

**Chemical Process Utilities**  
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**Lecture – 40**  
**Design of Pipeline - Natural Gas Transmission**

Welcome to the design of pipelines and in this particular chapter, we are going to discuss about the natural gas transmission. Let us have a brief outlook about what we discussed in the previous lecture. We discussed about the natural gas transmission. We derived the general flow equation in steady state with respect to the kinetic energy term, with respect to the pressure energy term, potential energy term and friction loss term.

In this particular lecture, we are going to discuss about the various flow regimes including fully turbulent flow that is rough pipe flow, partially turbulent flow that is smooth pipe flow, pressure drop calculation. We will discuss the pipelines in series, pipelines in parallel, pipeline in segmental looping.

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**Natural gas transmission**

**Flow Regimes**

In high pressure gas transmission lines with moderate to high flow rates, two types of flow regimes are normally observed;

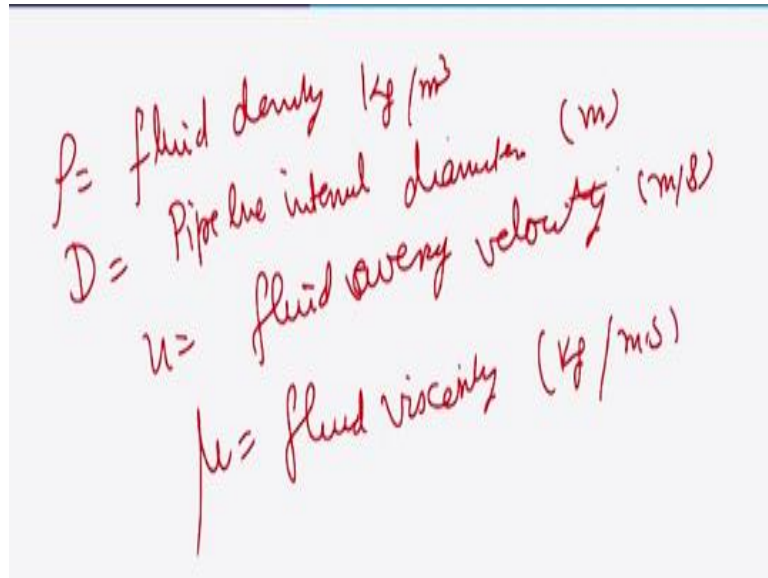
- Fully turbulent flow (Rough pipe flow)
- Partially Turbulent flow (smooth pipe flow)

Now, let us talk about the flow regimes. Now, in high pressure gas transmission lines with moderate to high flow rates, there are two types of flow regimes which are normally observed. One is the fully turbulent flow that is rough pipe flow and second one is the partially turbulent flow. So, the regime of flow is defined by the Reynolds number which is dimensionless and Reynolds number is  $Re = \rho D u$  over  $\mu$ .

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The regime of the flow is defined by Reynolds number (Dimensionless);

$$Re = \frac{\rho \cdot D \cdot u}{\mu}$$



Now, here if you see that the term used in the Reynolds number that is rho is equal to fluid density in kilogram per meter cube, D is the pipe diameter or the pipeline internal diameter m, u is the fluid average velocity in meters per second and mu is the fluid viscosity that is kilogram per meter second.

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## Natural gas transmission

### Note;

- Re less than 2000 the flow is normally laminar, or stable
- Re greater than 2000, the flow is turbulent or unstable
- In high pressure line only two types of flow regimes are exists i.e., fully turbulent and partially turbulent flow.

Now, if Reynolds number is less than 2000, the flow is normally laminar or stable. Now, if Re is greater than 2000, the flow is turbulent or unstable. In high pressure line only two type of flow regimes they are exist, fully turbulent or partially turbulent flow.

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**Natural gas transmission**

**Partially Turbulent Flow Regime;**  
 The partially turbulent flow is defined by Prandtl-Von Karman equation;

$$\sqrt{\frac{1}{f}} = 4 \log_{10} \frac{Re}{\sqrt{1/f}} - 0.6$$

**Note:** It is applicable in which the flow is fully turbulent in the center region of the pipe, with a laminar sublayer covering the interior surface of the pipe.

Now, let us talk about the partially turbulent flow regime. The partially turbulent flow is defined by the Prandtl-Von Karman equation and this equation is square root of 1 upon  $f = 4 \log$  to the base 10  $Re$  upon  $1$  upon  $f - 0.6$  where  $f$  is the friction factor  $re$  dimensionless and  $Re$  is the Reynolds number. Now, it is applicable in which the flow is fully turbulent in the centre region of the pipe with a laminar sublayer covering the interior surface of the pipe.

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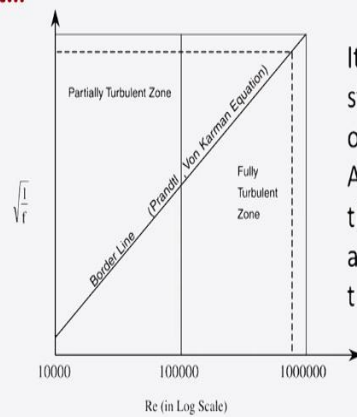
**Partially Turbulent Flow Regime;**

The partially turbulent flow is defined by Prandtl-Von Karman equation;

$$\sqrt{\frac{1}{f}} = 4 \log_{10} \frac{Re}{\sqrt{1/f}} - 0.6$$

Where,  $f$  = friction factor (dimensionless),  $Re$  = Reynolds Number (dimensionless)

Cont...



It is a semi-log graph, where straight line shows the max. limit of partially turbulent flow. All points to the right hand side of the line exhibit fully turbulent flow and left side remaining partially turbulent.

Fig: Shown fully turbulent/partially turbulent zones by Prandtl-Von Karman equation

Now, here you can see that it is a semi-log graph where the straight line shows the maximum limit of partial turbulent flow. Now, all points to the right hand side of the line this exhibit fully turbulent flow and left hand side remain partially turbulent. This is a fully turbulent, partially turbulent zones by Prandtl-Von Karman equation.

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### Fully Turbulent Flow Regime;

the transmission factor for fully turbulent flow is given by the Nikuradse equation as follows;

$$\sqrt{\frac{1}{f}} = 4 \log_{10} \left[ 3.7 \frac{D}{k_e} \right]$$

$D \rightarrow$  pipe's internal diameter  
 $k_e =$  effective roughness  
 $\frac{k_e}{D} =$  relative roughness (dimensionless)

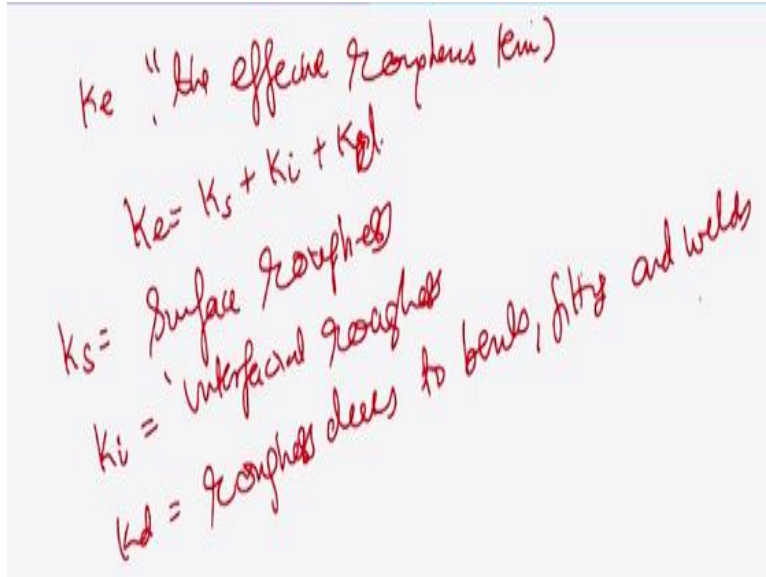
Let us talk about fully turbulent flow regime. The transmission factor for fully turbulent fluid is given by Nikuradse equation which is as represented  $1 \text{ upon } f = 4 \log \text{ to the base } 10 \text{ } 3.7 D \text{ upon } K e$ , where  $1 \text{ upon } f$  this is the transmission factor which is dimensionless in nature,  $D$  is the pipeline internal diameter,  $K e$  is the effective roughness that is represented in  $m$  and  $K e \text{ upon } D$  is the relative roughness that is dimensionless.

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### Fully Turbulent Flow Regime:

the transmission factor for fully turbulent flow is given by the Nikuradse equation as follows;

$$\sqrt{\frac{1}{f}} = 4 \log_{10} \left[ 3.7 \frac{D}{K_e} \right]$$



Now, this  $K_e$  the effective roughness term this can be defined as  $K_e = K_s + K_i + K_d$  now where  $K_s$  is the surface roughness,  $K_i$  is the interfacial roughness and  $K_d$  is equal to roughness due to bend, fitting sometimes they are very common and wells. Now, with high pressure gas transmission lines with high flow rate and fully turbulent flow regime and natural gas is almost dry and  $K_d$  and  $K_i$  are negligible if you compare with the  $K_s$ .

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$K_e$  "the effective roughness term" can be defined as;

$$K_e = K_s + K_i + K_d$$

### Cont...

- The value of  $K_s$  and  $K_e$  is important in fully turbulent flow regime without the laminar sublayer, the surface roughness of the pipe play important role in determining the flow and pressure drop.
- The Nikuradse equation shows that if the effective roughness of the pipeline is increased, the transmission factor decrease and it's result in high pressure drop.
- For internally uncoated commercial pipe, when  $K_e$  is unavailable, **700  $\mu$**  inches may be assumed.



Now, the values of  $K_s$  and  $K_e$  is very important in fully turbulent flow regime without the laminar sublayer, the surface roughness of the pipe play an important role in determining the flow and pressure drop. The Nikuradse equation shows that if the effective roughness of the pipeline is increased the transmission factor decrease and its result in high pressure drop. So, for internally uncoated commercial pipe where this  $K_e$  is unavailable 700 microns inch maybe assumed.

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Calculations of  $Re$  in gas ~~trans~~ transmission system

$$Re = \frac{\rho D u}{\mu}$$
$$u = \frac{Q}{\pi D^2 / 4}$$
$$Re = \frac{\rho D Q}{\mu \pi D^2 / 4}$$

Now, the calculation of Reynolds number in gas transmission system,  $Re$  in gas transmission system, so this  $Re = \rho D u$  upon  $\mu$ ,  $u = Q$  upon  $\pi D$  square by 4 where  $Re = \rho D Q$  upon  $\mu \pi D$  square by 4.

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We know that Reynolds number can be defined as;

$$Re = \frac{\rho \cdot D \cdot u}{\mu}$$

Where,

$$u = \frac{Q}{\pi D^2/4}$$

Therefore;

$$Re = \frac{\rho \cdot D \cdot Q}{\mu \cdot \pi D^2/4}$$

Handwritten derivation showing the substitution of density into the Reynolds number equation. It starts with  $\rho Q = \rho_b Q_b$ , leading to  $Re = \frac{4 Q_b \rho_b}{\mu \pi D}$ . Then it states "and if  $\rho_b = \frac{P_b M}{Z_b R T_b}$ " and "for natural gas value of  $Z_b = 1$  and  $M = 29 G$ ", resulting in  $Re = \frac{4 Q_b \cdot 29 G P_b}{\mu \pi D R T_b}$ .

Now, at steady state condition  $\rho Q = \rho_b Q_b$ , this is the Reynolds number =  $\frac{4 Q_b \rho_b}{\mu \pi D}$  and if  $\rho_b = \frac{P_b M}{Z_b R T_b}$ . For natural gas value of  $Z_b = 1$  and  $M = 29 G$ . So,  $Re = \frac{4 \cdot 29 G P_b}{\mu \pi D R T_b}$ .

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**At steady-state condition;**

$$\rho Q = \rho_b Q_b$$

$$\Rightarrow Re = \frac{4 Q_b \cdot \rho_b}{\mu \pi D}$$

And if,

$$\rho_b = \frac{P_b \cdot M}{Z_b \cdot R \cdot T_b}$$

For, Natural gas the value of  $Z_b=1$  and  $M= 29G$ ;

$$\Rightarrow Re = \frac{4 Q_b \cdot 29 G \cdot P_b}{\mu \cdot \pi \cdot D \cdot R \cdot T_b}$$

On substitution of value of variables  
 $\pi, R = 10.73 \text{ Psi ft}^3/\text{lbmoles} \cdot \text{R}$   
 $P_b = 14.7 \text{ psi} \text{ \& } \mu = 7.23 \times 10^{-6} \text{ lbm/ft} \cdot \text{s}$   
 $\Rightarrow Re = 45 \frac{Q_b G}{D}$   
 $Q_b \rightarrow \text{gas flow rate (ft}^3/\text{h)}$   
 $G \rightarrow \text{gas gravity}$   
 $D \rightarrow \text{inside diam. of pipe (in)}$

So, on substitution of value of variables  $\pi R = 10.73$  psi cubic feet per ton moles  $R$ ,  $P_b = 14.7$  psi,  $\mu = 7.23 \times 10^{-6}$  pound metre per second, the  $Re = 45 Q_b G$  upon  $D$ . Now  $Q_b$  is equal to gas flow rate in cubic feet per hour,  $G$  is equal to gas gravity that is dimensionless,  $D$  is inside diameter of pipe that is in inch. This is the simplified equation and that gives the Reynolds number in terms of pipeline parameters.

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On substitution of the value of variables  $\pi, R=10.73 \text{ Psi.ft}^3/\text{lbmoles} \cdot \text{R}, P_b=14.7 \text{ Psi}$ , and  $\mu=7.23 \times 10^{-6} \text{ lb m/ft. s}$

$$\Rightarrow Re = 45 \frac{Q_b G}{D}$$

Steady State flow equation

$$Q_b = \frac{\pi R g_c}{1856} \frac{z_b T_b}{P_b} \sqrt{\frac{P_1^2 - P_2^2 - 50 G^2 D H^2}{R T_{avg} z_{avg}}} \sqrt{\frac{L}{f D^{5.31}}}$$

$$f = 0.03754 D H \frac{P_{avg}^2}{T_{avg} z_{avg}}$$



Now, let us talk about steady state flow equations. So, the general flow equation of natural gas in pipeline is given by  $Q_b = \pi \frac{R \cdot g_c}{1856} \cdot \frac{Z_b \cdot T_b}{P_b} \sqrt{\frac{P_1^2 - P_2^2 - \frac{58G \cdot \Delta H \cdot P_{avg}^2}{R \cdot T_{avg} \cdot Z_{avg}}}{58Z_{avg} \cdot T_{avg} \cdot G \cdot L}} \cdot \sqrt{\frac{1}{f}} D^{2.5}$ . Now, assume potential energy term that is  $E = 0.0375 G \Delta H \frac{P_{avg}^2}{T_{avg} Z_{avg}}$ .

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**Steady state flow equations;**

The general flow equation of natural gas in pipeline is;

$$Q_b = \pi \sqrt{\frac{R \cdot g_c}{1856}} \cdot \frac{Z_b \cdot T_b}{P_b} \sqrt{\frac{P_1^2 - P_2^2 - \frac{58G \cdot \Delta H \cdot P_{avg}^2}{R \cdot T_{avg} \cdot Z_{avg}}}{58Z_{avg} \cdot T_{avg} \cdot G \cdot L}} \cdot \sqrt{\frac{1}{f}} D^{2.5}$$

Assume, Potential Energy term;

$$E = 0.0375G \cdot \Delta H \cdot \frac{P_{avg}^2}{T_{avg} Z_{avg}}$$

$$Q_b = 38.774 \frac{T_b}{P_b} \sqrt{\frac{1}{f}} \sqrt{\frac{P_1^2 - P_2^2 - E}{Z_{avg} T_{avg} G \cdot L}} D^{2.5}$$

Then on upon simplifying we get  $Q_b = 38.774 \frac{T_b}{P_b} \frac{1}{\sqrt{f}} \sqrt{\frac{P_1^2 - P_2^2 - E}{Z_{avg} T_{avg} G \cdot L}} D^{2.5}$ . Now, this is the most common and widely used flow equation and that is suitable for design of large diameter high pressure gas transmission line.

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**Then, we have on simplifying;**

$$Q_b = 38.774 \frac{T_b}{P_b} \cdot \sqrt{\frac{1}{f}} \cdot \sqrt{\frac{P_1^2 - P_2^2 - E}{Z_{avg} \cdot T_{avg} \cdot G \cdot L}} D^{2.5} \quad \text{.....Equation (4)}$$

**Note; This is the most common and widely used flow equation that are suitable for design of large diameter, high-pressure gas transmission lines.**

## Partially turbulent flow regime

### Partially turbulent equations;

**Panhandle A;** Equation is normally used for medium to relatively large diameter pipelines with moderate gas flow rate, operating under medium to high pressure.

$$Q_b = 435.83 \left( \frac{T_b}{P_b} \right)^{1.0788} \left[ \frac{P_1^2 - P_2^2 - E}{G^{0.8539} \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5394} \cdot D^{2.6182}$$

Transmission factor  
 $\Rightarrow \sqrt{\frac{1}{f}} = 6.87 Re^{0.07305}$

Now, let us talk about the partially turbulent equation, Panhandle equation. This equation is normally used for medium to relatively large diameter pipeline with moderate gas flow rate operating under medium to high pressure. Now, here we can see that  $Q_b = 435.83 \left( \frac{T_b}{P_b} \right)^{1.0788} \left[ \frac{P_1^2 - P_2^2 - E}{G^{0.8539} \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5394} \cdot D^{2.6182}$ . Now, the transmission factor is defined as  $\sqrt{\frac{1}{f}} = 6.87 Re^{0.07305}$ .

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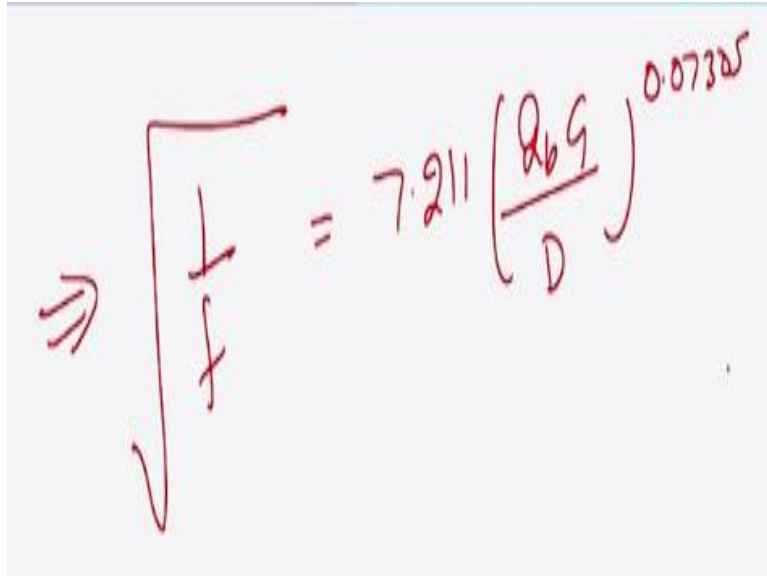
### Partially turbulent equations;

**Panhandle A;** Equation is normally used for medium to relatively large diameter pipelines with moderate gas flow rate, operating under medium to high pressure.

$$Q_b = 435.83 \left( \frac{T_b}{P_b} \right)^{1.0788} \cdot \left[ \frac{P_1^2 - P_2^2 - E}{G^{0.8539} \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5394} \cdot D^{2.6182}$$

Transmission factor is defined as;

$$\Rightarrow \sqrt{\frac{1}{f}} = 6.87 Re^{0.07305}$$


$$\Rightarrow \sqrt{\frac{1}{f}} = 7.211 \left( \frac{Q_b G}{D} \right)^{0.07305}$$

Or this can be  $1 \text{ upon } f = 7.211 Q_b G \text{ upon } D \text{ to the power } 0.07305$ . Now, we can link all these parameters which we have discussed earlier.

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Or,

$$\Rightarrow \sqrt{\frac{1}{f}} = 7.211 \left( \frac{Q_b \cdot G}{D} \right)^{0.07305}$$

**Note; All the parameters are as discussed before.**

### AGA Partially turbulent;

The AGA partially turbulent equation is highly dependent on Re, this equation is used for medium diameter and medium flow and high pressure systems.

$$Q_b = 38.774 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}} \cdot D^{2.5}$$
$$\sqrt{\frac{1}{f}} = 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}}$$

Now, AGA partially turbulent, this AGA partially turbulent equation is highly dependent on Reynolds number. Now this equation is used for medium diameter and medium flow and high pressure system. Now, let us write this particular equation this  $Q_b = 38.774 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}} \cdot D^{2.5}$ . Now, the transmission factor is defined as  $\frac{1}{f} = 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}}$ .

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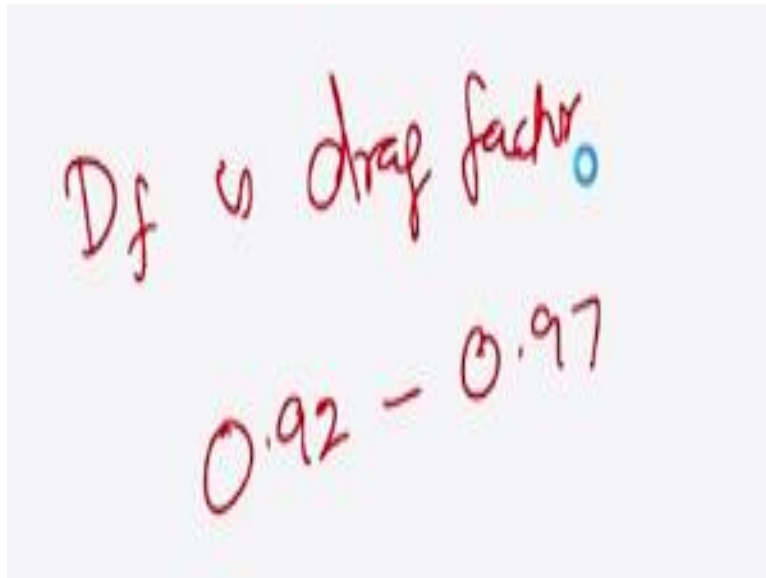
### AGA Partially turbulent;

The AGA partially turbulent equation is highly dependent on Re, this equation is used for medium diameter and medium flow and high-pressure systems.

$$Q_b = 38.774 \frac{T_b}{P_b} \cdot \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}} \cdot D^{2.5}$$

Transmission factor is defined as;

$$\Rightarrow \sqrt{\frac{1}{f}} = 4D_f \log \frac{Re}{1.4126 \sqrt{\frac{1}{f}}}$$



Now where  $D_f$  is drag factor, normally appears in the partially turbulent flow equation and its numerical value is ranging from 0.92 to 0.97.

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Where,

$D_f$  is drag factor, normally appears in partially turbulent flow equations. Its numerical value in the range from 0.92 to 0.97.

**Fully Turbulent Equations**

**Panhandle B:**  
 This equation is suitable for high flow rate, large diameter and high pressure system. The equation is as following;

$$Q_b = 737.02 \left( \frac{bT_b}{P_b} \right)^{1.02} \left[ \frac{P_1^2 - P_2^2 - E}{G^{0.961} Z_{avg} T_{avg} L} \right]^{0.5} D^{2.53}$$

$$\sqrt{\frac{1}{f}} = 16.70 \left( \frac{Q_b G}{D} \right)^{0.01961}$$

Now, Panhandle B, this equation is suitable for high flow rate, large diameter and high system. Now, this equation can be represented as  $Q_b = 737.02 T_b$  upon  $P_b$  to the power 1.02  $P_1$  square –  $P_2$  square –  $E$  upon  $G$  to the power 0.961  $Z_{avg}$   $T_{avg}$   $L$  0.5  $D$  to the power 2.53. The transmission factor is usually defined as  $1$  upon  $f = 16.70 Q_b G$  upon  $D$  0.01961.

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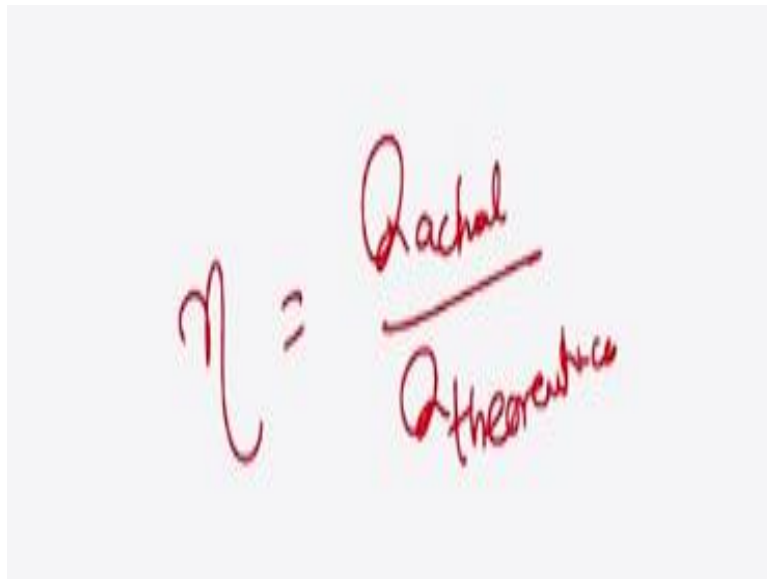
**Panhandle B;**

This equation is suitable for high flow rate, large diameter and high-pressure system. The equation is as following;

$$Q_b = 737.02 \left( \frac{T_b}{P_b} \right)^{1.02} \left[ \frac{P_1^2 - P_2^2 - E}{G^{0.961} Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot D^{2.53}$$

Transmission factor is defined as;

$$\Rightarrow \sqrt{\frac{1}{f}} = 16.70 \left( \frac{Q_b G}{D} \right)^{0.01961}$$



A handwritten equation in red ink showing the definition of efficiency:  $\eta = \frac{Q_{actual}}{Q_{theoretical}}$ . The text is written in a cursive style on a light background.

Now, the efficiency in Panhandle B equation is defined as Q actual upon Q theoretical. Now, it is multiplied in the equation to calculate more accurate value of Q b and all the parameters in the main equations are same as per which we have discussed.

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**Efficiency in Panhandle B equation is defined as;**

$$\eta = \frac{Q_{actual}}{Q_{Theoretical}}$$

It is multiplied in the equation to calculate more accurate value of Q<sub>b</sub> and all the parameters in the main equation are same as discussed above.

## Fully Turbulent Equations

### Weymouth Equation;

It is used for high flow rate, large diameter and high pressure system. This equation is helpful in pressure drop prediction and contains low degree of accuracy relative to other equations.

This is used in distribution networks for safety in predicting pressure drop.

$$Q_b = 432.7 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot D^{2.667}$$

Now, let us talk about the Weymouth equation. Now, this equation is used for high flow rate, large diameter and large pressure system. This equation is helpful in pressure drop prediction and contains low degree of accuracy relative to other equation. So, this is used in the distribution network for safety in predicting the pressure drop. Now, this equation can be written as  $Q_b = 432.7 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot D^{2.667}$ .

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**Weymouth equation can be written as:**

$$Q_b = 432.7 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot D^{2.667}$$



Transmission factor

$$\sqrt{\frac{1}{f}} = 11.19 D^{1/6}$$

And the transmission factor can be defined as  $1 \text{ upon } f = 11.19 D \text{ to the power } 1 \text{ by } 6$ .  
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**The transmission factor can be defined as;**

$$\sqrt{\frac{1}{f}} = 11.19(D)^{1/6}$$

**AGA Fully Turbulent;**

It is most frequently and widely used equation in high pressure, high flow rate system for medium to large diameter pipelines.

It will help in to predict both flow rate and pressure drop and also effective roughness values with high degree of accuracy.

$$Q_b = 38.774 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - B}{G \cdot 2 \log \frac{3.7D}{k_e} L} \right]^{0.5} D^{2.5}$$

$$\sqrt{\frac{1}{f}} = 4 \log \frac{3.7D}{k_e}$$

Now, let us talk about the AGA fully turbulent equation. It is most frequently and widely used equation in high pressure, high flow rate system for medium to large diameter pipelines. It will help in to predict the flow rate and pressure drop and also effective roughness values with a high degree of accuracy. So, this equation is again represented as  $Q_b = 38.774 \frac{T_b}{P_b} \text{ upon } P_b P$

$1$  is square –  $P_2$  square –  $E$  upon  $G Z$  average  $T$  average  $L$   $0.54 \log \frac{3.7 D}{K_e}$  to the power  $2.5$ . And the transmission factor can be defined as  $1$  upon  $f = 4 \log \frac{3.7 D}{K_e}$ .

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**AGA Fully Turbulent;**

It is most frequently and widely used equation in high pressure, high flow rate system for medium to large diameter pipelines.

It will help in to predict both flow rate and pressure drop and also effective roughness values with high degree of accuracy.

$$Q_b = 38.774 \frac{T_b}{P_b} \cdot \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot 4 \log \frac{3.7 D}{K_e} \cdot D^{2.5}$$

The transmission factor can be defined as;

$$\sqrt{\frac{1}{f}} = 4 \log \frac{3.7 D}{K_e}$$

### Colebrook-White;

This equation used for both partially turbulent and fully turbulent flow regimes and also suitable when pipeline is operating in transition zone.

It is used for large diameter, high pressure and medium to high flow rate system.

$$Q_b = 38.774 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot \left[ -4 \log \left( \frac{3.7 D}{K_e} + \frac{1.4126 \sqrt{1/f}}{Re} \right) \right] \cdot D^{2.5}$$

Now, another equation is Colebrook-White. Now, this equation used for both partially turbulent and fully turbulent flow regime and also suitable when pipeline is operating in transition zone. So, it is used for large diameter, high pressure and medium to high flow rate system. Let us write this particular equation  $Q_b = 38.774 \frac{T_b}{P_b} \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot \left[ -4 \log \left( \frac{3.7 D}{K_e} + \frac{1.4126 \sqrt{1/f}}{Re} \right) \right] \cdot D^{2.5}$ . Now, it predicts a high pressure drop and low flow rates then AGA equation.

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### Colebrook-White;

$$Q_b = 38.774 \frac{T_b}{P_b} \cdot \left[ \frac{P_1^2 - P_2^2 - E}{G \cdot Z_{avg} \cdot T_{avg} \cdot L} \right]^{0.5} \cdot \left[ -4 \log \left( \frac{3.7 D}{K_e} + \frac{1.4126 \sqrt{1/f}}{Re} \right) \right] \cdot D^{2.5}$$

$$\sqrt{\frac{1}{f}} = -4 \log \left( \frac{3.7D}{K_e} + \frac{1.4126 \sqrt{\frac{1}{f}}}{R_e} \right)$$

Now, for this we need to define the transmission factor. So, the transmission factor  $1$  upon  $f$  is defined as  $-4 \log 3.7 D$  upon  $K_e + 1.4126$   $1$  upon  $f$  upon  $R_e$ .

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The transmission factor can be defined as;

$$\sqrt{\frac{1}{f}} = -4 \log \left( \frac{3.7 D}{K_e} + \frac{1.4126 \sqrt{\frac{1}{f}}}{R_e} \right)$$

### Pressure drop calculation for pipelines

#### Pipelines in series;

For pipelines in series with different diameters and length, the pressure drop can be calculated as;

On simplifies from general flow equation;

$$\begin{aligned} P_1^2 - P_2^2 &= K_1 Q_0^2 \\ P_2^2 - P_3^2 &= K_2 Q_0^2 \\ P_3^2 - P_4^2 &= K_3 Q_0^2 \end{aligned}$$

Now, let us go for the pressure drop calculation for pipelines because pressure drop is very common phenomena in the pipelines. So, there are two cases says, one is the pipeline in series and other one is the pipeline in parallel. So, the pipeline is series with a different diameter and

length, the pressure drop can be calculated in a very generalized flow equation like  $P_1^2 - P_2^2 = K_1 Q_b^n$ ,  $P_2^2 - P_3^2 = K_2 Q_b^n$ , then  $P_3^2 - P_4^2 = K_3 Q_b^n$  where  $K_1, K_2, K_3$  these are the pipeline resistance at each segment and  $n$  is the flow exponent depending upon the type of equation used.

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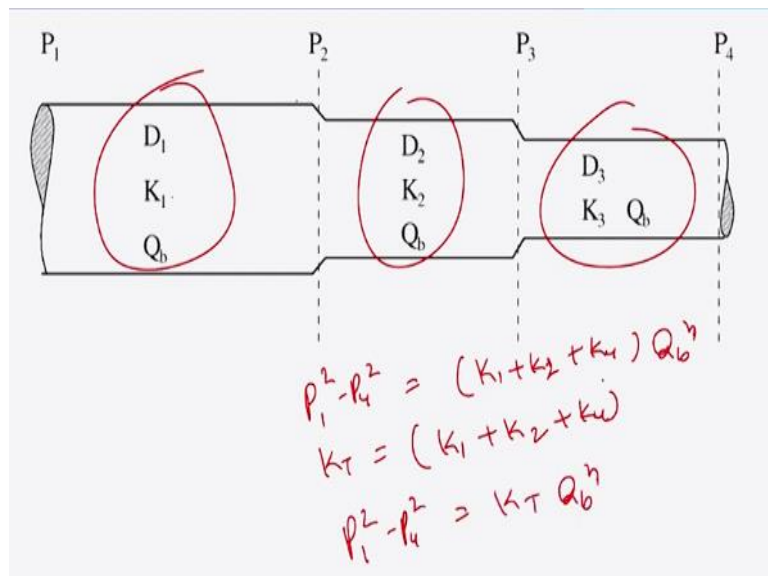
**Pipelines in series;**

$$P_1^2 - P_2^2 = K_1 Q_b^n$$

$$P_2^2 - P_3^2 = K_2 Q_b^n$$

$$P_3^2 - P_4^2 = K_3 Q_b^n$$

Where,  $K_1, K_2,$  and  $K_3$  are pipeline resistance at each segment and  $n$  is the flow exponent depending upon the type of equation used.



Now, here we represented this in the form of pictorial diagram. Here the  $P_1, P_2$  and  $P_3, P_4$  these are the pressure regime and  $D_1, K_1, Q_b$  this is the parameters at this juncture and  $D_2$  that is the diameter  $K_2 Q_b$  at this juncture and  $D_3 K_3$  to be at this juncture. So, if three

equations are added together, then we get  $P_1^2 - P_4^2 = K_1 + K_2 + K_4 Q_b^n$  to the power n and  $K_T$  is equal to all  $K$ 's to be added. So, if we combine these two equations, then we get  $P_1^2 - P_4^2 = K_T Q_b^n$  to the power n.

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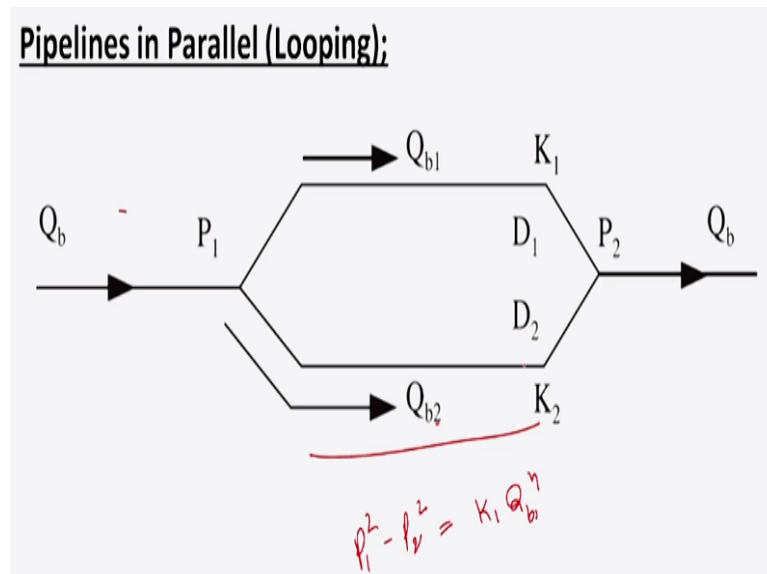
If above three equations are added together, we have;

$$P_1^2 - P_4^2 = (K_1 + K_2 + K_4)Q_b^n$$

Assume,  $K_T = (K_1 + K_2 + K_4)$

On combining above equations, we have;

$$P_1^2 - P_4^2 = K_T Q_b^n$$



Now, let us talk about the pipelines in parallel or looping. So, we need to consider the two different pipes are connected in parallel as shown in this figure  $Q_b$ ,  $P_1$ ,  $Q_{b1}$ ,  $Q_{b2}$  and these are the two pipelines  $K_1$  and  $K_2$ ,  $D_1$  and  $D_2$  and  $P_2$  is the outlet temperature. So, the governing equation for pressure drop for each segment will be represented as  $P_1^2 - P_2^2 = K_1 Q_{b1}^n$ .

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The governing equation for pressure drops for each segment will be represent as;

$$P_1^2 - P_2^2 = K_1 Q_{b1}^n$$

$P_2^2 - P_3^2 = K_2 Q_{b2}^n$   
 $Q_{b1} + Q_{b2} = Q_b$   
 $P_1^2 - P_2^2 = K Q_b^n$   
 $K \rightarrow$  total resistance of a pipe  
 $Q_{b1} = \frac{n \sqrt{P_1^2 - P_2^2}}{n \sqrt{K}}$

Now,  $P_2^2 - P_3^2 = K_2 Q_{b2}^n$  where  $Q_{b1} + Q_{b2} = Q_b$  and generally  $P_1^2 - P_2^2 = K Q_b^n$ . Now,  $K$  is the total resistance of a pipe substituted for loop. So, if we rearrange the above equation, we get  $Q_{b1} = \frac{P_1^2 - P_2^2}{K}$ .

(Refer Slide Time: 23:17)

$$P_2^2 - P_3^2 = K_2 Q_{b2}^n$$

Where,  $Q_{b1} + Q_{b2} = Q_b$

Generally,  $P_1^2 - P_2^2 = K Q_b^n$

Where  $K$  is the total resistance of a pipe substituted for loop, on rearranging the above equations we have;

$$Q_{b1} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}}$$

Similarly

$$Q_{b1} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}} \quad \& \quad Q_{b2} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_2}}$$

$$Q_b = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K}}$$

$$Q_{b1} Q_{b2} \& Q_b = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}} + \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_2}}$$

$$\frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K}} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}} + \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_2}}$$

Now, similarly  $Q_{b1}$  is equal to or  $Q_{b1}$  is represented as minus  $P_2$  square upon  $n$ th root of  $K_1$  and  $Q_{b2} = n$ th root of  $P_1$  square –  $P_2$  square upon  $n$ th root of  $K_2$  and the general equation can be represented as  $Q_b = n$  root of  $P_1$  square –  $P_2$  square upon  $n$ th root of  $K$ . Now, if we substitute the value of  $Q_{b1}$ ,  $Q_{b2}$ , and  $Q_b$  we have  $n$ th root of  $P_1$  square –  $P_2$  square upon  $n$ th root of  $K$  that is equal to  $n$ th root of  $P_1$  square –  $P_2$  square upon  $n$ th root of  $K_1$  +  $n$ th root of  $P_1$  square –  $P_2$  square upon  $n$ th root of  $K_2$ .

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Similarly,

$$Q_{b1} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}} \quad \text{and} \quad Q_{b2} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_2}}$$

General equation,

$$Q_b = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K}}$$

Now substitute values of  $Q_{b1}$ ,  $Q_{b2}$  and  $Q_b$ , we have;

$$\frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K}} = \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_1}} + \frac{\sqrt[n]{P_1^2 - P_2^2}}{\sqrt[n]{K_2}}$$



Similarly

$$K = \frac{K_1 K_2}{(K_1^{1/n} + K_2^{1/n})^n}$$

if  $n=2$

$$K = \frac{K_1 K_2}{(K_1^{1/2} + K_2^{1/2})^2}$$

$K = \frac{1}{4} K_1$

Similarly,  $K = \frac{K_1 K_2}{(K_1^{1/n} + K_2^{1/n})^n}$ . Now if  $n = 2$  this above equation gives the total resistance of two pipelines in parallel and which can be given as  $K = \frac{K_1 K_2}{(K_1^{1/2} + K_2^{1/2})^2}$ , where  $K$  is the total resistance of two pipeline looped together. Now, if two pipelines have equal diameter, then  $K = \frac{1}{4} K_1$ .

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Similarly,

$$K = \frac{K_1 \cdot K_2}{(K_1^{1/n} + K_2^{1/n})^n}$$

If  $n=2$ , the above equation giving total resistance of two pipelines in parallel is given as;

$$K = \frac{K_1 \cdot K_2}{(K_1^{1/2} + K_2^{1/2})^2}$$

Where,  $K$  is the total resistance of the two-pipeline looped together. If two pipelines have equal diameters, then  $K = \frac{1}{4} K_1$ .

## Pipeline Segmental Looping

### Segmental Looping;

- It is not necessary to loop the entire pipeline to obtain the desired flow or downstream pressure but only segment of the pipeline is looped to meet the requirements.
- Let us assume that the pipeline has length  $L$ , diameter  $D$ , total resistance of  $K_1 + K'_1$  and inlet and outlet pressure are  $P_1$  and  $P_2$ .
- To increase the existing gas flow rate from  $Q_1$  to  $Q_2$  without any change in downstream pressure, the value of  $X$ , the length of pipeline to be looped to existing system, must be determined.



Now, let us talk about the pipeline segmental looping. Now, segmental looping it is not necessary to loop the entire pipeline to obtain the desired flow or downstream pressure, but only segment of the pipeline is looped to meet the requirement. Now, let us assume that the pipeline has the length  $L$  and diameter  $D$  and the total resistance is  $K_1 + K'_1$  and the inlet and outlet pressures are  $P_1$  and  $P_2$ . Now to increase the existing gas flow rate from  $Q_1$  to  $Q_2$  without any change in the downstream pressure, the value of  $X$  that is the length of the pipeline to be looped to existing system must be determined.

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**Cont...**

### Note;

- By using larger diameter pipes, the required length of the segment to be looped is reduced.
- Weymouth equation will be used to obtain total pipeline resistance, which is start with one of the major transmission equations and continue to develop the equation to calculate the length of the loop.



Now, by using the larger diameter pipes, the required length of the segment to be looped is usually reduced. Now, Weymouth equation can be used to obtain total pipeline resistance, which is start with one of the major transmission equations and continue to develop the equation to calculate the length of the loop.

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The Weymouth equation;

$$P_1^2 - P_2^2 = \frac{0.000466 G T_f L}{D_1^{16/3}} Q_1^2$$

$P_1^2 - P_2^2 = K Q_1^2$   
 $K = K_1 + K_1' \rightarrow$  total resistance of the single line  
 $0.000466 G T_f \rightarrow C$

So, again coming back to Weymouth equation, that is  $P_1^2 - P_2^2$  and that is equal to  $0.000466 G T_f L$  upon  $D_1^{16/3} Q_1^2$  or  $P_1^2 - P_2^2 = K Q_1^2$  where  $K = K_1 + K_1'$ , this is the total resistance of the single line. For the total resistance of Weymouth equation, the value of  $0.000466 G T_f$  is constant and named as  $C$ .

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The Weymouth equation;

$$P_1^2 - P_2^2 = \frac{0.000466 G \cdot T_f \cdot L}{D_1^{16/3}} Q_1^2$$

Or  $P_1^2 - P_2^2 = K \cdot Q_1^2$

$$K'_1 = \frac{C \cdot X}{D_1^{16/3}} \quad K'_2 = \frac{C \cdot X}{D_2^{16/3}} \quad K_1 = \frac{C(L-X)}{D_1^{16/3}}$$

$$K = \frac{C \cdot L}{D_1^{16/3}}$$

Equivalent resistance for looped segment is

$$K_e = \frac{\frac{C \cdot X}{D_1^{16/3}} \cdot \frac{C \cdot X}{D_2^{16/3}}}{\left( \frac{C \cdot X}{D_1^{16/3}} + \frac{C \cdot X}{D_2^{16/3}} \right)^2}$$

Now,  $K_1 = C \times D_1^{16/3}$ ,  $K_2 = C \times D_2^{16/3}$ ,  $K_1 = C(L - X) / D_1^{16/3}$  and  $K = C \cdot L / D_1^{16/3}$ . The equivalent resistance for looped segment is  $K_e = \frac{C \cdot X \cdot D_2^{16/3}}{D_1^{16/3} \cdot C \cdot X + D_2^{16/3} \cdot C \cdot X}$  whole square.

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Where,  $K = K_1 + K'_1$  is the total resistance of the single line.

For total resistance of Weymouth equation, the value of  $0.000466GT_f$  is constant and named as C.

$$K'_1 = \frac{C \cdot X}{D_1^{16/3}}, \quad K'_2 = \frac{C \cdot X}{D_2^{16/3}}, \quad K_1 = \frac{C \cdot (L - X)}{D_1^{16/3}}, \quad \text{and} \quad K = \frac{C \cdot L}{D_1^{16/3}}$$

The equivalent resistant for the looped segment is;

$$K_e = \frac{\frac{C \cdot X}{D_1^{16/3}} \cdot \frac{C \cdot X}{D_2^{16/3}}}{\left( \frac{C \cdot X}{D_1^{16/3}} + \frac{C \cdot X}{D_2^{16/3}} \right)^2}$$

$$K_e = \frac{C X}{\left(D_1^{16/3} + D_2^{16/3}\right)^2}$$

$$K_{E \text{ Total}} = K_e + K_1 + \frac{C(L-X)}{D_1^{16/3}}$$

$$K_E = \frac{C X}{\left(D_1^{16/3} + D_2^{16/3}\right)^2} + \frac{C(L-X)}{D_1^{16/3}}$$

Now, if you simplify then then  $K_e = C \times D_1^{16/3} + D_2^{16/3}$  whole square. Now  $K_{E \text{ Total}} = K_e + K_1$ . So, if we rearrange  $K_e$ , then  $K_e$  becomes  $C \times$  upon  $D_1^{16/3} + D_2^{16/3}$  square +  $C L - x$  upon  $D_1^{16/3}$ .

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On simplification  $K_e$ , we have;

$$K_e = \frac{C \cdot X}{\left(D_1^{16/3} + D_2^{16/3}\right)^2}$$

$$K_{E \text{ Total}} = K_e + K_1 \text{ (i.e., Pipes in series)}$$

Then, on rearranging for  $K_{E \text{ Total}}$  we have;

$$K_E = \frac{C \cdot X}{\left(D_1^{16/3} + D_2^{16/3}\right)^2} + \frac{C \cdot (L - X)}{D_1^{16/3}}$$

$$\frac{P_1^2 - P_2^2}{P_1^2 - P_2^2} = \frac{\frac{CL}{D_1^{16/3}}}{K_E} \left(\frac{Q_1}{Q_2}\right)^2$$

$$1 = \frac{\frac{CL}{D_1^{16/3}}}{\frac{CX}{(D_1^{16/3} + D_2^{16/3})^2} + \frac{C(L-X)}{D_1^{16/3}}} \left(\frac{Q_1}{Q_2}\right)^2$$

Now, upon dividing the flow equation for existing pipeline after segmental looping we have  $P_1^2 - P_2^2$  upon  $P_1^2 - P_2^2 = D_1 C L D_1$  to the power 16 by 3 upon  $K_E Q_1$  upon  $Q_2^2$  or  $1 = \frac{CL D_1}{D_1^{16/3} + D_2^{16/3}} + \frac{C(L-X)}{D_1^{16/3}}$  upon  $Q_1$  upon  $Q_2^2$ .

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**On dividing the flow equations for existing pipeline and after segmental looping, we have;**

$$\frac{P_1^2 - P_2^2}{P_1^2 - P_2^2} = \frac{\frac{CL}{D_1^{16/3}}}{K_E} \cdot \left(\frac{Q_1}{Q_2}\right)^2$$

$$\text{Or, } 1 = \frac{\frac{CL}{D_1^{16/3}}}{\frac{C \cdot X}{(D_1^{16/3} + D_2^{16/3})^2} + \frac{C \cdot (L - X)}{D_1^{16/3}}} \cdot \left(\frac{Q_1}{Q_2}\right)^2$$

$$X = L \frac{\left(\frac{Q_1}{Q_2}\right)^2 - 1}{\left[1 + \frac{D_2^{8/3}}{D_1}\right]^{-1}}$$

So, the equation becomes  $X = L \frac{Q_1^2 - Q_2^2}{Q_2^2 \left[1 + \frac{D_2^{8/3}}{D_1}\right]^{-1}}$ .

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The equation will become;

$$X = L \frac{\left(\frac{Q_1}{Q_2}\right)^2 - 1}{\left[1 + \frac{D_2^{8/3}}{D_1}\right]^{-1}}$$

Where,

$X$  = length of pipeline to be looped, miles

$L$  = length of existing pipeline, miles

$Q_1$  = initial gas flow rate

**Where,**

$X$ = length of pipeline to be looped, miles

$L$ = length of existing pipeline, miles

$Q_1$ = initial gas flow rate ✓

$Q_2$ = final gas flow rate

$D_1$ = existing pipeline inside diameter, inches

$D_2$ = looped segment inside diameter, inches

Now where  $X$  that is a length of pipeline to be looped that may be in miles,  $L$  is the length of existing pipeline in miles.  $Q_1$  that is the initial gas flow rate,  $Q_2$  is the final gas flow rate if you see and  $D_1$  is the existing pipeline inside diameter in inches and  $D_2$  is the looped segment inside the diameter which is represented in inch.

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**Note;**

- The above equation demonstrates that looping will increase pipeline flow capacity without any changes to the upstream and downstream pressures.
- There are two important parameters to consider when choosing the location for a pipeline loop; temperature and pressure.

Now, this equation demonstrates that the looping will increase pipeline flow capacity without any changes to the upstream and downstream pressures. Now, there are two important parameters which we need to consider when choosing the location for a pipeline loop that is temperature and pressure. So, a class in this particular segment we discuss the various pipeline configuration series and a parallel, we devise the equations with respect to the other parameters in question.

**(Refer Slide Time: 31:59)**



## References

- M. Mohitpour, H. Golshan, A. Murray, PIPELINE DESIGN & CONSTRUCTION: A Practical Approach; Third Edition, American Society of Mechanical Engineers., (2007), ISBN 0-7918-0257-4.

For reference, we have enlisted a reference for your convenience. Thank you very much.