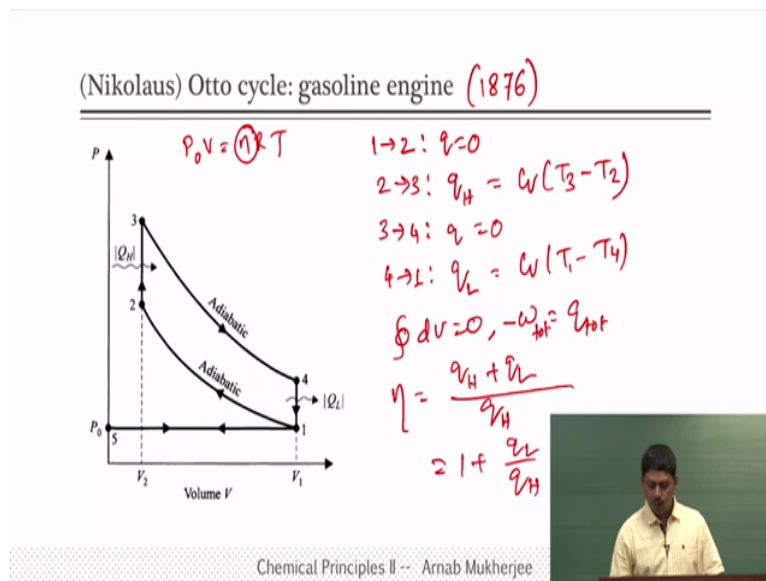


Chemical Principles II
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Module 05
Lecture 28
Gasoline Engine and Diesel Engine

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Now we are going to talk about two internal combustion engine, so one of that internal combustion engine is called gasoline engine which was proposed by Nikolaus OTTO around 1876 a long after of course Stirling engine. Internal combustion engine means wherever the heat is produced inside the engine, external combustion engine that combustion happens to get the heat. So here we are not having any combustion but we are giving the heat from outside.

So if the engine is designed such a way that the heat is getting generated inside the engine then we call it that as internal combustion engine and gasoline engine is one of the internal combustion engine. So it has these typical four steps again, however there is a fifth step or the first step where the engine takes away the fuel gas combination, but fuel and gas it takes in the first step, initially there is nothing inside the engine so because of volume is 0 as you can see.

The first step is called intact step it goes to 1 meaning it takes away the gas inside the engine followed by an adiabatic compression. Now we know that in adiabatic compression what

happens, the temperature increases. So in 1 to 2 the temperature you know suddenly increases from 1 to 2 and then this 2 to 3 is called a combustion step where the fuel that is there because of the high temperature the fuel gets burned, suddenly volume does not change but the burning of the fuel generates lot of heat.

And that heat will now help to move the piston in an adiabatic manner from 3 to 4 and that is called power stroke, this is what actually drives the piston and drives everything and then that followed by a cooling step from 4 to 1 where heat will go outside and then the fuel 1 to 5 the fuel will be ejected out of the or fuel gas combination ejected out is called exhaust this is the exhaust step.

In 1 step also the pressure in this 4 to 1 the pressure decreases where some of the gas is released unless until the pressure come to one atmospheric pressure, otherwise at 4 pressure is high than the atmospheric pressure, then at 1 it becomes atmospheric, so P_0 is the atmospheric pressure. Now in this particular step we are going to calculate again the efficiency of this particular engine.

So you can see that in 1 to 2 step it is an adiabatic compression process, okay. We can talk about 5 to 1 step which is nothing but if you talk about an ideal gas, so $P V$ equal to nkT or nRT , so in that volume is 0, so at constant atmospheric pressure gas is just taken in, so n goes from 0 to some value that is it. Now main thing is I wanted to which is the compression process in which your q equal to 0, so no heat is ejected or taken in so therefore we do not have to worry about that.

In 2 to 3 you know that the q that is q in or you can say q_H as it is given here is again $C_v T_3$ minus T_2 , 3 to 4 q equal to 0 again and 4 to 1 q_L which is $C_v T_1$ to T_4 . Now you see I have not done the work done and all because we know that for any cyclic process U is going to be 0, if U is going to be 0 then we know that q equal to minus W . So total work done by the system is nothing but the negative of the heat or total work done by the system is just the heat.

So we know for a cyclic process cyclic process your U equal to 0, so therefore total work done by the system is nothing but total heat. So now if I calculate the efficiency of the engine it will be total work done by the system which is q_{tot} which is q_H plus q_L and the input heat is just q_H so that is the efficiency of the engine, which again gives us q_L by q_H . Now this is always the case, every engine we see that it is 1 plus q_L by q_H except the way it is if

it is done the way that in two steps you take in the heat and throw out the heat, but if you take the heat in multiple steps of course it will not be the case.

Now here there are two adiabatic steps so no heat is taken in and out, so it turns out that we can write that as 1 plus q L by q H.

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(Nikolaus) Otto cycle: gasoline engine (1876)

$P_0 V = nRT$

1→2: $q=0$
 2→3: $q_H = C_V(T_3 - T_2)$
 3→4: $q=0$
 4→1: $q_L = C_V(T_1 - T_4)$

$\oint dU = 0, -w_{tot} = q_{tot}$

$$\eta = \frac{q_H + q_L}{q_H} = 1 + \frac{q_L}{q_H}$$

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Efficiency of Gasoline engine

$$\eta = 1 + \frac{q_L}{q_H} = 1 + \frac{C_V(T_1 - T_4)}{C_V(T_3 - T_2)} = 1 + \frac{T_1 - T_4}{T_3 - T_2}$$

$$= 1 - \frac{T_4}{T_3} \quad \left| \quad \eta = 1 - \frac{300}{500} = 1 - \frac{3}{5} = 0.4 \right.$$

$T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$
 $T_4 V_4^{\gamma-1} = T_3 V_3^{\gamma-1}$
 $\frac{T_1}{T_4} = \frac{T_2}{T_3} \quad (V_1 = V_4, V_2 = V_3)$
 $\frac{T_1 - T_4}{T_4} = \frac{T_2 - T_3}{T_3} \quad \left| \quad \frac{T_1}{T_4} = \frac{T_2}{T_3} \right.$
 $\frac{T_1 - T_4}{T_2 - T_3} = \frac{T_4}{T_3} \quad \left| \quad \frac{T_1}{T_2} = \frac{T_4}{T_3} \right.$

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Now what will be the value of that? So Eta is 1 plus q L by q H and we know that q L is C v let us go back and see what is the q L, C v T 1 minus T 4 and q H is C v T 3 minus T 2. So 1 plus T 1 minus T 4 by T 3 minus T 2, now in order to simplify this process we have to get some relations from this. So let me draw it again just for remembering. Now you see that this 1 to 2 is an adiabatic process so we can use the formula for an adiabatic process which is T 1 V 1 to the power gamma minus 1 is T 2 V 2 to the power gamma minus 1.

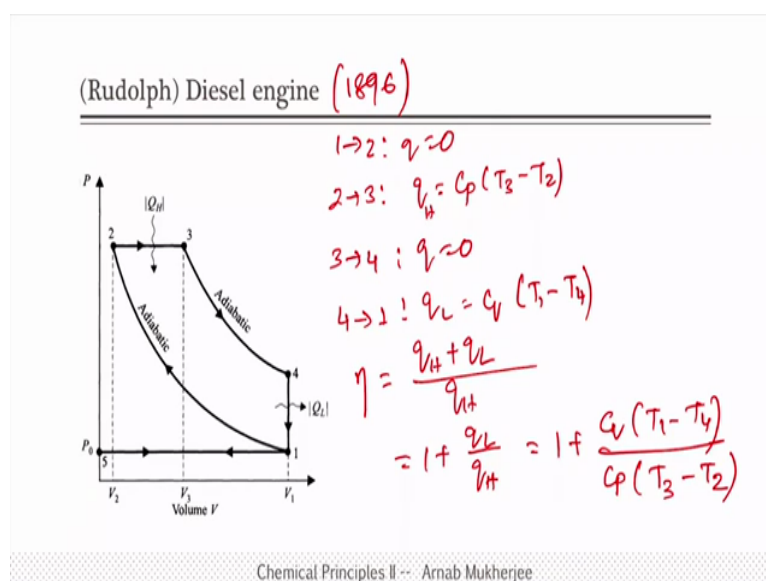
For 3 to 4 also we can do the same thing $T_4 V_4$ to the power $\gamma - 1$ is $T_3 V_3$ to the power $\gamma - 1$. Now once we take the ratio of that we will get T_1 by T_4 is equal to T_2 by T_3 because $V_1 = V_4$ and $V_2 = V_3$, okay. So now once we get that we know that I can put minus 1 on both sides, we can get $T_1 - T_4$ by T_4 , $T_2 - T_3$ by T_3 , okay.

So now I can go $(1 - \frac{T_1 - T_4}{T_4})$, I can take the numerator on this side to down $T_2 - T_3$ is equal to $T_4 - T_3$, but I have $T_1 - T_4$ and $T_3 - T_2$, so I need a minus sign so this one becomes $1 - \frac{T_4 - T_3}{T_3}$, also we know from this relation is that T_1 by T_4 is equal to T_2 by T_3 and if I rearrange that I will get T_1 by T_2 is equal to T_4 by T_3 , you can also write as $1 - \frac{T_1}{T_2}$.

So you see now the efficiency of this particular engine depends on the difference in temperature between 1 and 2 that is a difference of a compression, so during the compression how much difference of temperature you can make that will determine the efficiency of the engine. So typically at 1 it is at normal temperature 300 kelvin and in 2 by compression it goes approximately 500, so if you take that then you can calculate the efficiency to be $1 - \frac{300}{500}$, $1 - \frac{3}{5}$ to 0.4, okay.

So basically depending on 500, 600 whatever so you get ideal efficiency as 0.4, 0.5, however the actual efficiency goes to 0.35 because of losses and many other things. So depending on how much you can compress that will give rise to the amount of temperature and that will give rise to efficiency, so that is the gasoline engine.

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And little bit later like 20 years down the line around 1896 Rudolph Diesel proposed another type of engine called diesel engine and again we have the diesel cars also which works in that way. So the difference between gasoline engine and diesel engine is that, in diesel engine only air is taken in not the air fuel mixture. So again in the first step there is an intact step where the air is taken in and again it gets compressed to very large extent and during this compression process the air gets compressed so of course the temperature goes very very high and then in the 2nd to 3rd step the fuel gets injected.

And in that high temperature the fuel gets burned, you do not need any spark or anything to burn the fuel because the temperature is high enough at the stage 2 that the fuel gets burned and it is injected in such a way that the pressure remains constant between 2 to 3 and once that gets burned then the next step is the power stroke where it will push the piston and come from 3 to 4 and then the other two steps like 3 to 4 and 4 to 1 is same like a gasoline engine. So the only difference is that here it is like a air diesel engine where only the air is compressed, not the air fuel mixture that is the only difference.

Now here also you can calculate the efficiency, let us do that so again in the first step 1 to 2, it is an adiabatic step so q is 0 and 2nd to 3rd step is it is a constant pressure process so q is $C_P T_3 - T_2$ this is the q_H actually and 3 to 4 step again q equal to 0 and 4 to 1 step where the q_L is $C_V T_1 - T_4$, you see here that I am not using any minus sign or anything because since I am going in a cyclic manner the signs will automatically come in.

For example if you look at q_H , since T_3 is higher than T_2 , q_H is the positive quantity. So a positive heat is as I told you in the first law of discussion time that a positive heat is heat that goes into the system because that is going to increase the internal energy of the system and negative heat automatically means that heat is going out of the system. Now you see that T_1 is less than T_4 , so therefore q_L by itself is a negative number which means the heat is going out of the system.

So now we have these 4 values, so when you calculate the efficiency η , this is again the same the total work done by the system is q_H plus q_L as I explained just now and the heat input is nothing but q_H on the so it will be $1 + q_L / q_H$. Now let us calculate the you know we can write down one more step here $1 + C_V T_1 - T_4 / C_P T_3 - T_2$.

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Efficiency of Diesel engine

$$\eta = 1 + \frac{C_V (T_1 - T_4)}{C_P (T_3 - T_2)}$$

$$= 1 + \frac{1}{\gamma} \left(\frac{T_1 - T_4}{T_3 - T_2} \right)$$

$$= 1 + \frac{1}{\gamma} \frac{(1 - T_4/T_1) T_1}{\left(\frac{T_3}{T_2} - 1 \right) T_2}$$

$$= 1 - \frac{1}{\gamma} \left(\frac{T_4/T_1 - 1}{T_3/T_2 - 1} \right) \frac{T_1}{T_2}$$

$$= 1 - \frac{1}{\gamma} \left(\frac{r_E^\gamma - 1}{r_E - 1} \right) \frac{T_1}{T_2}$$

$$T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$$

$$T_4 V_4^{\gamma-1} = T_3 V_3^{\gamma-1}$$

$$\frac{T_1}{T_4} = \frac{T_2}{T_3} \left(\frac{V_2}{V_3} \right)^{\gamma-1}$$

$$\frac{T_4}{T_1} = \frac{T_3}{T_2} \left(\frac{V_3}{V_2} \right)^{\gamma-1}$$

$$\frac{T_4}{T_1} = \left(\frac{V_1}{V_2} \right) \left(\frac{V_3}{V_2} \right)^{\gamma-1}$$

$$= r_E r_E^\gamma$$

$$= r_E^{\gamma+1}$$

$$\frac{V_3}{V_2} = r_E$$

$$\frac{V_3}{V_2} = \frac{V_3}{T_3} \frac{T_2}{V_2} = \frac{V_3}{T_3} r_E$$

$$\frac{V_3}{V_2} = \frac{T_2}{T_3} r_E$$

$$r_E \approx 5$$

$$\gamma = 1.4$$

T1=300 K
T2=1000 K
η=0.5

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(Rudolph) Diesel engine (1896)

1→2: $q=0$
2→3: $q_H = C_P (T_3 - T_2)$
3→4: $q=0$
4→1: $q_L = C_V (T_4 - T_1)$

$$\eta = \frac{q_H + q_L}{q_H}$$

$$= 1 + \frac{q_L}{q_H} = 1 + \frac{C_V (T_1 - T_4)}{C_P (T_3 - T_2)}$$

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So efficiency η is $1 + \frac{C_V (T_1 - T_4)}{C_P (T_3 - T_2)}$. Now we know that $\frac{C_P}{C_V}$ is γ , so it is $1 + \frac{T_1 - T_4}{\gamma (T_3 - T_2)}$. Now let us simplify this process and I am going to draw it here just for remembering this is a constant pressure process so 1, 2, 3 and 4 these are two adiabatic processes and this is a constant pressure process is constant volume process just to remember that this is a handy way to have that.

Now let us write the relation, so first relation that we write is between the adiabatic step, so $T_1 V_1^{\gamma-1} = T_2 V_2^{\gamma-1}$ to the power $\gamma - 1$ is $T_2 V_2^{\gamma-1}$. Similarly $T_4 V_4^{\gamma-1} = T_3 V_3^{\gamma-1}$ to the power $\gamma - 1$. Take the ratio T_1 by T_4 and we know that $V_1 = V_4$ because it is a constant process but however volume

of 2 and 3 are not same. So here we are going to get T_2 by $T_3 V_2$ by V_3 to the power $\gamma - 1$, okay.

Now V_2 and V_3 so there is a volume change between 2 and 3, so V_3 by V_2 is typically called expansion ratio r_E because here the expansion is happening and ratio between 1 and 2 is called compression ratio, these ratios are important in order for the efficiency that we can see you know in a moment. Now we have this relation, just we will invert it so T_4 by T_1 is T_3 by $T_2 V_3$ by V_2 to the power $\gamma - 1$.

Now what is the relation of T_3 and T_2 let us understand that for that we are going to use the relation between 2 and 3. Now since it is an ideal gas we can always write $P_2 V_2$ by T_2 is equal to $P_3 V_3$ by T_3 we can do that for any two points. Now you see that the pressure is same between P_2 and P_3 so cancels, so therefore V_3 by V_2 by expansion ratio is T_3 by T_2 , okay.

So now we are going to get T_4 by T_1 as V_3 by V_2 into V_3 by V_2 to the power $\gamma - 1$, so since V_3 by V_2 is expansion ratio we are going to get r_E r_E to the power $\gamma - 1$, so therefore r_E to the power γ . So we got that and so now let us come back to this left hand side, so it is $1 + 1$ by γ let us take a T_1 common so if I take T_1 common it will become $1 - T_4$ by T_1 and T_1 outside, let us take T_2 common so T_3 by T_2 minus $1 - T_2$.

Now we see that let us take a negative of these numerators so $1 - 1$ by γT_4 by T_1 minus $1 - T_3$ by T_2 minus $1 - T_1$ by T_2 now let us just put the values $1 - 1$ by γT_4 by T_1 is r_E to the power γ you can see here r_E expansion ratio to the power $\gamma - 1$ and T_3 by T_2 is simply r_E so r_E minus $1 - T_1$ by T_2 , so this is the you know efficiency of at diesel engine which of course depends on the expansion ratio as I said before and also on the γ , so one can have a calculation typically expansion ratio as 5 r_E you know typical values of thing will be 5 γ typical value will be like say 1.4 and you are going to get an efficiency of around 0.5, ideal efficiency is also almost like 0.3, 0.4 similar to like gasoline engine although we know that a little bit more efficient than gasoline engine the diesel engine is right.

Okay, so one important thing to discuss here is that in both the gasoline engine and diesel engine there is this constant pressure process and constant volume process, in gasoline engine

there are two constant volume processes and in diesel engine one constant pressure and constant volume processes.

Now in constant pressure or volume processes the temperature changes all the time and therefore in order to make a reversible engine we need to place this system in infinite number of heat reservoirs. Therefore one you know it is difficult to compare with a Carnot engine which says that it has to work Carnot engine works between a fixed two temperature reservoirs. In this case it is not possible to do so, although we are getting an efficiency which is $(T_2 - T_1)/T_1$ temperatures, but it cannot be directly compared with the Carnot engine which says that the efficiency is $1 - T_2/T_1$ because in that case there is only two temperatures T_1 and T_2 but in case of diesel engine there are all temperatures are different 1, 2, 3 and 4 all are different and so it does not really work between only just two temperature reservoirs.

However, given that they are all reversible steps one can have an effective two temperature differences to represent the efficiency of this engine if possible, but it cannot be directly compared with that. We are going to show that all reversible engines have basically same efficiency, the point is that the diesel engines cannot have that you know reversibility because of this constant pressure and constant volume steps.

So now we are going to show later that Carnot engine has the highest efficiency for working within the two temperature reservoirs and so that means all reversible engines have highest efficiency than the irreversible engines and all reversible engines have the same efficiencies. So that is why I was telling that given that diesel engine and gasoline engine can be constructed in reversible manner its efficiency will be as good as the Carnot engine because all reversible engine will have to have the same efficiency, but practically it is not possible because a constant temperature difference process cannot be done in reversible.