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NATIONAL PROGRAMME ON
TECHNOLOGY ENHANCED LEARNING

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Geotechnical
Engineering
Laboratory

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Department of civil engineering, IIT Bombay

Lecture No – 22
Consolidation

So you know for this particular loading.

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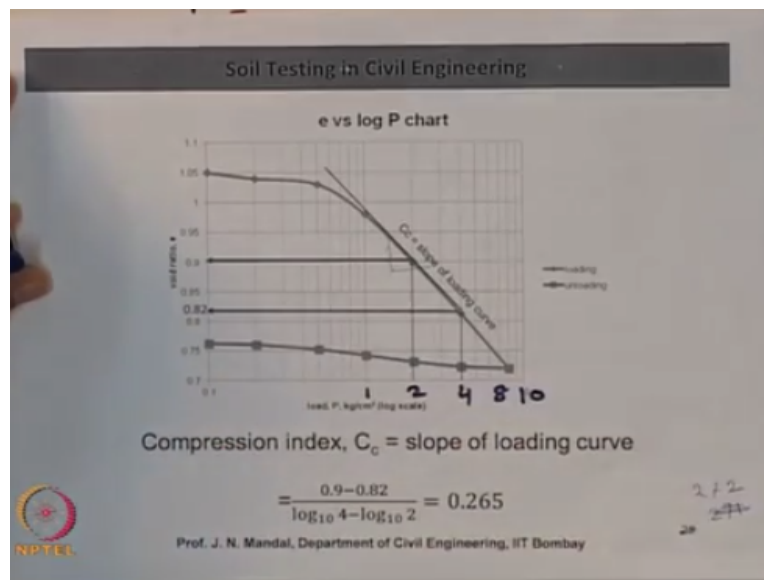
Soil Testing in Civil Engineering									
Specimen calculations for consolidation test :									
	Load applied (kg/cm ²)	Final dial gauge reading (mm)	Compression, d, (mm)	Height of voids, h _v = (h _w - d)	Void ratio e = h _v /h _s	Δe	Δσ' (kg/cm ²)	a _v (cm ² /kg)	m _v (cm ³ /kg)
loading	0.0	16.865	-	13.06	1.09	-	-	-	-
	0.1	16.434	0.431	12.629	1.05	-0.040	0.1	0.4	0.191
	0.2	16.243	0.622	12.438	1.04	-0.010	0.1	0.1	0.048
	0.5	16.101	0.764	12.305	1.03	-0.010	0.3	0.03	0.016
	1.0	15.539	1.326	11.734	0.98	-0.050	0.5	0.1	0.048
	2.0	14.662	2.203	10.857	0.90	-0.080	1	0.08	0.038
	4.0	13.517	3.348	9.712	0.813	-0.087	2	0.04	0.021
	8.0	12.410	4.455	8.605	0.72	-0.093	4	0.02	0.011
	4	12.443	4.422	8.386	0.723	0.003	-4	0	0.000
	2	12.543	4.322	8.738	0.731	0.008	-2	0	0.002
Unloading	1	12.667	4.198	8.862	0.742	0.011	-1	0.01	0.005
	0.5	12.791	4.074	8.986	0.752	0.010	-0.5	0.02	0.010
	0.2	12.890	3.975	9.085	0.760	0.008	-0.3	0.03	0.013
	0.1	12.909	3.956	9.104	0.762	0.002	-0.1	0.02	0.010
	0.0	13.410	3.455	9.605	0.804	0.042	-0.1	0.42	0.201

How to calculate the void ratio and how you can calculate the range of void ratio and the A_v, B_v and the M_v similarly you can calculate for different applied loading that mean in 0.2, 0.02 and then 0.6, 1, 2, 4 and weight so now we will draw the relationship between the applied load okay that is from 0, 0.1, 0.2 like that up to 8kg/ cm² verse that void ratio, so what should be the change

of the void ratio that means you know the void ratio we have calculated here the void ratio that is the e value.

So we know that what is e value so e value here is starting from this is 1.09 to up to 8kg/cm² load is 0.72 okay so x axis's will be the loading from point 1, 2, 8 kg/cm² and correspondingly this void ratio will be from 1.09 to up to this is 0.72 so you can say this coloration and representing here in the form of graph so this is the load applied.

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That is P kg/cm² this is log s scale, so this I say at 1, 2, 4, 8 like this, this is load in the x axis's kg/cm² load P is applied and this y axis's is the void ratio so void ratio is staring from here.

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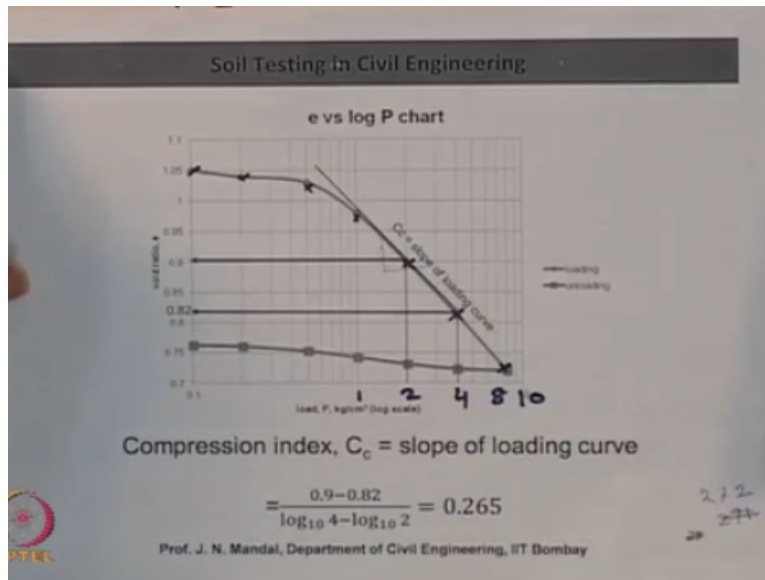
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	0.1	16.434	0.431	12.629	1.05	-0.040	0.1	0.4	0.191
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	0.0	13.410	3.455	9.605	0.804	0.042	-0.1	0.42	0.201

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You can see that void ratio it is bases 0.72 and correspondingly load 8, then this void ratio correspondingly load this so like this up to 1.09.

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So this is 1.5 under the load of 0.1 so you know the load and you know what is the corresponding void ratio, so e can have this different point like this under different and so this is the load okay and this is the reloading card so when you are reloading.

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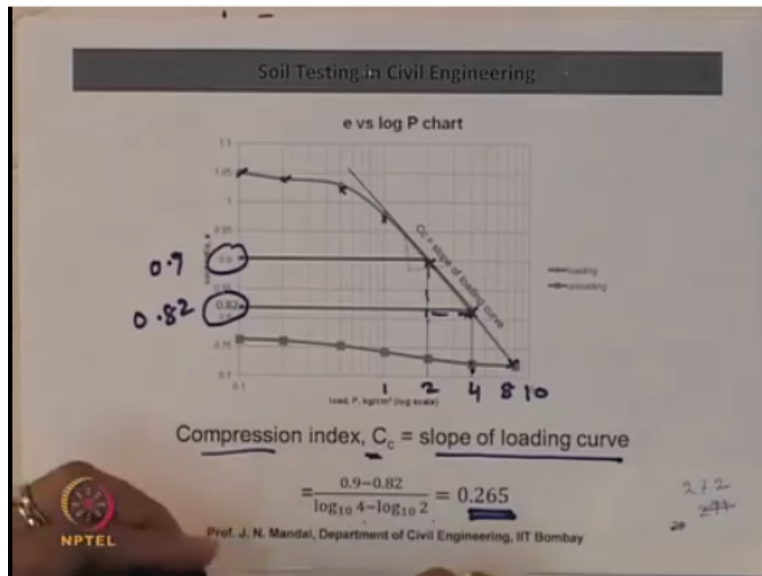
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	0.5	16.101	0.764	12.305	1.03	-0.010	0.3	0.03	0.016
	1.0	15.539	1.326	11.734	0.98	-0.050	0.5	0.1	0.048
	2.0	14.662	2.203	10.857	0.90	-0.080	1	0.08	0.038
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	8.0	12.410	4.455	8.605	0.72	-0.093	4	0.02	0.011
	4	12.443	4.422	8.386	0.723	0.003	-4	0	0.000
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	1	12.667	4.198	8.862	0.742	0.011	-1	0.01	0.005
	0.5	12.791	4.074	8.986	0.752	0.010	-0.5	0.02	0.010
	0.1	12.890	3.975	9.085	0.760	0.008	-0.3	0.03	0.013
	0.1	12.909	3.956	9.104	0.762	0.002	-0.1	0.02	0.010
	0.0	13.410	3.455	9.605	0.804	0.042	-0.1	0.42	0.201

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This unloading these again here that from starting from here it is here it is starting from this 4 to 0.1 and correspondingly void ratio so you have this curve.

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So you can draw the curve like this okay curve like this so this is the which you call the e log p curve that is e verse log P curve and from this e log P curve this part is the loading and this part is unloading okay so you can see from the e log P curve and this portion in the straight line, so you take a slope of this loading curve, so if this is the slop of the reading loading curve so this slope you can determine what is compression index so compression index that is designated as C_c okay.

This is compression index designate C_c – slope of the loading curve so you can see take this 2 point so when it is if you take this point and the void ratio is 0.9 here 0.9 this is 0.9 and when this value you have to take this point then your void ratio is 82 0.82 that means when you are taking that load is reload is 2 kg / cm² your having the void ratio value here it is 0.9 that is this is 0.9 so this is 0.9 and when the applied load is 4 kg / cm² and then you having this void ratio is 0.82 so you are writing 0.82.

This under the log of this is 4 – log of this 2 so if you calculate this 0.9 – 0.82 log of 4 – log of 2 is get this compression index that is 0.265 okay so from this e log P curve you can calculate that what will be the compression index and that is what is called the C_c this is important parameter to determine the settlement of any curve.

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Elapsed time in minutes	t	Load increment in kg/cm ²					
		0.1-0.2	0.2-0.5	0.5-1.0	1.0-2.0	2.0-4.0	4.0-8.0
	min	Dial gauge reading					
0.00	0	16.434	16.243	16.101	15.539	14.662	13.517
0.25	0.5	16.392	16.180	16.007	15.116	13.989	12.941
1.00	1	16.378	16.173	15.939	15.002	13.888	12.828
2.25	1.5	16.362	16.169	15.891	14.930	13.813	12.744
4.00	2	16.349	16.167	15.858	14.884	13.757	12.682
6.25	2.5	16.339	16.163	15.832	14.850	13.716	12.634
9.00	3	16.325	16.162	15.813	14.820	13.686	12.598
12.25	3.5	16.318	16.161	15.796	14.806	13.664	12.571
16.00	4	16.312	16.160	15.783	14.790	13.630	12.550
20.00	5	16.299	16.156	15.761	14.785	13.617	12.521
24.00	6	16.291	16.151	15.742	14.745	13.596	12.501
28.00	7	16.281	16.147	15.726	14.727	13.580	12.484
32.00	8	16.268	16.141	15.711	14.715	13.567	12.470
36.00	9	16.261	16.133	15.696	14.701	13.556	12.456
40.00	10	16.252	16.123	15.681	14.675	13.542	12.420
400.00	37.9	16.243	16.101	15.539	14.662	13.517	12.410

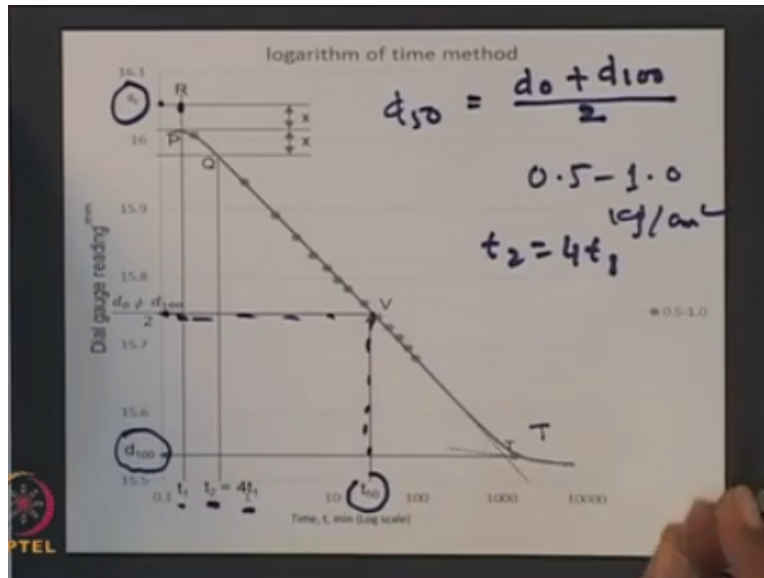
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I can show you here another table that is this is the elapsed time okay it is starting from 0, 0.25 to up to 400 40 that is minutes and this is root of t root of time so if you do the root of time you can have this value these are the further root of t okay and this is the load increment under that is 0.1 to 0.2 kg/ cm² so what are the reading similarly for this 0.2 to 0.5 kg/ cm² then 0.5 to 1 kg/ cm² what you dual gauge reading.

The 1 to 2 kg / cm² is called load applying then what will be the dual gauge reading and 2 to 4 kg/ cm² what is the dual gauge reading and then 4 to 8 kg/ cm² what are the dual gauge reading here from this table we wanted to draw the what should be the dual gauge reading and corresponding the time root t that is this is the dual gauge reading and this is the root of t value t time value that means we have to draw a correlation between the time and the dual gauge reading.

So here it is the dual gauge reading okay and here it is the root of t time, so I am saying that how you can draw a correlation between that time and the dual gauge reading.

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So here the time x axis's is the time so this is the time okay and this is the dial gauge reading this is log time in log s scale okay and this the different dial gauge reading so you know that what should be the dial gauge reading you know is the time so correspondingly you can draw this curve so this curve will be like this okay, so this is call the logarithm of time method from the logarithm of time method how you can calculate that what will be the degree of consultation and this logarithm time method for a loading of 0.5.to 1 kg / cm² under this loading.

So this curve is 0.5 to 1 kg / cm² under this loading what will be the time that is t in minutes and this dial gauge reading you can draw a curve line that so you have to calculate that what should be the coefficient of consolidation that is logarithm of trim method, so form this curve you know this is the dual reading and this is the time in the log scale so you plot the dial gauge reading verses time curve on a similar graph paper first.

And then secondly you choose plot P and the Q, P and Q on the curve corresponding to time this is t₁ and this is t₂ such that t₂ will be equal to 4 of t₁ so t₂ will be equal to 4t₁ so you have to choose the point P and Q if P is t₁ and Q will be t₂ will be equal to 4 of t₁ now differences is number 3 the difference between this dial gauge reading corresponding to P and the Q let us say is x here which is being and x if it is a x mark a point R here mark a point R okay here such that P of R is equal to x that means P R = x.

So P Q = x and PR = x so dial gauge reading corresponding to R this R each d₀ so it is called d₀ this d₀ okay and this d₀ is for 0% consolidation now fourthly you draw a tangent to the curve here

you can see curve is like this so you draw a tangent on curve tangent on the curve and intercepting at the point t here is the t point at the point t and corresponding dial gauge reading here that is d of 100 and this reading d 100 corresponding to 100% consolidation so here it is the 0% consolidation d_0 .

Here it is the 100% consolidation by the logarithm of time method you can determine that 100% consolidation apart from this 100% consolidation you can also draw for the 50% also consolidation that means you can also calculate what will be the d of 50 okay so d of 50 will be equal to $d_0 + \frac{d_{100} - d_0}{2}$ okay so that means we know d_0 you know d_{100} so $d_0 + \frac{d_{100} - d_0}{2}$ that means it is the 50% that means time is equal to t_{50} and correspondingly you can calculate that what will be the 50% also d of 50 we can calculate. So from this curve you can calculate that what should be the coefficient of consolidation.

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Elapsed time in minutes	t	Load increment in kg/cm ²					
		0.1-0.2	0.2-0.5	0.5-1.0	1.0-2.0	2.0-4.0	4.0-8.0
	min	Dial gauge reading					
0.00	0	16.434	16.243	16.101	15.539	14.662	13.517
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4.00	2	16.349	16.167	15.858	14.884	13.757	12.682
6.25	2.5	16.339	16.163	15.832	14.850	13.716	12.634
9.00	3	16.325	16.162	15.813	14.820	13.686	12.598
12.25	3.5	16.318	16.161	15.796	14.806	13.664	12.571
16.00	4	16.312	16.160	15.783	14.790	13.630	12.550
25.00	5	16.299	16.156	15.761	14.765	13.617	12.521
36.00	6	16.291	16.151	15.742	14.745	13.596	12.501
49.00	7	16.281	16.147	15.726	14.727	13.580	12.484
64.00	8	16.268	16.141	15.711	14.715	13.567	12.470
81.00	9	16.261	16.133	15.696	14.701	13.556	12.456
100.00	10	16.252	16.123	15.681	14.675	13.542	12.420
37.9	37.9	16.243	16.101	15.539	14.662	13.517	12.410

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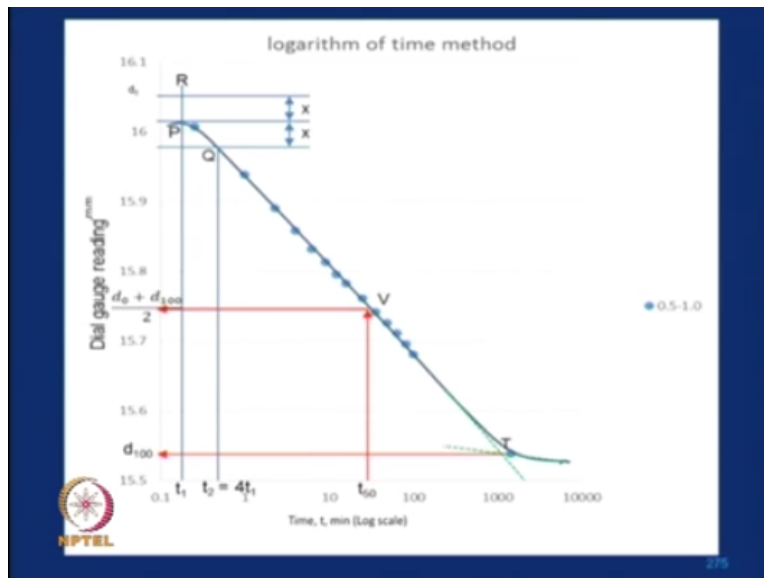
So coefficient consolidation that is call the c of v so have to calculate that c of v so C of v you know that.

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$$C_v = \frac{0.197 H^2}{t_{50}} \quad (6)$$
$$T_v = 0.197 \text{ for } 50\%$$

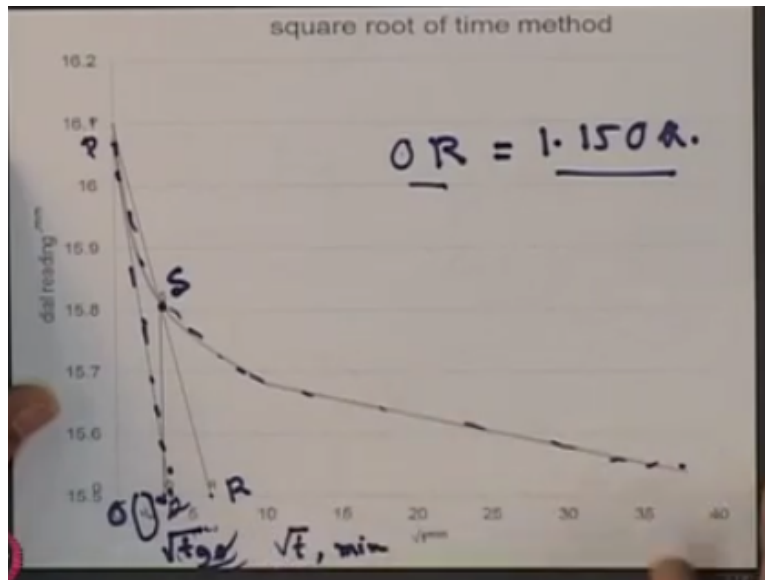
Earlier we have discussed this coefficient of consolidation is 0.197 in H^2 this divided by t_{50} let us say for 50 and for the 50% consolidation then T_v value = 0.197 so you know what T_v 0.197 for 50% consolidation and this t_{50} that time okay for 50 so from this data you can calculate what will be the coefficient of consolidation you know that height you know that what is t_{50} which we can determine time so you can calculate that what will be the coefficient of consolidation from this time logarithm plot okay. So you can calculate, now this is one method to calculate the coefficient of the consolidation.

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Now you can draw the square root of time method this another method okay you have to calculate the coefficient of consolidation by square root of time method.

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So here this y axis is the dial gauge reading and x axis is the root of t in minute this is root of t this is in minute so from the plot or table so I have shown you what is root of time that is 0, 5, 10, 15, 20, 35 etc and correspondingly dial gauge reading so you know the what you target region so you can draw a curve is like that this is for the course square root of the time fitting method, so what the dial gauge verse square root time curve on a graph now draw a tangent okay this tangent you draw a tangent that is P and Q this is Q and this is P.

So the curve is like this okay and you draw a tangent like this that is P of this is Q okay this is P, Q and draw another line this is P and this is R another line starts that this OR will be equal to 1.15 of OQ that means this will be O of R will be equal to 1.15 O of Q that means this is O OR will be 1.15 of O of Q so mark this point is this is the s where PR intersect the curve and S is of the S this axis are of the S okay where the PR intersects the curves so axis of the S give the her axis of the which will give the t of 90 root of t 90 so this give the root of t of 90 okay.

So then you can calculate that what will be the coefficient of consolidation from the square root of time method we can calculate for the root of t 90 okay.

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Soil Testing in Civil Engineering

Calculations for coefficient of consolidation:

Square root of time method

1. Plot the dial gauge reading vs square root time curve on a graph.
2. Draw tangent PQ.
3. Draw another line PR such that $OR = 1.15OQ$
4. Mark point S where PR intersect the curve. Abscissa of S gives \sqrt{t}_{90} .

$$C_v = \frac{0.848H^2}{t_{90}} = \frac{0.848 \times \left(\frac{25}{2}\right)^2}{9} = 14.72 \text{ mm}^2/\text{min}$$

($T_v = 0.848$ for 90% consolidation, $\sqrt{t}_{90} = 3$, $t_{90} = 9$ min)

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So how to calculate the coefficient of consolidation for 90%, degree of consolidation.

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$$C_v = \frac{0.848 H^2}{t_{90}} = \frac{0.848 \times \left(\frac{25}{2}\right)^2}{9} = 14.72 \text{ mm}^2/\text{min.}$$

$T_v = \frac{0.848}{\sqrt{t_{90}}} = 3$ for 90% Consolidation.
 $t_{90} = 9 \text{ min.}$

So we know this coefficient consolidation this is $0.848 \times H^2 / t_{90}$ okay so you know this is 848 that is $t_b = 1$ you know that $t_b = 0.848$ for 90% consolidation okay these value you know and you have to calculate that what should be the corresponding of t of 90 okay so then you can calculate the what is t_{90} so first you can calculate that coefficient of consolidation let us say that height of the sample is 25 so this will be equal to $25/2$ this is both way then is and this divided by we have to calculate what is t_{90} .

Okay so root of t_{90} you can have this value is about 3 so t_{90} value will be equal to 9 that is minute so t_{90} value will be equal to 9 here so from this equation you can calculate the coefficient of consolidation about 14.7 to this is mm^2/min okay so we can calculate the 90% consolidation so from this square root of time method you can calculate the 90% of consolidation what else that earlier I showed you that method you can calculate the 100% degree of consolidation 50% degree of consolidation okay Now how to calculate the pre consolidation pressure okay.

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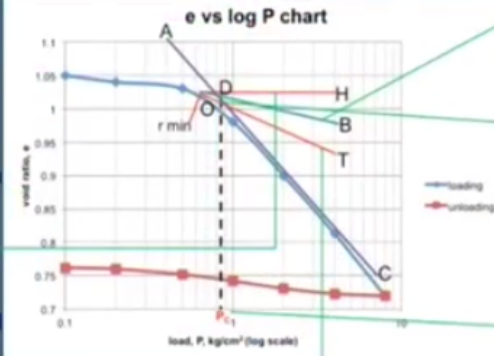
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Determination of preconsolidation pressure

1. Locate a point O such that radius of curvature is minimum

2. Draw a horizontal line OH from the point O

3. Draw a tangent OT from the point O



4. Bisect angle TOH

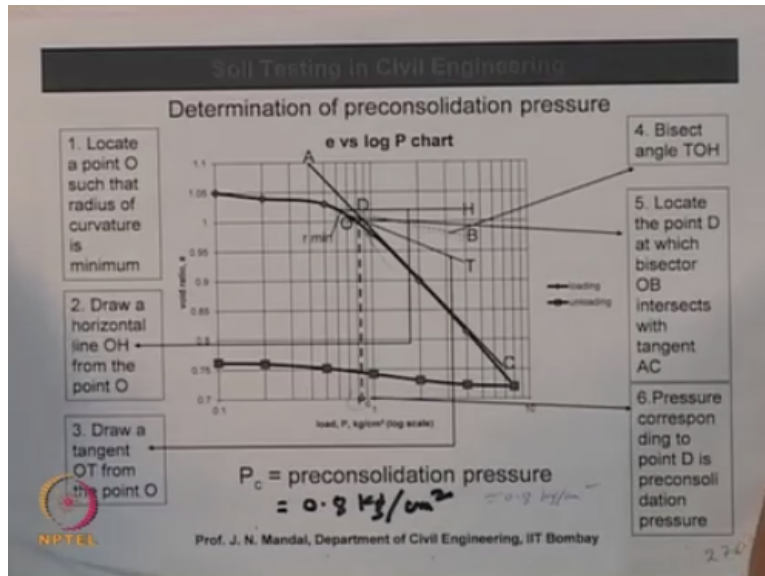
5. Locate the point D at which bisector OB intersects with tangent AC

6. Pressure corresponding to point D is preconsolidation pressure

$P_c =$ preconsolidation pressure

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So this is the curve which is the curve which you called e verse log P so x axis is the log P that is load applied in the log scale and kg/cm^2 that is 0.1 this is 1 to this is 10 and this is the void ratio that is e so form the earlier table so you can draw that e log p curve this is the curve tit is like this the curve this is like this unloading this is loading and then it is the unloading curve so you can have a curve like this okay so this all the void ratio verse load curve in the log s scale so you have to determine that what will be the pre consolidation ratio so first you can see the curve is like this first you locate the point O here such that radius of the curvature is minimum okay.

And then you draw a horizontal line to draw a horizontal line okay OH from the point O we are dawning horizontal line and draw the tangent that is O T either tangent from the point O and then you bisect the angle TOH you bisect the angle and locate the point D at which bisect OB look at this point bisect OB intersect with the tangent this is the tangent AC okay then the pressure corresponding to the point D is call the reconsolidation pressure.

So from this curve you can determine that P consolidation pressure so you know that how to calculate the P consolidation pressure and P consolidation pressure is designated at that P of C and here that P consolidation pressure is somewhere here okay so this is 0.1 this is 1 so here p consolidation pressure is about 0.8 kg/cm^2 so we can write that P consolidation pressure is equal 0.8 kg/cm^2

So in this consolidation test so we can determine that logarithm that square root of time method logarithm method or the determination of the coefficient of consolidation and you can also

determine that P consolidation pressure so this consolidation chapter is very important so we have learnt how to have to take the reading dual gauge reading or the different timing under the different loading of the load is increment it goes up to the 49 40 minutes and again you go for incremental loading and it continue like that okay.

And from the dual gauge reading time method you can calculate that part should be the void ratio you can calculate the what will be the change of void ratio you can calculate the what is the AV you can calculate the what is the MV and from this table you calculate that what is either relationship for the e and $\log P$ and how to calculate that compression index that is TC and apart from the C_c from the curve that is load verses the time or the dual gauge reading you have also can calculate that part will be the degree consolidation okay.

Under the two verse style and you also can calculate that P consolidation pressure that is void ratio verse the \log of P curve and you can determine the P consolidation pressure so now you have an idea in the consolidation that how you can determine and then how we can also calculate the settlement and also you can calculate that what should be the coefficient of permeability and coefficient permeability can be determined by the consolidation test even indirect method.

But if you know that what should be the void ratio what should be the C_c value compression index value and then you can also calculate that what will be the settlement and in this consolidation chapter because settlement is very important you know the settlement equation and from this consolidation test may though you can determine that what is the compression index that is C_c you can determine the what would be the void ratio and you know that under different loading then you can calculate the what will be consolidation settlement of the soil apart from consolidation settlement you can also determine the P consolidation pressure thank you.

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**Online Editor
& Digital Video Editor
Tushar Deshpande**

**Digital Video Cameraman
& Graphic Designer
Amin B Shaikh**

**Jr. Technical Assistant
Vijay Kedare**

**Teaching Assistants
Ankita Kumar
Sunil Ahiwar
Maheboobsab Nadaf
Aditya Bhoi**

**Sr. Web Designer
Bharathi Sakpal**

**Research Assistant
Riya Surange**

**Sr. Web Designer
Bharati M. Sarang**

**Web Designer
Nisha Thakur**

**Project Attendant
Ravi Paswan
Vinayak Raut**

**Music
Stardust Sandwich-
by smilingcynic**

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