

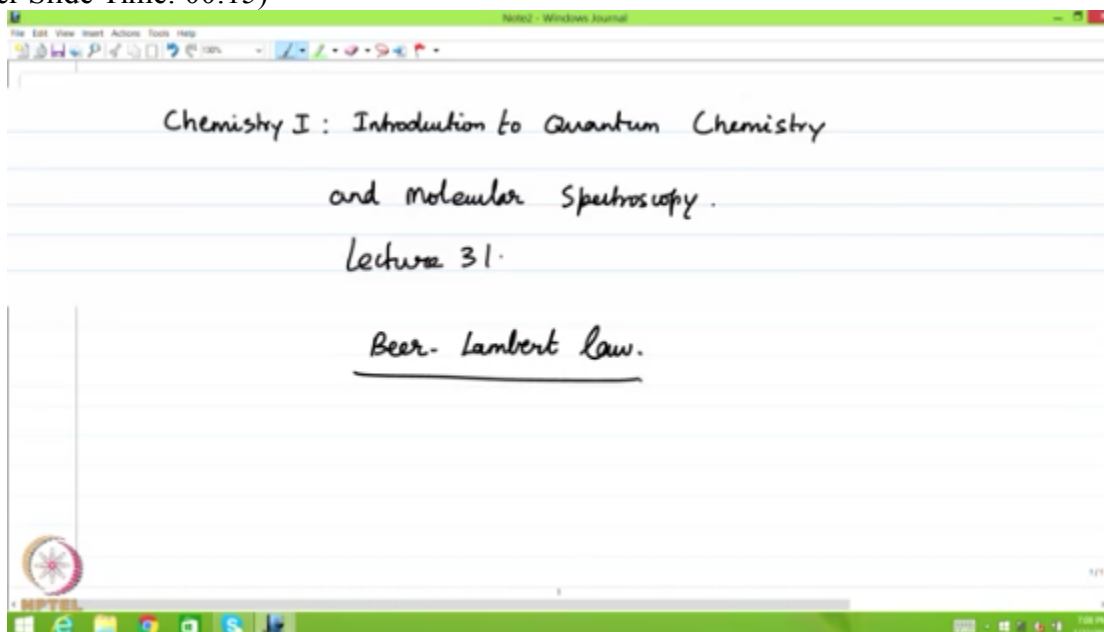
**NPTEL
NPTEL ONLINE CERTIFICATION COURSE**

**Chemistry 1
Introduction to Quantum Chemistry and
Molecular Spectroscopy**

**Lecture 31
Beer – Lambert Law**

**Prof. Mangala Sunder Krishnan,
Department of Chemistry,
Indian Institute of Technology Madras**

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Welcome back to the lecture on spectroscopy, the introduction to molecular spectroscopy and chemistry 2. This is a very short lecture on an important quantitative law known as Beer Lambert law which is used to study the fluorescence properties and also determine concentrations of compounds which show fluorescence character in samples, therefore it's a quantitative law used to measure concentrations of species through fluorescence basically absorption of light, absorption of visible light.

And I shall just write down the law in a simple form,
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Chemistry I: Introduction to Quantum Chemistry

and molecular Spectroscopy.

Lecture 31.

Beer-Lambert Law.

Used to measure concentrations

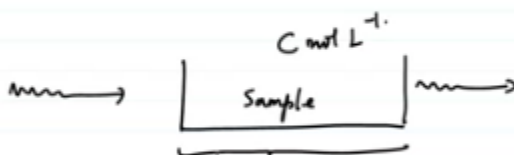
through absorption of visible light

we'll say more of it when we study electronic spectroscopy with some applications and properties of molecules and so on, in a very simple and elementary form the Beer Lambert law goes like this. Suppose we have light falling on a sample tube containing the sample, and let the concentration be C moles per liter, and let the length of the spectroscopic cell the photometrically spectrophotometer the cell but which we use to measure the absorption and also take the spectrum,

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Used to measure concentrations

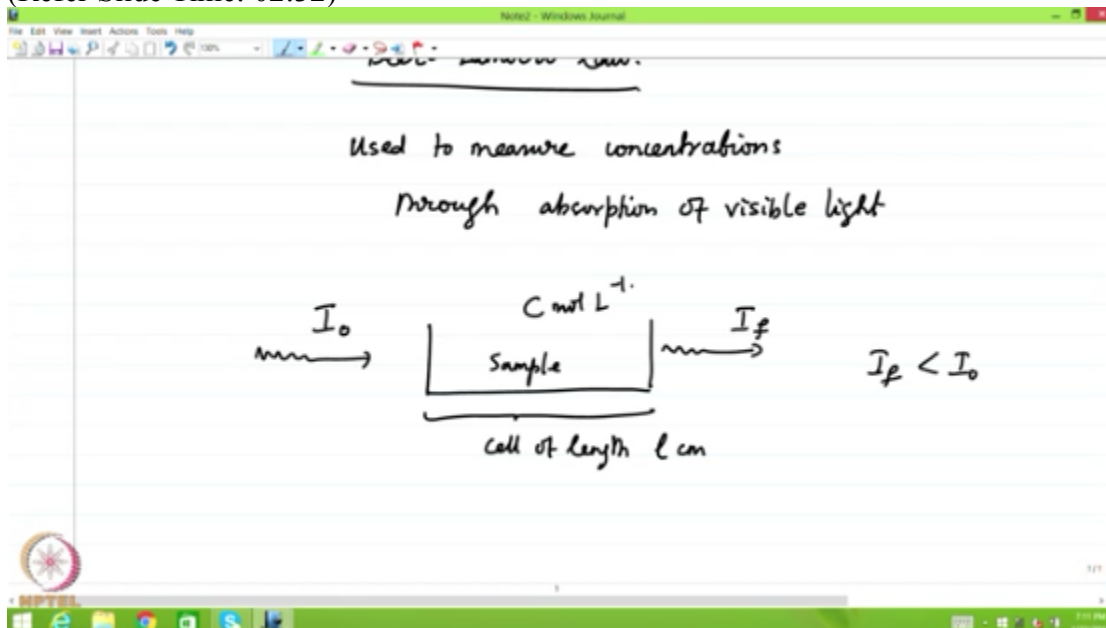
through absorption of visible light



this is the cell of length say L centimeters, so usually 1 centimeter or even less than that.

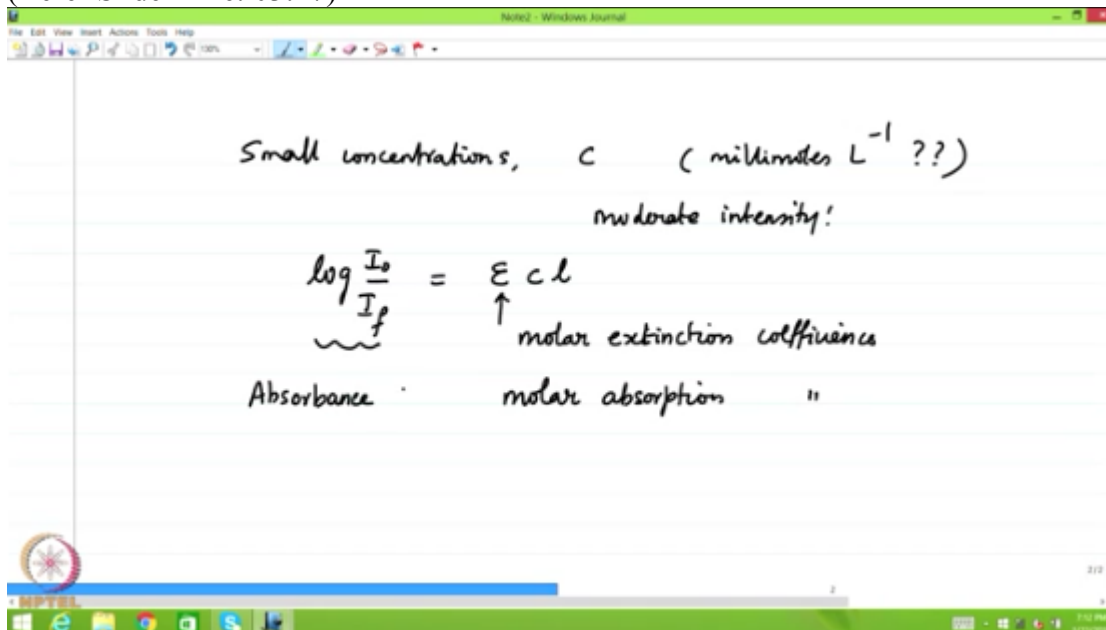
And if light with a certain initial intensity I_0 of visible light falls on the sample and light with the intensity I is emitted obviously I is less than I_0 , okay, that means that the sample has absorb some light

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and this phenomenon for certain small concentrations and reasonably low intensities of light absorptions, small concentrations C like millimoles per liter kind of concentrations or even less, okay, typical example.

And then for light of moderate intensity, satisfies the law that $\log I_{\text{naught}}/I_f = \text{a constant times the concentration of the substance and there is the length of the cell and this constant is called the molar extinction coefficient or molar absorption coefficient, and this is called absorbance,}$
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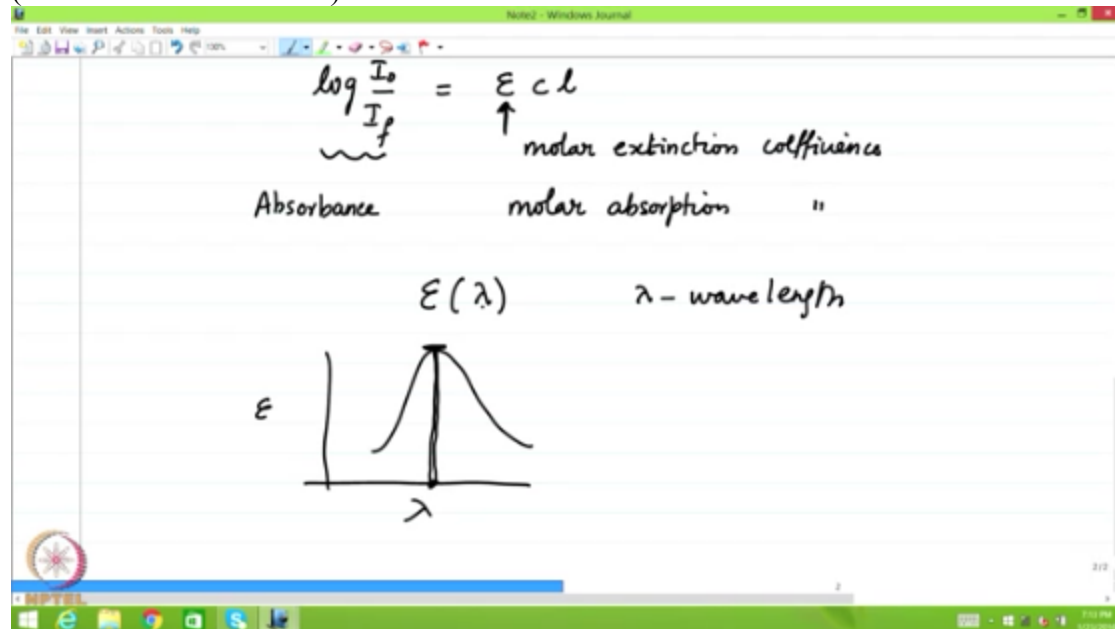


you can also write this in the form of transmitted radiation, and so this can be written in the form of light that is, this is the light that is transmitted therefore this ratio the logarithm of I_{naught}/I_f

gives a constant associated with each system, each chemical species and one important is that this epsilon is actually a function of the wavelength of light, lambda B the wavelength.

So typically if a species absorbs light and so function of the lambda and you write the epsilon, as a function of epsilon lambda you choose that value of epsilon for which the absorption is the maximum, that is, that value of the light, lambda, so you choose that lambda and perform the 6 pyramid,

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and these are tabulated in all electronics spectra textbooks and also in analytical chemistry textbooks.

Now how do we get this law? Log I naught/IF is equal to this constant epsilon times concentration and length, okay, so very simple argument that if you have a cell of length L consider a small, and extremely small what is known infinite simile small DL, because at that level you can imagine that most things will be linear,

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Handwritten notes on a digital notepad. At the top, a horizontal line with arrows at both ends is labeled with the Greek letter λ . Below this, the Beer-Lambert law is written as $\log \frac{I_0}{I_f} = \epsilon c l$. The dl part of the equation is underlined with two vertical lines. A bracket is drawn underneath the entire equation.

if there is an absorption that absorption will be roughly proportional to the concentration in that region and the absorption, I mean if there is more species obviously that will be more absorption that linear law can be obtained from starting with this kind of infinite decimals, therefore if you do that the DL which is also a very small length tells you that the absorption is dependent on DL itself, if DL is slightly more, more absorption and so on.

So what you do is you take the differential if I is the intensity at this point and $I - dI$ is the intensity of light that is emitted passing through DL then you can write the $-dI$ as roughly proportional to the concentration and proportional to the DL, and obviously also proportional to the intensity of light that all format.

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Handwritten notes on a digital notepad, similar to the first image. It includes the same λ diagram and the equation $\log \frac{I_0}{I_f} = \epsilon c l$. The dl is underlined. A diagram shows a light beam of intensity I entering a medium of thickness dl from the left, and emerging with intensity $I - dI$ on the right. To the right of this diagram, the following proportionalities are listed:

$$\begin{aligned}
 -dI &\propto c \\
 &\propto dl \\
 &\propto I
 \end{aligned}$$

Therefore if you write this the linear law simply gives you $-dI$ is some constant which I'll write as say kappa, okay some K times C times DL times I and so you can write $-dI/I$ is a kappa, a constant C DL, and now you extend this argument that this is what happens throughout and therefore if you start with I_0 here as the initial intensity and if you end up with I_f as the intensity of light emitted at the other side of the cell
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$\log \frac{I_0}{I_f} = \epsilon c l$

$I_0 \rightarrow \left| \begin{array}{c} I \\ \hline I-dI \end{array} \right| \xrightarrow{dl} I_f$

$-dI \propto C$
 $\propto dl$
 $\propto I$

$-dI = \kappa c dl I$
 $-\frac{dI}{I} = \kappa c dl$

then you know when you integrate this equation you integrate it between the limits I_0 and I_f , you can write dI/I and write that as the length being also integrated it is kappa times say DL, starting from the length 0 here to the length L, so this gives you immediately L and I between the limits I_0 and I_f is kappa C L, between the limits 0 and L,
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$I_0 \rightarrow \left| \begin{array}{c} I \\ \hline I-dI \end{array} \right| \xrightarrow{l} I_f$

$-dI \propto C$
 $\propto dl$
 $\propto I$

$-dI = \kappa c dl I$
 $-\frac{dI}{I} = \kappa c dl$

$-\int_{I_0}^{I_f} \frac{dI}{I} = \kappa c \int_0^l dl$
 $\ln I \Big|_{I_0}^{I_f} = \kappa c l \Big|_0^l$

and therefore you know immediately that you get L and I_0 by I_f is kappa times C times L, and LN is of course 2.303 times logarithm to the base 10 of I_0/I_f and that's equal to

κ times CL and so you write logarithm of to the base 10 I_0/I_f is equal to $\kappa/2.303$ which is again a constant times CL , and this is what is called the epsilon or the molar extinction coefficient.

And by dimension please remember this is dimension less because they both refer to intensities, so this is left hand side is dimensionless, right hand side is moles per liter, and usually L is expressed in centimeter therefore epsilon is liter per mole per centimeter, (Refer Slide Time: 08:39)

$$\ln \frac{I_0}{I_f} = \kappa c l$$

$$2.303 \log_{10} \frac{I_0}{I_f} = \kappa c l$$

$$\Rightarrow \underbrace{\log_{10} \frac{I_0}{I_f}}_{\text{dimensionless}} = \left(\frac{\kappa}{2.303} \right) c l$$

ϵ
↓
molar extinction

$$\epsilon \text{ L mol}^{-1} \text{ cm}^{-1}$$

and at low concentrations and low intensities epsilons are additive, so if you have two substances the differing concentrations then the absorption or that frequency of or the wavelength of light by both the substances is roughly additive that the absorbance of the first one and the absorbance of the second one and in the logarithmic ratio and here they add in terms of the concentration times the molar extinction coefficient, some small numerical problems will give you how to do this in a, and how to do this for different concentrations and also sometimes determine the unknown concentration of the substance that you want to find out in by a fluorescence experiment, this is an important rule and we shall see more of it, but I just wanted to introduce this as something to remember before we do the electronic spectroscopy.

From the next lecture onwards we shall start with the microwave and then the vibrational and the electronic spectroscopy. And also talk about the molecular properties like dipole moment, the polarizabilities, the moments of inertia as we start looking up microwave spectroscopy, that will be some numerical problems given on this in some pure assignments to make you familiar with some of these elementary concepts, okay. We'll continue this with the subsequent lectures on rotational spectroscopy, until then thank you very much.

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