

Environmental Quality: Monitoring and Analysis
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Lecture-42
Gaussian Dispersion Model - Example, Additional topics

(Refer Slide Time: 00:13)

Example



SO₂ emission from a stack

Estimate SO₂ concentration at ground level, centerline, 500 m from the stack

$$\rho_{ij}(x, y, z, H) = \frac{Q}{2\pi u_i \sigma_y \sigma_z} \left[\exp\left(-\frac{y^2}{2\sigma_y^2}\right) \cdot \left[\exp\left(-\frac{(z-H)^2}{2\sigma_z^2}\right) + \exp\left(-\frac{(z+H)^2}{2\sigma_z^2}\right) \right] \right]$$

$$\rho_{ij}(500, 0, 0, 60) = \frac{Q}{2\pi u_i \sigma_y \sigma_z} \left[2 \cdot \exp\left(-\frac{(H)^2}{2\sigma_z^2}\right) \right]$$

Data: Q = 160 g/s H = 60 m u = u_x = 6 m/s
 Overcast conditions No adjustments necessary



So in this, small example just to illustrate what we are doing. This is all there in the PPT you can go and look at it. So we want to look at SO₂ emission from a stack. So this is what we want, estimate SO₂ concentration at ground level center line 50 and 500 meters from the stack. So there is a stack there is a stack here and we are looking at a distance 500 meters from the stack and we want to know, what is the concentration? Center line at ground level which means y equals to 0, z equals 0.

Equation rho A1 500, 0, 0, 60, the height of the stack is 60 meters, it is already given to you. What do you mean by height on the stack is H. H equals H_s plus delta h plume rise all of that is added given to you. You do not have it you have to calculate all that and put it there. So data that we need is Q is 1 that is given to you is this Q is 160 gram per second. Each one of this you have to come if you do not know anything about this problem, you have to compute all of this individually during this u and we are given that this overcast conditions.

(Refer Slide Time: 01:18)

Example contd.

Stability Class Calculation

$u = u_x = 6 \text{ m/s}$

Overcast conditions Overcast \rightarrow slight insolation \rightarrow Stability class = **D**

Computing σ_y and σ_z -

(a) Horizontal dispersion coefficient $\sigma_y = 36 \text{ m}$

(b) Vertical dispersion coefficient $\sigma_z = 18.5 \text{ m}$

Data: $Q = 160 \text{ g/s}$ $H = 60 \text{ m}$ $u = 6 \text{ m/s}$ $\sigma_y = 36 \text{ m}$ $\sigma_z = 18.5 \text{ m}$

$$C_p(500, 0, 0, 60) = \frac{160 \cdot 10^6}{\pi(36)(18.5)} \cdot \exp\left(-\frac{(60)^2}{2(18.5)^2}\right) = 66.0 \text{ } \mu\text{g/m}^3 \text{ of SO}_2$$

From the overcast conditions of the table the Pascal differs table with class. I calculate that overcast slight insolation stability class is D. Now, this is a matter of judgment, so I think some of you may determine this as stability class C, some may be doing as D, therefore your numbers will be different. So this is an estimate not the true value because a lot of other factors that will Gaussian dispersion model is either ideal model everything is very symmetrical and all that.

There are non idealities in systems transports that will occur which you have taken into account. Based on that. So we use the, we are looking at x equals 500, so it means that the computation of sigma y at x equals 500 will take this is 500 this is 500 meters. We go to stability class D i am saying the stability class D here. This line is stability class D and then I pick my value for sigma y at 36 meters there and similarly I do this for the this thing also the 500 and I am going through this line.

And I get the value of the sigma z as 18.5, if the stability class where A then my value of sigma y would be around 150 or 120 something like that, so I have other this I put it in there and I get a value of 66 microgram meter cube of SO2. This is the concentration at that point. This is the single computation for one coordinate, one point, one location anywhere around the source, it could be anywhere around the source, hopefully it is in the direction of wind.

So that you have to calculate that, you need to know which direction is going and there is in the direction of wind that should be implicit in the problem, it is not said anywhere in the problem as we mentioned yesterday.

(Refer Slide Time: 03:20)

Example 2



SO₂ emission from a stack Estimate SO₂ concentration at ground level, 50m crosswind, 500 m from the stack

$$\rho_{SO_2}(x,y,z,H) = \frac{Q}{2\pi u \sigma_y \sigma_z} \left[\exp\left(-\frac{y^2}{2\sigma_y^2}\right) \cdot \left[\exp\left(-\frac{(z-H)^2}{2\sigma_z^2}\right) + \exp\left(-\frac{(z+H)^2}{2\sigma_z^2}\right) \right] \right]$$

$$\rho_{SO_2}(500,50,0,60) = \frac{Q}{2\pi u \sigma_y \sigma_z} \left[2 \cdot \exp\left(-\frac{(H)^2}{2\sigma_z^2}\right) \right] \left[\exp\left(-\frac{y^2}{2\sigma_y^2}\right) \right]$$

$$\rho_{SO_2}(500,50,0,60) = 66 \cdot \exp\left(-\frac{50^2}{2 \cdot 36^2}\right) = 23.0 \mu\text{g}/\text{m}^3 \text{ of SO}_2$$



Second example; so here we set 50 meters crosswind, which means that y is not 0 anymore, y is of the x axis 50 meters away, so we put y equals to 50. See in some cases it is not clear so most of the time when you are doing the problem this is not important, people are not only examination people will give crosswind and central line and all that, we will see what the real application is, we do not care about all of this things, we are interested finding out a lot of points.

We just calculate everywhere and find out what is, so this is just from a single, if you are writing an exam somebody will ask what is central line or what is cross line? Otherwise the real situations we do not use this for this kind of calculations;

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Application of Dispersion Models

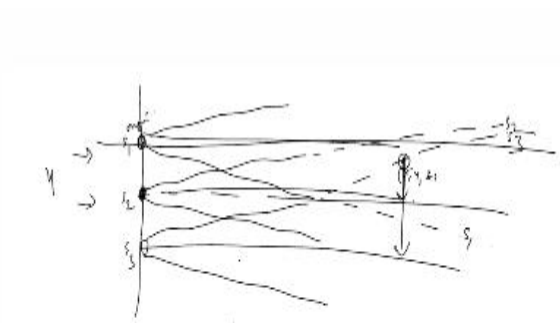


- Estimation of pollutant concentration in air at any given set of coordinates.
 - Assessment of the impact of one source on air quality
 - Assessment of air quality from large number of sources in a given location
 - Application
 - Define a grid of measurement coordinates (also referred to as receptors)
 - Estimate the emission rates of all sources, location of source to a reference origin
 - Estimation of meteorological parameters
 - Estimation of concentration of pollutant at all receptors
- Representation of the dispersion is effectively achieved by plotting ISOPLETHS (or lines joining points of same concentration OR concentration contour maps) over a geographical map.



We are not just interested in central line, so how do we apply this dispersion model, the estimation of; what we are using it for is estimation of pollutant concentration of any given set of coordinates whatever it is, assess the impact of one source on air quality, you can also assess from a large number of sources you just add large number of sources.

(Refer Slide Time: 04:32)



For example, if you are interested in doing a large number of sources, I am looking at a top view of map there is a source here, we call it a source 1, the source 1 has plume. Source 2 somewhere nearby assuming that wind is in this direction source 2 also has plume, source 3 also as a plume it may have different q_1, q_2 what we are assuming in dispersion model is let us say if I want to

measure the concentration at this point from location x, y and z there is a contribution from source 1 for this S1.

There is also a contribution from source 2, there could also be contribution from source 3 all of these 3 will contribute concentration here. The models we are add all of them, that is it. Now we have a frame of reference if we assume this to be origin, x equals 0 or something. We will just take this as the point of reference and everything else will calculate from here, so in the dispersion model when we are assuming this we can transpose all of this.

Even if we do the calculation for this we add this contribution to this to this based on a set of coordinates based on one of them when you are doing the calculation this is x, this is some y, this y is different for this one, this y is different for this one, this y is different for this one, each one of them this y is different. But in the real system y is y there is one fixed coordinate, but when you are doing calculate individual sources you have to transpose that, you have to adjust that y.

So you take frame of reference, fixed frame for the point from this; you have to do separately for this. I am not sure clear on this part, when you do 3 sources you will know what you talking about contributions to this source from particular points.

(Refer Slide Time: 06:55)

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The application when we do this we define a grid of measurement coordinates also called as receptors. We say receptors what we are doing is we are trying to measure concentration exposure which means there is a receptor there, instead of receptor what we are doing we are putting the coordinates x , y and z on the left hand side of the Gaussian dispersion model that is the receptor which is the coordinator.

We defined as grid of coordinate; we can calculate this resource, the concentration at those coordinates, the large set of coordinates. We estimate emission rates for all sources and location reference to some origin that described earlier. We estimate metallurgical parameters. We also estimate concentration of pollutants at all receptors.


Once we do this we have to represent it somehow so there are large number of sources they said one source they even if there is one source. I will show you the example of one source. How do we effectively represent this?

(Refer Slide Time: 07:57)

Application of Dispersion Models ISaPLE779



The superposition of isopleths on a geographical map gives a good indication of the pollutant behaviour and provides guidance for pollution management strategies.



The way we do it is by mapping it. So this the very good way to doing it, say for example; this is a map of Chennai and this is a garbage dump in South Chennai. This is a source, I am assuming this is my source one source. So if I plot, if I measure large set of coordinates all around this. I am assuming that the wind is coming from this direction. If my wind is in this direction, I am defining that as my x axis and then I am measuring it in a y set of coordinates.

We have a Cartesian grid; I can just define a bunch of this entire zone, I am measuring the concentration. Say your 100 locations. Then I get different I get a table of concentration versus coordinates. Then there is what we do is this. We join the lines, it is like an isopleth. What is called an isopleth? An isopleth is the line joining points of equal concentration, so this gives you a contour map.

So here I have written the contour map but this is a source very close to the source. This boundary of the source this radius around source is 100 milligrams of micrograms of meter cube will concentration of some pollutant. They are going out you are expecting concentration will decrease. So this contour is 80, this contour is 50; this contour is 50, this contour is 40, so on. So you get a map of where the pollutant is going. You get a visual map of where the pollutant is going.

So this is the superposition of your Gaussian dispersion model calculation with reference to a real source. So, on a map this is how people apply this on a map you have different sources. There are only one source. Now, I can have multiple sources, I can have source 2 here, source 3 here, and whatever. And I do not have I can just put a contour map of one particular pollutant. So the contour map is a one pollutant because the pollutant concentration depends on the emission factor and emission rates.

So even if they are burning coal in all those four places the emission factor for sulphur dioxide, if they are doing the same process, it should be the same but you still have estimated differently for all these four sources depending on the emission rate is estimated differently based on activity rates and all that. So each of these things have done separately and then you apply the Gaussian dispersion model and then plot. What is going to be the contour map?

So what this gives you is application is; let us say that 50 milligrams per meter cube is the ambient exposure level you cannot anything above 50 is supposed to be not safe. So then you can say that I will mark these regions in this radius to be seriously affected. So this is very useful in

planning an emergency response. So say you have to evacuate say there is a leak. There is a factory and there is a leak and this leak happens.

An immediate response you want to say who are the people going to be affected immediately and you can say this is a radius worst case scenario, worst case scenario means, very high winds dispersion happens very fast, you have to find out what is the worst case scenario, run the dispersion model and find out which case is the lowest. So you have to map these things.

So there are companies that do this emergency response planning. So there are scenarios there are worst case scenarios. We know the wind, we know the behavior of wind and we know extreme events they say there is a big cyclone or something happens and. So for different events, they will have different plans. So if they know it is something happen, they know exactly what to do.

Which area should be targeted first and if you know that that area is going to be under high risk you give them some safety equipment, there is a leak this put on this mask of staying indoors or something whatever something do some remedial measure. If you are unable to evacuate from there, so this is emergency response measure dispersion modeling can give you a great deal off. The second type of application in sense how you can use this information is to plan this sighting of industry.

This is a very, very common thing in the reason people used to do this very heuristically. So you have the industrial estates or what we call as this, in India, we have this, in Tamil Nadu, we have the sipcot small industries, so there are located in some locations some places which are far away from typically urban places and the idea behind that is given the wind patterns and all that even if there is an emission something there is nobody downwind that will get exposed to it.

So essentially away from far away from all the exposure all receptors. You do not take that into account this is why you see a lot of debates right where do you site the particular thing this is dangerous you cannot put it here, because it will cause groundwater pollution at the same thing

what we are talking about air here applies to other media as well, you are talking about soil pollution, water pollution and all that.

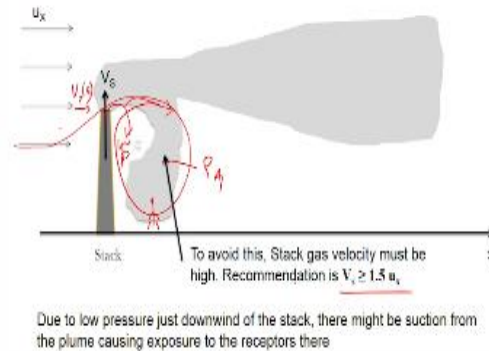
You do not want things to reach receptor by the time it reaches it should be concentration should be small enough because of dilution or dispersion, so the models, mathematical models give you a very good preliminary handle on this what we talk of preliminary handle is not accurate by no means it is accurate but it gives you a general idea that you know 5 kilometers is a reason that some going to be great interest worst case scenario.

If it is better than this fine very good no problem, but it is worst case scenario what we have planning for dispersion models are reasonably good under this condition. So you can also plan in you can the way you apply the dispersion model depends on whatever you are trying to do your objective. A lot of companies which do this it is very common in the West, it is catching up here people are trying to find out scenarios in urban areas.

For example, there are a lot of places in India where right now there are industries in the middle of a large city where in Chennai itself, if supposed to be in the outskirts now around that there is a lot of residential areas it is happened in all cities in India. There is large amount of urban residential locations in the middle of that there is a cluster of industry. So therefore the regulation and the way they operate and all that comes under scrutiny.

(Refer Slide Time: 14:47)

Stacktip Downwash



There are a couple of small Artifacts to this dispersion, these are the non-idealities one of them is called as stacktip downwash, now this is not important for ambient pollutions, this is important for the in the place in the source, for example a factory and you have a stack you have a chimney which is releasing emissions. There is a possible scenario that this plume will not disperse but it will come back.

Right below next to the stack, so the reason for this is the same reason why particles get absorbed with it is, the wind is here. The streamline of the wind flows around the stack when that happens there is a low pressure region that is created here right behind the stack because its low pressure if anything comes in this region, it gets sucked into this low pressure region and circulates there.

Why does this happen? It happens when you do not the material coming out of the stack does not have enough momentum to clear out of this region, so it happens only when the velocity of the stack gas is smaller than the wind. Where it must, so what happens is as soon as it comes pushed in you get pushed to the side and it can get into this slow pressure zone and it can recirculate there.

So when this happens this stack will go on this region the concentration of rho A1 can increase can accumulate over grade of temperature, which means that for exposures of people standing

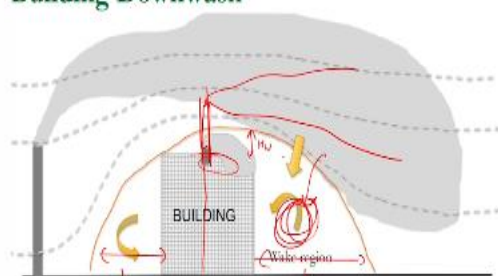
here can be very high. So implant exposure can be very that is not very safe for the plant, whoever is working there, so to avoid that people have a recommendation that the stack velocity the gas velocity coming from a stack must be at least one and a half times greater than the wind speed at that point.

The stack here, this is the U_x at the stack. The U_x at stack should be greater than should the velocity of stack must be 1.5 times greater than this much, by this much.

(Refer Slide Time: 17:14)


Building Downwash

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NPTEL



The presence of a BUILDING in the path of air causes streamline separation resulting in the formation of low pressure regions called "wakes". These can pull in the pollutant plume from a different source. Alternatively, sources on top of the building that are within the wake will circulate locally causing higher concentration and exposure.

The dimensions of the WAKE must be estimated and then the sources must be located appropriately for optimum clearance and least air pollution impact.



The other type of Artifacts is called the Building Downwash. This is more serious this affects people away from the source, so there is a streamline. This dotted lines, we see a big building in the pathway this streamline more around it and they create this regions around the building called as wakes, the same as the stack tip downwash but this is huge stack is as a small the reason we say stack means many of these industry stacks are huge.

They are not like 20 centimeters, they are big several meters and diameter and all that, so at least a ground level. These buildings can be big, so these buildings the streamlines separation around buildings causes this low pressure regions called as the wake and now if there is a plume that is going here and this plume gets near the wake it can get sucked into this peak, so it can get pulled in and it will recirculate here.

Over a pair of names, that is one second problem; suppose you have a stack on top of this building. Because this region marked by this red line the red curve is not part of the inside the wake which means it is not mixing very well with the outer this thing. There is no air circulation in this there is no air movement here, if your stack releases right on the roof of a building and there is a height of this wake there is this is some distance is the length of the wake.

Depending on the size of the building this dimensions form and the velocity of the air. So if this stack is below this height, it will not get out, it will stay there. This entire thing will accumulate in this region around the building. It can sink in, it will accumulate their concentration will have spins its exposure to people in the building or near the building can be high. The only way to do this you have to extend here.

So that it gets carried by the general wind that is crosswind is happening and so there then it will disperse nicely. This can happen in a lot of building which are not planned. Can you give me an example of this? Stack on top of a building, which is not extending into the building. There a lot of examples you can go around seeing; Dispersion, stacktip downwash, building downwash, small sources.

What is one of the major urban sources of emission combustion sources that you can think off? Not vehicles other stationary sources? Kitchen is one, second; there is one more source. So kitchen is one very good example. So lot of this big corporation offices, they have a food court or something and they have a long chimney that will be rising. Well, you will go to the roof and stop here sometimes.

And you can see in some other buildings nearby there will be a big black mark in the top part of the building, which is indication that is not gone up, it is there, it has to extend further up. That is a cause because you have to pump all its exhaust a few meters high pumping is expensive. You have to work against this thing. So that is costs of people do not plan it ahead. That is one second what is the second source, large buildings?

You can see it; you can see it next to research park here, the IT park. What is one common source of combustion that people use in current urban scenarios in India, is a generator. Diesel generator people have used huge diesel generators, you can see in buildings lot of residential buildings have a lot of commercial buildings have it. There is an exhaust and diesel generation diesel exhaust is considered to be diesel engines have a very bad history with exhaust.

So it is improving now but a lot of fine particulate matter that comes out of it and this diesel exhaust supposed to go all the way. If you follow the rules of dispersion, proper dispersion you have to stack height has to be reasonably high. So for this in the middle of an urban cluster, where will you send it you have to send it out really high? There is building downwash it is not going anywhere everything is accumulating in the road, it will stay there.

Lot of carbon dioxide and is zinc and it will road level pollution be very high. So it is supposed to go out all the way up into the region above the wake and get out, disperse. All of times, it is not done. So this design of these kind of devices has you we use dispersion model and we use these kind of things to do this.