

Elementary Electrochemistry
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Measurement of Cell EMF

Welcome back to the course entitled elementary electrochemistry. In the previous lecture, we have discussed a few problems related to the EMF measurements. So, we will continue from there and we will try to understand how the cell EMFs are physically measured experimentally? And also how they are related to in terms of oxidation and reduction processes?

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EMF of a cell :-

(anode) $- \text{Zn} | \text{Zn}^{2+}(\text{aq}) || \text{Cu}^{2+}(\text{aq}) | \text{Cu}$ + (cathode)

left $\xrightarrow{\text{ox}}$ right

$\text{Zn} + \text{Cu}^{2+} \rightleftharpoons \text{Zn}^{2+} + \text{Cu}$

$E_{\text{cell}} = E_{\text{ox}}^{\text{ox}} - E_{\text{re}}^{\text{ox}} = E_{\text{L}}^{\text{ox}} - E_{\text{R}}^{\text{ox}} = E_{\text{anode}}^{\text{ox}} - E_{\text{cathode}}^{\text{ox}}$

$= -E_{\text{re}}^{\text{red}} - (-E_{\text{re}}^{\text{red}})$

$= E_{\text{re}}^{\text{red}} - E_{\text{re}}^{\text{red}} = E_{\text{R}}^{\text{red}} - E_{\text{L}}^{\text{red}} = E_{\text{cathode}}^{\text{red}} - E_{\text{anode}}^{\text{red}}$

So, when you try to write the EMF of a cell we first need to construct a particular cell for which we want to do the measurement of EMF. So, let us assume that we are talking about the Daniell cell which is nothing but you have already learned zinc metal dipped in a solution of Zn^{2+} plus ions in aqueous medium and it is kept separated from a solution of Cu^{2+} plus in aqueous medium with copper as the electrode and by convention the way we write these cells, the right hand side electrode is plus, the cathode and the left hand side electrode is the minus or the anode and in this particular cell, at anode the oxidation takes place.

So, zinc is reacting with Cu^{2+} plus to get converted to Zn^{2+} plus which is oxidation and copper is getting reduced to copper zero. So, this is the oxidation and this is reduction, this all of you I think you can understand.

So, we call this electrode on the left hand side is as just left and the other one as right. While considering the EMF of a cell, we should write E_{cell} that E_{cell} is conventionally written as if I consider in the oxidation direction, it is electrical potential of the negative electrode minus the E_{ox} of the positive electrode which essentially means, we are talking about $E_{\text{oxidation}}$ of the left minus $E_{\text{oxidation}}$ of the right electrode or we can also write $E_{\text{ox anode}} - E_{\text{ox cathode}}$.

Now, parallelly if we want to write both the potentials in the opposite direction that is the reduction direction, so then, immediately you will write minus of $E_{\text{reduction}}$ of negative electrode minus minus of reduction potential of the positive electrode. So, immediately we will write by rearranging it as $E_{\text{reduction positive}} - E_{\text{reduction of the negative electrode}}$ and then we keep writing whether positive electrode is now on the right hand side. So, when we write reduction then $E_{\text{right}} - E_{\text{left}}$ in the reduction potential direction or you can write $E_{\text{reduction cathode}} - E_{\text{reduction anode}}$.

So, depending on whether we use the oxidation potentials or the reduction potentials, the value of E_{cell} does not change. What changes is the corresponding values of the cathode and anode E^0 values which are exactly the opposite and when you change the sign for both and then again the take a difference you will end up with the same value of E_{cell} .

So, now, when we try to measure the EMF of a particular cell we need to know both the E_{anode} and E_{cathode} whether in the oxidation or reduction mode. So, to know the electrode potentials of different electrodes, one has to learn one has to know how to consider which is zero and from there we will do the calculation.

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Standard Hydrogen Electrode: -
 $\text{H}_2(\text{g}) | \text{Pt} | \text{H}^+(\text{aq})$ at all temperatures.
 $E^\circ_{\text{H}_2/\text{H}^+} = 0$
 $a = 1$

If $a_{\text{H}^+} \neq 1$, then $E_{\text{H}_2} = E^\circ_{\text{H}_2} - \frac{RT}{2F} \ln a_{\text{H}^+}$
 $= -\frac{RT}{2F} \ln a_{\text{H}^+}$, where $a_{\text{H}^+} \neq 1$, $E_{\text{H}_2} \neq 0$

Calomel Electrode: -
 $\text{Hg}(\text{l}) | \text{Hg}_2\text{Cl}_2(\text{s}) | \text{Cl}^-(\text{aq})$ | Cal - $\text{H}_2(\text{g}) | \text{Pt} | \text{H}^+(\text{aq})$ | $\text{KCl}(\text{aq}) | \text{Hg}_2\text{Cl}_2(\text{s}) | \text{Hg}(\text{l})$
 $E_{\text{cell}} = E^\circ_{\text{H}_2} - E^\circ_{\text{Cal}} = -E^\circ_{\text{Cal}}$
 $= -E^\circ_{\text{Cal}} + \frac{RT}{2F} \ln a_{\text{Cl}^-}$
 at 25°C , $E^\circ_{\text{Cal}} = -0.268\text{V}$

E_{cell} in diff. conc. diff. conc. of KCl solution
 Conc. KCl Standard 1M 0.1M
 E°_{Cal} -0.2415V -0.268V -0.3335V
 at 25°C or 298K

So, to consider the zero potential we need to consider a standard hydrogen electrode which is nothing but hydrogen gas bubbled at 1 atmospheric pressure along a platinum electrode and that platinum electrode is dipped in a solution of H plus ions an aqueous solution with activity equal to 1.

So, if such a condition is achieved that you have a solution of H plus ion of activity 1 and you are passing H2 gas at 1 atmospheric pressure at the platinum electrode then the reaction what happens is half H2 giving you H plus plus electron. So, the EMF of that cell or E0 of that half H2 H plus electrode is taken as 0 at all the temperatures. So, that is the potential of standard hydrogen electrode which is considered to be 0. Using this standard hydrogen electrode we have to calibrate or we have to determine the potential of any other electrodes.

Now, in case if the activity of H plus is not equal to 1 then EH2 that is the cell EMF is nothing but E0H2 which is 0 minus RT by F ln activity of H plus or you can simplify as minus RT by F ln activity of H plus where activity of H plus is not equal to 1 and in that condition E cell is not equal to 0 or EH2 is not equal to 0.

So, to determine the potential or the electrode potential of any other cell, one has to first couple it with the standard hydrogen electrode and then determine the potential of that cell. But then what happens is it is very difficult always to use hydrogen gas at one atmospheric pressure because it is a flammable gas and this electrode is a cumbersome electrode. So, to avoid such a situation,

one can use another standard electrode first you couple it with standard hydrogen electrode determine its electrode potential and use that electrode to calibrate the other possible electrodes that you may be using in your lab.

So, one such electrode is calomel electrode which is used as a standard electrode and that electrode is nothing but mercury liquid is made a paste with mercurous chloride which is solid and it is kept in equilibrium with the chloride ion in aqueous medium, in general it can be the KCl solution.

So, this electrode is then coupled with the standard hydrogen electrode, so, then the cell after coupling the hydrogen electrode with calomel electrode is written as hydrogen gas at 1 atmosphere, platinum electrode, we have H^+ ion with activity of H^+ equal to 1 in connection with a KCl solution aqueous where the activity of Cl^- is taken as a_{Cl^-} and it is coupled with the electrode that is Hg_2Cl_2 solid and mercury liquid, so, it is a paste of mercury with mercurous chloride.

So, then when you try to write down the value of E_{cell} , you will simply write, so, in this particular case this side is positive, this side is negative by convention as usual. So, when we write $E_{cell} = E_{H_2 \text{ oxidation}} - E_{\text{calomel oxidation}}$ and it is nothing but minus of $E_{\text{calomel oxidation}}$. So, you can replace it by denoted equation, so, one can write minus E^0_{calomel} in oxidation mode plus $RT \ln a_{Cl^-}$.

So, now at 25 degree centigrade in an experimental setup this value of E_{cell} with unit activity of for KCl, one can, one has determined the E^0_{calomel} the oxidation potential to be equal to minus 0.268 volts. So, this is experimentally determined value for E^0 for calomel electrode in the oxidation mode. So, it means that this is lower than the hydrogen electrode what is also found is that this potential E_{cell} is determined with different concentration of KCl solution and the corresponding E_{cell} values were also determined.

So, if we write try to write down the concentration of KCl and the corresponding E oxidation of calomel it is $E^0_{\text{oxidation}}$ for a saturated solution this value was found to be minus 0.2415 volt, for one normal KCl solution it was found to be 0.2800 and for 0.1 normal KCl it was found to be 0.3338 minus volt all were done at 25 degree centigrade or 298 Kelvin temperature.

So, with these different values of E calomel with different concentration of KCl being determined one can couple these calomel electrodes with any other known electrode any other unknown electrode and determine their corresponding E0 value and find out whether it acts as a cathode or an anode when you couple this with your calomel electrode.

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Electrode	Electrode Reaction	Standard Potential E° (V)
K ⁺ /K	K ⁺ + e ⁻ → K	+2.925
Na ⁺ /Na	Na ⁺ + e ⁻ → Na	+2.714
Mg ²⁺ /Mg	Mg ²⁺ + 2e ⁻ → Mg	+2.34
Zn ²⁺ /Zn	Zn ²⁺ + 2e ⁻ → Zn	+0.761
Fe ²⁺ /Fe	Fe ²⁺ + 2e ⁻ → Fe	+0.441
Cr ³⁺ /Cr	Cr ³⁺ + 3e ⁻ → Cr	+0.410
Co ²⁺ /Co	Co ²⁺ + 2e ⁻ → Co	+0.402
Ni ²⁺ /Ni	Ni ²⁺ + 2e ⁻ → Ni	+0.280
Ag ⁺ /Ag	Ag ⁺ + e ⁻ → Ag	+0.240
Sn ²⁺ /Sn	Sn ²⁺ + 2e ⁻ → Sn	+0.126
Pb ²⁺ /Pb	Pb ²⁺ + 2e ⁻ → Pb	+0.126
H ⁺ /H ₂	2H ⁺ + 2e ⁻ → H ₂	0.000
AgCl/Ag	AgCl + e ⁻ → Ag + Cl ⁻	+0.2223
Hg ₂ Cl ₂ /Hg	Hg ₂ Cl ₂ + 2e ⁻ → 2Hg + 2Cl ⁻	+0.2680
Cu ²⁺ /Cu	Cu ²⁺ + 2e ⁻ → Cu	+0.337
Li ⁺ /Li	Li ⁺ + e ⁻ → Li	-0.535
Fe ³⁺ /Fe ²⁺	Fe ³⁺ + e ⁻ → Fe ²⁺	-0.771
Ag ⁺ /Ag	Ag ⁺ + e ⁻ → Ag	-0.799
Br ₂ /Br ⁻	Br ₂ + 2e ⁻ → 2Br ⁻	-1.0652
Fe ²⁺ /Fe	Fe ²⁺ + 2e ⁻ → Fe	-1.250
As ³⁺ /As	As ³⁺ + 3e ⁻ → As	-1.300
Cl ₂ /Cl ⁻	Cl ₂ + 2e ⁻ → 2Cl ⁻	-1.359
Cr ³⁺ /Cr	Cr ³⁺ + 3e ⁻ → Cr	-1.810

So, here what I have brought is a standard electrode reaction and the corresponding standard electrode potential table which you can find in any standard textbook, what you see here hydrogen is in the middle of it there are electrodes up and there are electrodes down below this. See this is written in the mode of oxidation, so, these are the oxidation potentials.

So now, what does it mean? It means that the potential for potassium to get oxidized to potassium plus is more compared to the oxidation of hydrogen to H plus. So, what will happen if I add potassium to water it will form K plus and release hydrogen gas. So, I am not I have not balanced it one has to balance the equation it essentially means potassium will get oxidized and hydrogen will get reduced.

On the other hand, if you use a silver silver plus electrode, so, in that case the hydrogen will be oxidized, so, hydrogen will get converted to H plus and silver will get converted silver plus will get converted to silver 0. So, the ones which are lower than hydrogen will not be able to liberate hydrogen or rather it will react with the H plus 2, it will react with H₂ to generate H plus,

whereas the ones which are above hydrogen in the oxidation potential table will be able to liberate hydrogen gas.

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Determination of activity coefficient from EMF measurements: -

Cell notation: $\text{H}_2(\text{gas}, 1 \text{ atm}), \text{Pt} | \text{HCl}(\text{aq}, m) | \text{AgCl}(\text{s}), \text{Ag}$
 m : molality of the solution

Cell reaction: $\text{AgCl} + \frac{1}{2} \text{H}_2 \rightarrow \text{Ag} + \text{HCl}$

Nernst equation:
 $E_{\text{cell}} = E_{\text{cell}}^0 - \frac{RT}{F} \ln a_{\text{H}^+} a_{\text{Cl}^-}$
 $= E_{\text{cell}}^0 - \frac{RT}{F} \ln (a_{\pm})^2$
 Let γ_{\pm} be the mean ionic activity coefficient, $\gamma_{\pm}^2 m = a_{\pm}$

Debye-Hückel limiting law for dilute solutions:
 $\log \gamma_{\pm} = -Z \sqrt{m}$
 $Z = n$ a constant = 0.5 for uni-univalent ions.
 $(E_{\text{cell}} + 0.118 \log m) = E_{\text{cell}}^0 + \frac{RT}{F} \ln \frac{1}{C + \text{const} \times \sqrt{m}}$

Graph of $E_{\text{cell}} + 0.118 \log m$ vs \sqrt{m} showing a linear relationship with slope $-Z$.

So, now, we will try to use the concept of EMF measurement for determination of a few physical quantities like the activity coefficient. So, it is determination of activity coefficient from EMF measurements. Let us consider the cell as usual hydrogen gas at 1 atmosphere is in touch with platinum electrode and we have a solution of HCl in aqueous medium having concentration m molality m molal solution is again in connection with AgCl solid with silver as electrode.

As usual this side is plus and that is minus and this m is molality of the solution. Molality is a way of expressing the concentration which means a certain number of moles of a substance dissolved in one kg of this solvent. So, the cell reaction that one can easily write is AgCl plus, you see here AgCl plus half H₂ getting silver converted to silver 0 plus HCl.

So, hydrogen is oxidized and silver is reduced in this particular case. So, when we write E_{cell} is equal to E_{cell}^0 minus RT by F it is one electron transfer \ln activity of H plus into activity of Cl minus. So, now, this activity of H plus is equal to activity of Cl minus because both are coming from HCl, so, the concentration of HCl is m as a result these two are same.

So, one can easily write that it is equal to E_{cell}^0 minus RT by F \ln activity of the plus minus electrodes at plus minus or cation anion together as a average square. So, this is called the mean

ionic activity and let γ_{\pm} be the mean ionic activity coefficient such that γ_{\pm} into m is equal to a_{\pm} . So, when you replace it in this equation E_{cell} is equal to $E^{\circ}_{\text{cell}} - \frac{RT}{F} \ln \gamma_{\pm} m$.

Now, if we try to simplify $E^{\circ}_{\text{cell}} - \frac{RT}{F} \ln \gamma_{\pm} m$ as $E^{\circ}_{\text{cell}} - \frac{2RT}{F} \ln m$ and then we further simplify as $E^{\circ}_{\text{cell}} - \frac{2RT}{F} \ln m$, I am now bringing this $\ln m$ before and converting \ln to \log and applying the values for R and T at 25 degrees centigrade and multiplying by 2 dividing by F that number turns out to be $118 \log m - 0.118 \log \gamma_{\pm}$. So, now, in the next step we rearrange this E_{cell} minus or rather plus we bring this $\log m$ to the left hand side, so $0.118 \log m$ is equal to $E^{\circ}_{\text{cell}} - 0.118 \log \gamma_{\pm}$.

Now, I am continuing here and without changing the slide for your benefit, so, now using the Debye-Huckel limiting law for dilute solutions, this $\log \gamma_{\pm}$ is equal to $-\frac{Z^2}{\sqrt{m}}$ where Z is a constant and its value is 0.5 for uni-univalent ions, so, one can rewrite this equation as $E_{\text{cell}} + 0.118 \log m$ equal to $E^{\circ}_{\text{cell}} + \frac{Z^2}{\sqrt{m}}$.

So, now this equation looks like $Y = C + \frac{1}{x}$ and the constant C is another constant, $Y = mx + C$. So, when we try to plot this Y versus x which is square root of m and with varying concentration of that HCl solution, the molality with by varying that molality one can determine the value of Y using a potentiometer that is the total potential that is coming in the potentiometer for this particular cell one can measure that and one can get a few readings like this, with increasing molality the value for the entire value of Y within the bracket will keep on increasing with increase in m this $\log m$ will increase so the value will keep on increasing and square root of m .

So, when I am increasing m square root of m is also increasing. So, one has to join those dots with a line and then when you extrapolate what you get here at m equal to 0, this value gives you the value of E_{cell} and from the slope one can calculate the value of Z which now again is, it can be varied can be verified whether it comes out to be half or not because we as we said that Z is a constant which is true for uni-univalent pair of ions. So, when this E_{cell} is known Y is known we know the value of Z , for a given value of m we calculate the value of E_{cell} and one can easily calculate the value of E°_{cell} .

Now, E0 cell when it is found out, one can also calculate the value of gamma plus minus using this expression for different values of m from this expression because now you replace this Z square root of m by gamma plus minus log gamma plus minus and from there you can easily calculate the value of log gamma plus minus when you know the value of this Y from the potentiometer readings.

So, this is how one can determine the physical quantity, the mean activity coefficient gamma plus minus using the EMF measurement method. So, we will continue in the next lecture from here. Thank you.