the depletion excessive depletion we may have to go for built-up sections right. So, today first I will go through 1 example I do not know how much I will be able to finish because this is a long example. And you must give your concentration to each steps otherwise it will be difficult to understand the entire process thoroughly. I will try to go as slow as possible, but again as we have limited time means only 1 hour we can spend for a particular lecture. So, I will try to finish the entire example in this lecture itself.

(Refer Slide Time: 02:41)



We will just see how much we can do. Now, built-up section means generally we feel in case of beam as like this say I section. And then plate section most commonly we use right say it may be symmetrical it may be unsymmetrical. Then if we use more than 1 plate generally either we use same width of the plate or maybe larger than that. We can use like this. But never we use say like this then this. What is the beneficial of this because when we are using the higher section higher width of or higher area of plate at the outermost the moment of inertia will become high.

But, in this case moment of inertia will become will become with same arrangement suppose if we make here the moment of inertia will become less. And our motto is to make the arrangement in such a way that the moment of inertia of the built-up section is become as high as possible with the same material.

(Refer Slide Time: 03:59)

**Example:-**  
A beam of 7m effective length, carrying a uniform load of 50kN/m inclusive of self weight over the entire span. The compression flange of the beam is laterally supported throughout. If the overall depth of the beam is restricted to 300mm, design the beam with a suitable section. Assume for steel,  $f_y = 250 \text{ N/mm}^2$

*Handwritten notes:*  
 $\sigma_{bc} = \sigma_{bt} = 0.66 f_y$   
 $= 0.66 \times 250$   
 $= 165 \text{ MPa}$   
Simply supported beam  
7m  
50 kN/m  
D  $\leq$  350

This example is like this that a beam of 7 meter effective length carrying a uniform load of 50 kilo Newton per meter including of self weight over the entire span right. The compression flange of the beam is laterally supported throughout. If the overall depth of the beam is restricted to 3 100 mm design the beam with a suitable section. Assume for steel  $f_y$  has 2 50 millimeter right.

So, what we have seen that a beam that is 7 meter effective length is carrying a uniform load of 50 kilo Newton per meter right which include self weight also. The compression flange is laterally supported. So,  $\sigma_{bc}$  will be  $\sigma_{bt}$  will be point 6 six  $f_y$ . And  $f_y$  is 2 fifty. So, this will become 1 65 MPa. So,  $\sigma_{ac}$  and  $\sigma_{bt}$  is known now. And now other thing is that. So, design the beam which is suitable to this here it is not given.

Assume that it is a simply supported beam simply supported beam. So, let us assume simply supported beam. And this also hum it was by mistake 300 it was say 350 restricted to 350 mm the beam depth is restricted to 350 mm right. So,  $D$  should not be greater than 350 mm over all. So, these are things, which has been given right. So, now what we will do we will go for the solution.

So, you just write down that a simply supported beam which is carrying 50 kilo Newton 50 kilo Newton per meter load which includes the self weight also the span length is 7 mm 7 meter. And the maximum depth is limited to 350 and this is simply supported right.

(Refer Slide Time: 07:09)

**Solution:**

**Step1:** Expected load on the beam,  $w = 50\text{kN/m}$

**Step2:** Maximum bending moment,  $M = \frac{wl^2}{8}$   
 $M = \frac{(50 \times 7 \times 7)}{8} = 306.25 \text{ kn-m}$   
Maximum shear force,  
 $V = \frac{(50 \times 7)}{2} = 175\text{kN}$

**Step3:** Section modulus,  
 $Z = \frac{306.25 \times 1000000}{155} = 1975800\text{mm}^3$

So, with these conditions let us make it. So, now we will solve the problem whichever was given. In first step what we will do we will find out the load on the beam and it was told that load is 50 kilo Newton per meter right 50 kilo Newton per meter which includes self weight also. Now, in next step we will find out the maximum moment as for the case of the simply supported beam with ideal load. We know that maximum bending moment will be  $wl^2$  by 8. So,  $w$  is 50 and  $l$  is 7. So,  $wl^2$  by 8 is becoming 306 point 25 kilo newton meter right.

Then maximum shear force we are going to get as  $wl$  by 2 this is 175 kilo Newton maximum shear force as we know it will occur at the support for this particular case and this will be  $wl$  by 2. So, if we calculate this value we will get  $V$  is equal to  $wl$  by 2 is equal to 50 into 7 by 2 is equal to 175 kilo Newton right. Now, we will find out the section modulus in step 3 we will find out section modulus on the basis of developed moment and the allowable shear allowable bending stress.

Now, as the beam is laterally supported throughout its length. So, we can write  $\sigma_{bt}$  is equal to  $\sigma_{bc}$  that will become 165 right. Because, this is  $0.66 f_y$  and  $f_y$  is 250. So, after multiplication we will get 165 MPa right. So, we can find out  $Z$  is equal to  $M$  by  $\sigma_{bc}$ . Now,  $M$  is 306.25 kilo Newton. So, this we are making Newton with multiplying  $10^6$ . By  $\sigma_{bc}$  or  $\sigma_{bt}$  that is supposed to be 165. But, we are making 155 thinking that as we are going to use plate and for that we need to provide some rivet connection.

So, the net area of the flange will be less that is why to accommodate that we are slightly reducing the permissible stress. That means, from 165 to we are making 155, so that we will in higher side in terms of section modulus. So, that the section whatever we will be choosing will be little higher side. Because later when we will be reducing the area because of the presence of rivet hole then the stress will become high. So, to adopt that 1 at the beginning itself we are choosing little less stress so that the section modulus become little high.


(Refer Slide Time: 10:15)

A plate beam will be provided.  
A reduced allowable bending stress of 155 N/mm<sup>2</sup> is assumed to account for rivet holes in the tension flange.

350

Step4: Let us provide ISMB 250 @ 373 N/m. the relevant properties of the section are:

$A = 4755 \text{ mm}^2$   
 $B = 125 \text{ mm}$   
 $T = 12.5 \text{ mm}$   
 $t = 6.9 \text{ mm}$



So, that is what I have written here a reduced allowable bending stress of 155 Newton per millimeters is assumed to account for rivet holes in the tension flange. Now, as the restriction is given that maximum height will become 350. So, we cannot go up to a

certain means whatever we want the section we cannot go beyond that right. So, considering this let us use say ISMB 250 at 373 Newton per meter. And if we are going to use ISMB 250 then what are the properties, which is given in SP 6 in tabular form it is given like.

Area of ISMB 250 is given 4755 millimeter square. Width is given 125 if I see the diagram we will see it is like this because this will be required case to case. So, let us make the diagram here. So, this is 250 and b the width of flange is 125 right. And thickness of flange T is equal to 12.5 and thickness of web is equal to 6.9 right. So, these are the things we can find out from the code.

(Refer Slide Time: 11:51)

Handwritten calculations on a blue background:

$$\begin{aligned}
 I_{xx} &= 51316000 \text{ mm}^4 \\
 Z_{xx} &= 410500 \text{ mm}^3 \\
 h_2 &= 27.95 \text{ mm} \\
 g &= 65 \text{ mm} \\
 Z_p &= Z_{req} - Z_{xx} \\
 &= 1975800 - 410500 \\
 &= 1565300 \text{ mm}^3 \\
 A_p &= Z_p / D = 1565300 / 250 \\
 &= 6261.2 \text{ mm}^2 \\
 \text{Area of plate} &= 6261.2 \text{ mm}^2
 \end{aligned}$$

Along with that  $I_{xx}$  the moment of inertia about the major axis and similarly  $Z_{xx}$  which is given in the code. That is  $I_{xx}$  is 51316000 millimeter to the power 4. And  $Z_{xx}$  will be 410500 millimeter cube.  $h_2$  will be 27.95 millimeter. Gauge distance  $g$  will be 65 millimeter. So, these are the things which we will be required in different places for the calculation of the design of the built-up section. So, now what will be  $Z_p$  as we know required minus the available. So,  $Z$  required was this 1 this we found here  $Z$  required this is the  $Z$  required 1975800 millimeter cube. And  $Z$  available is this one. So, 1975800 minus available is 410500.

So,  $Z_p$  means section modulus has to provide this much with the additional plate. So, 1565300 millimeter cube has to be provided. So, area of the plate has to become  $Z_p$  by  $D$  which will be becoming 1565300 by 250. And if we take the ratio of this we will get the value of  $A_p$  area of plate this will become 6261.2 millimeter square. So, area of plate will be required 6261.2 millimeter square.

(Refer Slide Time: 13:49)

**Step 5:** As per clause 3.5.2.1 of IS 800-1984, the maximum outstand of flange from the connection should not exceed  $16T_1$  in the case of compression flange, where  $T_1$  = aggregate thickness of flange cover plates.

Maximum outstand from connections =  $16T_1$   
 $= 16 \times 32 = 512 \text{ mm}$

Provide 2 plates 16mm thick on each flange  
width of the cover plate =  $\frac{6261.2}{32}$   
 $= 195.66 \text{ (say 200 mm)}$

*Diagram:* A rectangular flange with a cover plate of thickness  $t_1$  and width  $A$ . The area is labeled as  $A = 6261.2$ .

Now, let us come to step 5. As we know as per clause 35020.1 of IS 8984 the maximum outstand of flange for the connection should not exceed  $16 T_1$  in the case of compression flange where  $T_1$  is equal to aggregate thickness of flange cover plates. So, maximum outstand from connection will be  $16 T_1$ . So,  $16$  into  $T_1$   $T_1$  is  $32$ . So, we are going to get 512 millimeter right. Now, if we provide 2 plates of 16 mm thickness on each flange then width of cover plate can be found.

That will be the total area by thickness because we are providing 2 plate. So, 2 plate of thickness 16 mm and sixteen mm right. And the area is given as 6261.2. So, the cover plate width will become 6261.2 by 32 is equal to 195.66. So, let us use say 200 mm width of cover plate right. And as we know maximum will become means can be made 512 millimeter.

(Refer Slide Time: 15:30)

Outstand flange cover plate from connection

$$= (200 - 65)/2 \quad (\text{as } g = 65 \text{ mm})$$

$$= 67.5 \text{ mm}$$

$$< 512 \text{ mm}$$

Hence, provide two plates 200mm x 16mm on each flange

$$I_{xx, \text{gross}} = 5131.6 \times 10^4$$

$$+ \left[ 2 \times \frac{200 \times 32^3}{12} + 2 \times 32 \times 200 \times (125 + 16)^2 \right]$$

$$= 30688.5 \times 10^4 \text{ mm}^4$$

So, it is. So, outstand flange cover plate from connection will be 200 minus 65 by 2. Where the gauge is 65 for this ISMB section whatever we have chosen for that from code we got that g was 65. So, 200 minus 65 by 2; so 67.5 which is less than 512 millimeter. So, it is right. Hence we can provide 2 plate of this; that means 16 millimeter thickness and 200 millimeter width. So, the plate we are going to provide is 16 mm thickness and 200 millimeter width. And 2 plates we are going to provide right 2 plates in top and 2 plates in bottom.

Now, with this let us find out the total moment of inertia of the section; that means, gross moment of inertia right. So, gross moment of inertia will be the moment of inertia of the I section which is given it was given here right the gross moment of inertia that is 51316 000. So, gross then the plate will be how much. Say if this is the I section now we are going to give plate here right. So, what we have to do we have to find out the gross moment of inertia of the combined section. So, moment of inertia of this section plus 2 into means bd cube by 12 bd cube by 12 and bd cube by 12.

So, 2 into b d means 16 into 2. So, 32 because here total is 32 and total width is 32. So, bd cube by 12 plus Ar square because now we have to transfer to here. So, A is 2 into 32 into 200 r square r square means 125 this is the 125 plus 16 right I hope it is understood



right. So, 5131.6 into 10 to the power 4 plus 2 into 200 into 32 cube by 12 plus 2 into 32 into 200 into 125 plus 16 square this is r this is A this is b this is d right. So, finally, the gross moment of inertia about xx is 30688.5 into 10 to the power 4 millimeter to the power 4. So, Ixx is 30688.5 into 10 to the power 4 millimeter to the power 4.

(Refer Slide Time: 18:45)

The image shows a handwritten calculation for bending stress in tension. The formula used is  $\sigma_{bc} = \frac{M}{I} \times y$ . The values are  $M = 306.25 \text{ kNm}$ ,  $I = 30688.5 \times 10^4 \text{ mm}^4$ , and  $y = 125 + 32 \text{ mm}$ . The result is  $\sigma_{bc} = 156.67 \text{ N/mm}^2$ , which is compared to an allowable stress of  $166 \text{ MPa}$ . A diagram shows a T-beam cross-section with a flange of width 125 mm and thickness 12.5 mm, and a web of height 200 mm and thickness 16 mm. The rivets are shown in two rows, staggered.

$$\sigma_{bc} = \frac{306.25 \times 10^3}{30688.5 \times 10^4} \times (125 + 32)$$

$$= 156.67 \text{ N/mm}^2 < 166 \text{ MPa}$$
 (as  $M = 306.25 \text{ kNm}$ )

**Step 6: Check for bending stress in tension.**  
 Let us connect the cover plates with the flange by 20mm diameter rivets. The rivets provided staggered in two rows.

Gross area of tension flange  
 $= 125 \times 12.5 + 2 \times 16 \times 200$   
 $= 7962.5 \text{ mm}^2$

Now, we can find out sigma bc. So, sigma bc will be how much M by I into y at the extreme fiber. So, M was calculated here earlier 306.25 that is maximum moment. And gross moment of inertia is 30688.5 into 10 to the power 4. And I will become 125 plus 32 because at the extreme fiber we have to calculate if I see. So, this is 125 and this is 32 right. So, this 1. So, after calculating this we will get sigma bc cal is equal to 156.67 Newton per millimeter square which is less than 166 right. Because, this is the allowable permissible stress in bending because of the beam flange is supported laterally right.

Now, we will go for step 6. Now, we will in step 6 what we will do we will check for bending stress in tension bending stress in tension. It will be will have to check because of the presence of the rivet because of the presence of the rivet the net area of the tension flange will be going to reduce. And that is why the tensile stress will develop more because of the hole. So, that we have check that whether it is exceeding or not. Now, let

us see now say let us connect the cover plates with the flange by twenty mm diameter rivets. And the rivets are provided staggered in 2 rows.

So, if this is the I section sorry if say let me draw the I section right. Now, we are providing some plate here right and we are having the rivet here right and 20 mm diameter power driven soft rivet let us use. So, if we use then gross area of tension flange will be what will be the gross area here. That will be 125 into 12.5 because this is 125 125 and this thickness is 12 point 5 right. So, area of the flange of the I section is 125 into 12.5 right. Then area of the plate there is 2 plates are there. So, 2 into 16 into 202 into 16 into 200. So, we are going to get gross area of tension flange as this 1 right 7962.5 millimeter square.

(Refer Slide Time: 22:08)

Net area of tension flange

$$= 7962.5 - 21.5(11.8 + 2 \times 16)$$

$$= 7020.8 \text{ mm}^2$$

$\sigma_{bt, cal} = \frac{156.67 \times 7962.5}{7020.8}$

$$= 177.68 \text{ N/mm}^2$$

$> 165 \text{ N/mm}^2 (= \sigma_{bt})$

which is unsafe.

Try two 18 mm thick plates on each flange.

So, the net area of the tension flange will be this minus 21.5 into 11 point 8 plus 2 into 16 because the plate is there because of plate because it is the hole is existing on plate also. So, net area of tension flange will become this 1. So, the sigma bt cal; that means, the developed tensile stress due to bending at the bottom will become this 1 right. That means gross area by net area gross area was this 1 gross area of tension flange this is the gross area 2 into this and this. And net area is this 1 right because of deduction of hole.

So, the area tensile stress is coming 177.68 Newton per millimeter square which is greater than the sigma bt the allowable bending stress in tension. Allowable bending stress in tension which is equal to point 66 fy and in this case it will be 165 Newton per millimeter square right. So, sigma bt cal; that means, the calculated bending stress in tension is coming higher than the allowable 1. So, we can say that this is unsafe.

That means if it is unsafe what we have to do we have to increase the plate thickness or plate diameter plate width or something. So, now let us use some higher thickness of the plate. Say let us try with 218 mm thickness plate on each flange right.

(Refer Slide Time: 24:19)

Handwritten calculations on a blue background:

$$I_{x, gross} = 5131.6 \times 10^4 + 2 \times \frac{200}{12} \times \frac{36^3}{12} + 2 \times 200 \times 36 \times \frac{(125+18)^2}{2}$$

$$= 34595.26 \times 10^4 \text{ mm}^4$$

$$\sigma_{b, cal} = \frac{306.25 \times 10^6}{34595.26 \times 10^4} \times (125+36) \left( \frac{M}{I} \right)$$

$$= 142.52 \text{ N/mm}^2 < \sigma_{bc} = 165$$

Gross area of tension flange

$$= 125 \times 12.5 + 2 \times 18 \times 200$$

$$= 8762.2 \text{ mm}^2$$

So, with that now again we can calculate the same things that Ixx gross Ixx gross means the moment of inertia about x direction. Grossly it will be this much that is the moment of inertia of the I section that ISMB 250 moment of inertia of this 1. Then this is the moment of inertia about its own axis 2 into 12 into bd cube by 12 right bd cube this will be cube bd cube by 12 plus. This will be 2 into area into this area 200 into 36 into Ar square right. So, if I make this, this will become this 1 right.

(Refer Slide Time: 25:21)

Outstand flange cover plate from connection  
 $= (200 - 65)/2$  (as  $g = 65$  mm)  
 $= 67.5$  mm  
 $< 512$  mm

Hence, provide two plates 200mm x 16mm on each flange

$$I_{xx, gross} = 5131.6 \times 10^4$$

$$+ \left[ 2 \times \frac{200 \times 32^3}{12} + 2 \times 32 \times 200 \times (125 + 16)^2 \right]$$

$$= 30688.5 \times 10^4 \text{ mm}^4$$

So, if you see earlier the gross area we have calculated like this you see this plus 2 into this plus this. This was 30688 into 10 to power 4. And here it is coming 34595 into 10 to power 4. So, it is going to increase. So, what we are doing for gross area that a moment of inertia of the section ISMB then moment of inertia about its own axis. That is 2 into b sorry b will be 200 bd cube by 12 plus A this is Ar square, right.

So, after calculating we are getting 34595.26 into 10 to power 4 millimeter to the 4. So, now we can find out sigma bc calculated the bending stress in compression. So, that is M by I into y right. So, M is 306.25 into 10 to the 6. I is 3459.59 5.26 into 10 to the power 4. And y is the distance from cg to the extreme fiber that is 125 plus 36 because 18 millimeter plate thickness of 2 plate. So, 36 plus 125 is the means half depth of the section.

So, after calculating this we are going to get sigma bc calculated as 142.52 newton per millimeter square which is less than allowable sigma bc that is 165. So, this is ... Now, similarly again we will find out the gross area of tension flange gross area of tension flange will be simply 125 into 12.5. That is the flange of the section I section and this is the plate 2 into 18 into 200. So, area will be 8762.2.

(Refer Slide Time: 27:39)

Net flange area of tension flange  
 $= 8762.5 - 21.5(12.5 + 2 \times 18)$   
 $A_{net} = 7719.75 \text{ mm}^2$  (with a circled '20φ' next to it)  
 $\sigma_{bt,cal} = \frac{142.52 \times 8762.5}{7719.75}$   
 $= 161.77 \text{ N/mm}^2$   
 $< 165 \text{ N/mm}^2 = \sigma_{bt}$   
which is all right

Then net flange area will be the gross area minus the whole the area of whole area of whole will be the 21.5 into 12 point into 5 plus 2 into 18 because this is the as we are using 25 rivet diameter. So, whole area will become 21.5. And this it the thickness of the flange and this is the thickness of the plate. So, after calculating this we are going to get as 7719.75 millimeter square. So, net area; area net of tension flange is becoming 7719.75. So, sigma bt cal will become simply the ratio of that gross area by net area.

So, that is becoming 1 61.77 Newton per millimeter square. And this is less than 165 Newton per millimeter square which is sigma bt right. That means which is all right. So, now with the modified thickness of the plate the tensile stress whatever is developing is. That means when we are using plate thickness of sixteen mm each the built-up section is not safe in tension. Now, after increasing we have seen that the built-up section is safe under tension and compression both, right.

(Refer Slide Time: 29:25)

**Step7: Check for shear**

$$\tau_{vu} = \frac{175 \times 1000}{(250 \times 6.9)}$$
$$= 101.4 \text{ (almost equal to } 100 \text{ N/mm}^2)$$

Hence safe.

ISMB 250

**Step8: Check for deflection**

$$\delta_{all} = \frac{l}{325} = \frac{7000}{325} = 21.53 \text{ mm}$$
$$\delta_{cal} = \frac{5}{384} \times \frac{50 \times (7 \times 10^3)^4}{2 \times 10^7 \times 34595.26 \times 10^4}$$

$\delta = \frac{5}{384} \times \frac{50 \times 2401 \times 10^{12}}{6.919 \times 10^{11}}$

Now, what we will do. We will go to next step for checking of shear. So, for checking of shear as we know we have to find out the stress that is we know 175 kilo Newton it was. So, V is 175 kilo Newton which we have calculated. And this is the depth D and this is the web thickness  $t_w$  means V by D into t sorry D into  $t_w$  web thickness. So, from this we are going to get 101.4 Newton per millimeter square. And the allowable stress is tau here is 100 Newton per millimeter square.

So, this is slightly greater than the allowable 1. So, what we have to do. Now, we have increase the dimension of the section in terms of either what you call we have means here what we are seeing that stress is depending on D and  $t_w$ . So, we have to increase the I section whatever I section we have used that ISMB 250 is not sufficient from shear stress point of view because if bending point of view it is also. But, shear stress point of view the shear stress will be carried by only this. So, this is not.

However, as it is slightly greater than this we can assume that it can be taken care for the sake of calculation. But; however, here you see because of shortage of time I am not going to check with another increased section. For actual design we have to increase the section from ISMB 250 to say suppose 275 or something then we have to do the same

thing again thoroughly. But, as here we are demonstrating some example say for the sake of calculation let us see what other thing has to be done.

If it is safe then what we will do we will go to next step that is step 8 check for deflection let us see other condition whether it is going to satisfy or not. As we told for shear there is only option is to increase the dimension of the section; that means the rolled section whatever available we have to increase there is no way right. So, now allowable deflection, as per codal provision is the span by 325.

So, span length is 7 meter or 7000 millimeter and 7000 millimeter by 325 is coming 21.53 millimeter right. And developed deflection is becoming as we know for simply supported beam with UDL load it will be  $\delta = \frac{5}{384} \frac{w l^4}{EI}$  So,  $\frac{5}{384}$  into  $w$  is 50 kilo Newton per meter if we make into Newton per millimeter also because of same unit we have to make. So, this will become 50 Newton per millimeter also if we change the unit.

So, that is a 50 has been written 7000 millimeter whole to the power 4 by  $EI$   $E$  is  $2 \times 10^5$  Newton per millimeter square and  $I$  is the gross moment of inertia. So, that is also calculated earlier that is 34595.26 into  $10^4$ . So, with this we can find out  $\delta$  calculated ...

(Refer Slide Time: 33:32)

$= 22.6 \text{ mm} > 21.53 \text{ mm}$

Since the deflection is not serious, a chamber of 5mm may be provided.

**Step 9: Design of connection**

Let us provide 20 mm diameter rivets in two rows to connect cover plate with the flange. The rivets will be staggered.

Gross diameter of the rivets =  $20 + 1.5 = 21.5 \text{ mm}$

Max. shear force = 175000 N

$I_{xx} = 345952600 \text{ mm}^4$

PDS

Which is becoming 22.6 mm right. So, this is greater than 21.53 millimeter. So, what we have seen here also is that from the depletion point of view this is not sufficient the assumed section is not sufficient from depletion point of view also. So, what we have to do we have to increase the depth of the cross section. That means depth of the section in terms of either the rolled section, we can increase the dimension or the plate thickness etcetera we have to increase and then only we can make it.

Or the plate thickness or plate width something we have to increase just to increase the moment of inertia right. Also we can see that since the deflection is not serious a chamber of 5 mm may be provided. Some other way also we can just make in this way also. However, it is also suggested that to recheck by the changing the dimension of the built-up section. Then what we will do we will go to next step that is design of connection right.

So, in connection say let us provide twenty mm diameter of rivets rivet means say power driven soft rivets as we told let us use in 2 rows to connect cover plate with the flange. And the rivets are will be staggered why rivets will be making staggered because you see if we make rivet in same line, then the area of whole has to be deducted 2 times right. So,



net area will become less, but if we make like this then only 1 hole area has to be deduct from the gross area.

So, net effective area will be more. So, we will provide for means we will go for rivets with staggered join means staggered combination right. Now, as we know we are providing the 20 mm diameter of rivets. So, the gross diameter of rivet will become 21.5 millimeter. And we have calculated already the maximum shear force as 175 kilo Newton and gross moment of inertia Ixx. Already we have calculated 345952600 millimeter to the 4 which will be required to find out right rivet number etcetera right.

(Refer Slide Time: 36:21)

$$Q = \bar{A}y = (200 \times 36 - 21.5 \times 36)(125 + 18)$$

$$= 918910 \text{ mm}^3$$

The rivets will be in single shear as the cover plates are tied together

Rivets value in single shear =  $\frac{\pi}{4} d^2 \tau_v$   
 $= \frac{\pi}{4} \times 21.5^2 \times 100$   
 $= 36305.03 \text{ N}$   
 $= 36.3 \text{ kN}$

Rivet value in bearing =  $d t \sigma_p$   
 $= 21.5 \times 12.5 \times 300$   
 $= 80625 \text{ N}$   
 $= 80.6 \text{ kN}$

$R_v = 36.3 \text{ kN}$

Now, Ay that is means Q that we have to find out that will become 200 into 36 because as we know this is 2 100 and this is 36. And then the area of the hole that will be 21.5 into 36, area of hole will be there in staggered way. Say. So, in 1 section only 1 rivet hole will be deducted. So, this is the area 200 into 36 minus 21.5 into 36 right. Then y bar y bar will become if this is the neutral axis then this is 125 because total depth is 250 then 125 plus Cg of this; that means, plus 18 because total is 36.

So, this is y bar is 1 25 plus 18. So, Q is becoming 918910 millimeter to the power cube 918910 millimeter cube. So, we found ... Now, the rivets will be in single shear as the

cover plates are tied together. So, we have to find out the rivet value rivet value single shear and rivet value in bearing. There are 2 scope of failure 1 is for shear failure that is single shear failure another is bearing failure. So, failure of rivet point of view we have to find out what is the rivet value is coming. So, for single shear the rivet value can be find out that  $\pi \times d^2 \times \tau \times v_f$ .

So,  $d$  is 21.5 and allowable stress is 100. So, we are going to get 36 36305.03 Newton; that means, 36.3 kilo Newton right. And similarly, for bearing it will be  $\sigma \times v_f \times d$  into  $t$  diameter is 21.5 thickness is 12.5 and  $\sigma \times v_f$  is 300. So, we are going to get 80625 Newton or 80.6 kilo Newton. So, from this 2 we can find out the rivet value as 36.3 kilo Newton because the lesser of this will be assumed as the rivet value for calculating the number of rivets right.

(Refer Slide Time: 39:11)

therefore, rivet value,  $R_v = 36305.03 \text{ N}$  36.3 kN

$$s = \frac{2I}{VA_y} \times R_v$$

$$R_v = \frac{VA_y \cdot s}{2I}$$

$$s = \frac{2 \times 34595.26 \times 10^4 \times 36305.03}{175 \times 10^3 \times 918.91 \times 10^3}$$

$$= 156.20 \text{ mm} > 50 \text{ mm} \quad (2.5 \times 20)$$

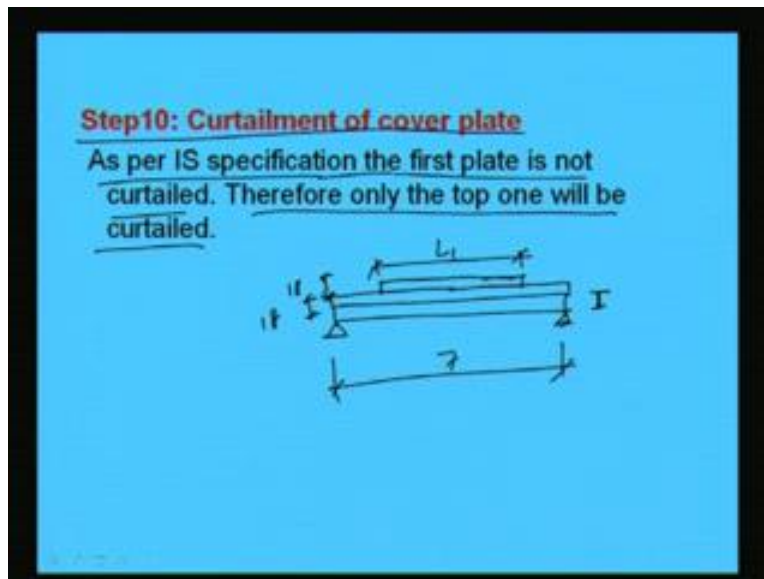
Hence provide rivets at a pitch of 150mm.

$s = 150 \text{ mm}$

So, next what we will do next we will. So, rivet value here 36.3 kilo Newton. Next we will find out the spacing right. So, from the formula we can find out we know that  $s$  will be becoming  $2I$  by  $VA_y$  into  $R_v$ . Because,  $R_v$  was as we calculated  $VA_y$  by  $2I$  into  $s$  if you remember in last lecture we have derived, this where this is number of rows it was  $n$  here it will be 2. So, if we provide those values it will become 2 into  $I$  means 34595.26 into ten to the power 4 into  $R_v$  is the rivet value.

That is  $36305.03$  by  $V$  is the shear force that is  $175$  kilo Newton. So, we are making as Newton  $175$  into  $10$  cube Newton. And  $A_y$  we have calculated here that is  $918910$ ,  $918910$  millimeter cube. So,  $918910$  millimeter cube that we are multiplying with  $10$  cube. So, this is becoming this right. So, after calculating this we are going to get  $156.2$  millimeter right and which is greater than  $2.5 D$  as per codal provision right. So, at least it has to be greater than  $2.5 D$ . So, we can provide the rivets at a pitch of  $150$  mm, because it is coming  $156$ . So, we can provide pitch  $150$  mm. And minimum pitch has to be at least greater than  $2.5 D$ .

(Refer Slide Time: 41:25)



So, pitch we can find out in this way. Next what we will do next we will go for curtailment of cover plate. So, as per IS specification the first plate is curtailed therefore, only the top 1 will be curtailed. First plate will not be curtailed because there is 2 plate. So, what we will do along the length. If we see that if this is the beam right and if this is the cross section of the beam then first plate of  $18$  mm thickness will be provided throughout. And then second plate will be provided somewhere right.

So, now this thickness is already decided that is  $18$  and this is also  $18$  right only this distance has to be decided say  $L_1$  right because  $L$  is already decided that is  $7$  meter right,

because of 2 plates. So, only 1 curtailment will be there here. So, in this way let us see where we have to curtail.

(Refer Slide Time: 42:37)

Net  $Z_{xx}$  (with two cover plates)

$$I_{xx, \text{gross}} = 345952600 \text{ mm}^4$$

$$I_{xx, \text{net}} = I_{xx, \text{gross}} - \text{moment of inertia of rivet holes}$$

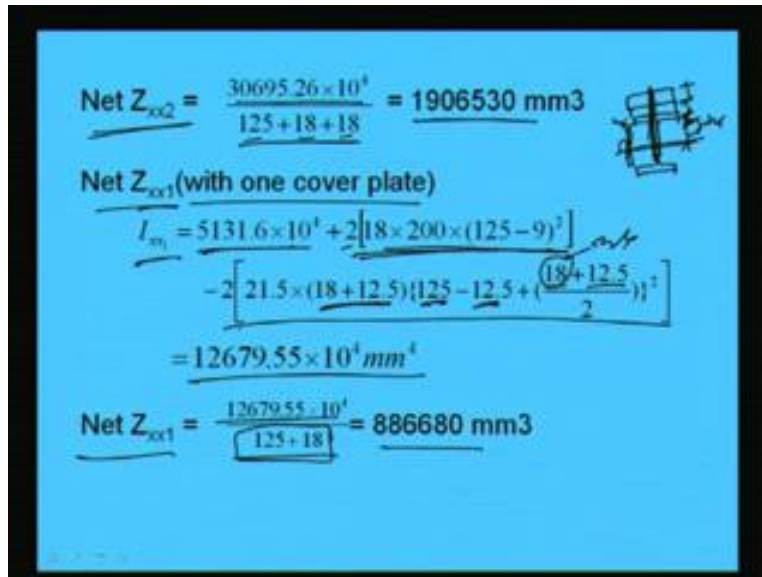
$$= 34595.2 \cdot 10^4 - 2 \left[ \underbrace{21.5}_{d+d+tf} \cdot (18 + 18 + 12.5) \left( 125 - 12.5 + \frac{18 + 18 + 12.5}{2} \right)^2 \right]$$

$$= 30695.26 \times 10^4 \text{ mm}^4$$

Now, we have to find out the net  $Z_{xx}$   $Z_{xx} / 2$  with 2 cover plate right. As we know gross moment of inertia is this which has been calculated earlier 345952600 millimeter to the 4. So, net will be gross minus moment of inertia of rivet holes right. So, net let us find out. So, gross minus moment of inertia of rivet hole rivet hole is given here that is diameter into depth, depth means 2 plates were there. So, 18 plus 18 plus thickness of flange right  $d$  plus  $d$  plus  $tf$  this is the thing.

So, this is the area into  $A r$  square. So,  $A r$  square when we are going to make 125 minus 12.5 plus 18 plus 18 plus 12 point 5 by 2 whole square right. So; that means,  $A r$  square we are making. So, deduction of hole we are making use for calculation of the net moment of inertia. So, after calculating we are getting 30695.26 into 10 to power 4 millimeter to the 4. So, net moments of inertia about  $xx$  direction are calculated which is 30695.26 into 10 to power 4 millimeter to the 4 right.

(Refer Slide Time: 44:25)



$$\text{Net } Z_{xx2} = \frac{30695.26 \times 10^4}{125 + 18 + 18} = 1906530 \text{ mm}^3$$

$$\text{Net } Z_{xx1} \text{ (with one cover plate)}$$

$$I_{xx} = 5131.6 \times 10^4 + 2 \left[ 18 \times 200 \times (125 - 9)^2 \right] - 2 \left[ 21.5 \times (18 + 12.5) \left( 125 - 12.5 + \frac{(18 + 12.5)}{2} \right)^2 \right]$$

$$= 12679.55 \times 10^4 \text{ mm}^4$$

$$\text{Net } Z_{xx1} = \frac{12679.55 \times 10^4}{125 + 18} = 886680 \text{ mm}^3$$

Next what we will do next. So, we can find out  $Z_{xx2}$ .  $Z_{xx2}$  will be  $I_{xx}$  net by  $y$  right.  $I_{xx}$  net is calculated here 30695.26 and this is the  $y$  125 plus 18 plus 18, because if we see say this is I section. Now, there is 1 plate another plate. So, this is 18 this is 18 and this is 12.5. This is not required because this is 125 from here to here we have to calculate right to extreme fiber. So,  $Z_{xx2}$  is becoming 1906530 millimeter cube.

Similarly,  $Z_{xx1}$  will become means for 1 cover plate with 1 cover plate if you want to calculate the section modulus let us calculate in similar way. So,  $I_{xx1}$  will become say this is the  $I_{xx}$  of the I section then for 1 plate right for 1 plate. This is 2 into  $A r$  square minus this is the due to hole because of hole in similar way we have calculated. That is minus 2 into 21.5 into 18 plus 12.5 this is the thickness into 125 minus 12.5 plus 18 plus 12.5 by 2. Remember this was 36 for 2 cover plates and this is 18 for 1 cover plate right. So, this is the change.

So,  $I_{xx1}$  we are getting 12679.55 into 10 to power 4 millimeter to the 4 right. So, in this way we can find out net  $Z_{xx1}$ . So,  $Z_{xx1}$  will become  $I_{xx1}$  by  $y$  bar. So, in this case  $y$  bar will be 125 plus 18 because single plate we are going to use. So, we are going to get net  $Z_{xx1}$  has 886680 millimeter cube. So, I hope you have understood that how to find out the  $Z_{xx1}$   $Z_{xx2}$ . And similarly, now we will find out L 1 right.

(Refer Slide Time: 47:11)

$$\begin{aligned}L_2 &= L \sqrt{(Z_{xx2} - Z_{xx1}) / Z_{xx2}} \\ &= 7 \sqrt{(1906.53 \times 10^3 - 886.68 \times 10^3) / (1906.53 \times 10^3)} \\ &= 5.12 \text{ m.} \\ X_2 &= (L - L_2) / 2 = (7 - 5.12) / 2 = 0.94 \text{ m.} \\ \text{Moment of resistance of the section with one} \\ \text{curtail plate} &= \sigma_{bt} \times Z_{xx1} \\ &= 165 \times 886680 \\ &= 146302200 \text{ N-mm} \\ M_r &= 146.3 \text{ kNm}\end{aligned}$$

So, from the formula as we know we have discussed in last class that  $L_2$  will become  $L$  into square root of  $Z_{xx2}$  minus  $Z_{xx1}$  by  $Z_{xx2}$  right. So, from that if we put those value  $L$  is 7  $Z_{xx2}$  is 1906.53 into 10 cube.  $Z_{xx1}$  is 886.68 into 10 cube by  $Z_{xx2}$  that is 1906.53 into 10 cube. So, if we make this we are going to get  $L_2$  is equal to 5.12 meter. So,  $L_2$  we are going to make 5.12 meter. So,  $X_2$  will become  $L$  minus  $L_2$  by 2 right. So,  $L$  is 7 and  $L_2$  is 5.12. So, this is becoming 0.94 right.

So, plate length the upper plate length was 5.12. So,  $X_2$  means curtailment from 1 side we can find out as 0.94 meter. Now, moment of resistance of the section with 1 curtail plate can be calculated as  $\sigma_{bt}$  into  $Z_{xx1}$  which is becoming 165 into 886680. That is this 146302200 Newton millimeter. That means we can find out as 146.3 kilo Newton meter right. So,  $M$  with 1 curtail plate the moment of resistance will become 146.3 kilo Newton meter with 1 curtail plate say  $M_r$ .

(Refer Slide Time: 49:14)

Average stress in curtailed plate

$$= \frac{146302.2 \times 10^3}{1906.53 \times 10^3} \times \frac{(125 + 18 + 18) - 9}{125 + 18 + 18}$$

= 72.44 N/mm<sup>2</sup>.

Force at the curtailed section = 72.44 × 200 × 18  
= 260812 N

Let us provide 20mm power driven rivets .  
Gross diameter = 20 + 1.5 = 21.5mm

So, average stress in curtailed plate can be find out that will become like this. That is the M we found out here 14630. So, M by I into this ... So, if we make this calculation of this I is 1906, I means Z 1906.53 M by Z; so M by Z into this to get the average stress right. So, we are getting 72.44 Newton per millimeter square. And force at the curtailed section will become this 1 that is the average stress into area that is 200 into 18. So, this is the force of the curtailed section. So, now if we provide 20 mm power driven soft rivets then we can find out the number of rivets required for this. So, gross diameter as we are using twenty mm diameter of rivets. So, gross diameter will become 21.5 mm.

(Refer Slide Time: 50:38)

Value of rivets in single shear =  $\frac{\pi}{4} \times 21.5^2 \times 100$   
= 36305.03 N

Value of rivets in bearing =  $21.5 \times 12.5 \times 300$   
= 80625 N

Value of rivet,  $R_v = 36305.03 \text{ N} = 363 \text{ kN}$

Number of additional rivets =  $\frac{260812}{36305.03}$   
= 7.18 (say 8)

Provide 8 rivets, 20mm diameter in two rows

Minimum pitch =  $2.5 \times 20 = 50 \text{ mm}$ .

So, with this we can find out the number of rivets because as we know value of rivets in single shear. The rivet value will become simple pi by 4 into D square into tau vf right and tau vf will be hundred. So, after calculation we will get the rivet value as 36305.03 Newton as a single shear. And from bearing point of view similarly sigma Pf into D into t if we make that will be becoming 80625 Newton.

So, from this 2 the lesser value will be will be the rivet value that is 363.3 kilo Newton right. And then number of rivet will be required the force whatever it is coming by the rivet value. So, this is becoming 7.18 say let us use 8. Now, let us ... So, provide 8 rivets of 20 mm diameter in 2 rows and minimum pitch will be 2.5 into 20 that is 50 mm right. So, providing 8 rivets of 8 rivets of 20 mm diameter in 2 rows we can use pitch as 50 mm right.



(Refer Slide Time: 52:00)

For 20mm diameter rivets minimum edge distance is 29mm  
Let us provide a 30mm edge distance  
Extra length of cover plate =  $(50 + 3 \times 30) \times 2$   
= 280mm  
Total length of top cover plate =  $5.12 + 0.28$   
= 5.4 m.

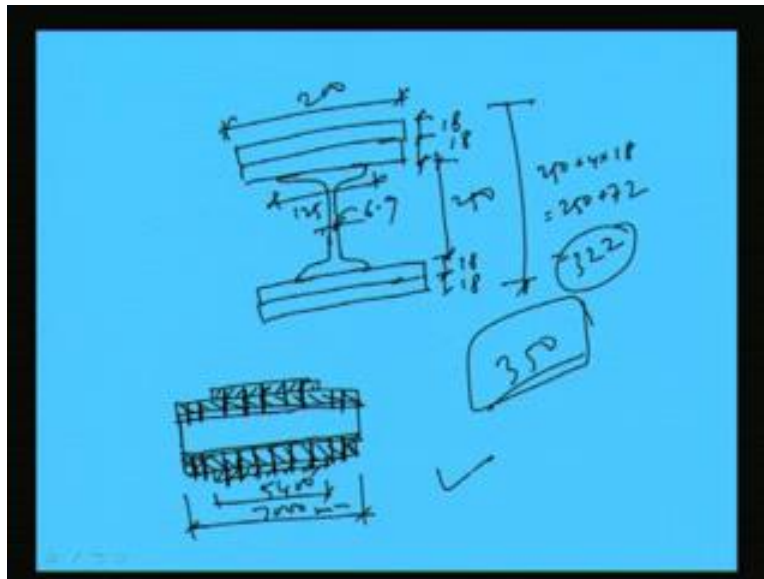
Then for 20 mm diameter rivets minimum edge distance is given as per codal provision as 20 9 mm. So, let us provide a 30 mm edge distance. So, the extra length of cover plate will become 50 plus 3 into 30 because 2 rows we have given into 2; so 2 80 mm. Therefore, the total length of top cover plate will become 5.12 plus 0.2828 means 28 mm 280 mm. So, this is becoming 5.4 meter.

(Refer Slide Time: 52:43)

Thus, the details of the built-up section is as follows:  
Use ISMB 250  
Plate size 18 x 200 x 7000 mm at top & bottom throughout at top & bottom (1<sup>st</sup> cover plate)  
Plate size 18 x 200 x 5400 mm at top & bottom throughout at top & bottom (2<sup>nd</sup> cover plate)  
Provide 8-20Φ PDS rivets in two rows with a pitch of 50 mm and edge distance of 30 mm

So, finally, what we are getting the details of built-up section can be like this. Say use ISMB 250. And let us use plate size 18 by 200 by 700 mm at top and bottom throughout at the top and bottom throughout. This is first cover plate and and plate size of 18 mm by 200 mm by 540 mm 5400 mm at top and bottom throughout for the second cover plate. And provide 8 number of rivets of 25 diameter power driven soft rivets in 2 rows with a pitch of 50 mm and edge distance of 30 mm. So, these are the gist of the design results.

(Refer Slide Time: 53:40)



So, now if you see the drawing we can say this is the I section. So, this is the I section now we are going to provide 2 plate of this right. And this will be 200 this will be 18 and 18 and this is 250 this is 18, 18 right and this is 6.9. So, and this is 125. So, total depth of the section is becoming 250 plus 4 into 18; that means, 250 plus 72; that means, 322 and restriction was 350. So, within the restricted depth we could find out a suitable built-up section. And across the length if we see the sections will look like this.

Say this is the I section a cover plate is given here at top and at bottom and I section this is the flange right. And another plate is given here at top and bottom with some curtailment. So, this is 700, 5400 millimeter means 5.4 meter and this is 7000 millimeter. So, this is how the plate is given. So, this 1 plate and this is another this is another plate. The first plate is the first plate is 7 meter and second plate is 5.4 meter right. So, I can

make like this right. And of course, we have to provide some rivet and rivet numbers we have already decided pitch we have decided accordingly we have to make it right.

So, these are all rivets we have provided as per the design calculations. So, this number has to be made properly or we have to inform here. So, in this way built-up sections can be designed. I hope though it is very quickly I made it, because of restriction of time. I hope you have some idea how to find out a suitable section for designing a built-up member. Now, with this I like to conclude today's lecture.

Thank you very much for your patience.