

Elementary Electrochemistry
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Lecture 28
Ionic Mobilities in terms of ion Conductivities

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Elementary Electrochemistry



A course designed for students studying B. Sc with Chemistry

Instructor

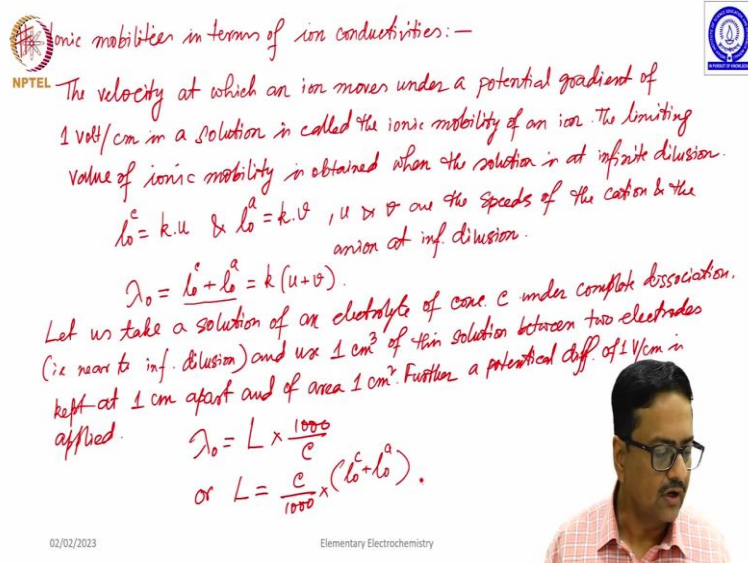
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Elementary Electrochemistry

Welcome back to the course entitled Elementary Electrochemistry. In this course, in the previous lecture, we have discussed about the ionic conductivities and based on the limiting ion conductivity is for different ions and then the corresponding limiting conductivity of the electrolyte that is the equivalent limiting conductivity or equivalent conductivity at conductance at in dilution. We have discussed how one can calculate the value of equivalent conduct insert infinite dilution for some unknown electrolyte which may be strong or a weak electrolyte.

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Ionic mobilities in terms of ion conductivities:—

The velocity at which an ion moves under a potential gradient of 1 volt/cm in a solution is called the ionic mobility of an ion. The limiting value of ionic mobility is obtained when the solution is at infinite dilution.

$\lambda_0^c = k \cdot u$ & $\lambda_0^a = k \cdot v$, u & v are the speeds of the cation & the anion at inf. dilution.

$\lambda_0 = \lambda_0^c + \lambda_0^a = k(u+v)$.

Let us take a solution of an electrolyte of conc. c under complete dissociation (i.e. near to inf. dilution) and use 1 cm³ of this solution between two electrodes kept at 1 cm apart and of area 1 cm². Further a potential diff. of 1 V/cm is applied.


$\lambda_0 = L \times \frac{1000}{c}$
 or $L = \frac{c}{1000} \times (\lambda_0^c + \lambda_0^a)$.

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So, in today's lecture, I am going to discuss about the ionic mobilities in terms of ion conductivities. The velocity at which an ion moves under a potential gradient of 1 volt per centimeter in a solution is called the ionic mobility of an ion. The limiting value of ionic mobility is obtained when the solution is at infinite dilution. So, one can write that λ_0^c is equal to some constant k into u and λ_0^a is equal to the same constant k into v where u and v are the speeds of the cation and the anion infinite dilution. So, the λ_0 is nothing but $\lambda_0^c + \lambda_0^a$. So, it is nothing but $k(u + v)$ this is what we have seen in the previous class.

Now, let us take a solution of an electrolyte of concentration c under complete dissociation that is near to infinite dilution and use 1 cubic centimeter of this solution between two electrodes kept at 1 centimeter apart and of area 1 centimeter square. Further a potential difference of 1 volt per centimeter is applied. So, what we know from our previous equations is that λ_0 is equal to L into 1000 by c or simply L is equal to c by 1000 into λ_0 is nothing but $\lambda_0^c + \lambda_0^a$.

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 If 'I' is the amount of current passed through the solution —

$$I = \frac{E}{R} = E \times \Lambda \quad \left(\Lambda = \frac{1}{R} \right)$$

$$I = E \times L \quad \left(\text{as } \Lambda = L \text{ when } l = 1 \text{ cm \& } a = 1 \text{ cm}^2 \right)$$

Now, $E = 1 \text{ V/cm}$.

$$I = L \quad (\text{once again the values are same}).$$

$$I = \frac{C}{1000} (l_0^+ + l_0^-)$$

$$I = \frac{C}{1000} \times k(u+v) \quad \text{--- (1)}$$


The total g. eqs of ions transported by this current I to the two electrodes per sec is given by


$$u \times \frac{C}{1000} \times 1 + v \times \frac{C}{1000} \times 1 = \frac{C}{1000} (u+v)$$

\therefore One g. eq. of ions carry 1 Faraday of electricity,

\therefore total charge carried/sec is,
$$I = \frac{C}{1000} \times (u+v) \times F \quad \text{--- (2)}$$

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 Ionic mobilities in terms of ion conductivities: —

The velocity at which an ion moves under a potential gradient of 1 volt/cm in a solution is called the ionic mobility of an ion. The limiting value of ionic mobility is obtained when the solution is at infinite dilution.

$$l_0^+ = k \cdot u \quad \& \quad l_0^- = k \cdot v, \quad u \text{ \& } v \text{ are the speeds of the cation \& the anion at inf. dilution.}$$


$$\lambda_0 = l_0^+ + l_0^- = k(u+v).$$

Let us take a solution of an electrolyte of conc. C under complete dissociation. (i.e. near to inf. dilution) and use 1 cm² of this solution between two electrodes kept at 1 cm apart and of area 1 cm². Further a potential diff. of 1 V/cm is applied.

$$\lambda_0 = L \times \frac{1000}{C}$$

or
$$L = \frac{C}{1000} \times (l_0^+ + l_0^-)$$

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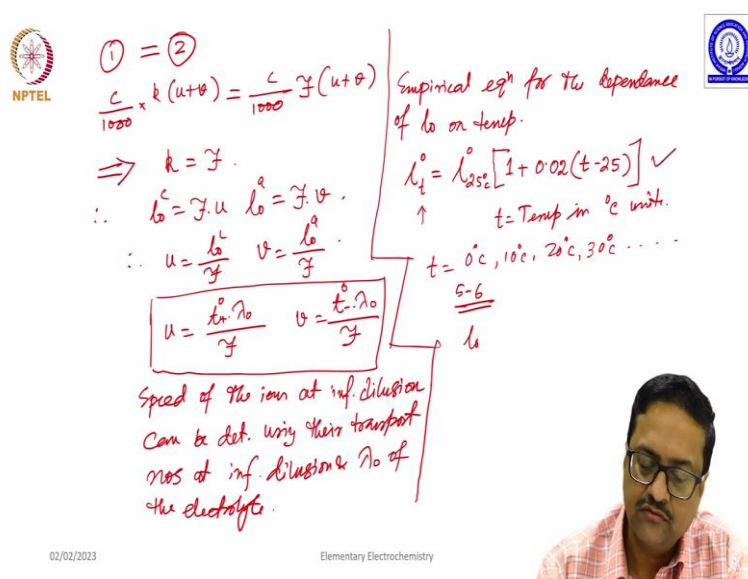
So, now if I is the amount of current passed through the solution then I equal to E by R which is equal E to into lambda where lambda is equal to 1 by R. So, now, one can further simplify I equal to E into L as capital lambda becomes equal to 1 when small l that is the path length is equal to 1 centimeter and the area of the cross section is 1 centimeter square. This equality is a numerical equality that is these values are same, but the units are different if you have remember.

Now, in this case E is equal to 1 volt per centimeter. So, therefore, one can write I equal to L once again the values are same do not confuse that the unit of L and I are same. So, I if it is ampere, so, Ls whatever the value of Ls it is in ampere. So, now, one can further write that I equal to L which is nothing but C by 1000 into 10 C plus 10 a or simply equal to C by 1000

into k into u plus v . Let us take this equation as equation number 1. We have written this from the previous page which is here.

Now, the total gram equivalent of ions transported by this current I to the two electrodes per second is given by u into C by 1000 into 1 that is the 1 volt per second and v into C by 1000 into 1. So, that is equal to C by 1000 into u plus v . Now, since 1 gram equivalent of ions carry F Faraday or rather 1 Faraday of electricity so, total charge carried is carried per second is I equal to C by 1000 into u plus v into F . This is the equation number 2. So, now, we see that equation number 1 and 2 has same quantity on the left hand side.

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The slide contains handwritten notes and equations. On the left, it shows the derivation of transport numbers u and v from the relationship $k = F(u + v)$. It concludes with $u = \frac{\lambda_0^+}{F}$ and $v = \frac{\lambda_0^-}{F}$, where λ_0 is the limiting molar conductivity. A box highlights these equations, with a note: "Speed of the ion at inf. dilution can be det. using their transport nos at inf. dilution & λ_0 of the electrolyte." On the right, it discusses the empirical equation for the temperature dependence of λ_0 : $\lambda_t = \lambda_{25} [1 + 0.02(t - 25)]$, where t is temperature in °C. It lists values for t as 0°C, 10°C, 20°C, 30°C, etc. A small inset shows a man speaking.

① = ②

$$\frac{C}{1000} \times k(u+v) = \frac{C}{1000} F(u+v)$$

$$\Rightarrow k = F$$

$$\therefore \lambda_0^+ = F \cdot u \quad \lambda_0^- = F \cdot v$$

$$\therefore u = \frac{\lambda_0^+}{F} \quad v = \frac{\lambda_0^-}{F}$$

$$u = \frac{\lambda_0^+}{F} \quad v = \frac{\lambda_0^-}{F}$$

Speed of the ion at inf. dilution can be det. using their transport nos at inf. dilution & λ_0 of the electrolyte.

Empirical eqⁿ for the dependence of λ_0 on temp.

$$\lambda_t = \lambda_{25} [1 + 0.02(t - 25)] \checkmark$$

\uparrow
 $t = \text{Temp in } ^\circ\text{C unit.}$

$t = 0^\circ\text{C}, 10^\circ\text{C}, 20^\circ\text{C}, 30^\circ\text{C} \dots$

$\frac{5-6}{\lambda_0}$

So, one can equate this equation 1 and 2 and write the following C by 1000 into k u plus v which is equal to C by 1000 F u plus v which essentially means that the value of k is nothing but F that is the quantity of electricity passed in columns. Therefore, one can write λ_0^+ equal to F into u λ_0^- is equal to F into v . So, therefore, you can write u equal to λ_0^+ by F , v equal to λ_0^- by F and then one can further replace this λ_0 by transport numbers u equal to λ_0^+ plus at infinite dilution into λ_0^+ by F and v equal to λ_0^- plus at infinite dilution into λ_0^- by F .

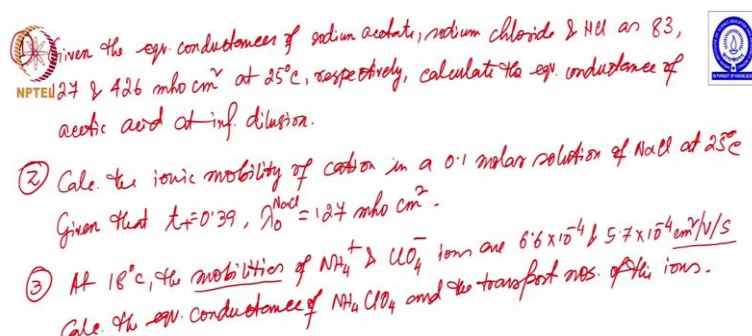
So, the speed of the ions at infinite dilution can be determined using their transport numbers at infinite dilution and the corresponding λ_0 of the electrolytes. So, the value of ion conductivity depends on certainly on the transport number of the ions and the transport number further depends on the concentration sorry, transport number depends on the

temperature as well. So, what happens is the ionic conductivity is that Λ_0^c or Λ_0^a depends on temperature.

So, based on several experimental determinations of ion conductivities of various ions we have there is we have arrived that in an empirical equation for the dependence of Λ_0 on different temperatures on temperature. What is the relationship? Λ_0 or rather Λ_t is equal to $\Lambda_{25} \times \left(1 + 0.02(t - 25)\right)$ where t is the temperature in degree centigrade unit. This is an empirical relationship which has been arrived that based on various experimental data for the ion conductances of a particular ion at different temperature.

So, you do the experiment at various temperatures t maybe this t can be 0 degrees centigrade, 10 degrees centigrade, 20 degrees centigrade like that 30 degree centigrade and you measure some 5 to 6 experiments at 5 to 6 different temperatures and based on the trends of those values of Λ_0 at all these temperatures this equation can be arrived at.

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Given the eqn. conductances of sodium acetate, sodium chloride & HCl are 83, 1.27 & 426 mho cm^2 at 25°C , respectively, calculate the eqn. conductance of acetic acid at inf. dilution.

② Calc. the ionic mobility of cation in a 0.1 molar solution of NaCl at 25°C .
Given that $t_+ = 0.39$, $\Lambda_0^{\text{NaCl}} = 124 \text{ mho cm}^2$.

③ At 18°C , the mobilities of NH_4^+ & ClO_4^- ions are 6.6×10^{-4} & $5.7 \times 10^{-4} \text{ cm}^2/\text{V/s}$.
Calc. the eqn. conductance of NH_4ClO_4 and the transport nos. of the ions.

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So, with this I will be giving you a few problems to solve based on the topics which we have learned in last couple of classes. So, the first problem is the following. Given the equivalent conductances of sodium acetate, sodium chloride and HCl as 83, 1.27 and 426 in mole centimeters squared unit at 25 degrees centigrade respectively. Calculate the equivalent conductance of acetic acid at infinite dilution. This is a straightforward question from the lecture that we have delivered already in the previous class.

Calculate the ionic mobility of cation in a 0.1 molar solution of NaCl at 25 degree centigrade given that t_+ is equal to 0.39 and λ_0 for NaCl is 127 mole centimeters squared. And the third problem is the following at 18 degrees centigrade the mobilities of ammonium and ClO_4^- ions are 6.6×10^{-4} and 5.7×10^{-4} centimeter squared per volt per second. Calculate the equivalent conductance of ammonium perchlorate and the transport numbers of the ions.

You see here the unit of the mobility is given here. So, you had to take care of the unit while doing any calculation related to electrochemistry rather you should keep in mind about the unit calculation for all the physical chemistry related problems because the physical quantities come with the correct appropriate unit. Any calculation without indicating their unit is meaningless. Therefore, I would emphasize that you should get yourself associated with the units of various physical quantities that we are discussing in this course. Because when you write your final examination, marks will not be awarded if the units are not correct.

So, we will stop here at this point and we will continue in the next lecture discussing about some of the applications of conductance measurements. Thank you.