

Elementary Electrochemistry
Professor Angshuman Roy Choudhury
Department of Chemical Sciences
Indian Institute of Science Education and Research, Mohali
Numerical Problems: Nernst Equation, EMF of Half Cell Reactions

Welcome back to the course entitled elementary electrochemistry. So, in the previous lecture, we have discussed about how one can calculate the EMF of a cell from the half cell potentials and we have discussed a few such cells and talked about how one can calculate the EMF of a cell.

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Calculate the equilibrium constant of the reaction $H_2 + Cl_2 \rightleftharpoons 2HCl$ if the EMF of the corresponding cell is 1.01 V.

Oxidation:
 $H_2 \rightleftharpoons 2H^+ + 2e^-$
 $E_{H^+/H_2}^0 = 0 \text{ V} \rightarrow \text{Anode}$

Reduction:
 $Cl_2 + 2e^- \rightleftharpoons 2Cl^-$
 $E_{Cl_2/Cl^-}^0 = +1.35 \text{ V} \rightarrow \text{Cathode}$

Overall Reaction:
 $H_2 + Cl_2 \rightleftharpoons 2HCl$
 $E_{cell}^0 = E_{cathode}^0 - E_{anode}^0 = 1.36 \text{ V}$

Nernst Equation:
 $E_{cell} = E_{cell}^0 - \frac{RT}{nF} \ln \frac{1}{a_{Cl_2}}$
 $E_{cell} = 1.01 \text{ V}$
 $1.01 = 1.36 - \frac{0.0591}{2} \log K_c$
 $\log K_c = \frac{E_{cell}^0 - E_{cell}}{0.0591/n} = \frac{1.36 - 1.01}{0.0591/2} = 23.018$
 $K_c = 1.02 \times 10^{23}$

So, in today's lecture, we are going to try to solve a few problems related to those what we have learned in last few classes. So, the question number one is calculate the equilibrium constant of the reaction H_2 plus Cl_2 in equilibrium with $2HCl$ if the EMF of the corresponding cell is 1.01 volt.

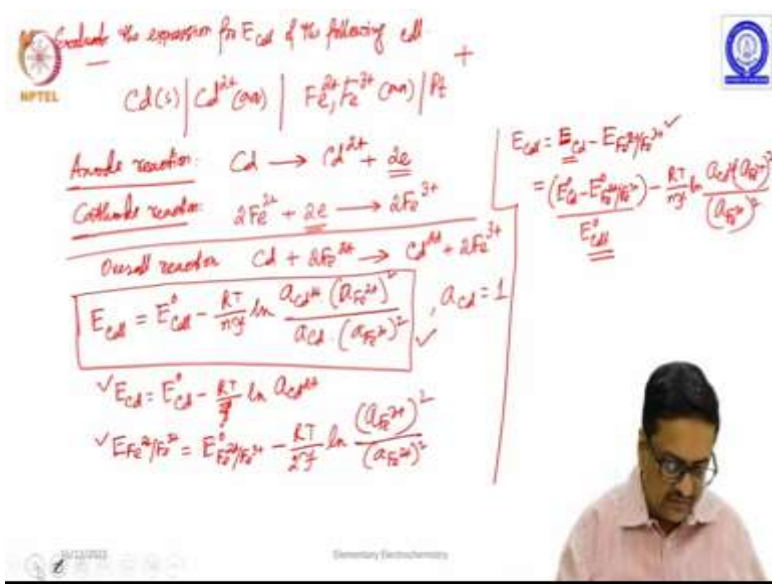
So, to solve this problem what we need to do is we need to first write down the chemical reaction that is happening at this electrode at this cell H_2 plus Cl_2 forming $2HCl$ which is given. So, here this H is getting oxidized, hydrogen is getting oxidized and chloride is getting reduced. So, if we write this reaction in the two half cell reactions, one can write it as half H_2 getting oxidized to H plus plus electron and half Cl_2 taking up one electron is getting up reduced to Cl minus and the overall reaction is half H_2 plus half Cl_2 giving you just HCl .

So, now, we have two electrodes here, one is the electrode H plus and half H₂ by convention we assume this potential to be equal to 0 and the other electrode which is E⁰ half Cl₂ Cl minus is taken from the literature value from a textbook is 1.35 volt. So, here we have this electrode is used as anode and this electrode is used as a cathode. So, then when you write E⁰ cell is nothing but E⁰ cathode minus E⁰ anode which is equal to 1.36 volt.

So, now what we know from our previous class the Nernst equation E⁰ is equal to RT by nF and then when we convert it to using the T equal to 298 Kelvin, then this constant turns out to be 0.0591 by n log K_a, so, then here instead of activity one can convert it into 1 by number of electron transfer is 1, one can write log K_c and then you can calculate that log K_c is equal to E⁰ divided by 0.0591 which turns out to be equal to 23.0118. So, one can easily calculate the value of K_c as 1.027 into 10 to the power 23, so, that is the equilibrium constant for that particular reaction.

You see this value is given it is the E cell which is equal to 1.01 volt and you can recall E cell is nothing but E⁰ cell minus RT by F ln, in this case the activity of Cl minus will be here. So, in this condition this is the EMF, that is the EMF of the cell and not the E⁰ cell. So, here we do not need to use this value at all, one has to use the E⁰ of the chlorine chloride electrode to calculate the equilibrium constant of this reaction.

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Calculate the expression for E_{cell} of the following cell

$$\text{Cd(s)} | \text{Cd}^{2+}(\text{aq}) || \text{Fe}^{2+}, \text{Fe}^{3+}(\text{aq}) | \text{Pt}$$

Anode reaction: $\text{Cd} \rightarrow \text{Cd}^{2+} + 2\text{e}^-$

Cathode reaction: $2\text{Fe}^{3+} + 2\text{e}^- \rightarrow 2\text{Fe}^{2+}$

Overall reaction: $\text{Cd} + 2\text{Fe}^{3+} \rightarrow \text{Cd}^{2+} + 2\text{Fe}^{2+}$

Nernst equation:

$$E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{nF} \ln \frac{a_{\text{Cd}^{2+}} (a_{\text{Fe}^{2+}})^2}{a_{\text{Cd}} (a_{\text{Fe}^{3+}})^2}, a_{\text{Cd}} = 1$$

Final expression:

$$E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{(a_{\text{Fe}^{2+}})^2}{(a_{\text{Fe}^{3+}})^2}$$

Alternative derivation:

$$E_{\text{cell}} = E_{\text{Cd}} - E_{\text{Fe}^{3+}/\text{Fe}^{2+}}$$

$$= \left(E_{\text{Cd}}^{\circ} - \frac{RT}{2F} \ln a_{\text{Cd}^{2+}} \right) - \left(E_{\text{Fe}^{3+}/\text{Fe}^{2+}}^{\circ} - \frac{RT}{2F} \ln \frac{(a_{\text{Fe}^{2+}})^2}{(a_{\text{Fe}^{3+}})^2} \right)$$

Final result:

$$E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{(a_{\text{Fe}^{2+}})^2}{(a_{\text{Fe}^{3+}})^2}$$

So, now, the question number two; evaluate the expression for E cell of the following cell. Cadmium solid is in equilibrium with cadmium $2+$ in aqueous medium is in connection with Fe^{2+} plus Fe^{3+} plus in aqueous medium with platinum as electrode and here this side is the positive electrode, this side is the negative electrode, the positive and left is negative. So, the anode reaction is Cd getting oxidized to Cd^{2+} plus plus 2 electrons and the cathode reaction is $2Fe^{2+}$ plus plus 2 electrons giving you $2Fe^{3+}$ plus, so, we had to make two electron to balance that two electron.

So, when you write the overall reaction then you can write it as Cd plus $2Fe^{2+}$ plus is getting converted to Cd^{2+} plus plus $2Fe^{3+}$ plus. So, we can write E cell as E^0_{cell} minus $\frac{RT}{nF} \ln$ activity of Cd^{2+} plus into activity of Fe^{2+} plus square divided by activity of Cd into activity of Fe^{3+} plus square and now, one can set activity of Cd equal to 1 because it is pure metal. So, one can write the E cell without the E_{Cd} sorry, activity of Cd .

See on the other hand one can write E_{Cd} is equal to E^0_{Cd} minus $\frac{RT}{2F} \ln$ activity of Cd^{2+} plus. Similarly, $E_{Fe^{2+}/Fe^{3+}}$ plus as $E^0_{Fe^{2+}/Fe^{3+}}$ plus minus $\frac{RT}{F}$ rather $2F$ \ln activity of Fe^{3+} plus square divided by activity of Fe^{2+} plus whole square.

So, one can easily write that E cell is equal to E_{Cd} minus $E_{Fe^{2+}/Fe^{3+}}$ plus which is again nothing but what we have obtained. Here if you replace E_{Cd} by this equation and $E_{ferrosoferric}$ by this equation and then you simplify you will end up getting the difference of E^0_{Cd} minus $E^0_{Fe^{2+}/Fe^{3+}}$ plus which will be replaced by E^0_{cell} minus $\frac{RT}{nF} \ln$ activity of Cd^{2+} plus into activity of Fe^{2+} plus square divided by activity of Fe^{3+} plus whole square and this is replaced by E^0_{cell} . So, this is how one can derive the equations for the corresponding cells for a cell from the corresponding half cell potentials.

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Calculate the potentials of the following electrodes at 25 °C.

① $\text{Ag}/\text{Ag}^+ (a=10^{-5})$ ② $\text{Cu}/\text{Cu}^{2+} (a=0.2)$ ③ $\text{Pt}/\text{Fe}^{2+} (a=0.1), \text{Fe}^{3+} (a=0.01)$

① $\text{Ag} \rightarrow \text{Ag}^+ + e^-$

$$E_{\text{Ag}/\text{Ag}^+} = E_{\text{Ag}/\text{Ag}^+}^0 - \frac{RT}{F} \ln a_{\text{Ag}^+}$$

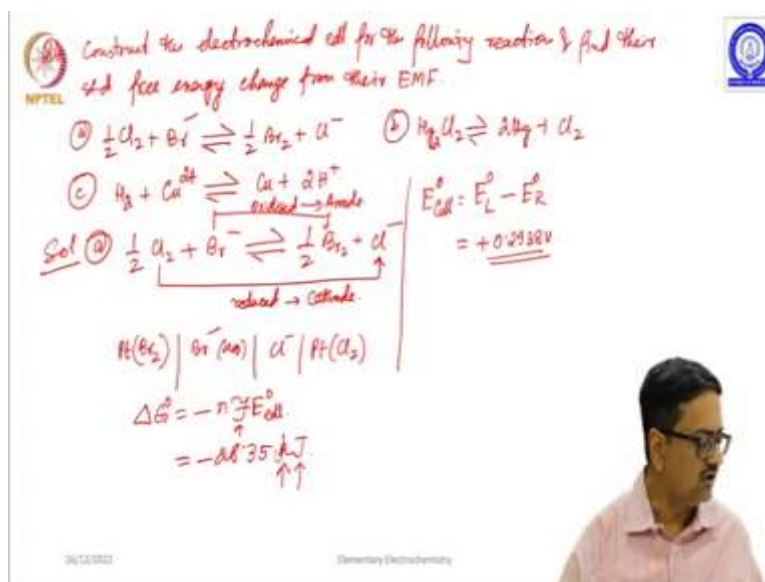
$$= (-0.799 - 0.0591 \log 10^{-5}) \text{ V}$$

$$= -0.119 \text{ V}$$

Let us see the question number 3, calculate the potentials of the following electrodes at 25 degree centigrade. So, 1 is Ag Ag plus with activity equal to 10 to the power minus 5. Number 2; Cu Cu2 plus with activity equal to 0.2. And number 3 is platinum electrode in equilibrium with Fe2 plus of activity equal to 0.1 and Fe3 plus of activity equal to 0.01. So, I will explain or I will show you how to do it with the first one and you should try to solve the other two. So, the reaction is Ag get going to Ag plus plus electron. So, $E_{\text{Ag}/\text{Ag}^+}$ is nothing but $E^0_{\text{Ag}/\text{Ag}^+}$ minus RT by F because it is one electron transfer \ln activity of a_{Ag^+} .

So, now, you take the value of this $E^0_{\text{Ag}/\text{Ag}^+}$ from the literature we found it to be 0.799 volts minus 0.0591 \ln , I think should be \log 10 to the power minus 5 and the unit is the volt. So, once you do this you should get it as 0.119 volt. So, this is the EMF of the half electrode with a given value of activity of silver. So, similarly, if you try to do this and that using the standard values available in any standard electrochemistry textbook which are prescribed for this course.

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Now, question number four is, construct the electrochemical cells for the following reactions and find their standard free energy change from their EMF. Once again you need to find out these EMFs from (a) any standard textbook and I am giving you three of them, we will solve one of them. Half Cl_2 plus Br^- is in equilibrium with half Br_2 plus Cl^- , b is Hg_2Cl_2 is in equilibrium with 2Hg plus Cl_2 and c is H_2 plus Cu^{2+} plus in equilibrium with Cu plus 2H^+ plus aqueous.

So, let us try to solve a, so, it is nothing but half Cl_2 plus Br^- giving you half Br_2 plus Cl^- minus. So, here what we see bromine is getting oxidized, so, that means this is happening at anode and chlorine is getting reduced, so, this is happening at cathode. So, as soon as we identify the corresponding cathode and anode, we quickly write down the possible cell with suitable electrode. So, what we write is platinum is in equilibrium with bromine gas and the solution and the solution contains Br^- in aqueous medium. It is in equilibrium with or it is in contact with Cl^- minus with platinum with chlorine.

So, now, what one can easily calculate here is E^0_{cell} is nothing but $E^0_{\text{L}} - E^0_{\text{R}}$. And when you try to find out those values from the textbook and do the math, you will get this to be plus 0.2938 volt. So, what we know is ΔG^0 is equal to minus nFE^0 and this E^0 is the E^0_{cell} which is this one.

So, when you do that you place the value of f as 96500 and n is a one electron transfer, one can easily calculate this number or the ΔG to be minus 28.35 kilo Joules, you see, one has to note that when we are writing kilo that k is small, and when we write the joule, it is the unit of energy, but then the unit comes from the name of a person as a result that J is capital. So, always whenever you are writing the unit one has to remember how to write the unit correctly with proper capital or small letters.

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NPTEL

If the potential of the cell is $Zn/ZnCl_2 (m=0.01) | AgCl(s) | Ag$ is 1.16V, calculate the mean ionic activity of $ZnCl_2$ solution.

Q2. Consider the cell
 $Tl | TlCl(s) | KCl_2 (m=0.1) | Hg_2Cl_2(s) | Hg$
 $E_{cell} = 0.73V, \frac{dE}{dT} = 7.5 \times 10^{-4}$
 What is the cell reaction?
 Calculate ΔG° and ΔH° of the cell.

Q3. Construct a suitable cell and calculate the E_{cell} value for the following cell reaction:

$$I_3^- + 2I^- \rightarrow 3I^-$$

oxidation

reduction

Elementary Electrochemistry

So, now, I want to give you a couple more problems for you to solve at home. So, to problems to be solved at home are this the following; If the potential of the cell is cell sorry, $Zn/ZnCl_2$ with molality 0.01 in connection with $AgCl$ solid with Ag as electrode is 1.16 volts then calculate the mean ionic activity of $ZnCl_2$ solution.

Question number two is consider the cell given below Tl in connection with $TlCl$ in solid form, it is in connection with KCl solution of molality 0.1 and the other end the electrode is Hg_2Cl_2 solid with mercury as your electrode. I think one should not write this slash because slash indicates phase boundary, one should write just comma. The value given is the E_{cell} as 0.73 volt and dE/dT equal to 7.5×10^{-4} . So, the question is what is the cell reaction? Calculate ΔG and ΔH of this cell.

And question number three is, construct a suitable cell and calculate the E_{cell} value for the following cell reaction; the reaction is $I_3^- + 2I^-$ getting converted to $3I^-$

indium plus. See here what is happening is the same element indium is getting reduced and here it is getting oxidized. So, you can understand that both the electrodes will have system of indiums. So, one has to find out the electrode potential of different indium cations with indium 0 and indium cations and another indium cations and so on to do this problem.

So, you need to find out the standard electrode potentials for various indium related systems from a textbook. So, here I leave these three problems for you to solve before the next class. Thank you.