

**Process Control and Instrumentation**  
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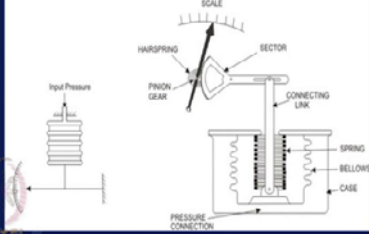
**Lecture - 43**  
**Pressure Measurement (Contd.)**

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**Elastic Pressure Transducer: Bellows Pressure Gauge**

A bellows element is a one piece expansible, collapsible, and axially flexible member. Bellows are essentially thin walled cylindrical shells with deep convolutions and are sealed at one end. The sealed end will undergo axial displacement when pressure is applied at the open end.

Bellows are made of materials with good elastic property such as: brass, phosphor bronze, beryllium copper etc. Stainless steel (not highly elastic) is also sometimes used for its anti-corrosive property. Carbon steel is easily corroded and difficult to machine.



- Used for measuring lower pressures, more sensitive than Bourdon tubes. Nominal range: 5 in of water to 100 psi
- Spring can be used to determine the range
- More sensitive than Bourdon type gauge

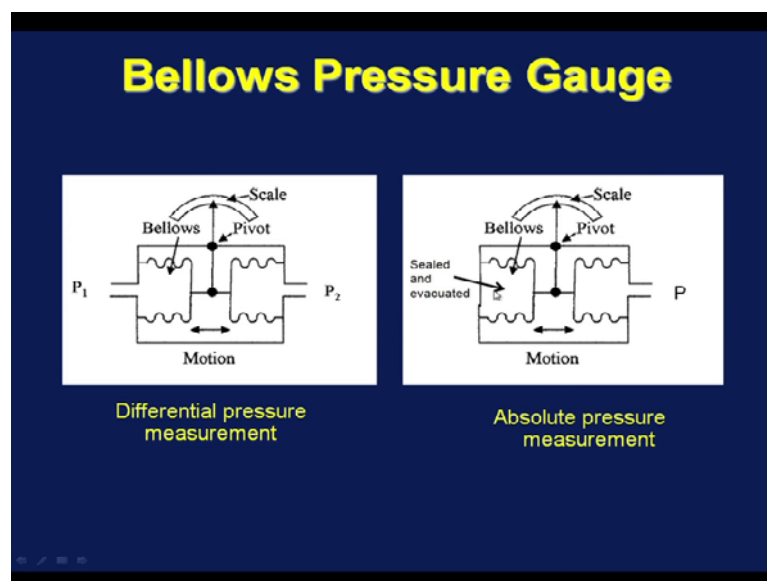
Let us continue with our discussion on Elastic Pressure Transducers. In our previous class we talked about Bourdon Gauges. Today let us talk about the next Elastic Pressure Transducer. Let us say Bellows Pressure Gauge. A bellows element is a one piece expansible, collapsible, and axially flexible member. Bellows are essentially thin walled cylindrical shells with deep convolutions and are sealed at one end. The sealed end will undergo axial displacement when pressure is applied at the open end this is a schematic of bellows element. It is essentially a thin walled cylindrical shell with deep convolutions it is sealed at one end and the other end we can apply the process pressure.

If, I apply pressure here the sealed end will undergo axial displacement which can be read by the deflection of the pointer against this scale. So, this essentially a collapsible member sealed at one end it has deep convolutions made of thin metallic shells. When I apply pressure at the free end the sealed end undergoes axial displacement and that displacement is a measure of the pressure being applied. This is a better representation of the bellows element, you have the bellows with deep convolutions it is spring loaded

inside. So, that the deflection can be controlled. And this deflection is read by this pointer and scale mechanism.

So, we have Connecting Link and we have a Sector. And give an assembly sector and Pinion assembly which helps this deflection to be read by the moment of the pointer against this scale. Bellows are made of materials with good elastic property such as brass, phosphor bronze, beryllium copper etcetera. They are all alloys. Stainless steel, is also sometimes used although it is not highly elastic, but because of its good anti-corrosive property we sometimes use stainless steel. Carbon steel is not a good choice because, it gets easily corroded and it is also difficult to machine. Bellows elements are Used for measuring lower pressure it is more sensitive than Bourdon tubes. The Nominal range over which a bellows element can be used is about 5 inch of water to about 100 psi.

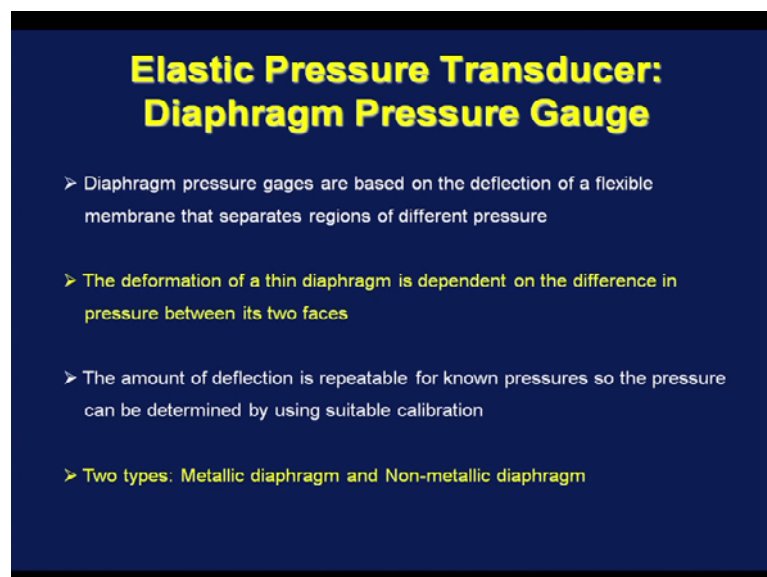
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Bellows Pressure Gauge can be used to measure gage pressure Differential pressure as well as Absolute pressure. Let us look at this arrangement. We have two bellows connected with each other and we have attached a pointer to the link that connects this two bellows. Now, when this two bellows are connected to a differential pressure source the combine movement of this the movement of the pointer against this Scale will be a result of the combine motion of these two bellows.

So, in that case the movement of this pointer against this scale will be a measure of the difference between P1 and P2 or the differential pressure. If, you one of this pressure says atmospheric pressure it is measuring Gauge Pressure. If, I sealed one of this Bellows and it is evacuated. So, there is 0 pressure inside in that case, the bellows element will measure Absolute pressure. So, to measure absolute measure with help of a bellows, what you will do is one of these bellows will be evacuated completely and sealed. So, that it has 0 absolute pressure. So, in that case the pressure that is being applied here will be will have a reference against 0 Absolute pressure. In other words we can measure absolute pressure.

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**Elastic Pressure Transducer:  
Diaphragm Pressure Gauge**

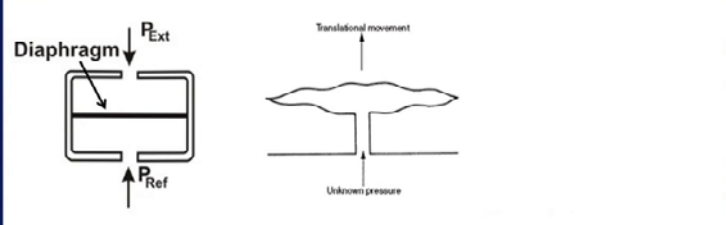
- Diaphragm pressure gages are based on the deflection of a flexible membrane that separates regions of different pressure
- The deformation of a thin diaphragm is dependent on the difference in pressure between its two faces
- The amount of deflection is repeatable for known pressures so the pressure can be determined by using suitable calibration
- Two types: Metallic diaphragm and Non-metallic diaphragm

Next, let us talk about another Elastic Pressure Transducer the Diaphragm Pressure Gauge. Diaphragm Pressure Gauge is are based on the deflection of a flexible membrane that is separates regions of different pressure. So, diaphragms are nothing, but are flexible membrane. It can be made of metal it can be made of non metalize as well. The deformation of a thin diaphragm is dependent on the difference in pressure between its two faces. So, if I have a thin flexible membrane. Let us call it a diaphragm and two different pressures are being applied on two faces then, the deformation or the deflection of the thin diaphragm will be a measure of these two pressures, that are being applied on its two faces. The amount of deflection is repeatable for known pressure. So, pressure can be determined by using suitable calibration. Both metallic diaphragms and nonmetallic diaphragms are used for pressure measurement.

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### Diaphragm Pressure Gauge

- A metal-diaphragm pressure gage uses a thin flexible diaphragm of materials like brass, bronze, monel, Ni Span C, etc. The force of the pressure against the effective area of the diaphragm causes a deflection of the diaphragm. The motion of diaphragm is a measure of pressure and the motion of diaphragm operates an indicating or recording type instrument
- Diaphragm can also be made of nonmetallic elements: rubber, plastic, leather
- Diaphragm gauges are typically spring-loaded so that the range and sensitivity can be varied
- Diaphragm element can measure both absolute and differential pressures



Let us now, talk about the Diaphragm Pressure Gauge in little more detail. A metallic diaphragm pressure gauge uses a thin flexible diaphragm of materials like brass, bronze, monel, Ni Span C etcetera. All these materials are very good elastic property. The force of the pressure against the effective area of the diaphragm causes a deflection of the diaphragm the motion of diaphragm is a measure of pressure and the motion of diaphragm operates an indicating or recording type instrument. This is a schematic of a diaphragm element.

So, when a pressure is applied here there is a Translational movement of this diaphragm element. This movement of the diaphragm can be used to move a pointer and scale mechanism. So, the deflection can be rate and that will be taken as a direct measure of the pressure being applied. Diaphragm can also be of nonmetallic elements such as rubber, plastic, leather etcetera. Diaphragm Gauges are typically Spring loaded, so that the range and sensitivity can be varied. For nonmetallic diaphragms they are usually spring loaded because, nonmetals do not have good elastic property like metal such as brass, bronze, monel, Ni Span C etcetera. Diaphragm elements can also be used for measurement of differential pressure as well as absolute pressure.

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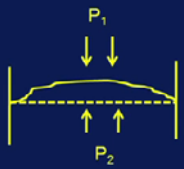
### Diaphragm Pressure Gauge

An approximate relation between the pressure differential ( $P_2 - P_1$ ) and the normalized deflection of the diaphragm at the center is given by:

$$P_2 - P_1 = \frac{256Et^4(r + 0.488r^3)}{3D^4(1 - \mu^2)}$$

$E$  = Elastic modulus  
 $t$  = thickness of diaphragm of diameter  $D$   
 $d$  = deflection at center  
 $r = d/t$  (normalized deflection)  
 $\mu$  = Poisson's ratio

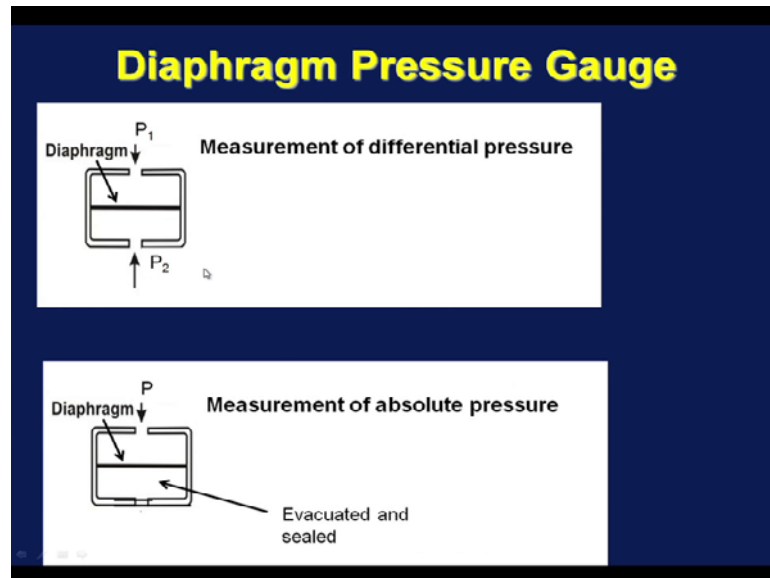
For a linear relationship, the requirement is  $0.488r^3 \ll r$



An approximate relation between the pressure differential and the normalized deflection of the diaphragm at the center is given by this equation. So, this equation relates the pressure differential to the normalized deflection of the diaphragm at the center. Let us consider this schematic. This is the diaphragm when there was no deflection. Now,  $P_1$  and  $P_2$  acts  $P_1$  and  $P_2$  are two different pressures they act on this diaphragm and there is this deflection at the centre. This deflection can be made normalized by dividing this deflection by the thickness of the diaphragm. So, this relates that normalized deflection to pressure differential  $P_2$  minus  $P_1$ .

So, the deflection of the diaphragm at the centre depends on Elastic modulus of the material of the diaphragm, thickness of the diaphragm, diameter of the diaphragm and the Poisson's ratio. In this equation  $E$  is elastic modulus,  $t$  is thickness of diaphragm,  $r$  is normalized deflection which is, deflection at the centre divided by thickness of the diaphragm and  $D$  is the diameter of the diaphragm and  $\mu$  is the Poisson's ratio of the diaphragm material. This equation is highly nonlinear for a linear relationship the requirement is this quantity  $488r^3$  should be much less than  $r$ . So, that this can be neglected, in that case we will get linear relationship between normalized deflection of the diaphragm at centre and pressure difference.

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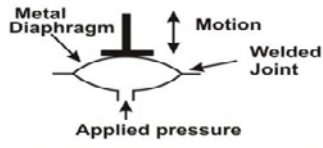
This schematic shows how we can measure differential pressure with help of a Diaphragm element. We have a Diaphragm here. So, this diaphragm divides this into two chambers. In one chamber we apply pressure  $P_1$  the other chamber we apply pressure  $P_2$ . So, the movement or the deflection of this diaphragm will be dependent on  $P_2$  minus  $P_1$ . So, this deflection can be read again by using a pointer and scale. We have to attach a pointer and scale with this diaphragm through appropriate mechanism and the deflection of this diaphragm we will be measure of the pressure differential  $P_2$  minus  $P_1$ . Again if, I evacuate one chamber and seal it we can measure absolute pressure. So, one chamber is evacuated completely and sealed. So, it has 0 absolute pressure. In that case the deflection of this diaphragm will measure absolute pressure.

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## Diaphragm Capsule

A capsule is formed by joining two diaphragm at the periphery  
The sensitivity of the pressure gage can be increased by cascading several capsules

When a pressure is applied to the capsule assembly by an inlet pipe passing through the center of all the capsules, the deflection of the gage will be the sum of the individual capsules



For  $N$  number of capsules, following empirical relation gives an estimate of the deflection  $d$ :

$$d = kN(P_2 - P_1)D^n t^m$$

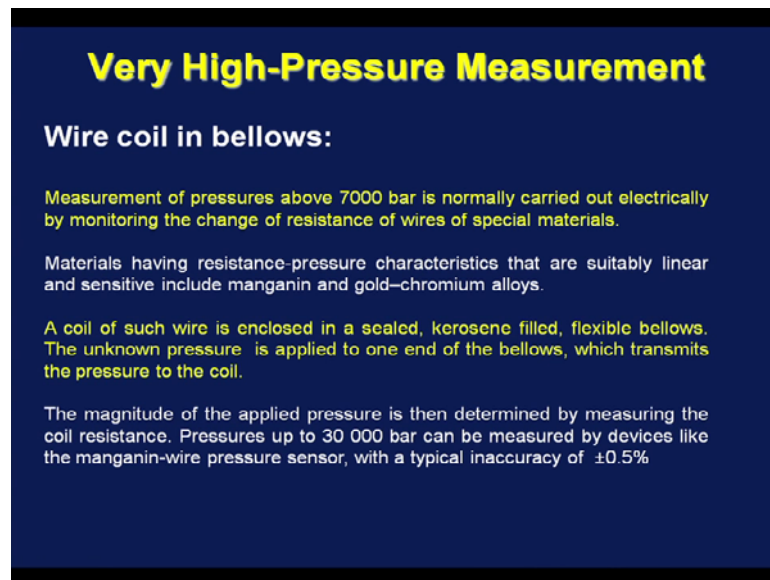
For most practical cases,  
 $m = 4$   
 $n = -1.5$

$k = \text{constant for the gage}$

Sometimes, we form a Capsule by joining two Diaphragm at the periphery. So, it takes two metallic diaphragm and join them to form a capsule. The sensitivity of the pressure gauge can be increased by cascading several capsules. So, we can form several such capsules and cascade them. So, we will have a assembly of capsules when a pressure is applied to the capsule assembly by an inlet pipe passing through the centre of all the capsules the deflection of the gauge will be the sum of the individual capsules. One such capsule is shown here, imagine several such capsules are stat and this inlet pipe passes through the centre of all the capsules. Then, the pressure applied through the inlet pipe will cause a very large deflection of the pressure gauge.

So, we can increase the sensitivity of the pressure gauge substantially. This equation an empirical relation tells us how much deflections will there be if you have in capsules in an assembly. This is an empirical relation which gives an estimate of the deflection of the pressure gauge and it shows that it depends on number of capsules the pressure differential, the diameter and the thickness.  $k$  is a constant for the gauge. For most practical cases this exponent  $m$  and  $n$  are chosen as  $m$  equal to 4 and  $n$  equal to minus 1.5. So, if we increase the number of capsules there will be more deflection.

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**Very High-Pressure Measurement**

**Wire coil in bellows:**

Measurement of pressures above 7000 bar is normally carried out electrically by monitoring the change of resistance of wires of special materials.

Materials having resistance-pressure characteristics that are suitably linear and sensitive include manganin and gold-chromium alloys.

A coil of such wire is enclosed in a sealed, kerosene filled, flexible bellows. The unknown pressure is applied to one end of the bellows, which transmits the pressure to the coil.

The magnitude of the applied pressure is then determined by measuring the coil resistance. Pressures up to 30 000 bar can be measured by devices like the manganin-wire pressure sensor, with a typical inaccuracy of  $\pm 0.5\%$

After, talking about pressure measuring measurements that are used for measurement of moderate pressure, let us now talk about how we can measure Very High Pressure. We are talking about pressures as high as 7000 bar. We can use an instrument called Wire coil in bellows. Measurement of pressures above 7000 bar is normally carried out electrically by monitoring the change of resistance of wires of special materials. So, to measure Very High Pressure we monitor the change of resistance of wires of special materials with pressure.

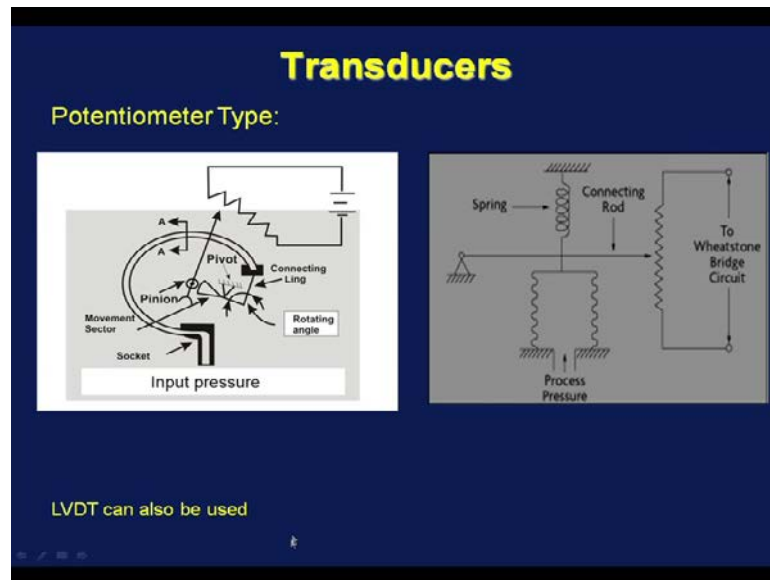
Materials having resistance pressure characteristics that are suitably linear and sensitive include manganin and gold-chromium alloys. So, you use manganin or gold-chromium alloys because, they have suitable resistance pressure characteristics. So, A coil of manganin or gold-chromium alloys is enclosed in a sealed kerosene filled flexible bellows. The unknown pressure is applied to one end of the bellows which transmits the pressure to the coil. The magnitude of the applied pressure is then determined by measuring the coil resistance. Pressures up to 30000 bar can be measured by devices like the manganin-wire pressure sensor with a typical inaccuracy of plus minus 0.5 percent.

So, to measure Very High Pressure we take wires with good resistance pressure characteristics such materials are manganin and gold-chromium alloys. A coil of such wires is enclosed in a sealed kerosene filled flexible bellows. The unknown pressure is applied to one end of the bellows and this pressure will be transmitted to the coil. So, the



coils resistance will change according to the magnitude of the pressure. Therefore, the magnitude of the applied pressure can be determined by measuring the coil resistance. We can measure pressures as I has 30,000 bar by devices like the manganin wire pressure sensor.

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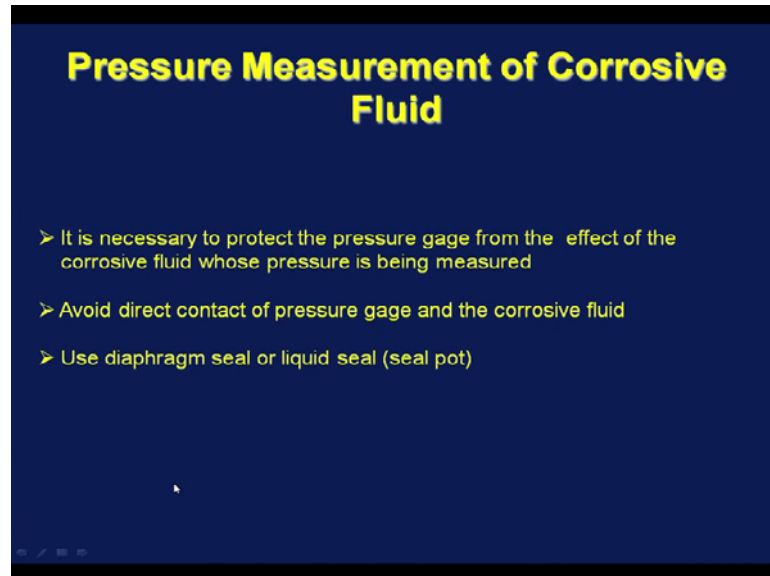


We have talked about Transducers in detail before. We can very easily convert the elastic pressure transducers to a transducers that gives us electrical signal think of a Bourdon tube as shown here. Here, the Bourdon tube is converted to a Potentiometer Type Transducer. So, instead of reading the position of this pointer against the scale, this will the pressure can be read from the electrical signal that is the output from this transducer. The same way a bellows element can be easily converted to a Potentiometer Type Transducer with help of this Wheatstone Bridge Circuit. As the process pressure changes the position of this pointer or the Connecting Rod changes, so the output of the Wheatstone Bridge Circuit changes. So, that electrical output will be taken as a measure of this Process Pressure.

So, the basic function or the way these two different pressure measuring elements are converted to a potentiometer type transducer is same. We can also use a linear variable differential transformer or LVDT to convert these to a transducer that gives us electrical signal. Because, we have seen in our previous lectures that LVDT is a distance

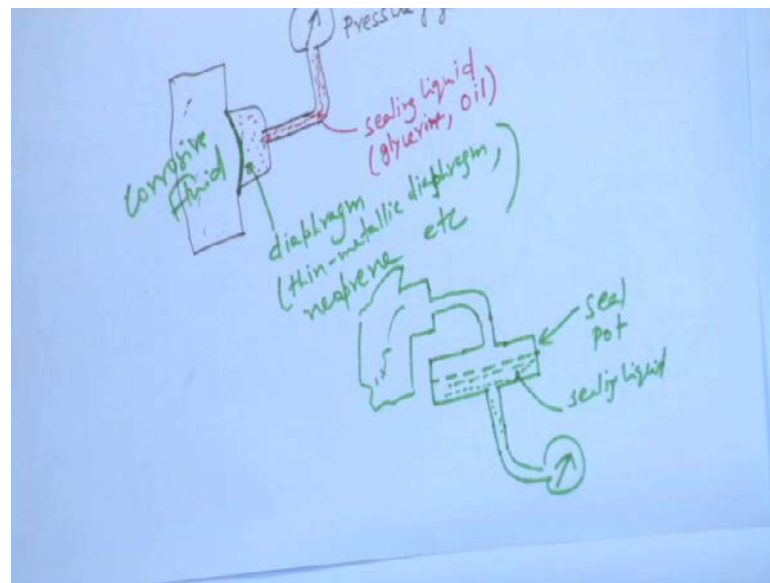
measuring transducer. So, the deflection of this pointer or this pointer or connecting rod can also be converted to an electrical signal by using LVDT.

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Let us now briefly talk about how we measure Pressure of Corrosive Fluid. When you want to measure the pressure of a corrosive fluid it is necessary to protect the pressure gauge from the effect of the corrosive fluid whose pressure is being measured. So, you should avoid direct contact of pressure gauge and the corrosive fluid. We can make Use of a diaphragm seal or liquid seal known as seal pot to avoid direct contact between the pressure gauge and the corrosive fluid. This can be done as follows.

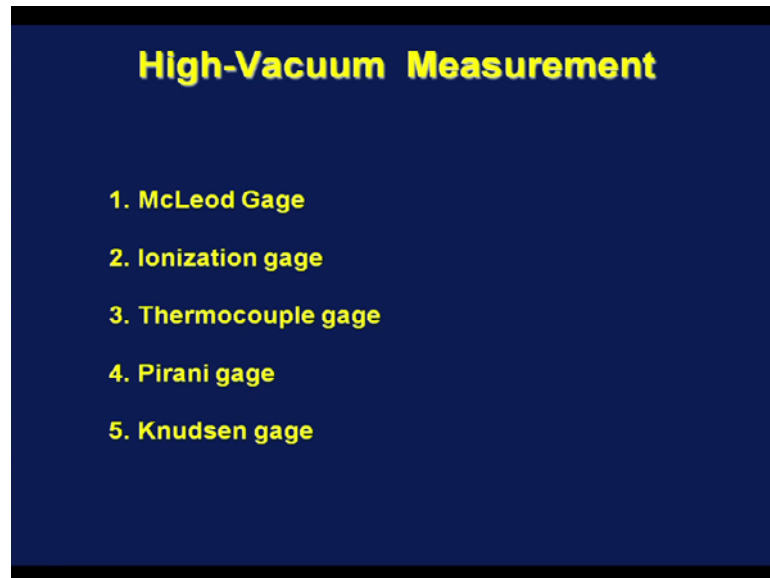
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This is the Pressure gauge. And let say this is the Corrosive Fluid. We use a diaphragm element here. It may be a thin metallic diaphragm or it may be made of say neoprene etcetera. This interpret is filled with a sealing liquid. So, this is completely filled with a sealing liquid it may be glycerin or some oil and this is the Corrosive Fluid, so now the corrosive that I want to measure the pressure of this Corrosive Fluid. So, we have a diaphragm here, which receives the pressure it reflects transmits this pressure to this pressure gauge through this sealing liquid. So, the diaphragm element does not allow this corrosive fluid to come in direct contact with the pressure gauge, but transmits the pressure to the pressure gauge through this sealing liquid. So, that way we can protect our pressure gauge. We can also make use of a seal pot or sealing liquid. So, we have a sealing liquid you have a Seal Pot this is the sealing liquid this is the pressure gauge this is the corrosive fluid.

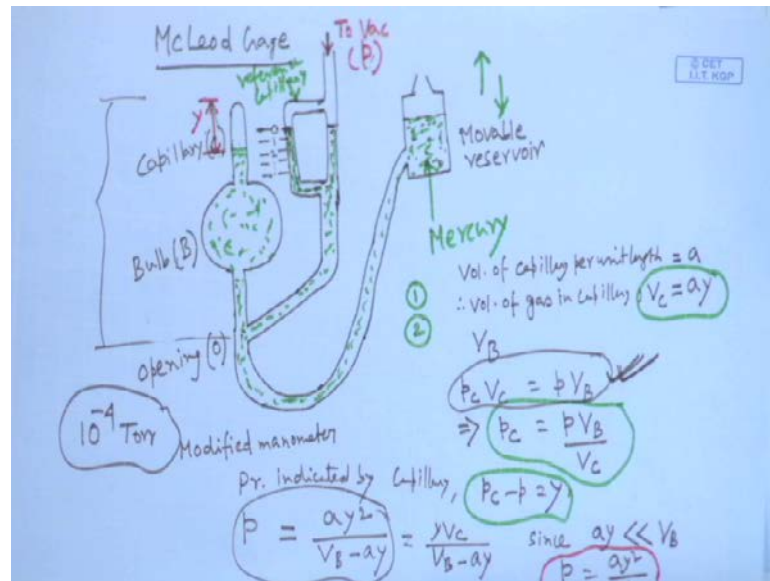
So, again the corrosive fluid is not being allowed to come in direct contact with the Pressure gauge. So, either with help of a diaphragm element or a liquid seal we, can protect a pressure gauge when we use it for measurement of pressure of corrosive fluid.

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Let us now talk about High Vacuum Measurement or measurement of very low pressure. We have several instruments for measurement of very low pressures. So, we are talking about pressures starting from say 1 Torr up to  $10^{-7}$  or  $10^{-10}$  Torr. The instruments commonly used for measurement of high vacuum or extremely low pressures are McLeod Gage which is essentially a modified manometer. Ionization gage, Thermocouple gage, Pirani gage working principle of Thermocouple gage Pirani gage are related together they can be clubbed as Thermal conductivity gage and also Knudsen gage. This is not much used these days. But, these instruments are widely used for measurement of very low pressure.

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So, let us start our discussion with Macleod Gage. So, Mcleod Gage is essentially a Modified Manometer. Let us draw the picture first. This is a Moveable reservoir. So, this is Mercury. This is Capillary. Let, us indicated it by C. This is Bulb called B. Here, we have an opening this called O and, this is the flexible tube which connects this to the moveable reservoir. So, this is a Mcleod Gage which is nothing, but a Modified Manometer. We have a scale attached here, we have scale here this is 0, 1, 2 and so on and so forth. So, this is the 0, 0 reading this is the 0 of the scale.

So, let us say this is all filled with the mercury. So, this is the construction of a Mcleod Gage. Which consist of a capillary a bulb and this is connected to a moveable reservoir. It can we can bring it up or down the way to as follows, the moveable reservoir is lower until the mercury column drops below the opening O. As we move this reservoir up or down. The mercury the level of the mercury in this capillary bulb will, go up or come down. So, the first step to pressure measurement is lower the moveable reservoir until the mercury column drops below the opening o. So, when it drops below opening o. The bulb B the Capillary C, are connected to the same pressure source as this. This one is connected to the vacuum whose pressure I am going to measure.

So, this is To Vacuum let us call P. So, this is connected to the vacuum or low pressure source whose pressure I am going to measure. So, first a lower the moveable reservoir until the mercury column drops below point o. So, when it goes below point o this entire

thing is connected to the same low pressure source or same vacuum so that was first step. In the second step the reservoir is raised until the mercury fills the bulb and rises in the capillary to a point where the level in the reference capillary is located at 0 point. The second step is the moveable reservoir is now raised and as we raised the moveable reservoir the mercury level the mercury also goes up here and we stop when the mercury column in this reference capillary call this reference capillary. We stop when the mercury level touches the 0 of the scale in this reference capillary.

Imagine under such situation this measurement is  $y$ . Will now, see that from this  $y$  which is the length of the capillary occupied by the gas the same gas whose pressure I am going to measure will be used to compute the pressure. So, the measurement has two major steps. In the first stage the moveable this is connected to vacuum or local the moveable reservoir is lower such that the mercury level falls below point o, in that case the entire capillary bulb the reference capillary etcetera is connected to the same pressure source. In the second stage I raise the moveable reservoir. So, the mercury level stops coming stops going up when it crosses the point o see that this part is now disconnected from the low pressure source.

So, in fact the gas inside is being compressed. So, I continue to raise the moveable reservoir until the mercury layer in this capillary reference capillary touches the 0 of the scale. Under such situation let us consider the length of the gas in the capillary is  $y$ . So, this length is  $y$ . Now let us see how we can calculate the pressure  $P$  from the measurement of  $y$ . Let, us consider the Volume of capillary per unit length is  $a$ . So, Volume of the gas in the capillary if you call it  $V_c$  should be equal to  $a$  into  $y$ . Because,  $a$  is the volume of the capillary per unit length my length is  $y$ . So, the volume of the gas in the capillary  $V_c$  is  $a$  times  $y$ . Let, us consider the volume of the capillary plus volume of the blub and the volume of the tube down to point o opening O that means, this entire part is  $V_B$ .

So, let us denote the volume of the capillary, volume of the bulb and volume of the tube up to point o is  $V_B$ . So, when we start it raising the reservoir at second stage and when we reached point o and got this part just got disconnected I have  $V_B$  as the volume of the gas. And I have now  $a$  times  $y$  as volume of gas when the reference when the mercury rest at 0 in the reference capillary. So, initially I had a gas of these volumes with pressure  $P$  now, I have a gas with this volume with some other pressure. If, we consider

isothermal compression of the gas in the capillary I can write  $p_c V_c$  equal to  $p V_B$ . Where,  $p_c$  is the pressure of the gas in the capillary now after compression or, we can write  $p_c$  equal to  $p$  which is the unknown pressure  $V_B$  by  $V_c$ . Now, the pressure indicated by the capillary we can write as  $p_c - P$  equal to  $y$ .

Now, if I use this relationship and this relationship if we combine this three equations we can write  $P$  the unknown pressure  $P$  equal to  $ay^2$  by  $V_B - ay$  which, can also be written as  $y V_c V_B - ay$ . Since, this volume is much less than this volume of this capillary plus bulb and plus volume of the tube up to point o that means, since  $ay$  is much, much less than  $V_B$  we can write from this  $P$  equal to  $ay^2$  by  $V_B$ . Because, we can safely neglect  $ay$  as this is much less than  $V_B$ . So, finally, the pressure  $P$  is related to this measurement  $y$ . For a given McLeod Gage  $a$  and  $V_B$  is fixed. So,  $P$  depends only on  $y$ .

So, for measurement from the measurement of this  $y$  alone which represents the length of the capillary or the length of the gas in the capillary I can measure the unknown pressure or unknown vacuum  $P$ . We need to remember one thing here, that the McLeod Gage is sensitive to condensed vapors that may be present in the sample because they can condense upon compression and then the relationship  $p_c V_c$  equal to  $p V_B$  may not be valid. Because, the working of the McLeod Gage depends on this relationship we should ensure that this holds true. We can measure pressures up to  $10^{-4}$  Torr using McLeod Gage; one important thing one important observation about the McLeod Gage we should know that the pressure is being measured from this dimension alone for given McLeod Gage. So, in the range up to  $10^{-4}$  Torr the McLeod Gage is often used as a primary standard. We still have some other pressure measuring instruments to discuss which are used for high vacuum namely ionized at namely Ionization Gage and thermal conductivity gages such as Thermocouple Gage and Pirani Gage.