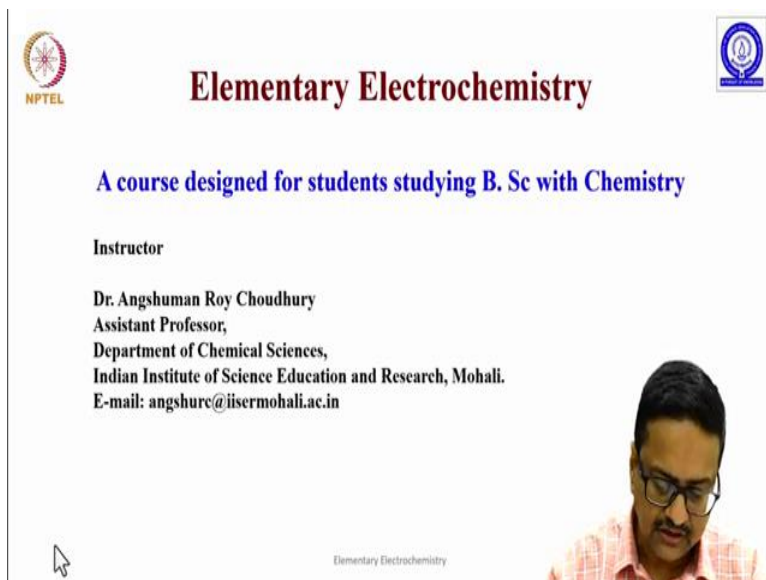


Elementary Electrochemistry
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Lecture 34
Solubility and Activity Product

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Elementary Electrochemistry

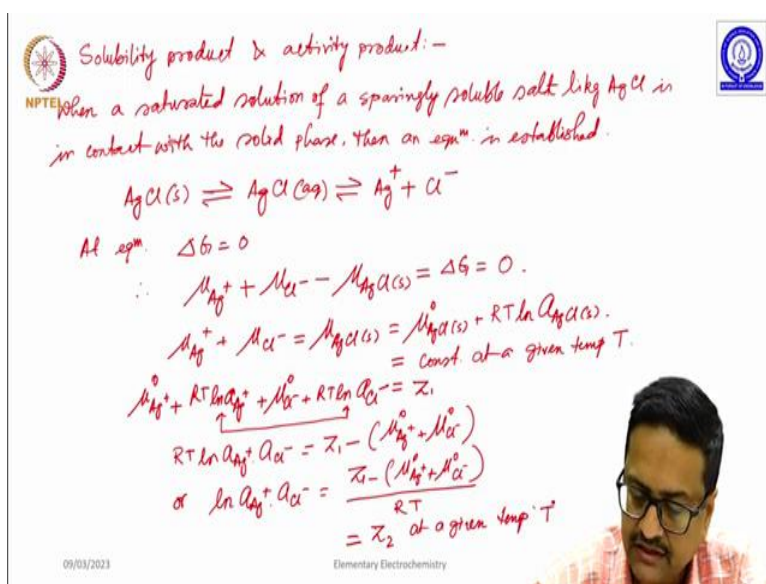
A course designed for students studying B. Sc with Chemistry

Instructor

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Welcome back to the course entitled Elementary Electrochemistry we are in the seventh week of this course and we are almost towards the end of the contents. So, today we are going to discuss how one can calculate or determine the ionic product or the other the solubility product or activity solubility product of a sparingly soluble electrolyte using the concepts that we have learned.

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Solubility product & activity product: -

When a saturated solution of a sparingly soluble salt like AgCl is in contact with the solid phase, then an eqm. is established.

$$\text{AgCl}(s) \rightleftharpoons \text{AgCl}(aq) \rightleftharpoons \text{Ag}^+ + \text{Cl}^-$$

At eqm. $\Delta G = 0$

$$\therefore \mu_{\text{Ag}^+} + \mu_{\text{Cl}^-} - \mu_{\text{AgCl}(s)} = \Delta G = 0.$$

$$\mu_{\text{Ag}^+} + \mu_{\text{Cl}^-} = \mu_{\text{AgCl}(s)} = \mu_{\text{AgCl}(s)}^\circ + RT \ln a_{\text{AgCl}(s)}.$$

$= \text{const. at a given temp } T.$

$$\mu_{\text{Ag}^+}^\circ + RT \ln a_{\text{Ag}^+} + \mu_{\text{Cl}^-}^\circ + RT \ln a_{\text{Cl}^-} = \mu_{\text{AgCl}(s)}^\circ$$

$$RT \ln a_{\text{Ag}^+} a_{\text{Cl}^-} = \mu_{\text{AgCl}(s)}^\circ - (\mu_{\text{Ag}^+}^\circ + \mu_{\text{Cl}^-}^\circ)$$

$$\text{or } \ln a_{\text{Ag}^+} a_{\text{Cl}^-} = \frac{\mu_{\text{AgCl}(s)}^\circ - (\mu_{\text{Ag}^+}^\circ + \mu_{\text{Cl}^-}^\circ)}{RT}$$

$= X_2 \text{ at a given temp } T$

So, we will discuss today the determination of solubility product and activity product. So, when a saturated solution of a sparingly soluble salt like AgCl is in contact with the solid phase then an equilibrium is established. So, what is that equilibrium? The equilibrium is AgCl solid is in equilibrium with AgCl aquatic and further there is an equilibrium between the dissociated Ag plus and Cl minus.

So, at equilibrium ΔG for this reaction is 0, so then one can write that $\mu_{\text{Ag}} + \mu_{\text{Cl}} - \mu_{\text{AgCl solid}}$ is equal to ΔG is equal to 0. So, now we rewrite this equation as $\mu_{\text{Ag}} + \mu_{\text{Cl}} - \mu_{\text{AgCl solid}}$ is equal to $\mu_{\text{AgCl solid}}$ which then can be written as $\mu_{\text{AgCl solid}} + RT \ln \text{activity of AgCl solid}$, this quantity on the right-hand side is a constant quantity at a given temperature t . So, suppose we write this constant as Z_1 and the left-hand side we can rewrite as $\mu_{\text{Ag}} + \mu_{\text{Cl}} - \mu_{\text{AgCl solid}}$ plus $RT \ln \text{activity of Ag plus}$ plus $RT \ln \text{activity of Cl minus}$.

So, now we can further rewrite by taking these two quantities together we can write $RT \ln \text{activity of Ag plus} + RT \ln \text{activity of Cl minus}$ equal to $Z_1 - \mu_{\text{AgCl solid}}$ or $\ln \text{activity of Ag plus} + \ln \text{activity of Cl minus}$ equal to $Z_1 - \mu_{\text{AgCl solid}}$ divided by RT which is again another constant say Z_2 at a given temperature t .

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$a_{\text{Ag}^+} a_{\text{Cl}^-} = e^{Z_2} = \text{const. at a given temp } T$
 This product is called the activity product of AgCl, written as L_a .
 $\therefore L_a = a_{\text{Ag}^+} a_{\text{Cl}^-} = e^{Z_2}$
 Using molar conc.,
 $L_a = (C_{\text{Ag}^+} \cdot f_{\text{Ag}^+}) \times (C_{\text{Cl}^-} \cdot f_{\text{Cl}^-})$
 $= C_{\text{Ag}^+} C_{\text{Cl}^-} f_{\pm}^2$
 Now, for saturated solution of salts like AgCl, BaSO_4 , ZnS etc., the conc. of the ions in pure water will be very little $\Rightarrow f_{\pm} \approx 1$.
 $C_{\text{Ag}^+} C_{\text{Cl}^-} f_{\pm}^2 \approx C_{\text{Ag}^+} C_{\text{Cl}^-} = L_s$ (solubility product).
 $\therefore L_a = L_s \times f_{\pm}^2 \rightarrow \text{This is valid for all AX types of So.}$

Therefore, one can further write that activity of Ag plus and to activity of Cl minus equal to e to the power minus Z_2 sorry e to the power Z_2 , this is a constant at a given temperature T , because Z_2 is constant at a given temperature T , this product is called the activity product of AgCl, which is written as L_a .

So, we write a_{\pm} equal to activity of Ag plus activity of Cl minus which is equal to e to the power of $Z/2$. Using molar concentrations one can rewrite this a_{\pm} equal to concentration of Ag plus into activity coefficient of Ag plus into concentration of Cl minus into activity of Cl minus which is nothing but concentration of Ag plus into concentration of Cl minus into f_{\pm} plus minus square.

So, now for saturated solutions of salts like AgCl, BaSO₄, zinc sulphide etcetera the concentration of the ions in pure water will be very little which indicates that one can assume f_{\pm} plus minus to be very close to 1. So, one can assume its ideal behaviour and you can assume that the mean activity coefficient for both cation and anion will be close to 1.

So, concentration of Ag plus multiplied by concentration of Cl minus into f_{\pm} plus minus square can be equated to concentration of Ag plus into concentration of Cl minus which is equal to L_s that is the solubility product. So, then one can write for all other solutions L_a equal to L_s into f_{\pm} plus minus squared and this is valid for all A_x types of solids or salts.

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$PbCl_2, Cu_2O \text{ etc.} \Rightarrow A_x B_y$
 $A_x B_y \rightleftharpoons x A^{n+} + y B^{m-}$ such that $xn = ym$
 $L_a = (a_{A^{n+}})^x \cdot (a_{B^{m-}})^y$
 $= (C_{A^{n+}})^x (f_{A^{n+}})^x \cdot (C_{B^{m-}})^y (f_{B^{m-}})^y$
 $= \frac{C_{A^{n+}}^x \cdot C_{B^{m-}}^y}{f_{\pm}^{x+y}}$ assuming $f_{A^{n+}} \approx f_{B^{m-}} = f_{\pm}$
 or $L_a = L_s \cdot f_{\pm}^{x+y}$, $x+y = z$
 The solubility product for AgCl is expressed as
 $L_s = C_{Ag^+} \cdot C_{Cl^-}$, if 'S' is the solubility of AgCl in pure water in g-mol/l unit,
 then $C_{Ag^+} = C_{Cl^-} = S \therefore L_s = S \cdot S = S^2$

But then all these solids or salts are not like A_x type, say for example there are salts like $PbCl_2$, Fe_3 , CO_2 etc which are very sparingly soluble in water. So, for those we assume the formula to be $A_x B_y$ where A and B have different oxidation states different charges as a result this stoichiometric coefficients are not same. So, when we consider this salt $A_x B_y$ in water it dissociates as $x A^{n+}$ plus $y B^{m-}$ such that xn equal to ym to maintain electro neutrality of the solution.

So, using this equation ΔG one can write ΔG equal to activity of A_n plus to the power x into activity of B_m minus to the power y and now when you replace the activity terms with concentration you can write concentration of A_n plus to the power x into f_{A_n} plus to the power x into concentration of B_m minus to the power y into f_{B_m} minus to the power y .

Further one can write that C_{A_n} plus to the power x C_{B_m} minus to the power y into f_{A_n} plus to the power x plus f_{B_m} minus to the power y assuming f_{A_n} plus is same as f_{B_m} minus or ΔG is equal to ΔG° which is this quantity multiplied by f_{A_n} plus to the power x plus f_{B_m} minus to the power y , where ΔG° is nothing but the sum of these two isometric coefficients x plus y .

So, now the solubility product for $AgCl$ is expressed as S , sorry expressed as LS into is equal to concentration of Ag^+ plus into concentration of Cl^- minus, if S is the solubility of $AgCl$ in pure water in gram moles per litre unit then concentration of Ag^+ plus is equal to concentration of Cl^- minus is equal to S , therefore LS equal to S into S that is S^2 , this is for one is to one salt like silver chloride.

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NPTEL **AxBy :-**

$$AxBy \rightleftharpoons xA^{n+} + yB^{m-}$$

Then if 'S' is the solubility of $AxBy$ in water, then

$$C_{A^{n+}} = x.S \quad C_{B^{m-}} = y.S$$

LS is const. at a given temp 'T' as the solubility of a sparingly soluble salt is const. at a given temp 'T'.

$$LS = (C_{A^{n+}})^x (C_{B^{m-}})^y$$

$$= (xS)^x (yS)^y$$

$$= x^x y^y S^{x+y}$$

$$\boxed{LS} = x^x y^y S^{x+y} \quad y = x+y$$

$$\therefore S^y = \frac{LS}{x^x y^y}$$

$$\text{or } S = \sqrt[y]{\frac{LS}{x^x y^y}}$$

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But then if we have a salt like this if we have a salt where the stoichiometric coefficients are different what will be the expression for the corresponding solubility product, as we have already written $A_x B_y$ we will dissociate as x into A_n plus plus y into B_m minus then if S is the solubility of $A_x B_y$ in water, then concentration of A_n plus is nothing but x into S similarly concentration of B_m minus is y into S .

Therefore, to calculate LS we need C_{A_n} plus to the power x C_{B_m} minus to the power y , so we have $x S$ to the power x , $y S$ to the power y which is equal to x to the

power x, y to the power y and S to the power x plus y which one can write as x to the power x, y to the power y, S to the power Nu where Nu is equal to which we have already written Nu is equal to x plus y. Therefore, S to the power Nu is equal to L_s by x to the power x, y to the power y or S equal to Nu at root of L_s by x to the power x, y to the power y.

So, if you know the soluble you can determine if you know the solubility you can determine the solubility product, if you can determine the solubility product by some titrimetric method or by a conductor metric method then you can determine the solubility of a sparingly soluble salt, what we see here is that L_s is constant at a given temperature T as the solubility of a sparingly soluble salt is constant at a giving temperature.

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① The sp. conductance of 0.01(N) KCl solution is $1.225 \times 10^{-3} \text{ mho cm}^{-1}$ at 18°C . In a cond. cell at 18°C , the resistance of 0.01(N) KCl solution was found to be 145 ohm and that of 0.002(N) K_2SO_4 solution was 712 ohm. Calculate the cell constant in appropriate unit and hence calculate the equiv. conductance of K_2SO_4 .

② At 25°C , the mobility of NH_4^+ & OAc^- at inf. dilution are 7.6×10^{-4} & $4.7 \times 10^{-4} \text{ cm}^2/\text{V.s}$. Then calculate the eqv. cond. of NH_4OAc and transport number of NH_4^+ ion.

③ The sp. cond. of TlBr and water are 8.16×10^{-4} & $0.04 \times 10^{-4} \text{ mho cm}^{-1}$ at 25°C . The eqv. cond. of TlBr at inf. dilution is $138.2 \text{ mho cm}^{-1}$. Then find out the solubility of TlBr at 25°C .

④ The sp. cond. of a sat. solution of AgCl is $155 \times 10^{-6} \text{ mho cm}^{-1}$ at 25°C . In pure water is $4.3 \times 10^{-7} \text{ mho cm}^{-1}$ at 25°C . In an electric field of 1 V/cm the mobility of Cl^- & Ag^+ ions are 5.6×10^{-4} & $6.8 \times 10^{-4} \text{ cm}^2/\text{V.s}$ respectively. Calculate the solubility prod. of AgCl at 25°C .

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So, now I would like to give a few problems to you to solve based on the concepts that you have learned in using conductivity and conductivity measurements. The specific conductance of 0.01 normal KCl solution is $1.225 \times 10^{-3} \text{ mho centimetre inverse}$ at 18 degree centigrade in a conductivity cell at 18 degree C the resistance of 0.01 normal KCl solution was found to be 145 ohm and that of 0.002 normal K_2SO_4 solution was 712 ohm calculate the cell constant in appropriate unit and hence calculate the equivalent conductance of K_2SO_4 .

So, here what we have given is the specific conductance using this value for specific conductance and the corresponding resistance one can determine the value of cell constant and once you have determined the value of cell constant then it should not be a difficulty to find out the specific conductance of this particular solution using the same expression and

then you can calculate the equivalent conductance which is nothing but $1000 \times C$ into specific conductance.

Question number 2, at 25 degree Centigrade the mobility of NH_4^+ plus and OAc^- minus at infinite dilution is 7.6×10^{-4} and 4.2×10^{-4} cm² per volt per second. Then calculate the equivalent conductance of NH_4OAc that is ammonium acetate and transport number of NH_4^+ plus ions. So, we have already discussed about the relationship between ionic mobility and ion conductivity from that you should be able to calculate the equivalent conductance and then one can easily calculate the corresponding transport numbers.

Question number 3 is the specific conductance of thallium bromide and water are 2.16×10^{-4} and 0.04×10^{-4} mho per centimetre at 25 degree centigrade, the equivalent conductance of thallium bromide at infinite dilution is 138.2 mho centimetre square. Then find out the solubility of thallium bromide at 25 degree centigrade.

And the 4th question is this one the specific conductance of a saturated solution of AgCl is 1.55×10^{-6} mho centimetre inverse and that of pure water is 4.3×10^{-7} mho centimetre inverse at 25 degree centigrade in an electric field of 1 volt per centimetre the mobility of Cl^- minus and Ag^+ plus ions are 5.6×10^{-4} and 6.8×10^{-4} cm² per second respectively. Calculate the solubility product of AgCl at 25 degree centigrade.

So, we will have another theory class in the next session and after that you will have the last week which will be the demonstration of conductometry related experiments followed by one more lecture where we will discuss about the solution or how to do the graph plotting out from those experimental data. Thank you very much.