

## Spectroscopic Techniques for Pharmaceutical and Biopharmaceutical Industries

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Lecture No. 12

### Problems on Rotational, Vibrational & Raman Spectroscopy

Hello students, welcome to lecture 12 of this course, the last 5 lectures I have discussed about rotational spectroscopy, vibrational spectroscopy, rotational-vibrational spectroscopy and Raman spectroscopy. We have looked at both theory and application of these spectroscopy techniques. In this lecture, I will discuss about problems related to this spectroscopy.

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**Problems: MCQs**

**Q1.** Calculate the frequency ( $\nu$ ) corresponding to the transition with a wavelength of 56 nm.

a)  $5.2 \times 10^{12}$  Hz  
b)  $5.4 \times 10^{15}$  Hz  
c)  $4.8 \times 10^{15}$  Hz  
d)  $5.4 \times 10^6$  Hz

**Ans: (b)**

$\nu = \frac{c}{\lambda} = \frac{3 \times 10^8 \text{ m/s}}{56 \times 10^{-9} \text{ m}}$



(Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press)

So, I will start with multiple choice question, first question is quite easy that tells you what frequency if wavelength is given. So, question is calculate the frequency corresponding to the transition with wave length of your 56 nanometer. So, we know that frequency related to  $c$  by  $\lambda$  where  $c$  is your velocity of light and  $\lambda$  is your wavelength  $\lambda$  is given it is 56 nanometer, it means that 56 into 10 per to power minus 9 meter. If you, we calculate this will get the frequency in per second which is basically hertz. So, it is quite easy question and if you do calculation and what will you get is 5.4 into 10 to power 15 hertz. So, this is the frequency of light of wavelength 56 nanometer.

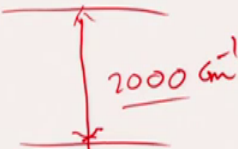
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**Problems: MCQs**

**Q2.** Identify the region of electromagnetic spectrum where the wavenumber of the given transition is  $2000\text{ cm}^{-1}$ .

- a) Infrared
- b) Ultraviolet-visible
- c) Radiowave
- d) Microwave

**Ans: (a)**



 (Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press)

Now, let us go to second question in this you have to identify the region of electromagnetic spectrum where the wave number of given transition is 2000 centimeter inverse. So, these are the 2 energy states and you have to tell that, if they have number of given transition is 2000 centimeter inverse, then what is the region of electromagnetic spectrum? And this is, this you have to know because the wavelength corresponding to 2000 centimeter inverse falls in IR region and so answer is infrared region.


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**Problems: MCQs**

**Q3.** The Selection rule for rotational transition is

- a)  $\Delta J = 0$
- b)  $\Delta J = \pm 1$
- c)  $\Delta J = \pm 2$
- d) All of above

**Ans: (b)**



The next question is what is the selection rule for rotational transition and what is the selection rule for rotational transition? There are 4 options  $\Delta J$  is equal to zero,  $\Delta J$  is equal to plus minus 1,  $\Delta J$  is equal to plus minus 2 and the all of the above we have already discussed this in our previous lecture. So, we know that selection rule for rotational transition is  $\Delta J$  is equal to plus minus 1. So, answer will be b.

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**Problems: MCQs**

**Q4.** Upon isotope substitution of higher mass


- Reduced mass increases ✓
- Energy of transition level decreases ✓
- Rotation constant decreases ✓
- All of above ✓

**Ans: (d)**

Handwritten notes:

$$B \propto \frac{1}{I} \propto \frac{1}{\mu}$$

$$\mu = \frac{m_1 \times m_2}{m_1 + m_2}$$

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$$


Next question is upon isotope substitution of higher mass what happens? Reduced mass increases, energy of transition level decreases, rotational constant decreases, all of the above. So, we need to know how to write to reduced mass and we know that it is mass is  $m_1$  into  $m_2$  divided by  $m_1$  plus  $m_2$ ,  $m_1$  plus  $m_2$  and so, if we substitute an element with its isotope with higher mass what we are going to get is your increase in reduced mass and then we know that frequency of your transition is equal to  $1$  by  $2\pi$  root  $k$  by  $\mu$ .

So, here your reduced mass will increase and if reduce mass increases, your frequency will decrease. So, this is also right and then about rotational constant, so,  $B$  is equal to, so, we need to know what is  $B$  and  $B$  is inversely proportional to your  $1$  by  $I$  and since  $I$  relates to  $\mu$ , you can also write  $1$  by  $\mu$  and so your  $B$  will decrease with increase in  $\mu$  which in reduced mass. So, basically all of the above that  $d$  option is correct.


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**Problems: MCQs**

**Q5.** Rotational-Raman transitions lie between

- a) two rotational levels
- b) two vibrational levels
- c) two electronic levels
- d) rotational & vibrational levels

**Ans: (d)**



Now, next question is the rotational Raman transitions lie between, 2 rotational levels, 2 vibrational levels, 2 electronic levels and rotational and vibrational levels. So, if you remember rotational Raman transition, you will be able to answer this question very easily and the answer is your d.


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**Problems: MCQs**

**Q6.** The Selection rule for rotational-Raman transition is

- a)  $\Delta J = 0$
- b)  $\Delta J = \pm 1$
- c)  $\Delta J = \pm 2$
- d) Both (a) & (b)

**Ans: (c)**



Now, next question is what is the selection rule for rotational Raman transition. So, the options given are  $\Delta J$  is equal to zero,  $\Delta J$  is equal to plus minus 1,  $\Delta J$  is equal to plus minus 2 and these both A and B to answer is your  $\Delta J$  is equal to plus minus 2. I have discussed this in

detail in the rotational Raman transition and it was quite clear that why  $\Delta J$  should be equal to plus minus 2. So, answer is c.


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**Problems: MCQs**

**Q7.** The region of a IR spectrum between  $1400-600\text{ cm}^{-1}$ , represents

- a) finger-print region ✓
- b) low frequency region ✓
- c) functional group region ✓
- d) none of above

**Ans: (a)**



(Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press)

Now, you go to a specifics of IR spectrum and next question based on that question is the region of IR spectrum between 1400 to 600 centimeter inverse represents. So, these are the regions fingerprint region, low frequency region, functional group region and none of the above and the answer is fingerprint region. And this is very important region if you want to get a structural feature of the molecule using IR spectroscopy.


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**Problems: MCQs**

**Q8.** Which of the following molecules possesses IR active vibrations

- a)  $\text{CF}_4$
- b)  $\text{D}_2$
- c)  $\text{NO}$  ✓✓
- d) All of these

**Ans: (c),** because  $\text{NO}$  possesses dipole moment.

 (Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press)

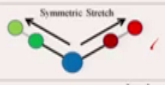
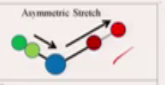


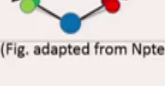

Which of the following molecule possesses IR active vibration? So, next question is based on the selection rule, you must know what is the selection rule for vibrational spectroscopy and rotational spectroscopy and the things we know is that dipole moment of the molecule must change during the vibration. So, in this the one which possesses IR active vibration is  $\text{NO}$ , because its dipole changes during the vibration.

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**Problems: MCQs**


**Q9.** Identify, which of the following is **not** a bending molecular vibration.

- a) Wagging ✓
- b) Twisting ✓
- c) Stretching ✓✓
- d) Scissoring ✓
- e) Rocking ✓

	
In-plane Bending	
	
Out of Plane Bending	
	

(Fig. adapted from Nptel, Bioanalytical Techniques)

**Ans: (c)**



Now, next question is, identify which of the following is not bending molecular vibration. So, there are 5 different kind of vibration is given one is wagging, then twisting, stretching,

scissoring, rocking, and we know that stretching is not a bending vibration a stretching is not a bending vibration. So, answer is c, you have a stretching, symmetric stretching vibration.

This is your asymmetric stretching vibration in plane bending. So, in plain bending can be up to type scissoring and rocking. So, scissoring both are moving in towards each other. Whereas, in rocking, there is like rocking between 2 different position. Out of plain bending and out of plain bending will be again of 2 types and your wagging and twisting, the wagging and twisting. So, you must remember these different types of vibrational modes in this wagging, twisting visiting and rocking are type of bending molecular vibration while stretching not so, answer is c.

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**Problems: Rotational Spectroscopy (spacing between rotational lines)**

10. For a gaseous HCl molecule, the internuclear distance is found to be 143 pm. If the rotational spectrum of HCl comprises of equally distance lines, calculate the spacing between the lines. (Given: atomic masses of  $^1\text{H}$  and  $^{35}\text{Cl}$  are  $1.673 \times 10^{-27}$  kg and  $58.06 \times 10^{-27}$  kg, respectively.)

Ans: The reduced mass for HCl:  $\mu = \frac{m_1 m_2}{m_1 + m_2} = 1.626 \times 10^{-27}$  kg


The internuclear distance,  $r = 143 \text{ pm} = 1.43 \times 10^{-10}$  m

The moment of inertia,  $I = \mu r^2 = 1.626 \times 10^{-27} \times (1.43 \times 10^{-10})^2 = 3.33 \times 10^{-47}$  kg.m<sup>2</sup>

The spacing between the lines,

$$2B = \frac{2 \cdot h}{8\pi^2 I c} = \frac{2 \cdot 6.626 \times 10^{-34} \text{ J.s}}{8 \times (3.14)^2 \times (3.33 \times 10^{-47} \text{ kg.m}^2) \times (3 \times 10^{10} \text{ cm.s}^{-1})} = 16.80 \text{ cm}^{-1}$$

*Handwritten notes: } 2B = \frac{2h}{8\pi^2 I c}*



Now, after multiple choice question let us go to some problems related to rotational spectroscopy. And this is a question based on the spacing between rotational lines. So, question is given for a gaseous is HCl molecule the inter nuclear distance is found to be 143 Pico meter. If the rotational a spectrum of HCl comprises of equally distance lines, calculate the spacing between the lines. So, you have to calculate a spacing between the lines what is given is internally or distance. So, a spacing between the lines is 2B if you remember where B is equal to h by 8 pi square Ic Ic where B is in wave number unit, wave number unit.

If we want to calculate the spacing between rotational line in hertz unit then the c will not be here, spacing will always be equal to 2B only thing is the formula will differ when you are expressing the in terms of hertz, then there will be no c, but if you are expressing B in terms of

centimeter inverse then you need to write  $h$  into  $8\pi^2 I c$ . So,  $2B$  will be  $2h$  divided by  $8\pi^2 I c$ ,  $2h$  divided by  $8\pi^2 I c$ .

So, first thing we need to know is  $I$  because  $h$  and  $c$  are constant and we know the value of  $h$  and  $c$  and  $h$  is your  $6.626 \times 10^{-34}$  Joule seconds, whereas, your  $c$  is  $3 \times 10^{10}$  by power 10 centimeter per second. So, here I have calculated  $B$  in terms of centimeter inverse unit, our wave number unit basically, and wave number unit can also be expressed as meter inverse or centimeter inverse if you are using meter inverse then we have to express  $c$  in terms of meter per second if you want answer in centimeter inverse then we have to express velocity of light in centimeter per second.

So,  $h$  and  $c$  are the constants whose values are already known, what we need to calculate is  $I$  and for  $I$  you need to know reduced mass which is  $\mu$ , your  $\mu$  is given by  $m_1 m_2$  divided by  $m_1 + m_2$  and  $m_1 m_2$  is given here this is  $m_1$ , this is  $m_2$  and you can calculate the reduced mass using this formula. One thing you must keep in mind that  $m_1$  is mass of 1 molecule mass of 1 molecule or mass of 1 atom it is not mass of 1 mole of atom or molecule.

So, what does that mean is that you have to express  $m_1$  in atomic mass unit, atomic mass unit not in gram per mole. So, but if you suppose take  $m_1$  in gram per mole unit, then you need to divide that by Avogadro number that will give you mass of 1 molecule or 1 atom not 1 mole of molecule or 1 mole of atom. So, this thing you need to keep in mind and then  $r$  you need to express in meter and then you can calculate  $I$  is equal to  $\mu r^2$ .

So, you can calculate moment of inertia using  $I$  is equal  $\mu r^2$ ,  $\mu$  already here calculated and  $r$  is  $1.43 \times 10^{-10}$  meter and so, your moment of inertia will be in kg per meter square. And once you put here in this equation, then you can get the value of  $2B$  which will tell you about the spacing between the lines which is equal to 16.8 centimeter inverse.



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**Problems: Rotational Spectroscopy (frequency/wavenumber of transition)**

**Q11.** From a pure rotational spectrum of NO molecule, the bond length of NO is found to be 1.15 Å. Calculate the frequency corresponding to the changes in rotational quantum number  $J=3 \rightarrow J=4$ .

**Solution:** Reduced mass of NO,

$$\mu_{NO} = \frac{m_N m_O}{m_N + m_O} = \frac{14 \times 16}{(14 + 16)} \frac{1}{6.023 \times 10^{23}} \text{ g}$$
$$= 1.24 \times 10^{-23} \text{ g} = 1.24 \times 10^{-26} \text{ kg}$$

Moment of inertia,

$$I = \mu r^2 = (1.24 \times 10^{-26} \text{ kg})(1.15 \times 10^{-10} \text{ m})^2$$
$$= 1.426 \times 10^{-46} \text{ kg.m}^2$$


(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

**Problems: Rotational Spectroscopy**


**Q11.** From a pure rotational spectrum of NO molecule, the bond length of NO is found to be 1.15 Å. Calculate the frequency corresponding to the changes in rotational quantum number  $J=3 \rightarrow J=4$ .

**Solution:**

Rotational constant,  $B = \frac{h}{8\pi^2 I c}$  (wave number unit)

$$= \frac{6.63 \times 10^{-34} \text{ J.s}}{8 \times (3.14)^2 \times (1.426 \times 10^{-46} \text{ kg.m}^2) \times (3 \times 10^{10} \text{ cm.s}^{-1})} = 1.96 \text{ cm}^{-1}$$

Frequency required for transition, ( $J=3 \rightarrow J=4$ ) will be

$$\tilde{\nu} = 2B(J+1) = 2 \times 1.96 \times 4 = 15.68 \text{ cm}^{-1}$$


(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

Let us go to next question in this question, you have to calculate frequency wave number of transition from the rotational spectrum. So, question is from a pure rotational spectrum of NO molecule the bond length of NO is found to be 1.15 angstrom, calculate the frequency corresponding to changes in rotational quantum number  $J$  is equal to 3 to  $J$  is equal to 4,  $J$  is equal to 3 to  $J$  is equal to 4. So, certainly we need to calculate  $B$  for that, first you need to calculate the moment of inertia and for moment of inertia we need reduced mass and bond length, bond length is already given.

So, first we need to calculate your reduced mass. So, reduced mass of NO will be given by mass of N multiplied by mass of O divided by mass of N plus mass of O, here we are taking mass of 1 nitrogen not 1 mole of nitrogen. Here you will take mass of 1 oxygen and again this is mass of 1 nitrogen plus mass of 1 oxygen. So, this is 14 and 16 divided by 14 plus 16 we now need to divide by Avogadro number, because 14 and 16 gram is basically the weight of 1 mole of nitrogen or mass of 1 mole of nitrogen and mass of 1 mole of oxygen respectively.

So, we need to divide by Avogadro number and once we divide by Avogadro number what we are going to get is your reduced mass in kg, first you will get reduced mass in grams and then you divide by 1000 you will get to this mass in kg. Now, we can calculate moment of inertia by using this equation,  $I$  equal to  $\mu$  into  $r$  square,  $r$  is already given that is 1.15 angstrom and that is basically 1.15 into 10 to the power minus 10 meter.

So, you square this and multiplied by this reduced mass you will get moment of inertia in kg meter square. So, now, we know what is the moment of inertia. Now, let us go and calculate your rotational constant, rotational constant in wave number unit is your  $h$  divided by  $8 \pi^2 I c$ . So,  $B$  is equal to  $h$  divided by  $8 \pi^2 I c$ , here this is in wave number unit wave number unit, wave number unit. If we want to express  $B$  in hertz unit then we need to just remove this  $c$ , this  $c$ .

So, now, we can go ahead and calculate  $B$  since we know what is the value of  $h$ , what is the value of  $c$  and what is the value of  $I$ . So, this is your value of  $h$ , this is what we calculated and this is your velocity of light in centimeter per second and so our  $B$  will be in centimeter inverse unit if you take  $c$  in meter per second then we will get the answer in meter inverse unit and the answer is 1.96 centimeter inverse and now, we can calculate what is the frequency required for transition from  $J$  is equal 3 to  $J$  is equal to 4.

Now, again you keep in mind some sometime you write  $\bar{\nu}$  as  $2B J$  and in some work you will find it  $2B J + 1$ , but that is not basically different because, when you express your  $\bar{\nu}$  in  $2B J$ , then I am talking about  $J$  value for the excited state and when I say  $\bar{\nu}$  is equal to  $2B J + 1$  then the  $J$  is the value from, value of the energy level from where transition is happening, from where transition is happening. So, here the value of  $J$  is 3 and so, you can get  $\bar{\nu}$  and  $\bar{\nu}$  will be  $2B$  into 4,  $B$  we have already calculated and so,  $\bar{\nu}$  is 15.68 centimeter inverse.

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**Problems: Rotational Spectroscopy, Effect of Isotopes**

**Q12.** If the bond length in both HF and DF molecules is same i.e. 0.053 nm, compare the value of (a) reduced mass ( $\mu$ ), (b) moment of inertia (I), (c) rotational constant (B) and (d) wavenumber ( $\bar{\nu}$ ) for the transition  $J=2 \rightarrow J=3$ .

Solution:(b) Moment of inertia (I),

For HF molecule,

$$I_{HF} = \mu r^2 = 4.44 \times 10^{-48} \text{ kg.m}^2$$

&

for DF molecule,

$$I_{DF} = \mu r^2 = 4.44 \times 10^{-48} \text{ kg.m}^2$$



(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

**Problems: Rotational Spectroscopy, Effect of Isotopes**

**Q12.** If the bond length in both HF and DF molecules is same i.e. 0.053 nm, compare the value of (a) reduced mass ( $\mu$ ), (b) moment of inertia (I), (c) rotational constant (B) and (d) wavenumber ( $\bar{\nu}$ ) for the transition  $J=2 \rightarrow J=3$ .

Solution:(c) Rotational Constant (B),

For HF molecule,

$$B_{HF} = \frac{h}{8\pi^2 I c} = 63.10 \text{ cm}^{-1}$$

&

for DF molecule,

$$B_{DF} = \frac{h}{8\pi^2 I c} = 33.24 \text{ cm}^{-1}$$

Another way, for DF molecule,

rotational constant (B) is inversely proportional to the reduced mass ( $\mu$ )

$$B_{DF} = \frac{B_{HF} \mu_{HF}}{\mu_{DF}} = 33.23 \text{ cm}^{-1}$$



(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

**Problems: Rotational Spectroscopy: Effect of Isotopes**

**Q12.** If the bond length in both HF and DF molecules is same i.e. 0.053 nm, compare the value of (a) reduced mass ( $\mu$ ), (b) moment of inertia ( $I$ ), (c) rotational constant ( $B$ ) and (d) wavenumber ( $\bar{\nu}$ ) for the transition  $J=2 \rightarrow J=3$ .

**Solution:** (d) Wavenumber ( $\bar{\nu}$ ) required for the transition  $J=2 \rightarrow J=3$

For HF molecule,

$$\bar{\nu}_{HF} = 2B_{HF}(J+1) = 2 \times 63.10 \times 3 = 378.6 \text{ cm}^{-1}$$

&

For DF molecule,

$$\bar{\nu}_{DF} = 2B_{DF}(J+1) = 2 \times 33.24 \times 3 = 199.38 \text{ cm}^{-1}$$

**Conclusion:** Replacing H with D,  $B$  and  $\bar{\nu}$  gets almost doubled while  $\bar{\nu}_{J=2 \rightarrow J=3}$  reduced to nearly half

NPTEL  
(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

Now, next question is basically to look at the effect of isotopes, question reads as if the bond length in both HF and DF molecule is same and it is given as (0.03) 0.053 nanometer. Now, we have to compare the value of reduced mass. So, when you are going from HF to DF and bond length is same then what is the effect of isotope on reduced mass, moment of inertia, rotational constant, a wave number for the transition  $J$  is equal to 2 to  $J$  is equal to 3.

So, let us go first calculate reduced mass,  $\mu$  HF will be mass of 1 hydrogen atom multiplied mass of 1 fluorine atom divided the mass of 1 hydrogen atom plus mass of 1 fluorine atom when you do the calculation, what you will get is  $1.58 \times 10^{-27}$  kg. Same calculation you can do DF molecule and the answer will be  $3.16 \times 10^{-27}$  kg and so, you can just divide  $\mu$  DF by  $\mu$  HF and you can see what will the value of reduced mass for these 2 molecules. If you notice it the  $\mu$  DF is almost twice that of  $\mu$  HF.

Now, let us go and calculate moment of inertia and moment of inertia is given by  $\mu r^2$  and  $r$  is taken to be constant and is equal to 0.053 nanometer when you do the appropriate substitution what you are going to get is moment of inertia in kg meter square and this is your  $4.44 \times 10^{-48}$ . And for DF it will be equal to I think this will be almost double of that this is wrong. So, please correct it probably this is 8.88 you do the calculation it is not very difficult why I am saying double because  $\mu$  of HF is half of  $\mu$  of DF.

So, please make the appropriate correction. Now, once we know the  $\mu$  value and  $I$  value we can go ahead and look at the rotational constant for these 2 molecules. And if you do a calculation for

HF, using  $B$  is equal to  $h$  by  $8\pi^2 I_c$ , you will get the  $B$  value for HF equal to 63.10 centimeter inverse and  $B$  of DF is 33.24 centimeter inverse, 33.24 (centi inverse) centimeter inverse, this is right. Now you see that this rotational constant is inversely proportional to moment of inertia. And since moment of energy, of FF is twice that of HF.

And so  $B$  value will be,  $B$  value of DF will be half of the value of HF approximately half of the value of  $B$  value of HF and that is what it is it in here that by using the concept that rotational constant inversely proportional to reduced mass we can calculate the  $B$  value of DF. Since we know  $B$  value of HF. So, we may not need to calculate this, we can simply do we can simply use this formula  $B_{HF}$  into  $\mu_{HF}$  by  $\mu_{DF}$ . So after the calculation of rotational constant for HF and DF now we will see what is the value of wave number for the transition  $J$  is equal to 2 to  $J$  is equal to 3.

So, we can use this formula to know the wave number again  $J$  is value of rotational level from where transition is happening, from where transition is happening. So, here transition is happening from  $J$  is equal to 2. So,  $J$  is equal to 2 here and so, you can calculate the  $2B$  into  $J$  plus 1 and this is 2 into 63.1 into 3 and the answer is 378.6 centimeter inverse. For DF molecule same equation can be used and then wave number what we get for  $J$  is equal to 2 to  $J$  is equal to 3 transition is 199.38 centimeter inverse. Again you can see your  $\nu_{DF}$  is half of  $\nu_{HF}$  and that is not surprising because  $B$  of DF is half of  $B$  for HF. So, replacing H with D  $\nu$  gets doubled. So, I think this is wrong  $\nu$  gets doubled whereas  $B$  and  $\nu_{DF}$  reduce to nearly half.

(Refer Slide Time: 25:49)

**Problems: Rotational Spectroscopy, Effect of Isotopes**

**Q13.** If the natural abundance of  $\text{H}_2^{18}\text{O}$  in  $\text{H}_2^{16}\text{O}$  is 1.3%, calculate the relative intensity of the two rotational lines for the same transition in case of  $\text{H}_2^{16}\text{O}$ .

**Solution:** Natural abundance of  $\text{H}_2^{18}\text{O} = 1.3$

□ Natural abundance of  $\text{H}_2^{16}\text{O} = 100 - 1.3 = 98.7$

Also, Natural abundance of  $\text{H}_2^{18}\text{O} = 1.3 = \frac{I^*}{I + I^*} \times 100$  ... (i)

where,  $I^*$  is the intensity due to  $\text{H}_2^{18}\text{O}$

Natural abundance of  $\text{H}_2^{16}\text{O} = 98.7 = \frac{I}{I + I^*} \times 100$  ... (ii)

Taking ratio of (ii) to (i), we get  $\frac{I}{I^*} = \frac{98.7}{1.3} = 76:1$

□ for same transition, rotational line for  $\text{H}_2^{16}\text{O}$  is 76 times intense than that of  $\text{H}_2^{18}\text{O}$

So, now, let us see another question based on effect of isotopes. So, question is, if the natural abundance of  $\text{H}_2^{18}\text{O}$  in  $\text{H}_2^{16}\text{O}$  is 1.3 percent, calculate the relative intensity of 2 rotational lines for the same transition in case of  $\text{H}_2^{16}\text{O}$ . So, natural abundance of  $\text{H}_2^{18}\text{O}$  is given 1.3. So, natural abundance of  $\text{H}_2^{16}\text{O}$  can be calculated and that is 100 minus 1.3 and that is 98.7

So, natural abundance of  $\text{H}_2^{18}\text{O}$  always 1.3 and that should be equal to intensity for this  $\text{H}_2^{18}\text{O}$  divided by intensity for  $\text{H}_2^{16}\text{O}$  plus intensity of  $\text{H}_2^{18}\text{O}$  multiplied by 100. So,  $I^*$  is intensity due to  $\text{H}_2^{18}\text{O}$  and  $I$  is intensity due to  $\text{H}_2^{16}\text{O}$ . So, natural abundance of  $\text{H}_2^{18}\text{O}$  is equal to your 90 sorry this is 160 natural abundance of  $\text{H}_2^{16}\text{O}$  will be equal to 98.7 and that will be equal to  $I$  divided by  $I + I^*$  into 100 and if you take the ratio of this, this  $I + I^*$  will get cancel out. So,  $I$  by  $I^*$  is equal to 98.7 divided by 1.3 and that gives you 76 is to 1 so, for the same transition, rotational line for  $\text{H}_2^{16}\text{O}$  is 76 times intense than that of  $\text{H}_2^{18}\text{O}$ .

(Refer Slide Time: 27:57)

**Problems: Rotational Spectroscopy: Calculation of Atomic masses**

**Q14.** For a diatomic molecule NX, the spectral lines are equally spaced in its pure rotational spectrum. If average value of spacing between the lines and the equilibrium distance of the NX molecule are  $3.551 \text{ cm}^{-1}$  and  $1.128 \text{ \AA}$ , respectively; calculate the atomic mass of X.


**Solution:** Given:  $2B = 3.551 \text{ cm}^{-1}$ ; i.e.  $B = 1.776 \text{ cm}^{-1}$  &  $r = 1.128 \text{ \AA} = 1.128 \times 10^{-10} \text{ m}$

The moment of inertia of the molecule NX will be,

$$I = \frac{h}{8\pi^2 Bc} = \frac{6.63 \times 10^{-34} \text{ Js}}{8 \times (3.14)^2 \times (1.776 \text{ cm}^{-1}) \times (3 \times 10^{10} \text{ cm. s}^{-1})}$$
$$= 1.578 \times 10^{-46} \text{ kg.m}^2$$

The reduced mass of the molecule NX will be,

$$\mu = \frac{I}{r^2} = \frac{1.578 \times 10^{-46} \text{ kg.m}^2}{(1.128 \times 10^{-10} \text{ m})^2} = 1.240 \times 10^{-26} \text{ kg} = \underline{1.240 \times 10^{-23} \text{ g}}$$

 (Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

**Problems: Rotational Spectroscopy: Calculation of Atomic masses**

**Q14.** For a diatomic molecule NX, the spectral lines are equally spaced in its pure rotational spectrum. If average value of spacing between the lines and the equilibrium distance of the NX molecule are  $3.551 \text{ cm}^{-1}$  and  $1.128 \text{ \AA}$ , respectively; calculate the atomic mass of X.

**Solution:**

Now we know, reduced mass is also expressed as,


$$\mu_{NX} = \frac{m_N m_X}{m_N + m_X} \times \frac{1}{6.023 \times 10^{23}}$$

or

$$1.240 \times 10^{-23} \text{ g} = \frac{14m_X}{14 + m_X} \times \frac{1}{6.023 \times 10^{23}}$$

Solving for  $m_X$ , we get  $m_X = 16.01 \text{ g}$

This implies that the X atom is Oxygen and the molecule is **NO**.

 (Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

Now, next question is calculation of atomic mass. The question is for a diatomic molecule NX the spectral lines are equally spaced in its pure rotational spectrum if average value of a spacing between the lines and the equilibrium distance of NX molecule  $3.551 \text{ cm}^{-1}$  and  $1.128 \text{ \AA}$  and calculate the atomic mass of X.

So, based on rotational spectra, you can calculate the atomic masses and this is 1 of the example. So, again first we will calculate the reduced mass and reduced mass is mass of N multiplied by mass of X divided by mass of N plus mass of X into 1 divided by  $6.023 \times 10^{23}$ . So,

this we are doing because we are taking mN as molar mass So, if you take mN as molar mass then we will divide it by Avogadro number.

So, this is your mN you know that 14 into mX divided by 14 plus mX into 1 by 6.023 into 10 to power 23 and this is equal to mu obtained from let me see this mu obtained from the mu is what 1.24 into 10 to power minus 23. So, if you put it here you can calculate mX is equal to 16.01 and since mX is equal to 16.01. So, your molecule is a NO and your atom X is oxygen, atom X is oxygen.

So, the question 14 is that if you record the rotational spectrum of a molecule in which you do not know the atomic mass of one of the atom, so, here we are talking about diatomic atom, diatomic molecule and what you do is you take a rotational spectrum look at the what is the spacing between 2 lines that will give you a B from B you can know I and I will give you reduced mass if you know bond length, if you know bond length and once you know mu then you can calculate the mass of the other atom which is X here and what we showed you is that mass of the unknown atom is 16 gram and that tells you that the X atom is your oxygen atom.

(Refer Slide Time: 31:16)

**15. Recap/Stark effect (calculation of dipole moment)**

- In absence of Electric Field

$$E_r = \frac{h^2}{8\pi^2 I} J(J + 1)$$

- In the presence of electric Field

$$E_r = \frac{h^2}{8\pi^2 I} J(J + 1) + \frac{\mu^2 E^2 [J(J + 1) - 3M_f^2]}{2hB J(J + 1)(2J - 1)(2J + 3)}$$

(Linear molecule)

*Handwritten notes: A red arrow points from the text "dipole moment" to the  $\mu^2$  term in the second equation. Another red arrow points from the  $\mu^2$  term to the  $\mu$  in the numerator of the second equation.*



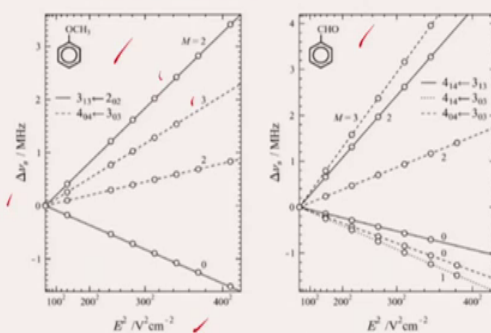
## Stark Shift in frequency

$$\Delta E_r = \frac{\mu^2 E^2 [J(J+1) - 3M_J^2]}{2hBJ(J+1)(2J-1)(2J+3)}$$

$$\Delta \nu = \frac{\mu^2 E^2 [J(J+1) - 3M_J^2]}{2h^2BJ(J+1)(2J-1)(2J+3)}$$



### The rotational spectra, electric dipole moments and molecular structures of anisole and benzaldehyde†



† of Stark effect measurements for selected *a*-type and *b*-type rotational transitions of anisole (left) and benzaldehyde (right).



Phys. Chem. Chem. Phys., 2005, 7, 1708–1715

Now, next question is calculation of dipole moment. I have not given a question, but I will show you one result from literature how to calculate dipole moment of molecule using rotational spectroscopy. So, for that, we know that in the absence of electric field, the energy of rotational levels is given by this  $h^2 / 8\pi^2 I J(J+1)$  and  $J$  is rotational quantum number and when you place the molecule in the electric field, then degeneracy is destroyed and in that case, for a linear molecule you give  $E_r$  with this equation,  $E_r$  with this equation and if I plot  $E_r$  versus  $E^2$  what I am going to get is  $\mu^2$  which is basically, here please do not confuse this  $\mu$  with the reduce mass.

This one is your dipole moment, dipole moment, moment. So, if you plot  $E_r$  versus  $E$  square, where is your electrical field you can get the dipole moment of a molecule, of a molecule. So,  $E_r$  is basically  $\Delta E_r$  is given by this value and then  $\Delta \nu$  is given by this value. So,  $\Delta \nu$  is basically  $\Delta E_r$  by  $h$  and you can see that it is  $2h$  square here it is  $2h$  and when I plot  $\Delta \nu$  vs  $E$  square, I can get the value of dipole moment where  $\nu$  is your dipole moment. So, I am showing you the calculation done in our paper.

This is paper from PCCP that is published in 2005. They calculated the dipole moment of anisole and benzaldehyde. And here you see data  $\mu$  versus  $E$  square. That is what we generally plot to get the dipole moment and they have calculated dipole moment, they have calculated dipole moment using this plot. Similarly, this is for anisole and this is for benzaldehyde. So, this is the way to calculate your dipole moment of a molecule using the splitting of rotational lines in electric field, electric field which is known as dark effect.

(Refer Slide Time: 34:21)

**Problems: Rotational-Raman Spectroscopy**

**Q16.** What will be the separation between the spectral lines in rotational-Raman spectrum?

**Solution:** The energies (in  $\text{cm}^{-1}$ ) of the rotational levels are given as:

$$F(J) = BJ(J+1)$$

The selection rule for the rotational transitions are  $\Delta J = \pm 2$ ,  
 the frequency of the absorption will be

$$\tilde{\nu} = F(J') - F(J) = BJ'(J'+1) - BJ(J+1) = B[J'(J'+1) - J(J+1)]$$

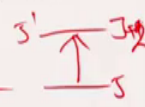
Now, we know that  $J' = J+2$ ; therefore,

$$\tilde{\nu} = B[(J+2)(J+3) - J(J+1)] = B(J^2 + 5J + 6 - J^2 - J) = B(4J + 6)$$

$$= 4B(J + 3/2)$$

Since  $J = 0, 1, 2, 3, \dots$  i.e. it increases by factor of 1, therefore the space between the spectral lines of the rotational-raman spectrum is  $4B$ .

(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)



Now, next question is from rotational Raman spectroscopy. So, what is the separation between spectral lines and rotational Raman spectrum, we know the separation between a spectral lines in rotational spectrum and that is equal  $2B$ . Now we are going to see what is the separation between spectral lines in rotational Raman spectrum. So, this is your energy of the rotational levels  $FJ$  is equal to  $BJJ$  plus 1. Now, if you take if in hertz unit, then  $B$  will be in hertz and if you take  $F$  in centimeter inverse unit then  $B$  will be in centimeter inverse.

So, this F is given by  $2J + 1$  and let us take this in centimeter inverse and B is in centimeter inverse. Now, selection rule for rotational transition, rotational Raman transition or  $\Delta J$  is equal to plus minus 2 that I have already discuss. So, let us calculate  $\bar{\nu}$ ,  $\bar{\nu}$  is your wave number for transition between  $J$  to  $J + 1$  level  $J$  to  $J + 1$  level. So, that is given by  $F(J) - F(J)$  this is let us take this as a  $J$  dash, so  $F(J)$  dash minus  $F(J)$ .

And if you take  $J$  dash for  $J$  dash, you can write  $F(J)$  dash  $J$  dash plus 1 minus  $F(J)$  plus 1. And  $J$  dash will be  $J$  plus 2 because your selection rule for rotational transition  $\Delta J$  is equal to plus minus 2. So, your  $\bar{\nu}$  is  $F(J)$  dash  $J$  dash plus 1 minus  $F(J)$  plus 1. And if you take B out, this is the expression and we know that  $J$  dash is equal to  $J$  plus 2 because that is what the selection rule for rotational Raman transition. So that is right rotational Raman, Raman transition.

And so,  $\bar{\nu}$  is equal to  $2B(J + 1)$  for  $J$  dash you put  $J + 2$   $J$  dash plus 1  $J$  plus 3 minus  $J$  plus 1 and what you get in this equation  $4B(J + 1)$  by  $2(J + 1)$  by 2. So since  $J$  is equal to 0, 1, 2, 3. So,  $J$  increases by 1 and so spacing between spectral lines of rotational Raman spectrum is  $4B$ . So, the separation between spectrum lines and rotational spectrum is  $2B$  whereas separation between spectral lines in rotational Raman spectrum is  $4B$ .

(Refer Slide Time: 37:22)

**Problems: Vibrational Spectroscopy**


**Q17.** For a diatomic molecule CO, the force constant is  $1906 \text{ Nm}^{-1}$ . Calculate its fundamental vibrational frequency in  $\text{cm}^{-1}$ .

**Solution:** The reduced mass,

$$\mu_{\text{CO}} = \frac{m_{\text{C}}m_{\text{O}}}{m_{\text{C}} + m_{\text{O}}} = \frac{12 \times 16}{(12 + 16)} \times \frac{1}{6.023 \times 10^{23}} \text{ g} = 1.138 \times 10^{-23} \text{ g} = 1.138 \times 10^{-26} \text{ kg}$$

The fundamental vibrational frequency will be,

$$\bar{\nu} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} = \frac{1}{2 \times 3.14 \times (3 \times 10^{10} \text{ m.s}^{-1})} \sqrt{\frac{1906 \text{ N.m}^{-1}}{1.138 \times 10^{-26} \text{ kg}}}$$

$$\bar{\nu} = 2172.2 \text{ cm}^{-1}$$


Now, next question is based on vibrational spectroscopy for a diatomic molecules CO the force constant is 1906 Newton per meter. So, you need to calculate what is the fundamental vibrational frequency in a centimeter inverse. Again first we have to calculate  $\mu$ . I have discussed

calculation of mu several times so, I am not going to discuss it again. The value which you obtained from mu for CO molecule is  $1.138 \times 10^{-26}$  kg.

So fundamental frequency will be  $\bar{\nu} = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$  again the wave number can be so this is wave number, so it will be in meter inverse or centimeter inverse unit. So, just put the values  $1/2\pi$  is your  $3 \times 10^{10}$  centimeter per second inverse. So, please correct this is a centimeter per second inverse and this is your k which is force constant it is given 1906 Newton per meter and this is your reduced mass which we just calculated for CO molecule and what will you get is wave number to be 2172.2 centimeter inverse.

(Refer Slide Time: 38:49)

**Problems: Vibrational Spectroscopy**

**Q18.** What will be the spacing (in eV) between the vibrational energy levels of a CO molecule, if the force constant is  $1748 \text{ Nm}^{-1}$ .

**Solution:** The reduced mass for CO:

$$\mu = \frac{m_1 m_2}{m_1 + m_2} = 11.4 \times 10^{-27} \text{ kg}$$


The frequency of the vibrational transition will be:

$$\bar{\nu} = \frac{1}{2\pi} \left( \frac{k}{\mu} \right)^{1/2} = \frac{1}{2 \times 3.14 \times (3 \times 10^{10} \text{ cm.s}^{-1})} \left( \frac{1748 \text{ kg.s}^{-2}}{11.4 \times 10^{-27} \text{ kg}} \right)^{1/2} = 2078 \text{ cm}^{-1}$$

The spacing between the energy levels,  $\Delta E = \bar{\nu} = 2078 \text{ cm}^{-1}$

Since,  $1 \text{ eV} = 8066 \text{ cm}^{-1}$

$$\Delta E = \frac{2078 \text{ cm}^{-1}}{8066 \text{ cm/eV}} = 0.258 \text{ eV}$$

 Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press

Now, next question is what will be the spacing in electron volt between vibrational energy level of a CO molecule if the force constant is 1748 Newton per meter. Now we are going to calculate the frequency of vibrational transition. Again we will calculate mu, mu just be calculated for CO, this is  $11.4 \times 10^{-27}$  kg. So, frequency of the vibrational transition is this formula we have already discussed and that equal to 2078 centimeter inverse or 2078 centimeter inverse and this we can convert into delta E, delta E and your nu bar is related by this equation 1 electron volt is equal to 8066 centimeter inverse and so delta E can be calculated by dividing 2078 with 8066 centimeter by electron volt and what you are going to get a 0.258 electron volts. So, this is your spacing between the vibrational levels of CO molecule.

(Refer Slide Time: 40:14)

**Problems: vibrational-Raman Spectroscopy**

**Q19.** In an experiment, a  $\text{H}^{35}\text{Cl}$  molecule is irradiated with a mercury lamp of a wavelength of  $443.6 \text{ nm}$ . If the fundamental vibrational frequency for the molecule is  $5.396 \times 10^{13} \text{ s}^{-1}$ , calculate the Raman line in nm.

**Solution:** The frequency of the mercury light,

$$\nu = \frac{c}{\lambda} = \frac{3 \times 10^8 \text{ m} \cdot \text{s}^{-1}}{443.6 \times 10^{-9} \text{ m}} = 6.763 \times 10^{14} \text{ s}^{-1}$$

The Stokes Raman line is observed at,

$$\nu_{\text{Raman}} = \nu_{\text{inc}} - \nu_{\text{vib}} = (6.763 \times 10^{14}) - (5.396 \times 10^{13}) = 62.234 \times 10^{13} \text{ s}^{-1}$$

& Stokes Raman line,

$$\lambda_{\text{Raman}} = \frac{c}{\nu_{\text{Raman}}} = \frac{3 \times 10^8 \text{ m} \cdot \text{s}^{-1}}{62.234 \times 10^{13} \text{ s}^{-1}} = 482.05 \times 10^{-9} \text{ m} = 482.05 \text{ nm}$$

(Adapted from Physical Chemistry Through Problems by Dogra & Dogra, Second Edition)

Now next question in this  $^{35}\text{Cl}$  molecule is a  $^{35}\text{Cl}$  molecule is irradiated with mercury lamp of a wavelength of 443.6 nanometer. If the fundamental vibrational frequency for the molecule is this second inverse what we need to calculate is what is the Raman line in nanometer. Stokes Raman line. The frequency of mercury light can be calculated using this formula  $\nu$  is equal to  $c$  by  $\lambda$   $c$  again we have taken in meter per second and you can express  $\lambda$  in meter and then we can get frequency in second inverse frequency in second inverse and so stokes line will be observed at  $\nu$  frequency of incident light minus frequency of vibration.

Here it is a fundamental vibrational frequency we have just calculated what is the frequency of incident light and that is  $67.63$  into  $10$  to power  $13$  second inverse and then fundamental frequency is given. So, you just subtract this from frequency of incident light and you can get frequency of the stokes Raman line and that is equal to  $62.234$  into  $10$  to power  $13$  second inverse and you can also calculate wavelength of Raman by using this we know that frequency and wavelength is related by this equation  $c$  by  $\nu$  and so you can calculate what will be the wavelength of stokes line, Raman line, stokes Raman line.

(Refer Slide Time: 42:18)

**Problems: Vibrational Spectroscopy**

**Q20.** Identify the allowed vibrational transition for a diatomic molecule:

(a)  $v = 1$  to  $v = 3$ ; ~~✓~~


(b)  $v = 3$  to  $v = 4$  and ✓  $\Delta v = +1$

(c)  $v = 5$  to  $v = 4$ . ✓  $\Delta v = -1$

**Solution:** For allowed vibrational transitions,

$\Delta v = \pm 1$ . ✓

Therefore, only (b) and (c) are allowed.



(Adapted from Engineering Chemistry by P. B. Joshi & Shashank Deep, Oxford University Press)


So, next question is, identify the allowed vibrational transition for a diatomic molecule and again this is based on selection rules. So, you know that for allowed vibrational transmission delta v is plus minus 1 and so, first is not allowed, second is allowed, third is allowed. In the b it is delta v is equal to plus 1 and here delta v equal to minus 1.

(Refer Slide Time: 42:53)

**Recap (Anharmonic Oscillator)**

$$E_v = \left(v + \frac{1}{2}\right) hc\omega_e - \left(v + \frac{1}{2}\right)^2 x_e hc\omega_e + \left(v + \frac{1}{2}\right)^3 y_e hc\omega_e + \dots$$

$G_v = \left(v + \frac{1}{2}\right) \omega_e - \left(v + \frac{1}{2}\right)^2 x_e \omega_e + \dots$  (in wave number unit)

$$G_{v+1} - G_v = \omega_e - 2x_e \omega_e (v + 1) + \dots$$


## Calculation of Dissociation energy

$$E_v = \left(v + \frac{1}{2}\right) hc\omega_e - \left(v + \frac{1}{2}\right)^2 x_e hc\omega_e + \dots (1)$$

$$\frac{dE}{dv} = hc\omega_e - 2\left(v + \frac{1}{2}\right) x_e hc\omega_e = 0 \dots$$

$$v = \frac{1}{2x_e} - \frac{1}{2} \dots (a)$$

Substituting (a) in (1); subtracting this from zero point energy

$$E = \left(\frac{1}{2}\right) hc\omega_e - \left(\frac{1}{2}\right)^2 x_e hc\omega_e \dots \dots \dots \text{zero point energy}$$

$$\text{Dissociation energy } D_e = \frac{\omega_e}{4x_e}$$



So, next question is basically to calculate dissociation energy using vibrational spectroscopy. Just before going to discuss that question, I will like to have recap for Anharmonic oscillator, so energy of vibrational levels for anharmonic oscillator is given by this equation where  $v$  is vibrational quantum number and if you try to express this in wave number unit you need to divide by  $hc$  and that is generally given by this symbol  $G_v$  and that is basically  $v$  plus half  $\omega_e$  minus higher wave number term.

So, now, you have wave number you can calculate the difference between 2 in wave number unit and when you 2 vibrational level from  $v$  to  $v$  plus 1 So, if you calculate the difference between this vibrational level centimeter inverse, you are going to get this formula. So,  $G_{v+1}$  minus  $G_v$  is equal to  $\omega_e$  minus  $2x_e\omega_e(v+1)$ . And so, if we plot this vs  $v+1$  then we can get  $x_e$  and  $\omega_e$ ,  $x_e$  and  $\omega_e$ .

And now, let us think of how to calculate the vibrational level with maximum energy. And if I want to calculate the vibrational level at which energy is maximum, then I need to differentiate that and put that equal to 0 when you do that, you will get to  $v$  equal to  $\frac{1}{2x_e} - \frac{1}{2}$ . And if you put this in this equation and then your subtract by zero point energy, what you are going to get a  $D$ . This I have explained in detail in the last lecture in the last lecture, I have explained this in detail, but what I showed you that  $D_e$  equal to  $\frac{\omega_e}{4x_e}$ .

(Refer Slide Time: 45:21)

**Q21. The fundamental and first overtone transitions are centred at  $1876.06 \text{ cm}^{-1}$  and  $3724.20 \text{ cm}^{-1}$ , respectively. Evaluate**

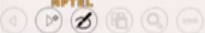

- Equilibrium vibrational frequency
- Anharmonicity constant
- Zero point energy
- Force constant
- Dissociation energy

○ Fundamental absorption,  $\omega_e(1-2x_e) = 1876.06 \text{ cm}^{-1}$  (1)  
First overtone,  $2\omega_e(1-3x_e) = 3724.20 \text{ cm}^{-1}$  (2)


Divide 2 by 1

$$\frac{2\omega_e(1-3x_e) = 3724.20}{\omega_e(1-2x_e) = 1876.06} \quad \left. \begin{array}{l} \text{ } \\ \text{ } \end{array} \right\} \begin{array}{l} \text{ } \\ \text{ } \end{array}$$

$\text{ } \rightarrow x_e = 0.007332$   
 $\text{ } \rightarrow \omega_e = 1903.98 \text{ cm}^{-1}$



### Continued.....

$$\text{ } \rightarrow G_0 = \frac{1}{2} \omega_e \left(1 - \frac{1}{2} x_e\right)$$
$$= \frac{1}{2} 1903.38 \left(1 - \frac{1}{2} \cdot 0.007332\right)$$
$$= 948.5 \text{ cm}^{-1}$$
$$\omega_e = \frac{1}{2\pi c} \sqrt{k/\mu}$$
$$\mu = 1.2397 \times 10^{-26} \text{ kg}$$
$$\omega_e = 1903.98 \text{ cm}^{-1}$$
$$k = 1.593 \times 10^3 \text{ m}^{-1}$$




Continued.....

$$v_{\max} = \frac{1}{2X_e} - \frac{1}{2}, v_{\max} = 68$$

$$G_{\max} = (v_{\max} + \frac{1}{2})\omega_e(1 - (v_{\max} + \frac{1}{2})X_e) = 64918.9 \times 10^2 \text{ cm}^{-1}$$

$$\text{E(dissociation)} = (G_{\max} - G_0) hc = 1.29 \times 10^{-18} \text{ J}$$



So, after this recap, let us see, this question. The question is a fundamental and first overtone transition are centered at 1876.06 centimeter inverse and 3724.20 centimeter inverse respectively, and you have to calculate these 5 parameters. So, let us first start with fundamental absorption, fundamental absorption frequency is given by a wave number is given by this  $\omega_e$  multiplied by  $1 - 2X_e$  and that is given 1876.06 centimeter inverse and for first overtone wave number is given by this equation.

So, for first overtone wave number is equal to  $2\omega_e$  multiplied by  $1 - 3X_e$ . So, you have this 2. And so, you have 2 equations, and 2 unknowns, unknowns are  $\omega_e$  and  $X_e$ . So, you can solve these 2 equation to get the value of  $\omega_e$  and  $X_e$  easiest way to do is divide 1 by 2, and when you divide 1 by 2, you can get the value of  $X_e$  and when you put  $X_e$  in one of the equation and you can get value of  $\omega_e$ .

So, it is simple calculation you can do it easily so, please do it. Now, once you know that, what is the value of  $\omega_e$  and  $X_e$ , you can calculate  $G_0$  which is basically zero point energy and the zero point energy is given by this equation, this equation has already been discussed in the last lectures, last 2 lectures, so, please just go and see these equations. So, what now I do is I just plug in the value of  $\omega_e$  and  $X_e$ , which I obtained in the previous slide.

And when you do that, you will get the value of  $G_0$  which is basically the zero point energy. Now, you can use  $\omega_e$  to get the value of  $k$  basically you have to calculate  $k$  because you know  $\mu$ , reduced mass is known, so reduced mass is basically this and  $\omega_e$  we have

already obtained so we can get the value of force constant. So, if you remember the question, the fourth point is to calculate force constant. And that is what we are calculating and force constant is  $1.593 \times 10^3$  inverse.

Now, we need to calculate your dissociation energy for that, I told that first you have to calculate the vibrational level with maximum energy. So, you need to find out the value of  $v$  at which the energy is maximum and this is a formula for  $V_{\max}$ . And once you solve that, you will get  $V_{\max}$  equal to 68. Now, we will put the value of  $V_{\max}$  in the equation for  $G_V$  when we do that will get  $G_{\max}$ . So,  $G_{\max}$  is  $V_{\max} + \frac{1}{2} \frac{h\nu}{hc}$  and  $1 - \frac{1}{2} \frac{h\nu}{hc}$ .

And when you solve this, you will get the value of  $G_{\max}$  that the energy of the vibrational level whose energy is maximum and it is given in centimeter inverse. And you can calculate  $E_{\text{dissociation}}$ ,  $E_{\text{dissociation}}$  is basically  $G_{\max} - G_0$  into  $hc$ ,  $hc$  is multiplied since, this the  $G$  value is in centimeter inverse. So, if you multiplied by  $hc$  then you can get the energy in joule unit, in joule unit. So, this is your dissociation energy in joule.

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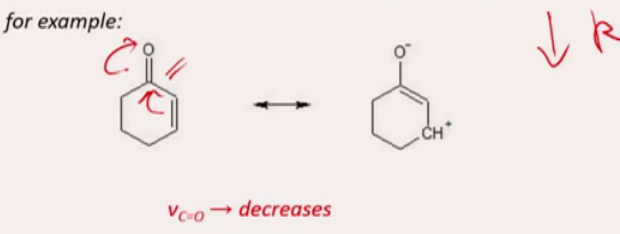
**Problems: Vibrational Spectroscopy: Applications**

**Q22.** How does conjugation to the carbonyl group affect its IR stretching frequency?

**Solution:**

**Conjugation weakens carbonyl  $\pi$  bond**

for example:



$\nu_{\text{C=O}} \rightarrow \text{decreases}$

NPTEL

Now, let us go to some application based questions particularly in vibrational spectroscopy. So, here first question is how does conjugation to the carbonyl group affects its IR stretching frequency? Conjugation weakens the carbonyl  $\pi$  bond. So, you can see that if we look at the resonance, so, this will get a double bond and that will get a partial single bond. So, conjugation

leads to weakening in carbonyl pi bond and that decreases the value of k, decreases the value of k and so, frequency of CO bond decreases. So, on conjugation frequency of CO bond decreases.

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**Problems: Vibrational Spectroscopy: Applications**

**Q23.** Why does the IR stretching frequency of carbonyl group in cyclic ketones increase with decrease in the number of carbon?

**Solution:**

As the number of carbon increases, the ring angle <sup>increase</sup> ~~decreases~~

Cyclohexanone < Cyclopentanone < Cyclobutanone

1710 cm<sup>-1</sup>      1750 cm<sup>-1</sup>      1780 cm<sup>-1</sup>

Ring strain increases with decrease in ring angle

Energy & thereby  $\nu$  for C=O bond increases

Now, we will look at how does IR stretching frequency of carbonyl group in cyclic ketone increase with a decrease in number of carbon. So, what happens that when number of carbon in cycle increases, then ring ring angle decreases and that affects the frequency. The ring strain increases with decrease in ring angle. So, here there should be increase. So, as the number of carbon increases, ring angle increase, so, if I going from this to this side, here ring, ring angle decreases and once ring angle decreases, ring strain increases with decrease in ring angle and so energy and thereby nu for CO bond increases.

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**Problems: Vibrational Spectroscopy: Applications**

**Q24.** Distinguish between the position of Keto group

*Example:* 1-Phenylpropan-1-one & 1-Phenylpropan-2-one

Aryl alkyl ketone  
 $\nu$  for C=O str =  $1650\text{ cm}^{-1}$

Dialkyl Ketone  
 $\nu$  for C=O str =  $1700\text{ cm}^{-1}$

**Conjugation weakens carbonyl  $\pi$  bond**

So, in this question what we are going to look at can we apply vibrational spectroscopy to distinguish between position of keto group, position of keto group. So, here if aryl alkyl ketone and dialkyl ketone. So, now you see that this one is involved in conjugation with the ring, benzene ring and we know that, on conjugation this  $k$  decreases and if  $k$  decreases your frequency will also decrease. and so frequency of CO stretching in aryl alkyl ketone comes at smaller wave number in comparison to dialkyl ketone. So, conjugation weakens the carbonyl  $\pi$  bond.

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**Problems: Vibrational Spectroscopy: Applications**

**Q25. Distinguish between the position of Keto group**

Example: 2,4-Heptanedione & 2,5-Heptanedione

Enol Form possible

$\beta$  diketone (highly enolic)

Broad:  $\nu$  for O-H str =  $3200\text{ cm}^{-1}$  //

$\nu$  for C=O str =  $1600\text{ cm}^{-1}$

Dialkyl Ketone

$\nu$  for C=O str =  $1700\text{ cm}^{-1}$

Now, again we will see another example, we want to distinguish between the position of keto group and this is your 2,4 heptanedione, this is a 2,4 heptanedione and this is 2,5 heptanedione. Can we distinguish between these two? So, here you see, this is, this CH is basically between 2 CO group, so, here h is acidic and so, this can exist in all forms, this can exist in all forms, and if it exists in all forms what will happen is you will have a peak for OH stretching which will come around 3200 centimeter inverse and your frequency for CO will be at smaller value because your k for CO will be small. Whereas this conjugation, this enol formation is not possible in this structure. And so your  $\nu$  for CO will be at 1700 centimeter inverse and there will be no peak for OH stretching, no peak for OH stretching.

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**Problems: Vibrational Spectroscopy: Applications**

**Q26. Distinguish between the two esters**

*Example:* Methyl benzoate & Phenyl acetate

CC(=O)c1ccccc1

Due to conjugation on C=O group  
 $\nu$  for C=O str = 1710 cm<sup>-1</sup>

CC(=O)Oc1ccccc1

Due to conjugation on -O- group  
 $\nu$  for C=O str = 1760 cm<sup>-1</sup>

NPTEL

So, now, next question is can we distinguish 2 esters the example is methyl benzoate and phenyl acetate and now you see that here the re-conjugation between these two bond and in this there is conjugation with the lone pair. So, due to conjugation on O group here frequency will be 1760 centimeter inverse whereas  $\nu$  for CO stretching in the above case will be at 1710 centimeter inverse.

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**Problems: Vibrational Spectroscopy: Applications**

**Q27. Distinguish between the Nitriles & iso-Nitriles**

*Example:* Propane nitrile & Propane iso-nitrile

CCC#N

$\nu$  for C≡N str = 2275 cm<sup>-1</sup>

CC(C)C#N

$\nu$  for C≡N str = 2180 cm<sup>-1</sup>

NPTEL

We can also distinguish between nitrile and iso-nitrile using vibrational spectroscopy for nitrile compound, the frequency for C triple bond N stretching will be at 2275 centimeter inverse.


Whereas,  $\nu$  for this iso-nitrile will be at 2180 centimeter inverse. So, using that you can distinguish between nitrile and iso-nitrile

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**Problems: Vibrational Spectroscopy: Applications**

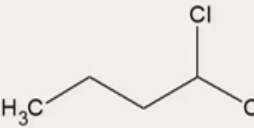
**Q28. Distinguish between the mono & poly substituted alkyl halides**

Example: 1-Chlorobutane & 1,1-Dichlorobutane



CCCCl

$\nu$  for C-Cl str = 705  $\text{cm}^{-1}$



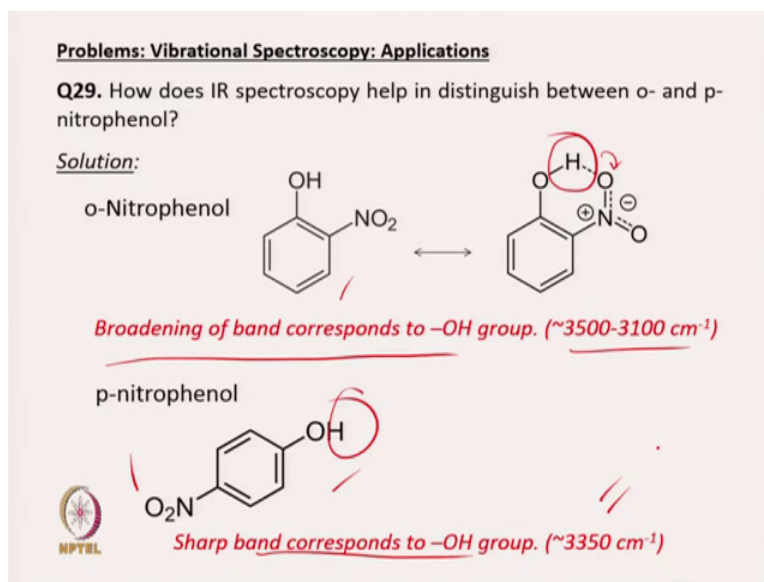
CCC(Cl)Cl

$\nu$  for C-Cl str = 790  $\text{cm}^{-1}$

NPTEL

Mono and polyalkylated poly substituted alkyl halide, mono and poly substituted alkyl halide can also be distinguished. For example, the for example, 1 chloro butane and 1, 1 dichloro butane can be distinguished by IRS spectroscopy, here frequency will be a lower wave number when you have only one Cl, but if you have 2 Cl then this frequency will increase to 790 centimeter inverse. So, you will be able to distinguish between mono and poly substituted alkyl halide.

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So, next question is how we can use IRS spectroscopy to distinguish between ortho and para-nitrophenol. So, you know that in ortho-nitrophenol the hydrogen of OH group in phenol is in hydrogen bond with nitro group and that basically leads to broadening of band. So, wherever there is a hydrogen bond of OH group there will be a broadening and this broadening will be observed between 3500 to 3100 centimeter inverse. In para-nitrophenol the hydrogen bonding is not possible between this hydrogen and this nitro group and so you will get a sharp band corresponding to OH group at 3350 centimeter inverse. So, ortho and para-nitrophenol can be distinguished using IRS spectroscopy.



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## Acknowledgements

- Modern Spectroscopy: J. M. Hollas, Wiley
- Fundamentals of Molecular Spectroscopy: C. N. Banwell & E.M. McCash
- Organic Spectroscopy: William Kemp, Palgrave
- Engineering Chemistry: P.B. Joshi and Shashank Deep, Oxford University Press (Chapter: Analytical Techniques)



So, in this lecture, I have looked at several different kinds of questions, some are multiple choice questions and some are problem based questions and some is application related question. So, there are a lot of different kind of application we can think of between rotational applications of rotational and vibrational spectroscopy and in the next lecture I will start with our atomic spectroscopy.

So, thank you very much for listening. Now books, I have already told you which books, I am using it, for example, in organic spectroscopy. I am taking help of William Kemp, Kemp book on organic spectroscopy, which is from Palgrave publication, and these two are for physical spectroscopy. And this is one basic books, book on your chemistry, basic book on chemistry. Thank you very much. And thank you for listening.