


Elementary Electrochemistry
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Lecture 32

Ionic Strength of an Electrolyte and its Importance

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Elementary Electrochemistry

A course designed for students studying B. Sc with Chemistry

Instructor


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Elementary Electrochemistry

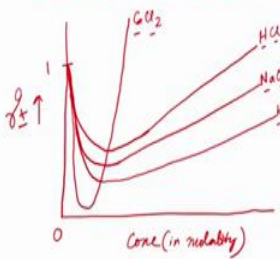
Welcome back to the course Elementary Electrochemistry, we have now started our week 7.

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Ionic Strength:-


When we look at the table of γ_{\pm} for diff. electrolyte with the conc. of the electrolyte, we see a complex behaviour. The value of γ_{\pm} is 1.0 at inf. dilution for all the electrolytes and the value decreases with increase in conc. till it reaches a minimum value and then starts to increase again and often goes above 1.0.



It is also observed that the value of γ_{\pm} for the same type of electrolytes follow same trend.

$$\ln \gamma_{\pm} = -A_1 \sqrt{C}$$

\uparrow \uparrow
 cond. conc. of the
 electrolyte in
 molality.



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And in this week, we are going to start discussing about the Ionic strength of an electrolyte and its importance. So, when we look at the table in a textbook, if you look at a table in a textbook of the values of gamma plus minus for different electrolyte with the concentration of the electrolyte, we see a complex behaviour. The value of gamma plus minus is 1 at infinite

dilution for all the electrolytes and the value decreases with increase in concentration till it reaches a minimum value and then starts to increase again and often goes above 1.0. So, when we plot these values of gamma plus minus versus concentration in molality for various electrolytes, we see a plot like this what I am going to draw here, concentration in molality versus gamma plus minus on Y axis with a value of 1 for this concentration 0.

So, what we see for solutions like for what we see is for HCL what we see is like this, for NaCl it follows nearly the same like HCL to certain value and then it deviates from the value of HCL, so this is for NaCl, HCl trend is observed for KCl, but then at some point it again deviates from NaCl as well and we see a pique layer behaviour for calcium chloride which goes further down and increases sharp and goes high above 1 even at a very low concentration.

So, this indicates something about the dependence of gamma plus minus on the nature of cation or specifically the charge of that cation. So, if it is also observed that the value of gamma plus minus for the same type of electrolytes follow same trend that is here you have Uni univalent they follow a similar trend where you have bivalent was univalent electrolyte the nature that you see is different.

And most of them are very similar at low concentration. So, an empirical relation for gamma plus minus versus concentration also was derived based on the experimental values that were observed and that empirical relationship is $\ln \gamma_{\pm} = -A_1 \sqrt{C}$ where A_1 is a constant quantity and C is the concentration of the electrolyte in molality, this is again an empirical relation that was derived based on the experimental observations of gamma plus minus.

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case of a mixture of 2 or more electrolytes, the value of γ_{\pm} was found to depend on the total conc. of the ions as also the nature (charges) of the individual ions involved.

Lewis & Randall observed that the influence of an ion in a mixture on γ_{\pm} of a given electrolyte is proportional to the square of the charge on the ion. It means that the ions like Ba^{2+} , Ca^{2+} etc. influence the activity coefficient (γ_{\pm}) of a salt in a mixture by 4 times than that done by Na^{+} or K^{+} .

By comparing the values of γ_{\pm} in the pure state, & with γ_{\pm} in a mixture, they introduced a new term "ionic strength", 'i' of a solution (mix. of many electrolytes) and defined 'i' as,

$$i = \frac{1}{2} \sum m_i z_i^2 = \frac{1}{2} \sum m_i z_i^2$$

m_i = molality of i^{th} ion. z_i = charge of i^{th} ion.

m_i = 0.008 of a mix. of $\text{BaCl}_2 + \text{KCl}$.

$$i = \frac{1}{2} [0.008 \times 2^2 + 0.008 \times 1^2 + 0.008 \times 1^2 + 0.008 \times 1^2] = 0.029$$

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In case of a mixture of 2 or more electrolytes the value of gamma plus minus was found to depend on the total concentration of the ions and also the nature that is the charges of the individual ions involved. So, based on many several experiments on strong electrolytes Lewis and Randall observed that the influence of an ion in a mixture on gamma plus minus of a given electrolyte is proportional to the square of the charge on the ions. It means that the ions like barium 2 plus calcium 2 plus etcetera influences the activity or the other activity coefficient that is gamma plus minus of a salt in a mixture by 4 times then that done by Na plus or K plus which are monovalent cations.

So, by comparing the values of gamma plus minus in the pure state and with the gamma plus minus in a mixture, they introduced a new term called the ionic strength which is written as small i of a solution which is essentially a mixture of many electrolytes and defined i that is the i strength as i equal to half of $m_1 z_1^2$ plus $m_2 z_2^2$ plus $m_3 z_3^2$ plus dot dot mn z_n^2 square that means there are n number of ions may be cation anion it does not matter and m terms are the corresponding concentration of those ions in terms of molality.

So, m_i is molality of i^{th} ion and z_i is molality of the i^{th} sorry the charge of the charge of i^{th} ion. So, i is equal to nothing but half of sum over $m_i z_i^2$ square, so just to give you an an idea of the ionic strength if m_i for all the ions is 0.008 of a mixture of BaCl_2 plus KCl , so then you should calculate i equal to half of 0.008×2^2 , 2^2 plus 0.008×1^2 square that is for barium chloride plus 0.008×1^2 square plus 0.008×1^2 square for KCl .

So, when you do this calculation the value of i turns out to be 0.029. So, this is the ionic strength of this solution which turns out to be a mixture of two different strong electrolytes.

So, this is an important parameter to identify how, what is the strength of a solution of two or more electrolytes.

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The Degree of dissociation of water from conductance measurement:-
 The purest form of water is obtained by 2-3 times distillation of water in a closed circuit and then the distilled water is passed through ion exchange column to remove any other dissolved ions like Cl^- , CO_3^{2-} etc. to get 'conductivity water'.
 For conductivity water, the sp. conductance, $[L = 0.58 \times 10^{-7} \text{ mho cm}^{-1} \text{ or } \text{S cm}^{-1}]$ at 25°C .
 Sp. conductance of conductivity water:-

$$\lambda = \frac{1000 \times L}{C}$$
 or
$$\lambda = 0.58 \times 10^{-7} \text{ mho cm}^{-1} \times V_m \text{ (molar vol)}$$

$$= 0.58 \times 10^{-7} \times \frac{9}{0.997} \text{ mho cm}^2/\text{gm}$$

$$\lambda = 0.52 \times 10^{-7} \text{ mho cm}^2/\text{g. equiv.}$$

So, now let us try to see how can we estimate the degree of dissociation of water from conductance measurement, see for conductance measurement we need to get a very high-quality water which essentially should not be dissociated and should not be conducting electricity but that is practically impossible.

So, the purest form of water is obtained by 2 to 3 times distillation of water in a closed circuit which essentially means that you distilled water from first container collect it in a second container which is isolated from the environment and then use the second container as a boiler boil that water again collect the water vapour in a third container and do the same again, so you do a three times distillation in a closed system and collect that fresh water.

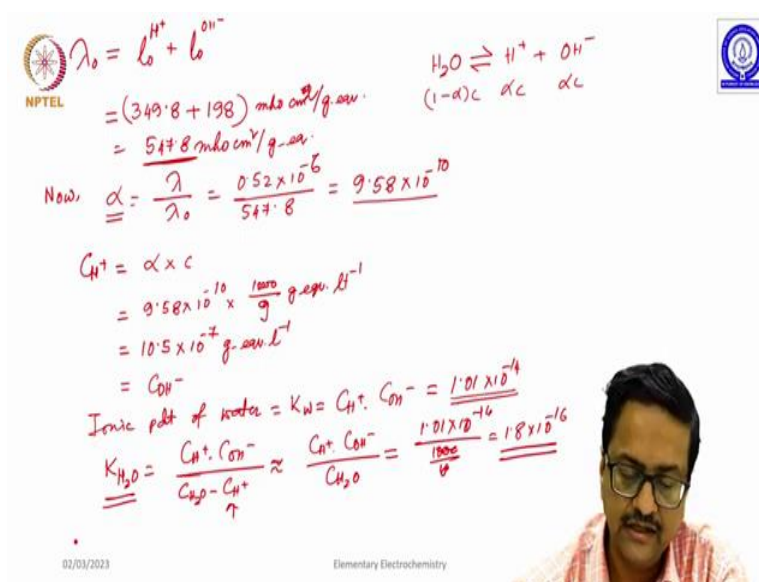
And then the distilled water is passed through ion exchange columns to remove any other dissolved ions, like sometimes you may have still have a dissolved chloride, carbonate, etcetera, to get something called a conductivity water. So, we use this conductivity water for all our practical experimental applications.

So, this the for this conductivity water, the much specific conductance that is L is determined to be $0.58 \times 10^{-7} \text{ mho centimetre inverse}$ or that is Siemens centimetre inverse, you see that the value is in 10 to the power minus 7 that means the resistance of this solution is extremely high.

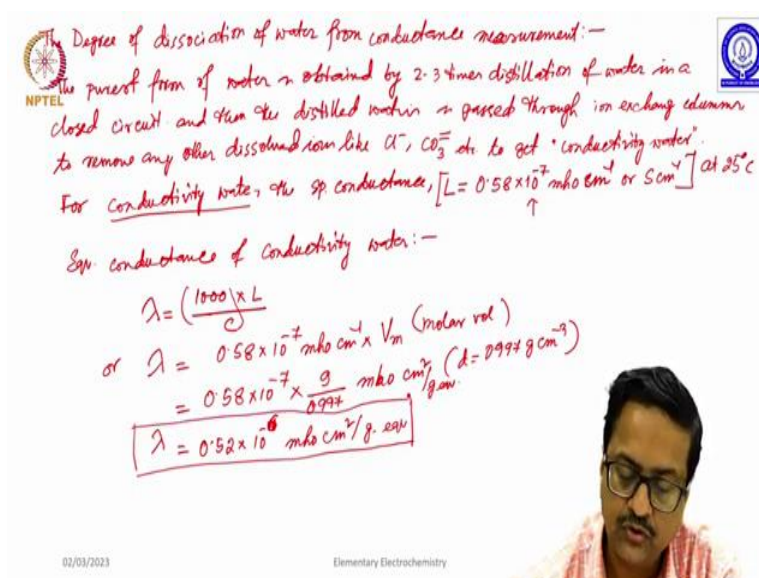
So, for this solution one for this water conductivity water one can calculate the equivalent conductance that is λ equal to $1000 \times L \times C$ or λ is equal to this L is 0.58 sorry 0.05 no, the value of L is 0.58 into 10 to the power minus 7 mho centimetre inverse into this term is nothing but the molar volume of water.

So, now you can do this calculation easily 0.58 into 10 to the power minus 7 molar volume of water is nothing but 9 by 0.997 and the unit becomes mho centimetre square where density of water is 0.997 gram per C 3. So, you can calculate this value as 0.52 into 10 to the power minus 7 per gram equivalent in meter, so mho centimetre square per gram equivalent. So, this is the equivalent conductance for water and this value is at 25 degree centigrade as usual.

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$\lambda_0 = \lambda_{H^+} + \lambda_{OH^-}$
 $= (349.8 + 198) \text{ mho cm}^2/\text{g. equiv.}$
 $= 547.8 \text{ mho cm}^2/\text{g. equiv.}$
 Now, $\alpha = \frac{\lambda}{\lambda_0} = \frac{0.52 \times 10^{-6}}{547.8} = 9.58 \times 10^{-10}$
 $C_{H^+} = \alpha \times c$
 $= 9.58 \times 10^{-10} \times \frac{1000}{9} \text{ g. equiv. l}^{-1}$
 $= 10.5 \times 10^{-7} \text{ g. equiv. l}^{-1}$
 $= C_{OH^-}$
 Ionic prod of water $= K_w = C_{H^+} \cdot C_{OH^-} = \frac{1.01 \times 10^{-14}}{10}$
 $K_{H_2O} = \frac{C_{H^+} \cdot C_{OH^-}}{C_{H_2O}} \approx \frac{C_{H^+} \cdot C_{OH^-}}{C_{H_2O}} = \frac{1.01 \times 10^{-14}}{18} = 1.8 \times 10^{-16}$



Degree of dissociation of water from conductance measurement:-
 The purest form of water is obtained by 2-3 times distillation of water in a closed circuit and then the distilled water is passed through ion exchange column to remove any other dissolved ions like Cl^- , CO_3^{2-} etc. to get 'conductivity water'.
 For conductivity water, the sp conductance, $[L = 0.58 \times 10^{-7} \text{ mho cm}^{-1} \text{ or } S \text{ cm}^{-1}]$ at 25°C
 Sp. conductance of conductivity water:-
 $\lambda = \frac{1000 \times L}{C}$
 or $\lambda = 0.58 \times 10^{-7} \text{ mho cm}^{-1} \times V_m \text{ (molar vol)}$
 $= 0.58 \times 10^{-7} \times \frac{9}{0.997} \text{ mho cm}^2/\text{g. equiv.}$
 $\lambda = 0.52 \times 10^{-6} \text{ mho cm}^2/\text{g. equiv.}$

So, now if you look the values for the λ_0 that is the equivalent conductance at infinite dilution for water if I want to calculate I need the value for λ_0 for H^+ plus λ_0 of OH^- . So, one can look at the corresponding table in the textbook and find the values for λ_0 for H^+ plus which happens to be 349.8 and the other one happens to be 198, so when you add these two of course the unit is $mho\ cm^2\ per\ gram\ equivalent$ which is equal to 547.8 $mho\ cm^2\ per\ gram\ equivalent$.

Now, we can easily calculate the value of degree of dissociation that is α as λ / λ_0 which we have discussed in the previous class, so you can calculate it as 0.52×10^{-6} , let me check whether I wrote 6 or 7 here it should be 6 please correct it, by 547.8 the unit gets cancelled, so the degree of dissociation of water is nothing but 9.58×10^{-10} .

So, now from this if we want to calculate the concentration of H^+ in this conductivity water it is nothing but the degree of dissociation α into concentration of water that is $\alpha \times C$ where C is concentration of water that is $1000\ g\ per\ litre$ or you can calculate it as $10^{-7}\ g\ per\ litre$, which is also same as C_{OH^-} because both H^+ and OH^- are dissociated from water. So, if the degree of dissociation is α in terms of concentration it is $\alpha \times C$ where C is concentration of water that is $1000\ g\ per\ litre$, so in terms of concentration it is multiplied by C .

So, then one can calculate the ionic product of water as equal to K_w which is $C_{H^+} \times C_{OH^-}$, if you do this product it turns out to be 1.01×10^{-14} and equilibrium constant of this dissociation of water that is K_w is nothing but $C_{H^+} \times C_{OH^-}$ divided by C_{H_2O} which is sort of equal to $C_{H^+} \times C_{OH^-}$ divided by C_{H_2O} , because C_{H^+} is extremely small compared to the overall concentration of un-dissociated water.

Now, if you do this calculation you will get the value as 1.01×10^{-14} for this product and concentration of water is $1000\ g\ per\ litre$ which is equal to 1.8×10^{-16} . So, these are the two very important physical quantities for water that is the ionic product of water and the equilibrium constant for the dissociation of water obtained from the value of α that is the degree of dissociation of water and this value of degree of dissociation of water is obtained from the limiting conductivities of the cation and anion and also the equivalent conductance of very pure water which is the conductivity water. So, along

with this we I am going to conclude today's lecture and I will give you some of the problems in the next class on these topics. Thank you.